

Assessment of various CFD models for predicting airflow and pressure drop through pleated filter system

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Abstract

Pleated filters, sometimes in combination with an electrostatic precipitator, are widely used to control particle contaminants in enclosed environments. Such a filter system can improve the health of occupants in these spaces. Computational Fluid Dynamics (CFD) can be a powerful tool for optimizing the design of pleated filter system. However, the performance of various CFD models has not been clearly understood for predicting transitional turbulent flows in pleated filter systems. This study evaluated the performance of several turbulence models, including the standard $k-\epsilon$ model, low Reynolds number $k-\epsilon$ models, the v2f model, Large Eddy Simulation (LES) models, and Detached Eddy Simulation (DES) models, for simulating the pressure drop and transitional flows through pleated filters both with and without an electrostatic precipitator. The simulated results from the models were compared with the experimental data from the literature and our measurements. The results indicate that the v2f, LES and DES (Spalart–Allmaras) can accurately predict the pressure drop and flow distributions in pleated filters. Because the LES requires high computing capacity and speed, the DES (Spalart–Allmaras) and the v2f models are recommended for the optimal design of a pleated filter system.

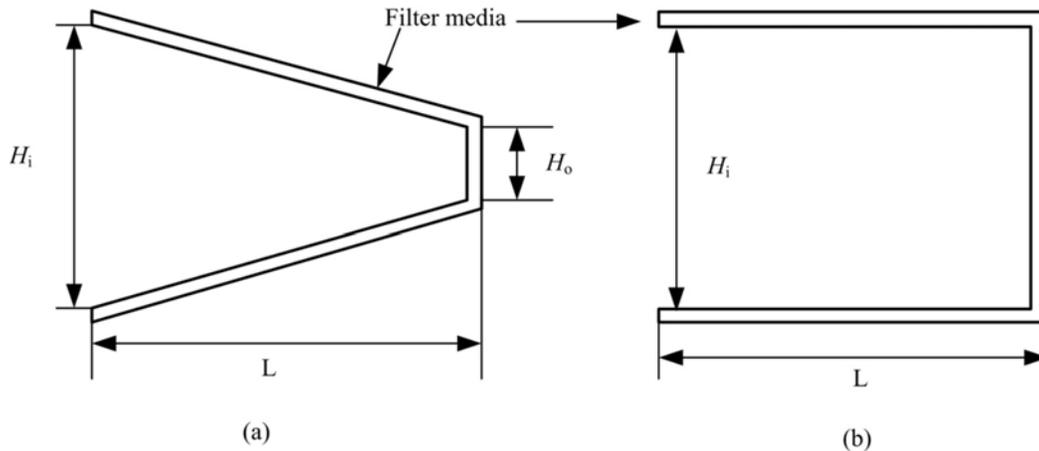
Keywords: Particulate; pleated filter; electrostatic precipitator; transitional flow; CFD

Introduction

Most people spend 90% of their time in enclosed environments such as buildings, cars, and public transportation. Particulates exist in these environments, and the health of occupants is related to particulate concentration (Chio and Liao, 2008), as in the cases of children's atopic dermatitis (Song et al., 2011) and lung cancer (Pope et al., 2002). Sometimes the particulates contain various types of bacteria and viruses that cause infectious diseases. These airborne particulates can create a very high risk for occupants (Mangili and Gendreau, 2005). Hence, the control of indoor airborne particles is very important.

Many technologies, including pleated filters and electrostatic precipitators, are available for removing air particles. Pleated filters, such as High-Efficiency Particulate Air (HEPA) filters, are widely used in buildings and airplanes. Properly maintained HEPA filters can remove at least 99.97% of airborne particles with a diameter of 0.3 micrometers or larger (Hocking, 2000). However, this type of filter has a limited working life because the pressure drop across it increases during the particle collection process. An increase in the pressure drop causes an increase in energy consumption by the fan, so that it is necessary to change the filter periodically. In addition, the particle layer on the surface of pleated filters may pollute the air (Clausen, 2004). Electrostatic precipitators (ESPs) collect the particles by use of an electric field. ESPs have a low pressure drop but also a low collection efficiency for submicron particles (Morawska et al., 2002). Therefore, hybrid filtering systems combining the two technologies have been developed to make use of their respective strengths. Croxford et al. (2000) found that a local ESP with a front pre-filter could significantly reduce the concentration of indoor airborne particles, especially for small particles. Skulberg et al. (2005) experimentally studied the performance of a hybrid local ESP and carbon filter system in an

44 office and found that this system could significantly reduce the indoor particle concentration. [Zuraimi and](#)
 45 [Tham \(2009\)](#) measured the particle concentration in an office building equipped with an ESP with a
 46 Pre-Filter (ESP-PF); they found that the hybrid system worked very well. The removal efficiency of the
 47 ESP-PF filter was close to 100% for particles with a diameter larger than $0.3 \mu\text{m}$. [Huang et al. \(2008\)](#)
 48 developed an enhanced low-efficiency filter with an air ion emitter to reduce the concentration of biological
 49 particles in a heating, ventilating, and air-conditioning (HVAC) system. [Park et al. \(2009, 2011\)](#) developed
 50 a carbon fiber ionized-assisted filter to improve the removal efficiency for submicron aerosol particles and
 51 bioaerosols in an HVAC system. These studies demonstrated the advantages of technologies that combine
 52 the ESP and pleated filters. As pleated filter systems become more and more complicated, it becomes
 53 challenging to create an optimization design.



54
 55 **Fig. 1.** The structures of pleated filters: (a) trapezoidal type; (b) rectangular type
 56

57 Numerical methods have been developed over the years for the optimization design of the ESP
 58 ([Gallimberti, 1998](#)), pleated filters ([Chen et al., 1995](#); [Subrenat et al., 2003](#); [Rebai et al., 2010](#); [Fotovati et](#)
 59 [al., 2011, 2012](#)) and hybrid systems ([Long and Yao, 2012](#)). The most important aspect of the optimization
 60 design is to determine the flow field through the filter systems. The flow pattern in the ESP is fully
 61 turbulent with a high Reynolds number, and many turbulence models can be used as recommended by
 62 [Kallio and Stock \(1992\)](#) and [Schmid et al. \(2002\)](#). However, simulations of the flow field through a
 63 pleated filter are more difficult. Figure 1 shows the structures of two types of pleated filter. In the ducts of
 64 common HVAC systems, the upstream air flow of the pleated filter is usually fully developed ([Liu et al.,](#)
 65 [2012](#)). But the flow in the porous media of the air filter is laminar ([Rebai et al., 2010](#); [Fotovati et al.,](#)
 66 [2011](#)). The flow in the air channel of the pleated filter changes from the turbulent flow to the laminar
 67 flow. Therefore, the air flow through the pleated air filter is very complex and a combination of the three
 68 basic types of the air flow: turbulent, laminar and transitional. Many semi-empirical models are available
 69 for predicting the flow field and pressure drop through a fiber or a flat filter. For example, [Feng \(2007\)](#)
 70 derived an analytical method by using Darcy's law for predicting pressure drop through a pleated filter,
 71 and the results matched the experimental data well. However, such a model assumes a uniform filtration
 72 velocity distribution along the surface of the filter media, which may not be accurate. [Rebai et al. \(2010\)](#)
 73 developed a semi-analytical model for simulating the flow field in pleated filters, which could predict
 74 both the pressure drop and the gas filtration velocity. However, their model provides only the
 75 one-dimensional velocity and does not account for the full details of the flow field information. As flow
 76 through a filter is governed by the Navier–Stokes equations, the Computational Fluid Dynamics (CFD)

77 technique has also been used to predict the performance of pleated filters. [Chen et al. \(1995\)](#) used the
78 laminar flow model to optimize pleated filters with a finite element method. [Subrenat et al. \(2003\)](#)
79 studied three-dimensional flow in a cylindrical pleated filter by solving the time-averaged Navier–Stokes
80 equations combined with the standard k - ε turbulence model ([Lauder and Spalding, 1974](#)), and the results
81 matched the experimental pressure drop data. [Rebai et al. \(2010\)](#) used a laminar flow model to simulate
82 the flow field in pleated filters for validating a semi-analytical model. [Fotovati et al. \(2011, 2012\)](#) used a
83 laminar flow model combined with a particle collection model to simulate the instantaneous transitional
84 flow field of pleated filters during a cake clogging process. Although the laminar flow model for flow
85 simulation in pleated filters appears to be acceptable in the above applications, the flow through the
86 pleated filter is actually not simple laminar. Especially in some hybrid systems ([Croxford et al., 2000](#);
87 [Skulberg et al., 2005](#); [Huang et al., 2008](#); [Park et al., 2009, 2011](#)), the gas flow is a combination of fully
88 turbulent, transitional and laminar flow. Thus, a suitable model that can simulate the turbulence flow
89 filed in the pleated filter system is necessary for the optimal design and performance analysis. Possible
90 models include the Low Reynolds Number (LRN) k - ε models, Large Eddy Simulation (LES) models, and
91 Detached Eddy Simulation (DES) models. To evaluate the performance of these models, it is essential to
92 use experimental data for flow through filters. However, almost all the available experimental data for
93 pleated filters focused on pressure drop ([Feng, 2007](#); [Rebai et al., 2010](#)), not flow field. Because the
94 turbulence intensity in the pleated area is very low, the turbulent characteristics are not used to evaluate
95 the models.

96 According to the above, the objectives of this investigation are: (1) to measure the flow filed
97 distributions in the pleated filter, (2) to evaluate the performance of various turbulence models for
98 predicting flow fields through pleated filters and (3) to assess the applicability of the selected turbulence
99 models to predict the flow in a combined ESP-pleated filter system. These objectives have led to the results
100 reported in this paper.

101 **Research methods**

102 *CFD models*

103 The CFD models assessed in this investigation can be written in a general form as:

$$104 \quad \rho \frac{\partial \bar{\phi}}{\partial t} + \rho u_j \frac{\partial \bar{\phi}}{\partial x_j} - \frac{\partial}{\partial x_j} \left[\Gamma_{\text{eff}} \frac{\partial \bar{\phi}}{\partial x_j} \right] = S_{\phi} \quad (1)$$

105 where ϕ is the flow variable, Γ_{eff} the effective diffusion coefficient, S_{ϕ} the source term, and u_j the velocity
106 component in the j direction, ρ the air density. Table 1 provides the various terms for the models ([Zhai et al.,
107 2007](#)) assessed in the present study. In Table 1, u_i is the velocity component in the i direction, k the
108 turbulence kinetic energy, ε the dissipation rate of the turbulence kinetic energy, P the fluid pressure, μ_t the
109 turbulent eddy viscosity, G_k the turbulence production, G_B the generation of turbulence kinetic energy due
110 to buoyancy, and S the rate of strain. σ_k and σ_{ε} are the turbulent Prandtl numbers for k and ε , respectively. f_1 ,
111 f_2 , and f_{μ} the damping functions, D and E are additional terms for low-Re model. τ_{ij} is the subgrid stress for
112 the LES model. C_1 , C_2 , C_3 , $C_{\varepsilon 1}$, $C_{\varepsilon 2}$, C_L , C_{η} and C_{μ} are the turbulence constants. The $\overline{v'^2}$ is the fluctuating
113 velocity normal to the nearest wall. The f is part of the $\overline{v'^2}$ source term that accounts for non-local
114 blocking of the wall normal stress, T the turbulence time scale for v2f model.

115

Table 1 Terms and coefficients for Eq. (1)

	ϕ	Γ_{eff}	S_ϕ	Constants and Coefficients
Standard k- ε (St-k ε)	k	$\mu + \mu_t / \sigma_k$	$G_k + G_b - \rho\varepsilon$	$\mu_t = \rho C_\mu k^2 / \varepsilon; G_k = \mu_t S^2; S = (2S_{ij}S_{ij})^{0.5}; G_b = \beta g_i (\frac{\mu_t}{\sigma_t}) (\frac{\partial T}{\partial x_j})$
	ε	$\mu + \mu_t / \sigma_\varepsilon$	$C_1(G_k + C_3 G_b) \varepsilon / k - C_2 \rho \varepsilon^2 / k$	
Low Re k- ε (LRN)	k	$\mu + \mu_t / \sigma_k$	$G_k - D - \rho\varepsilon$	$\mu_t = \rho f_\mu C_\mu k^2 / \varepsilon; G_k = \mu_t S^2; S = (2S_{ij}S_{ij})^{0.5}$
	ε	$\mu + \mu_t / \sigma_\varepsilon$	$C_1 f_1 G_k \varepsilon / k - C_2 \rho f_2 \varepsilon^2 / k + E$	
LES	u_i	μ	$-\frac{\partial p}{\partial x_i} - \frac{\partial \tau_{ij}^S}{\partial x_j}$	$\tau_{ij} \equiv \overline{\rho u_i u_j} - \overline{p u_i u_j}; \tau_{ij} - \frac{1}{3} \tau_{kk} \delta_{ij} = -2\mu_t \overline{S_{ij}}; \overline{S_{ij}} \equiv \frac{1}{2} (\frac{\partial \overline{u_i}}{\partial x_j} + \frac{\partial \overline{u_j}}{\partial x_i})$
v2f	k	$\mu + \mu_t / \sigma_k$	$G_k - \rho\varepsilon$	$f - L^2 \nabla^2 f = \frac{C_1}{T} (\frac{2}{3} - \frac{\overline{v'^2}}{k}) + C_2 \frac{G_k}{\rho k} + 5 \frac{\overline{v'^2}}{kT}; T = \max(\frac{k}{\varepsilon}, 6 \sqrt{\frac{\mu}{\rho\varepsilon}});$
	ε	$\mu + \mu_t / \sigma_\varepsilon$	$C_{\varepsilon 1} G_k \varepsilon / k - C_{\varepsilon 2} \rho \varepsilon^2 / k$	
	$\overline{v'^2}$	$\mu + \mu_t / \sigma_k$	$S_{v'^2}$	

119 The standard $k-\varepsilon$ model (Launder and Spalding, 1974) is a two-equation model that can obtain robust,
120 economical, and reasonable results for many engineering flows, although it was developed for
121 high-Reynolds-number flows. Because the model has been widely used, it was selected as a benchmark in
122 this study.

123 The LRN $k-\varepsilon$ models have similar turbulence transport equations but use damping functions
124 (Gürdamar, 2005; Schmidt and Patankar, 2003; Jagadeesh and Murali, 2005). The LRN $k-\varepsilon$ models require
125 a very fine grid near the wall, resulting in high computing costs. The LRN models used in the present study
126 include the Abid (AB) (Abid, 1993), Lam-Bremhorst (LB) (Lam and Bremhorst, 1981), Launder-Sharma
127 (LS) (Launder and Sharma, 1974), Yang-Shih (YS) (Yang and Shih, 1993), Abe-Kon-Doh (AKD) (Abe et
128 al., 1994), and Chang-Hsieh-Chen (CHC) (Chang et al., 1995) models. These models differ only in terms of
129 the constants and the expression of damping functions.

130 The v2f model was developed for low-speed and wall-bounded flow using the fluctuation of normal
131 velocity rather than kinetic energy to calculate the near-wall turbulence-eddy viscosity. This model uses
132 damping functions to limit the fluctuating value of normal velocity in nearly isotropic flow regions in order
133 to obtain accurate results (Durbin, 1991). The model has been recommended for simulating flows in
134 enclosed environments (Zhang et al., 2007). Because of the bounded porous wall flow characteristic in
135 pleated filters, the v2f model may provide good results; therefore, it was also used in this study.

136 The above models are based on Reynolds-Averaged Navier-Stokes (RANS) equations. LES is an
137 advanced turbulence model that directly calculates large eddies and models small eddies using
138 subgrid-scale models, based on the theory that small-scale eddies can be separated from large-scale eddies.
139 This study tested four widely used subgrid-scale models for LES: the Smagorinsky–Lilly model (SGS)
140 (Smagorinsky, 1963), Dynamic Smagorinsky–Lilly model (DSL) (Germano et al., 1996), Wall-Adapting
141 Local Eddy-viscosity (WALE) model (Nicoud and Ducros, 1999), and Dynamic kinetic energy (Dke)
142 model (Kim, 2004). The first three models use resolved velocity scales and several constants to calculate
143 the subgrid stress, and all of them are based on the assumption that the dissipation of subgrid kinetic energy
144 is equal to the transferred energy from the filter scale. The Dke model solves the transport equation of the
145 subgrid Dke rather than making an assumption.

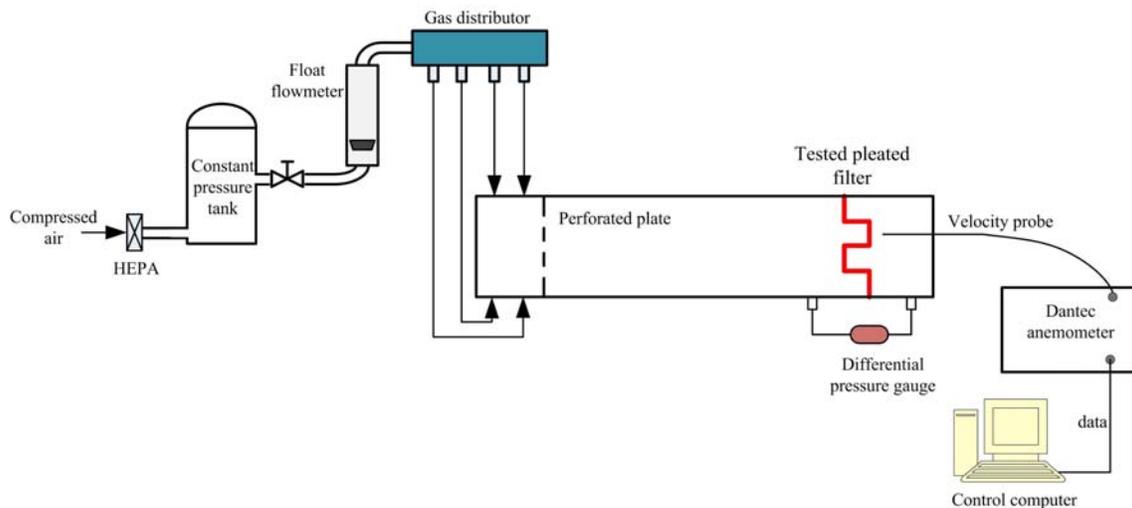
146 DES is a hybrid approach combining the LES and RANS models. For DES, the flow field of the
147 near-wall region is resolved by a RANS model, while the fully turbulent region is resolved by LES. This
148 investigation tested three RANS models used in DES: the Spalart–Allmaras model (SA) (Spalart and
149 Allmaras, 1992), Realizable $k-\varepsilon$ model (R- $k\varepsilon$) (Shih et al., 1995), and SST model (SST) (Menter, 1994).

150 The present study evaluated these turbulence models for flow through several pleated filters. A
151 commercial CFD software program, ANSYS Fluent (ANSYS Fluent, 2009), was used for the numerical
152 simulations. All the selected turbulence models were available in the CFD software. The SIMPLE
153 algorithm is utilized in the pressure correction equation. The pressure discretization scheme uses the
154 standard first-order upwind, and all the others uses the second-order upwind. For the simulation with
155 LES or DES models, the unsteady simulations were conducted and the time step was 0.001 s.

156 **Experimental setup**

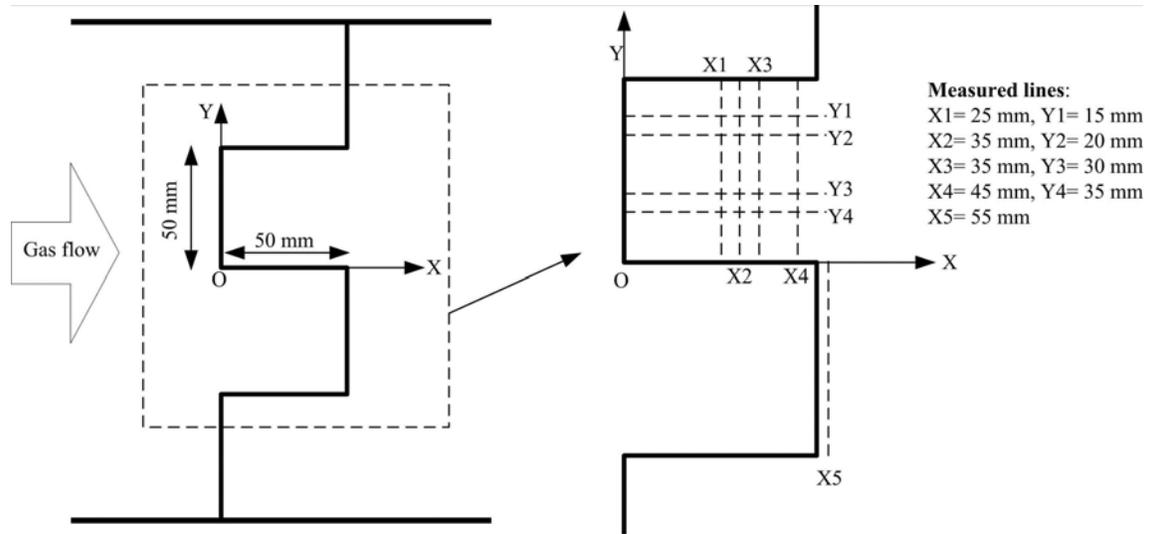
157 Figure 2 shows our experimental test rig for measuring the velocity distributions and turbulence
158 characteristics downstream from a pleated filter. Compressed air was first filtered by a HEPA filter and
159 stored in a constant-pressure tank for supplying clean compressed air to the system. A valve was used to
160 control the airflow rate, which was measured by a flow meter. The air was then divided into four parts
161 through a gas distributor. The four parts entered the experimental channel from the four sides of the
162 channel, which created a uniform flow field in the upstream section of the channel. The experimental

163 channel was 2 m long with a 200 mm square transverse section. A perforated plate was used to make the
 164 flow more uniform. Finally, the gas flowed through the pleated filter that was used for the experiment. The
 165 tested filter was rectangular, with a 50 mm pleat length and distance. The pressure drop across the filter
 166 was recorded using a differential pressure gauge. The flow velocities behind the filter were measured using
 167 a Dantec constant temperature anemometer, and the data were recorded with a computer. The flow
 168 velocities behind the filter were measured using a Dantec hot-wire anemometer, and the data were recorded
 169 by a computer. The measurement frequency of the anemometer is 2000Hz and the time constant is 0.0005s.
 170 The time period of one measurement is 1s. The mean velocity in the experiment is defined as the average
 171 value of 2000 samples in 1s. The pressure drop of the pleated filter is measured by a pressure sensor, the
 172 sample frequency of which is 10 Hz.
 173



174 **Fig. 2** Diagram of the experimental test rig
 175
 176

177 Figure 3 shows that the pleated filter was folded with a height of 50 mm and width of 50 mm; its depth
 178 extended across the entire width of the channel. The tested pleated filter is quite different from industrial
 179 products, which have a higher pleat density. One reason is that a high pleat density would make the pleat
 180 distance very small, so that it would be hard to position an anemometer for measuring air velocity. Another
 181 reason for making a filter with a short pleat distance is to reduce the laminar effect of the filter media on the
 182 flow field. Figure 3 illustrates the measurements that were taken in lines X1 to X4 and Y1 to Y5. Each line
 183 had 15–30 measurement points. The measurements were also performed in the Z-direction (along the depth
 184 of the filter) along three lines to verify that the flow was two-dimensional. Each measurement was repeated
 185 three times.



186
187 **Fig. 3** The geometry of the pleated filter tested and the measurement locations.
188

189 The through-plane permeability distribution of filter media may not be uniform, which will result in
190 non-uniform velocity distributions in the filter. This investigation tested the velocity uniformity of four
191 types of common air filter media used for pleated filters by measuring the velocity distributions
192 downstream of the flat filter media. The filter media were polypropylene (PP), glass fiber (GB),
193 polyethylene (PE), and polyester (PET). The size of the flat filter media was 200 mm × 200 mm. The
194 distance between the anemometer and the filter media was 3 mm. Table 2 shows the measured permeability,
195 which can be calculated by the equation:

$$196 \quad k = \frac{\mu U E}{\Delta P} \quad (2)$$

197 where U is the measured mean velocity (m/s), E the thickness of measured filter media (m), μ the kinetic
198 viscosity (m^2/s), ΔP the pressure drop across the flat filter media (Pa), and k the through-plane permeability
199 (m^2).

200
201 **Table 2** The parameters of the filter materials used in the tests

Filter media	Thickness (mm)	Through-plane permeability (m^2)
PP	0.30	8.33×10^{-12}
GB	0.38	1.20×10^{-13}
PE	0.38	4.70×10^{-11}
PET	0.38	3.80×10^{-11}

202 203 **Results**

204 *Preliminary experimental tests*

205 The flow in the channel was measured as one-dimensional along the longitudinal direction before a filter
206 was installed. To investigate the flow uniformity behind a filter, the air velocities in a transverse section
207 were measured carefully with a flat filter, as shown in Figure 4. The uniformity of the filter media was
208 evaluated according to the velocity distribution behind the flat filter. The assessment criterion is the relative
209 root mean square error (RRMSE) of the flow velocities:

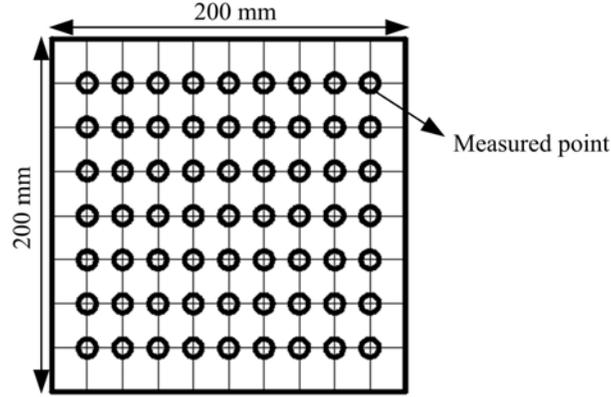
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$$RRMSE = \sqrt{\frac{\sum_{i=1}^N (U - \bar{U})^2}{N-1}} / \bar{U} \quad (3)$$

211

where U is the measured velocity (m/s), N is the number of measured points, and \bar{U} is the average measured velocity.

212



213

Fig. 4 The measured positions in a transverse section of the experimental channel

214

215

216

The mean velocity in the channel was fixed at 0.13 m/s; the air temperature was about 20°C; and the kinematic viscosity was about $1.46 \times 10^{-5} \text{ m}^2/\text{s}$. The measured turbulence intensity in the transverse section was strong, with an average of 15%. The mean velocity, temperature, and turbulence intensity were measured in the channel without a filter.

219

220

Figure 5 presents the RRMSE for channel flow without a filter and for the channel flow with the four types of filter media. The results indicate that the channel flow without a filter had a good uniformity with an RRMSE of 8%. The PP and GB media had very homogeneous structures, which can be easily modeled as porous media in numerical simulations. Meanwhile, the structures of the PE and PET media resulted in non-homogeneous flows with an RRMSE higher than 20%, which would be difficult to simulate numerically. The pleated filter used in the experiment was made by hand. Because the GB media were somewhat soft for the hand-made process, this investigation selected the PP media for our flow tests.

221

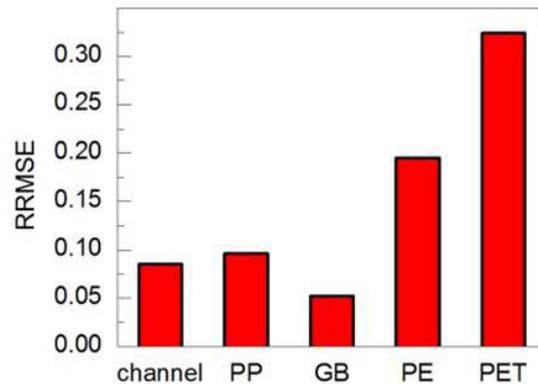
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Fig. 5 Non-uniformity of the channel flow without and with the four types of filter media

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Velocity measurements

231

After the pleated filter with the PP media had been installed in the test rig, this investigation measured

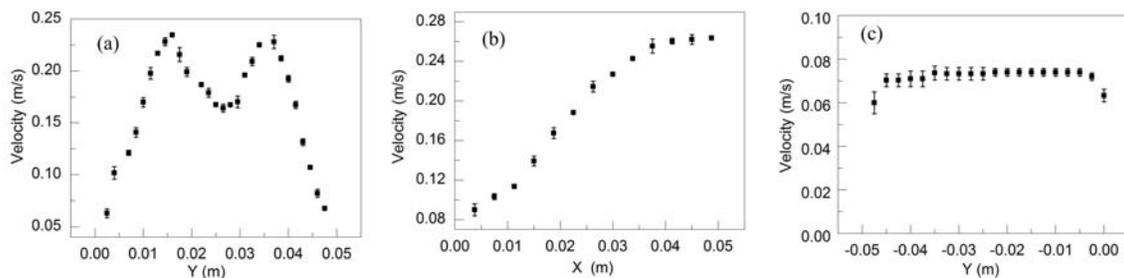
232 the velocity distribution in lines X1 to X5 and Y1 to Y5. The one-dimensional velocity component along
 233 the longitudinal direction was measured. Figure 6 shows the x-velocity component for lines X1, Y4, and
 234 X5, where the error bars represent the differences among the three measurements. The repeatability of the
 235 measurements was quite good. The x-velocity distribution along line X1, as shown in Figure 6(a), was
 236 bimodal with two peaks, and the x velocity at the middle point was about 70% of the peak velocity. Figure
 237 6(b) shows the relationship between the x velocity and the x position to be approximately linear, and the
 238 relatively uniform air flow across the filtration media caused a linear increase in the x velocity. The
 239 measured x-velocity profiles for X2 and X3 had a similar shape to that of X1, and those for Y1, Y2, and Y3
 240 had a similar shape to that of Y4 but with different values, although they are not shown here. Figure 6(c)
 241 shows the measured x-velocity profile of X5, with a very uniform distribution. The distance between the
 242 filter surface and line X5 was 2 mm, and the x-velocity at line X5 was approximately equal to the filtration
 243 velocity. Figure 7 explains why the x-velocity profile of X1 line is bimodal. Because of high pressure drop
 244 value of filter media, the filtration velocity along the filter media is uniform and perpendicular to the filter
 245 media surface. For the x-velocity profile of line X1, the value of x-velocity increases from point A to point
 246 B because of the y-velocity component of the air flow though the filter media and the value of x-velocity
 247 decreases from point B to point C because of the collision between air flow from upper and down filter
 248 media.

249 The average filtration velocity can be calculated by equation:

250
$$v_f = v \times \frac{A_s}{A_f} \quad (4)$$

251 where A_s is the area of the channel's transverse section, A_f is the total area of the filter surface, v is the
 252 upstream velocity before the filter, and v_f is the filtration velocity. The average filtration velocity calculated
 253 for line X5 was 0.072 m/s, which was very close to the experimentally measured velocity of 0.074 m/s.

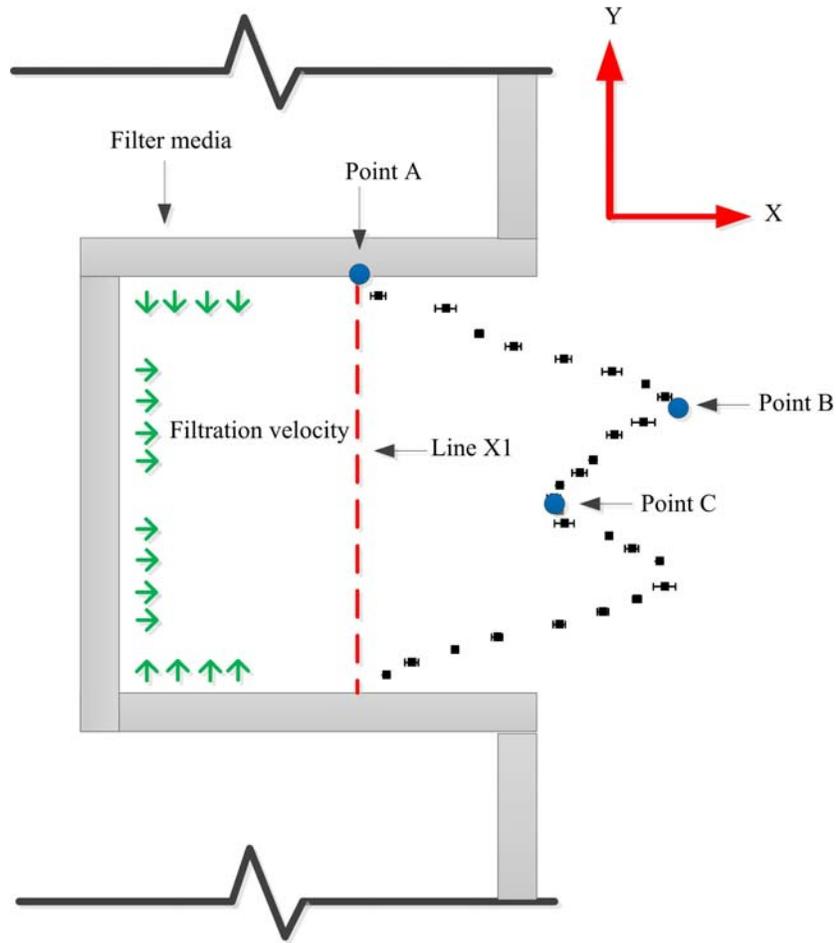
254 The measured pressure drop for this pleated filter was 470 Pa when the channel velocity was 0.13 m/s.
 255 The pleated filter experienced a slight deformation with the pressure drop. If this investigation had
 256 increased the channel velocity and pressure loss, the pleated filter may have had a serious deformation or
 257 even been destroyed. The iron grid commonly used in industrial filters would increase structural strength in
 258 test filters.



259

260

Fig. 6. The measured x-velocity profile along (a) line X1, (b) line Y4, and (c) line X5



261
262 **Fig. 7** The filtration process in pleated filter and measured x-velocity profile along line X1.

263 ***Numerical simulations of the pressure drop through the filter***

264 All the CFD models shown in Table 1 were used to calculate the pressure drop through the filter, but
 265 not all the results are presented here because of the limited space available in this paper. Only the LES
 266 (SGS), DES (SA), LRN (LS), standard $k-\epsilon$, and v2f models are presented because they are widely used. For
 267 the simulation with LES or DES models, the unsteady simulations are conducted and the time step is 0.001s.
 268 During the simulation, all the quantities were averaged every 1000 time-steps. The model predictions
 269 presented in the following figures are the values of the final average. The calculation flow time for LES and
 270 DES cases was about 17 second and 15 second, respectively. Their times ensured that the final flow
 271 reached the steady status.

272 Figure 8 shows the pressure drop calculated by these turbulence models. All the models provide similar
 273 and satisfactory results, but this does not imply that these models can accurately predict the performance of
 274 the pleated filter. The total pressure drop of the pleated filter is the sum of the pressure drop across the filter
 275 media and the pressure drop caused by the pleated channel. The pleated filter used in the experiment was
 276 made of PP filter media with a high resistance and permeability of $8.33 \times 10^{-13} \text{ m}^2$. Because of the high filter
 277 media resistance and low filtration velocity, the pleated channel pressure drop was negligible as compared
 278 to that of the filter media. The total pressure drop of the test filter was determined from the filter media
 279 rather than the detailed flow field around the filter. Hence, the use of pressure drop as a criterion for
 280 assessing different turbulence models could be misleading in this case.

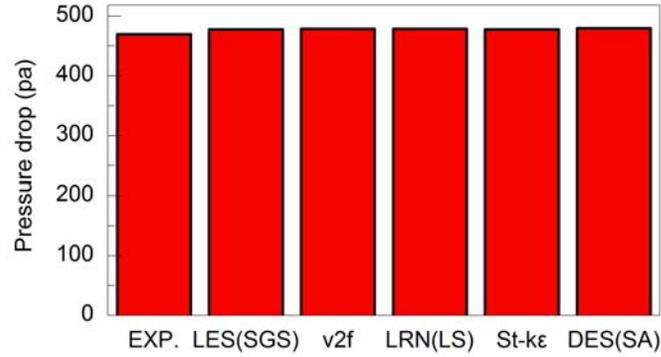


Fig. 8 Comparison of the pressure drop through the filter as predicted by various CFD models with the experimental data.

Therefore, this investigation simulated the cases from [Rebai et al. \(2010\)](#), and their measured pressure drop data were used to validate the CFD models. Table 3 summarizes the pleated filter characteristics and the boundary conditions used by [Rebai et al. \(2010\)](#), as compared with the parameters used in our experiment. In [Rebai's](#) case, the filter media resistance was not high, such that the pressure drop through the pleat channel was important. The ratio of the filter media pressure drop to the total filter pressure drop was 0.34, as compared to near zero in the present study.

Table 3 Comparison of filter media and test conditions used in [Rebai et al. \(2010\)](#) and the present study.

Case	Pleat width (mm)	Pleat height (mm)	Permeability (m ²)	Media thickness (mm)	Duct face velocity (m/s)
Rebai et al.	12.5	51	3.57×10^{-10}	1.45	2.400
Present study	50	50	8.33×10^{-12}	0.30	0.130

Figure 9 shows the simulated pressure drop as obtained by the CFD models for [Rebai's](#) case. The LES (SGS) and DES (SA) models can provide an acceptable pressure drop, as compared with the experimental data from literature. Most of the RANS models performed poorly in predicting the pressure drop, although many of the results are not presented in Figure 9. The v2f model can successfully predict the pressure drop, perhaps because the model accurately predicts the normal stress on the filter, which is an important feature of the pleated filter flow field. Because the pressure drop through the pleat channel was important in this case, prediction of the detailed flow field in the filter channel was crucial in predicting the total filter pressure drop. Because the flow was complex, advanced models, such as LES and DES, were capable of predicting the flow as well as the pressure drop, but most of the RANS models were not.

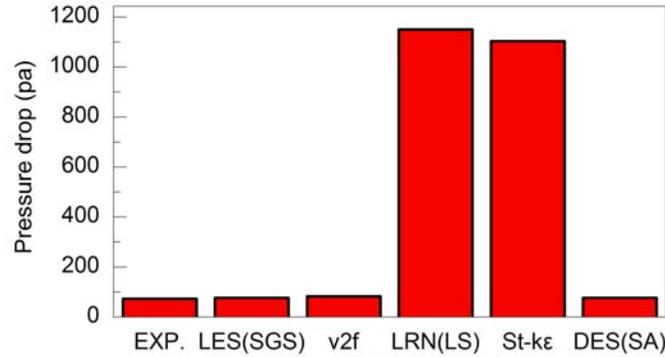


Fig. 9 Comparison of the pressure drop as predicted by various CFD models with the experimental data from Rebai et al. (2010).

Numerical simulations of the flow field

It is difficult to thoroughly evaluate the performance of turbulence models for a pleated filter using pressure drop as the only criterion because it is a lump sum value. The models should be also evaluated using the flow field data around the filter.

Figures 10-11 compare the velocity predicted by different CFD models with the experimental data in lines X1, X3, Y1, and X5. Figure 10(a) shows that the LES (SGS) model with the Smagorinsky-Lilly subgrid-scale model can successfully predict the velocity profile. The DES (SA) model provided good agreement with the experimental results. The v2f models provided acceptable velocity results, but slightly underestimated the peak value. The v2f model has been widely adopted for flow simulations in enclosed spaces using the fluctuation of normal velocity rather than the kinetic energy to calculate near-wall turbulence eddy viscosity. It is suitable for modeling low-speed and near-wall flow, such as the relatively low duct velocity and the complex porous wall in the pleated filter. The LRN (LS) model and the standard k- ϵ model had a slightly poorer performance than the v2f model. Figure 10(b) shows similar results for line X3, but the LRN (LS) and standard k- ϵ models performed very poorly for this location.

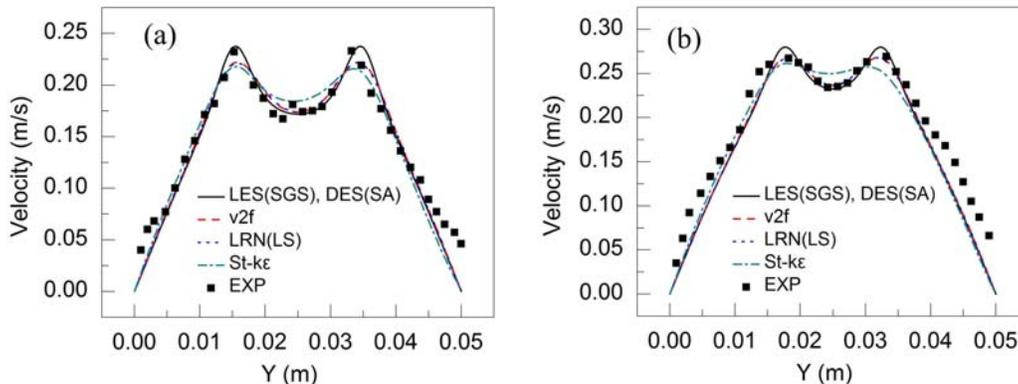
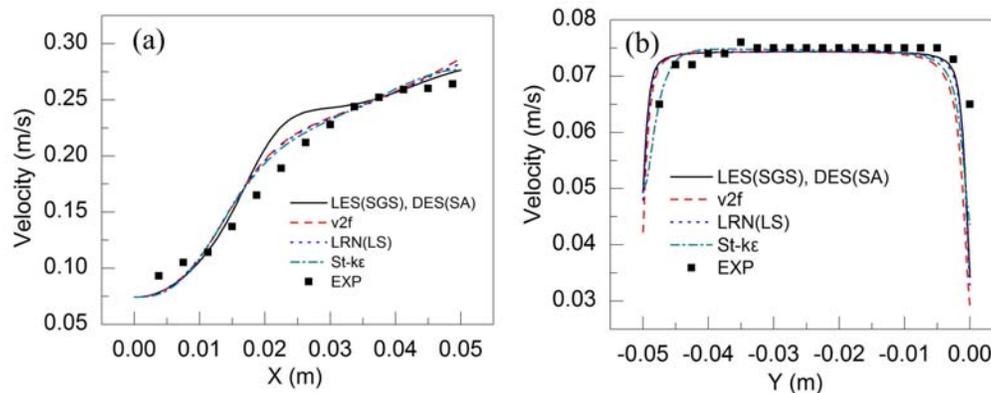


Fig. 10 The simulated and measured velocity profiles along (a) line X1 and (b) line X3.

Figure 11 further compares the simulated and measured velocity profiles along lines Y1 and X5. None of the models produced an accurate velocity profile, although the results are not too bad. It was surprising that the LES (SGS) and DES (SA) models did not perform better than the other models. The velocity distribution along line X5 was nearly constant because the distance between the measured positions and the

328 media surface was only 2 mm. The velocity was close to the filtration velocity, which was determined by
 329 the pressure drop across the filter media.

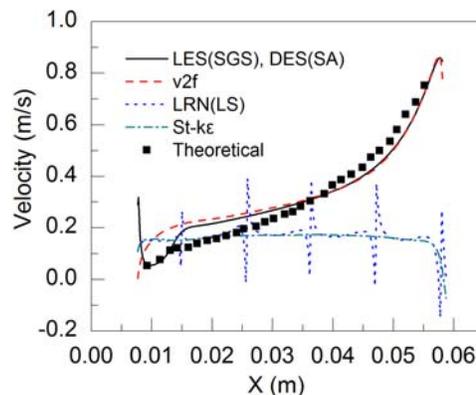


330

331 **Fig. 11** The simulated and measured velocity profiles along (a) line Y1 and (b) line X5.

332

333 [Rebai et al. \(2010\)](#) developed a theoretical method to calculate the filtration velocity along the filter
 334 surface and the pressure drop of the pleated filter. Figure 12 indicates that the velocity distributions
 335 predicted by the LES (SGS), DES (SA), and v2f models are in good agreement with that calculated by the
 336 theoretical model. As shown in Figure 9, the pressure drop across the filter is also predicted well by these
 337 models. In contrast, the St-kε model and LRN (LS) model gave unacceptable predictions. The filter in these
 338 cases had a relatively high pleat density and low permeability, resulting in a low pressure drop across the
 339 filter media but a high structural pressure drop in the air channel. The incorrectly predicted flow field
 340 would have a significant effect on the pressure drop, as depicted in Figure 9.



341

342 **Fig. 12** The filtration velocity distribution along the filter surface as determined by different models for Rebai's
 343 case.

344 Discussion

345 The LES (SGS), DES (SA), and v2f models provided acceptable pressure drop and velocity
 346 distributions for a pleated filter. However, the LES model required a very fine mesh and was
 347 computationally demanding. The computing time for the v2f model was the shortest among the validated
 348 models, but the initial flow field used for the computation was important for the convergence speed. The
 349 DES (SA) model was a stable model with acceptable computing costs. This investigation also tested LES
 350 with different subgrid scale models, including LES (WALE) and LES (Dke); DES with different RANS
 351 models, including DES (SST) and DES (R-kε); and five other LRN models. Different LES and DES

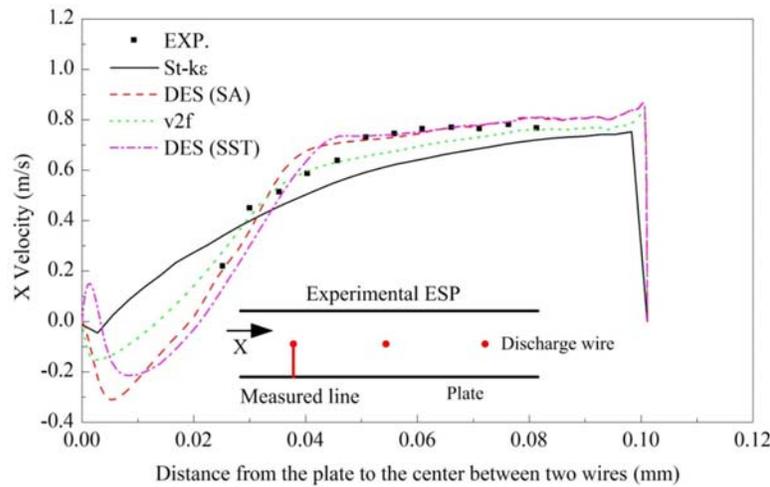
352 models successfully predicted the flow velocity profiles with similar accuracy, but the DES (R- $k\epsilon$) model
 353 failed. A unique characteristic of the R- $k\epsilon$ model is that it ensures that the normal Reynolds stresses are
 354 positive, which is suitable for flows with high Reynolds numbers, strong streamline curvatures, vortices,
 355 and rotations. This characteristic was not necessary for transitional flow in pleated filters. The performance
 356 of the other five LRN models was not as good as the LES and DES models because the two peak values
 357 were not well predicted, although the predictions may be acceptable in engineering applications.

358 In a pleated filter system that incorporates an ESP, the flow field is coupled with an electric field
 359 generated in the ESP, called the electro-hydrodynamic field (Yabe et al., 1978). The influence of the electric
 360 field on the flow field is taken into account by adding an electric force term to the source term when Eq. (1)
 361 represents the momentum equations (Long and Yao, 2010):

$$362 \quad S_\phi \text{ (new)} = S_\phi + F_{ci} \quad (5)$$

363 where F_{ci} is the electric body force (N/m^3).

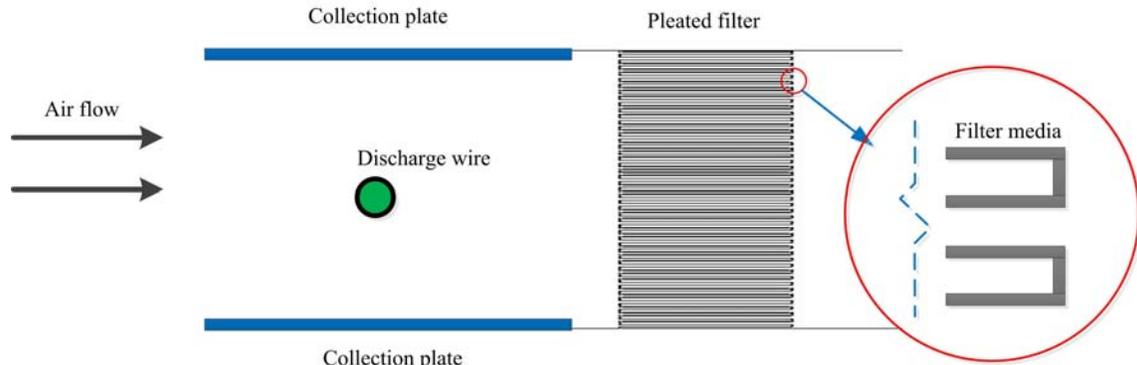
364 As LES is very time-consuming, this investigation used only the DES, v2f, and standard k- ϵ models to
 365 predict the electro-hydrodynamic flow. Figure 13 compares the velocity profiles predicted by these models
 366 with the experimental data (Kallio and Stock, 1992). The performance of the DES models was the best, and
 367 the v2f model was also very good. The standard k- ϵ model had poor performance, as it again failed to yield
 368 an acceptable profile.



369 **Fig. 13** Comparison of the velocity profiles as predicted by different turbulence models with the experimental
 370 data from Kallio and Stock (1992).
 371
 372

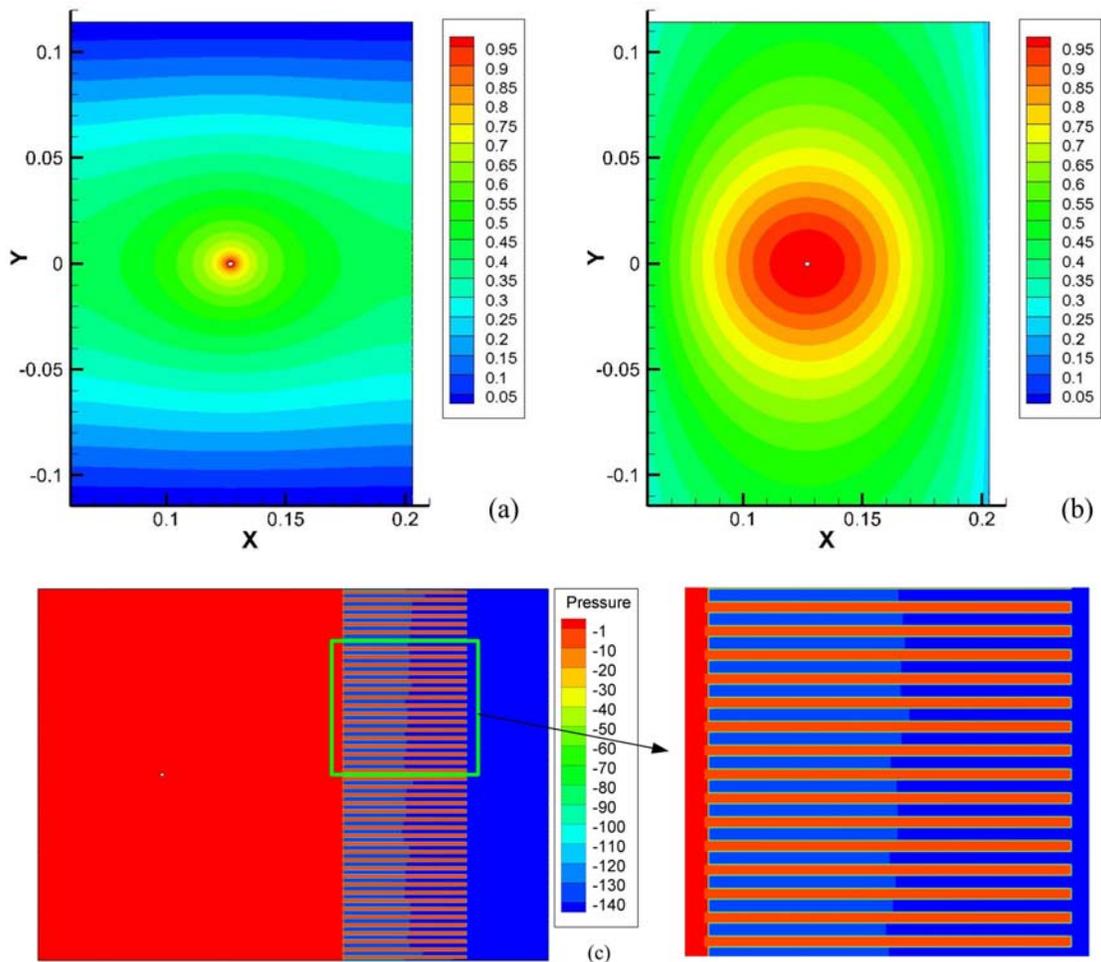
373 Figure 14 shows a hybrid system consisting of an electrostatic precipitator (ESP) and a pleated filter.
 374 The radius of the discharge wire is 1 mm and the length of the collection plate is 1524 mm, while the wire
 375 to plate distance is 1143 mm. The thickness of the pleated filter media is 0.3 mm and the media
 376 permeability is $1\text{E-}11 \text{ (m}^2\text{)}$. The pleat count density is 200 N/m . The inlet velocity is 0.8 m/s and average
 377 filtration velocity for pleated filter is 0.02 m/s. The finite volume method is used to solve the governing
 378 equations of the electric potential and the space density (Long et al. 2009). Based on the conclusions above,
 379 the flow field in this hybrid electrostatic filtration system is simulated by using the DES-SA turbulence
 380 model. The filter media is modeled as the porous media. Figures 15(a) and (b) show the normalized
 381 predictions of electric potential and space charge density. The simulated electric field is validated by the
 382 measured data in literature (Penney and Matick, 1960). Figure 15(c) shows the relative static pressure
 383 distribution in the hybrid system. The measured pressure drop of the pleated filter is 145 Pa. The DES

384 model prediction agrees well with this value. In the transverse direction, the pressure is evenly distributed.
 385 Based on these results, the particle deposition characteristics in this hybrid system can be studied, which is
 386 useful for the optimal design of the hybrid system.



387
 388

Fig. 14 The layout of the hybrid electrostatic filtration system.



389

390 **Fig. 15** The simulated results: (a) the normalized electric potential; (b) the space charge density; (c) the pressure
 391 distribution in the hybrid electrostatic filtration system.

392 **Conclusion**

393 This investigation evaluated the performances of several turbulence models for predicting the pressure

394 drop and flow field in pleated filter systems. The evaluation used experimental data for the pressure drop
395 through a pleated filter from the literature and the measured flow field in an experimental pleated filter. By
396 assessing the standard k- ϵ model, six low-Reynolds-number models, the v2f model, three LES models, and
397 three DES models, this investigation found that the v2f, LES, and DES (Spalart–Allmaras) model can
398 accurately predict the pressure drop and the flow field through a pleated filter. The other models failed in
399 predicting such a flow because of the high-Reynolds-number assumption used in the standard k- ϵ model or
400 the lack of a mechanism for solving the special flow characteristics in the filter. Among the useable models,
401 the LES requires the highest computation time. Besides, for the flow in the electrostatic precipitator, the
402 DES (Spalart–Allmaras) model has better performance than the v2f model. Finally, the DES
403 (Spalart–Allmaras) model is recommended for simulating the pressure drop and airflow through a pleated
404 filter both with and without an electrostatic precipitator.

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