Five kg of water is contained in a piston-cylinder assembly, initially at $5 \mathrm{bar}(\mathrm{abs})$ and $240^{\circ} \mathrm{C}$. The water is slowly heated at constant pressure to a final state. If the heat transfer into the water for the process is 2960 kJ , determine the temperature at the final state, in ${ }^{\circ} \mathrm{C}$, and the work done by the water on the piston, in kJ . Kinetic and potential energy effects are negligible.

## SOLUTION:

Apply the First Law to the water in the piston,

$$
\begin{equation*}
\Delta E_{\mathrm{H} 2 \mathrm{O}}=\underset{\substack{\text { into } \\ \mathrm{H} 2 \mathrm{O}}}{Q_{\mathrm{in}}}-\underset{\substack{\mathrm{by} 20}}{W_{\mathrm{H}}}, \tag{1}
\end{equation*}
$$

where


$$
\begin{equation*}
\Delta E_{\mathrm{H} 2 \mathrm{O}}=\Delta U_{\mathrm{H} 2 \mathrm{O}}=m\left(u_{2}-u_{1}\right) . \tag{2}
\end{equation*}
$$

The specific internal energy at the initial state (state 1) may be found from the thermodynamic tables for water at $p_{1}$ $=5 \operatorname{bar}(\mathrm{abs})$ and $T_{1}=240^{\circ} \mathrm{C}$. Note that saturation temperature for liquid water at 5 bar (abs) is $151.83^{\circ} \mathrm{C}$; hence, the water must be in the superheated vapor region since $T_{1}$ is greater than the saturation temperature. Using the SHV table,

$$
\begin{aligned}
u_{1} & =2707.9 \mathrm{~kJ} / \mathrm{kg}, \\
v_{1} & =0.46467 \mathrm{~m}^{3} / \mathrm{kg}, \\
h_{1} & =2940.2 \mathrm{~kJ} / \mathrm{kg} .
\end{aligned}
$$

The work done by the water on the piston is,

$$
\begin{equation*}
W_{\text {by н2O }}=\int_{V_{1}}^{V_{2}} p d V=p\left(V_{2}-V_{1}\right)=p m\left(v_{2}-v_{1}\right), \tag{3}
\end{equation*}
$$

where the pressure is constant $\left(p_{1}=p_{2}=5 \mathrm{bar}(\mathrm{abs})\right)$ throughout the process. Substituting into Eq. (1),

$$
\begin{align*}
& m\left(u_{2}-u_{1}\right)=Q_{\substack{\text { into } \\
\mathrm{H} 2 \mathrm{O}}}-p m\left(v_{2}-v_{1}\right)  \tag{4}\\
& m\left(u_{2}+p_{2} v_{2}-u_{1}-p_{1} v_{1}\right)=Q_{\substack{\text { intoo } \\
\mathrm{H} 2 \mathrm{O}}}  \tag{5}\\
& m\left(h_{2}-h_{1}\right)=Q_{\substack{\text { into } \\
\mathrm{H} 2 \mathrm{O}}}  \tag{6}\\
& h_{2}=h_{1}+\frac{Q_{\mathrm{into}}^{\mathrm{H} 2 \mathrm{O}}}{m} \tag{7}
\end{align*}
$$

where $h$ is the specific enthalpy of the water. Substituting values,

$$
\begin{aligned}
& h_{1}=2940.2 \mathrm{~kJ} / \mathrm{kg} \\
& Q_{\text {into }}=2960 \mathrm{~kJ} \\
& m=5 \mathrm{~kg} \\
& \Rightarrow h_{2}=3532.2 \mathrm{~kJ} / \mathrm{kg}
\end{aligned}
$$

From the thermodynamic two-phase liquid-vapor table for water at $p_{2}=5 \mathrm{bar}$ (abs), the saturated vapor specific enthalpy is $2748.1 \mathrm{~kJ} / \mathrm{kg}$, which is smaller than $h_{2}$. Hence, the water at state 2 will be in the superheated vapor state. Using the thermodynamic superheated vapor table with $h_{2}$ and $p_{2}$, and interpolating,

$$
\begin{aligned}
& T_{2}=522^{\circ} \mathrm{C} \\
& v_{2}=0.7313 \mathrm{~m}^{3} / \mathrm{kg}
\end{aligned}
$$

Using Eq. (3) and the values for $v_{1}, v_{2}, m$, and $p$,
$W_{\text {by } \mathrm{H} 2 \mathrm{O}}=667 \mathrm{~kJ}$
Sketches of the process on $T-v$ and $p-v$ plots are shown.



SLVM Table for H2O

|  |  | Liquid |  |  |  | Vapor |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Press. <br> (bar) | Temp. <br> (C) | $\begin{gathered} \text { Volume }\left(\mathbf{v}_{\mathrm{t}},\right. \\ \left.\mathrm{m}^{3} / \mathrm{kg}\right) \\ \hline \end{gathered}$ | Internal Energy ( $\mathrm{u}_{\mathrm{i}} \mathrm{kj} / \mathrm{kg}$ ) | Enthalpy $\left(h_{\mathrm{f}}, \mathrm{k} / \mathrm{kg}\right)$ | $\begin{array}{\|c} \text { Entropy }\left(s_{i t}\right. \\ \mathrm{kJ} / \mathrm{kg} / \mathrm{k}) \end{array}$ | $\begin{gathered} \text { Volume }\left(\mathrm{v}_{\mathrm{g}}\right. \\ \left.\mathrm{m}^{3} / \mathrm{kg}\right) \\ \hline \end{gathered}$ | $\begin{gathered} \text { Internal Energy } \\ \left(u_{g}, \mathrm{k} / \mathrm{kg}\right) \\ \hline \end{gathered}$ | Enthalpy $\left(\mathbf{h}_{\mathbf{g}}, \mathrm{kJ} / \mathrm{kg}\right)$ | $\begin{gathered} \text { Entropy } \\ \left(s_{g}, \mathrm{k} / \mathrm{kg} / \mathrm{K}\right) \end{gathered}$ |
| 5 | 151.83 | 0.0010925 | 639.54 | 640.09 | 1.8604 | 0.37481 | 2560.7 | 2748.1 | 6.8207 |

SHV Table for H2O

| Temp. (C) | Volume $\left(\mathrm{m}^{3} / \mathrm{kg}\right)$ | Internal <br> Energy <br> (kJ/kg) | Enthalpy <br> (kJ/kg) | Entropy <br> (kJ/kg/K) |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{p}=5.0 \mathrm{bar}=0.50 \mathrm{MPa}, \mathrm{T}_{\text {sat }}=151.83^{\circ} \mathrm{C}$ |  |  |  |
| Sat. | 0.37481 | 2560.7 | 2748.1 | 6.8207 |
| 180 | 0.40466 | 2610.1 | 2812.4 | 6.9673 |
| 200 | 0.42503 | 2643.3 | 2855.8 | 7.0610 |
| 240 | 0.46467 | 2707.9 | 2940.2 | 7.2322 |
| 280 | 0.50344 | 2771.5 | 3023.2 | 7.3880 |
| 320 | 0.54169 | 2835.1 | 3105.9 | 7.5323 |
| 360 | 0.57961 | 2899.1 | 3188.9 | 7.6677 |
| 400 | 0.61730 | 2963.7 | 3272.3 | 7.7955 |
| 440 | 0.65484 | 3029.1 | 3356.6 | 7.9170 |
| 500 | 0.71094 | 3129.0 | 3484.5 | 8.0892 |
| 600 | 0.80409 | 3300.4 | 3702.5 | 8.3543 |
| 700 | 0.89696 | 3478.5 | 3927.0 | 8.5977 |

