

In the book/movie *The Martian*, the mission of a crew of astronauts is derailed by a massive Martian windstorm. If the Martian atmosphere has a density of  $0.016 \text{ kg/m}^3$  and the wind speed is  $26.8 \text{ m/s}$  ( $= 60 \text{ mph}$ ), what is the drag force acting on astronaut Mark Watney? Based on wind tunnel testing, assume that the drag coefficient multiplied by the frontal projected area of a typical person is  $C_{DA} = 0.84 \text{ m}^2$  (see, for example, Table 7.3 in White, F.M., *Fluid Mechanics*, 7<sup>th</sup> ed., McGraw-Hill).



What wind speed on Earth would produce an equivalent drag force?

SOLUTION:

The drag force is given by,

$$D = C_D \frac{1}{2} \rho_{\text{Mars}} V^2 A, \quad (1)$$

where,

$$C_D A = 0.84 \text{ m}^2 \text{ (given),}$$

$$\rho_{\text{Mars}} = 0.016 \text{ kg/m}^3,$$

$$V = 26.8 \text{ m/s,}$$

$$\Rightarrow \boxed{D = 4.8 \text{ N (= 1.1 lbf)}}$$

Thus, we see that the author took considerable artistic liberty in portraying the damage caused by a Martian windstorm.

To determine the wind speed on Earth that would cause the same drag force, set the drag forces for Mars and Earth equal,

$$C_D \frac{1}{2} \rho_{\text{Mars}} V_{\text{Mars}}^2 A = C_D \frac{1}{2} \rho_{\text{Earth}} V_{\text{Earth}}^2 A, \quad (2)$$

$$V_{\text{Earth}} = V_{\text{Mars}} \sqrt{\frac{\rho_{\text{Mars}}}{\rho_{\text{Earth}}}}. \quad (3)$$

Using  $\rho_{\text{Earth}} = 1.23 \text{ kg/m}^3$ ,  $\boxed{V_{\text{Earth}} = 3.1 \text{ m/s (= 6.8 mph)}}$ , which corresponds to a light breeze.