

ME 200 (Thermodynamics I) Lecture 27

More Discussion on Entropy Production

Recall the Entropy Equation,

$$\frac{dS}{dt} = \sum_{in} \dot{m}s - \sum_{out} \dot{m}s + \int_{b} \frac{\delta \dot{Q}_{into}}{T} + \dot{\sigma}$$

or, after integrating in time,

$$\Delta S = \sum_{in} ms - \sum_{out} ms + \int_{b} \frac{\delta Q_{into}}{T} + \sigma$$

The entropy production/generation (σ , $\dot{\sigma}$) is used to determine if the process is:

- internally reversible $(\sigma, \dot{\sigma} = 0)$
- internally irreversible $(\sigma, \dot{\sigma} > 0)$
- impossible $(\sigma, \dot{\sigma} < 0)$

When considering a collection of components in a system, e.g., a turbine, a compressor, a boiler, etc., the entropy production can be used to determine which component introduces the most irreversibility, i.e., which component should be the focus of design improvements. The larger the σ , the more the irreversibility.

When evaluating the heat transfer term,

$$\int\limits_{b} \frac{\delta Q_{into}}{T}$$

one must know the temperature value where the heat transfer is crossing the system boundary.

 $T_{
m surroundings}$

What if the temperature at the system boundary isn't known? In reality, "thermal boundary layers" exist adjacent to an object's surface where the temperature changes in a continuous manner to match the temperature of the surroundings.



system

Tsurroundings



$$\frac{dS}{dt} = \sum_{in} \dot{m}s - \sum_{out} \dot{m}s + \int_{b} \frac{\delta \dot{Q}_{into}}{T} + \dot{\sigma}$$

Example (SecondLaw_22) Air expands isothermally at steady state with no internal irreversibilities through a turbine from 10 bar (abs) and 500 K to 2 bar (abs). Determine the heat transfer per unit mass flow rate of air and work per unit mass flow rate of air.

Example (SecondLaw_23)

An isolated system of total mass m is formed by mixing two equal masses of the same liquid, assumed incompressible with the same specific heat c, initially at the absolute temperatures T_1 and T_2 . Eventually the system attains an equilibrium state.

- a. Determine the amount of entropy produced in terms of m, c, T_1 , and T_2 .
- b. Demonstrate that *s* must be positive.

