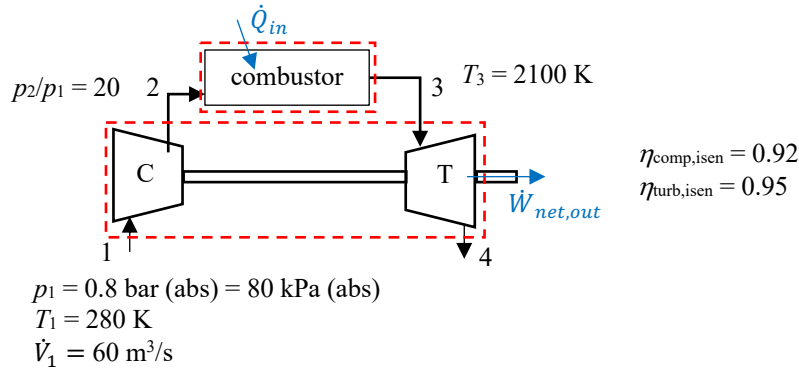


Air enters the compressor of an air-standard Brayton cycle with a volumetric flow rate of $60 \text{ m}^3/\text{s}$ at 0.8 bar (abs) and 280 K . The compressor pressure ratio is 20 and the maximum cycle temperature is 2100 K . The compressor and turbine isentropic efficiencies are 92% and 95% , respectively. Determine:

- a. the net power developed from the cycle,
- b. the rate of heat addition in the combustor, and
- c. the thermal efficiency of the cycle.

SOLUTION:



Apply the 1st Law to a control volume surrounding the compressor and turbine,

$$0 = \dot{m}(h_1 - h_2 + h_3 - h_4) - \dot{W}_{\text{out,net}}, \quad (1)$$

(assuming steady state, negligible KE and PE, and adiabatic conditions)

$$\dot{W}_{\text{out,net}} = \dot{m}(h_1 - h_2 + h_3 - h_4). \quad (2)$$

The mass flow rate can be found from the conditions at State 1 and using the ideal gas law,

$$\dot{m} = \rho_1 \dot{V}_1 = \left(\frac{p_1}{RT_1} \right) \dot{V}_1, \quad (3)$$

$$\Rightarrow \dot{m} = 59.731 \text{ kg/s}$$

Now determine the specific enthalpies at each of the states.

State 1:

$$T_1 = 280 \text{ K} \Rightarrow h_1 = 280.1 \text{ kJ/kg}, p_r(T_1) = 1.0889 \quad (\text{from the Ideal Gas Table})$$

State 3:

$$T_3 = 2100 \text{ K} \Rightarrow h_3 = 2377 \text{ kJ/kg}, p_r(T_3) = 2559 \quad (\text{from the IGT})$$

State 2:

$$\eta_{\text{comp,isen}} = \frac{h_{2s} - h_1}{h_2 - h_1} \Rightarrow h_2 = h_1 + \frac{h_{2s} - h_1}{\eta_{\text{comp,isen}}}. \quad (4)$$

State 2s: $p_2/p_1 = p_{2s}/p_1 = 20$,

$$\frac{p_{2s}}{p_1} = \frac{p_r(T_{2s})}{p_r(T_1)} \Rightarrow p_r(T_{2s}) = p_r(T_1) \left(\frac{p_{2s}}{p_1} \right) \quad (\text{isentropic compression of an ideal gas}), \quad (5)$$

$$\Rightarrow p_r(T_{2s}) = 21.778 \Rightarrow T_{2s} = 649.33 \text{ K}, h_{2s} = 659.29 \text{ kJ/kg} \quad (\text{from IGT})$$

Using Eq. (4) and the given and computed values,

$$h_2 = 692.26 \text{ kJ/kg}.$$

State 4:

$$\eta_{turb,isen} = \frac{h_4 - h_3}{h_{4s} - h_3} \Rightarrow h_4 = h_3 + \eta_{turb,isen}(h_{4s} - h_3). \quad (6)$$

State 4s: $p_3/p_4 = p_3/p_{4s} = p_2/p_1 = 20$,

$$\frac{p_3}{p_{4s}} = \frac{p_r(T_3)}{p_r(T_{4s})} \Rightarrow p_r(T_{4s}) = p_r(T_3) \left(\frac{p_{4s}}{p_3} \right) \quad (\text{isentropic expansion of an ideal gas}), \quad (7)$$

$$\Rightarrow p_r(T_{4s}) = 127.95 \Rightarrow T_{4s} = 1029.19 \text{ K}, h_{4s} = 1079.57 \text{ kJ/kg} \quad (\text{from IGT})$$

Using Eq. (6) and the given and computed values,
 $h_4 = 1144.44 \text{ kJ/kg}$.

Using the state data, mass flow rate, and Eq. (2),

$$\dot{W}_{out,net} = 49.0 \text{ MJ}.$$

The rate of heat addition into the combustor is found by applying the 1st Law to a control volume surrounding the combustor,

$$0 = \dot{m}(h_2 - h_3) + \dot{Q}_{in}, \quad (8)$$

(assuming steady state, negligible KE and PE, and a passive device)

$$\dot{Q}_{in} = \dot{m}(h_3 - h_2). \quad (9)$$

Using the previously calculated quantities,

$$\dot{Q}_{in} = 101 \text{ MW}.$$

The cycle's thermal efficiency is,

$$\eta = \frac{\dot{W}_{out,net}}{\dot{Q}_{in}},$$

$$\Rightarrow \eta = 0.487 = 48.7\%.$$

