

#### 4. Specific Speed, $N_s$

A useful dimensionless term results from the following combination of previously defined terms:

$$N_s \equiv \text{specific speed} = \frac{\Phi^{1/2}}{\Psi^{3/4}} = \frac{\omega Q^{1/2}}{(gH)^{3/4}} \quad (32)$$

Combining the terms in this manner eliminates the impeller diameter,  $D$ .

Notes:

- It is customary to characterize a machine by its specific speed at the design point, i.e.,  $N_s$  is usually only given for the BEP operating conditions.
  - low  $Q$ , high  $H \Rightarrow$  low  $N_s \Rightarrow$  centrifugal pumps
  - high  $Q$ , low  $H \Rightarrow$  high  $N_s \Rightarrow$  axial pumps

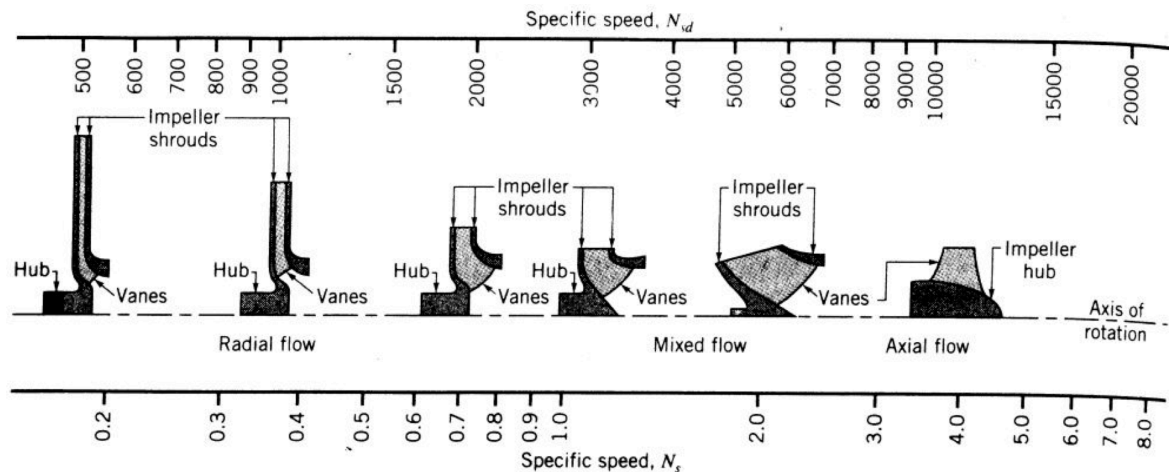
- In practice (especially in the US), a combination of units are used to describe  $\omega$ ,  $Q$ , and  $H$  such that  $N_s$  is dimensional (signified by  $N_{sd}$ ):

$$N_{sd} \equiv \frac{\omega(\text{rpm})\sqrt{Q(\text{gpm})}}{[H(\text{ft})]^{3/4}} \quad (33)$$

$N_s$  and  $N_{sd}$  have the same physical meaning but are different in magnitude by a constant factor:

$$N_{sd} = 2733 [\text{rpm} \cdot (\text{gpm})^{1/2} / (\text{ft})^{3/4}] N_s$$

- Given  $\omega$ ,  $Q$ , and  $H$ , we can calculate  $N_s$  (or  $N_{sd}$ ) and, using the following chart, determine which type of pump would be most efficient for the given conditions.



(From Munson, B.R., Young, D.F., and Okiishi, T.H., *Fundamentals of Fluid Mechanics*, 3<sup>rd</sup> ed., Wiley.)

Following are some rules of thumb:

- Positive displacement pumps are used for small flow rates,  $Q$ , and large head rises,  $H$ .
- Centrifugal pumps are for moderate  $H$  and large  $Q$ .
- For very large head rises, pumps are often combined in series (aka multi-stage).
- Axial flow pumps are for large  $Q$  and low  $H$ .