

Some cars come with a rear “spoiler” (actually an upside-down airfoil) mounted on the rear of the vehicle that is supposed to increase the down force on the car and improve traction. Calculate a typical down force caused by a rear wing used on a passenger vehicle.



SOLUTION:

The lift force is given by,

$$L = C_L \frac{1}{2} \rho V^2 A, \quad (1)$$

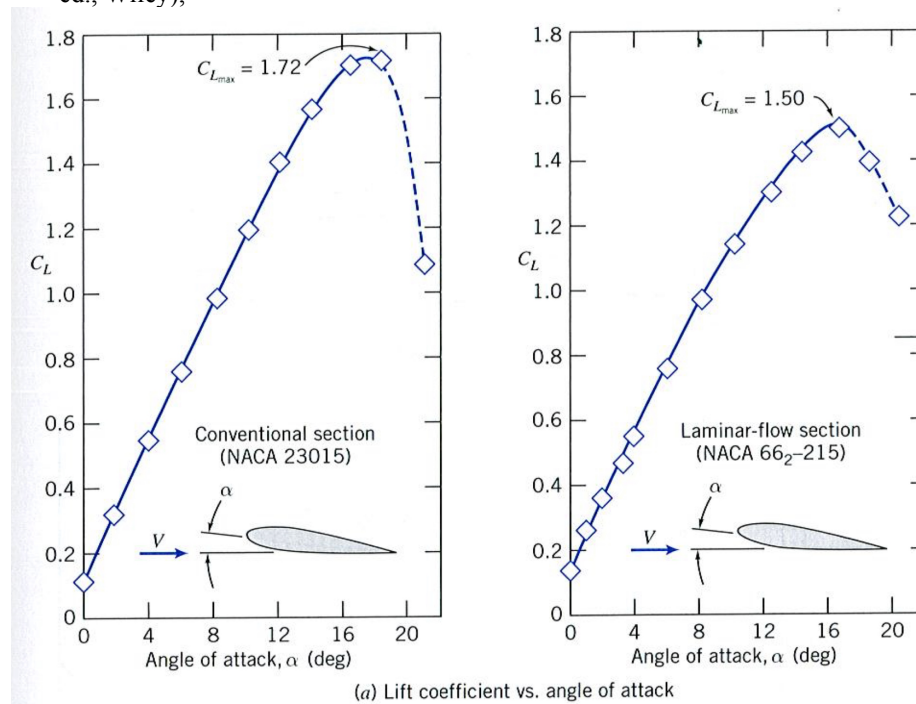
where,

$A = 2 \text{ ft}^2 (= 0.186 \text{ m}^2)$, assuming a span of 4 ft and a chord length of 0.5 ft (note that this is a planform area),

$\rho = 1.23 \text{ kg/m}^3$,

$V = 24.6 \text{ m/s} (= 55 \text{ mph})$,

$C_L = 1.4$, (a typical value based on Fig. 9.17 from Pritchard et al., *Introduction to Fluid Mechanics*, 8th ed., Wiley),



$$\Rightarrow \boxed{L = 96.9 \text{ N} (= 21.8 \text{ lbf})}$$

Thus, we see the spoiler produces very little down force on the vehicle.

To produce a down force of 200 lbf (= 890 N), the car would need to travel at a speed of 70.7 m/s (= 158 mph).

Note that rear spoilers are sometimes used to direct airflow downward to help reduce the size of the trailing wake and thus reduce drag.