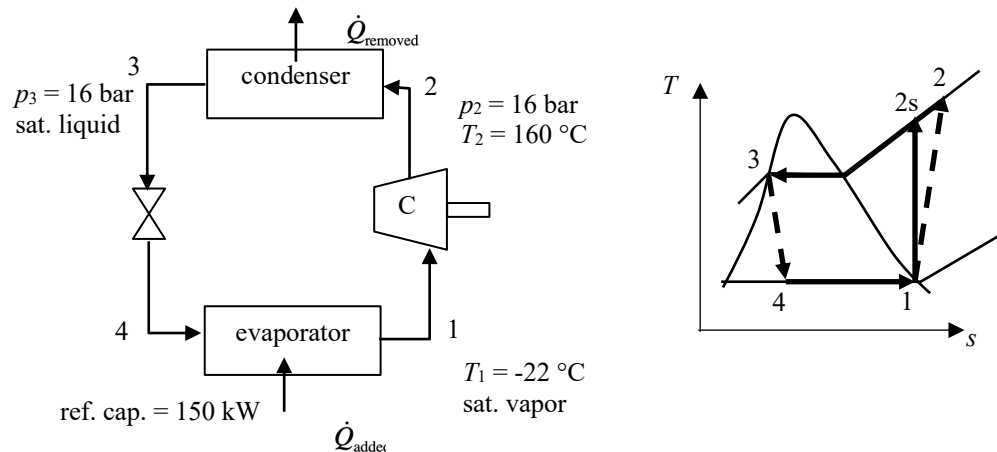


In a vapor-compression refrigeration cycle, ammonia exits the evaporator as saturated vapor at  $-22\text{ }^{\circ}\text{C}$ . The refrigerant enters the condenser at 16 bar (abs) and  $160\text{ }^{\circ}\text{C}$ , and saturated liquid exits at 16 bar (abs). There is no significant heat transfer between the compressor and its surroundings, and the refrigerant passes through the evaporator with a negligible change in pressure. If the refrigerating capacity is 150 kW, determine:

- a. the mass flow rate of refrigerant,
- b. the power input to the compressor,
- c. the coefficient of performance, and
- d. the isentropic compressor efficiency.

SOLUTION:



First determine the properties at the various states using Tables from Moran et al., 7<sup>th</sup> ed.

State 1:  $T_1 = -22\text{ °C}$ , saturated vapor (Table A-13)  
 $\Rightarrow p_1 = 1.7390\text{ bar}$ ,  $h_1 = 1415.08\text{ kJ/kg}$ ,  $s_1 = 5.6457\text{ kJ/(kg.K)}$

State 2:  $p_2 = 16\text{ bar}$ ,  $T_2 = 160\text{ °C}$   $\Rightarrow$  superheated vapor (Table A-15)  
 $\Rightarrow h_2 = 1798.45\text{ kJ/kg}$ ,  $s_2 = 5.7475\text{ kJ/(kg.K)}$

State 3:  $p_3 = 16\text{ bar}$ , saturated liquid (Table A-14)  
 $\Rightarrow T_3 = 41.03\text{ °C}$ ,  $h_3 = 376.46\text{ kJ/kg}$ ,  $s_3 = 1.3729\text{ kJ/(kg.K)}$

State 4: throttling process from 3 to 4, constant pressure from 4 to 1  
 $\Rightarrow h_4 = h_3 = 376.46\text{ kJ/kg}$ ,  $p_4 = p_1 = 1.7390\text{ bar}$

The mass flow rate may be determined by applying the 1<sup>st</sup> Law to the evaporator and making use of the refrigeration capacity ( $= \dot{Q}_{\text{added}} = 150\text{ kW}$ ),

$$\dot{Q}_{\text{added}} = \dot{m}(h_1 - h_4) \Rightarrow \dot{m} = \frac{\dot{Q}_{\text{added}}}{(h_1 - h_4)}, \quad (1)$$

$$\Rightarrow \boxed{\dot{m} = 0.144\text{ kg/s.}}$$

The power input into the compressor is found by applying the 1<sup>st</sup> Law to the compressor,

$$\dot{W}_{\text{on comp}} = \dot{m}(h_2 - h_1), \quad (2)$$

$$\Rightarrow \boxed{\dot{W}_{\text{on comp}} = 55.4\text{ kW.}}$$

The coefficient of performance for the refrigeration cycle is defined as,

$$\text{COP}_{\text{ref}} \equiv \frac{\dot{Q}_{\text{added}}}{\dot{W}_{\text{on}}}, \quad (3)$$

$$\Rightarrow \boxed{\text{COP}_{\text{ref}} = 2.71.}$$

The isentropic efficiency of the compressor is defined as,

$$\eta_{\text{comp}} \equiv \frac{\dot{W}_{\text{on comp},s}}{\dot{W}_{\text{on comp}}} = \frac{\dot{W}_{\text{on comp},s}/\dot{m}}{\dot{W}_{\text{on comp}}/\dot{m}} = \frac{h_{2s} - h_1}{h_2 - h_1}, \quad (4)$$

where

$p_{2s} = p_2 = 16$  bar and  $s_{2s} = s_1 = 5.6457$  kJ/(kg.K)  $\Rightarrow h_{2s} = 1755.38$  kJ/kg,  $T_{2s} = 143$  °C (interpolating from Table A-15),  
 $\Rightarrow \boxed{\eta_{\text{comp}} = 0.888}$ .