

$$3-2 \quad \bar{V}_{abs} = P \bar{\lambda}_{abs}$$

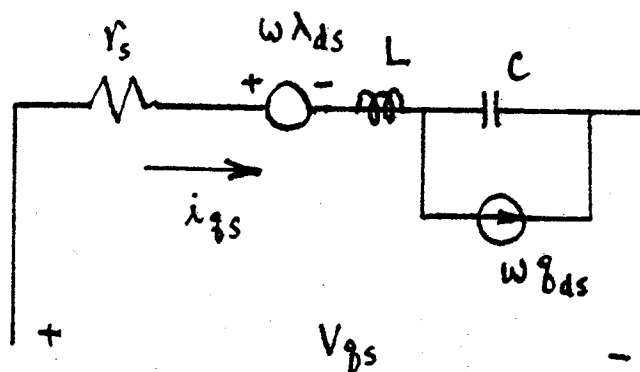
$$\text{where } \bar{V}_{abs} = [v_{as} \ v_{bs}]^T, \quad \bar{\lambda}_{abs} = [\lambda_{as} \ \lambda_{bs}]^T$$

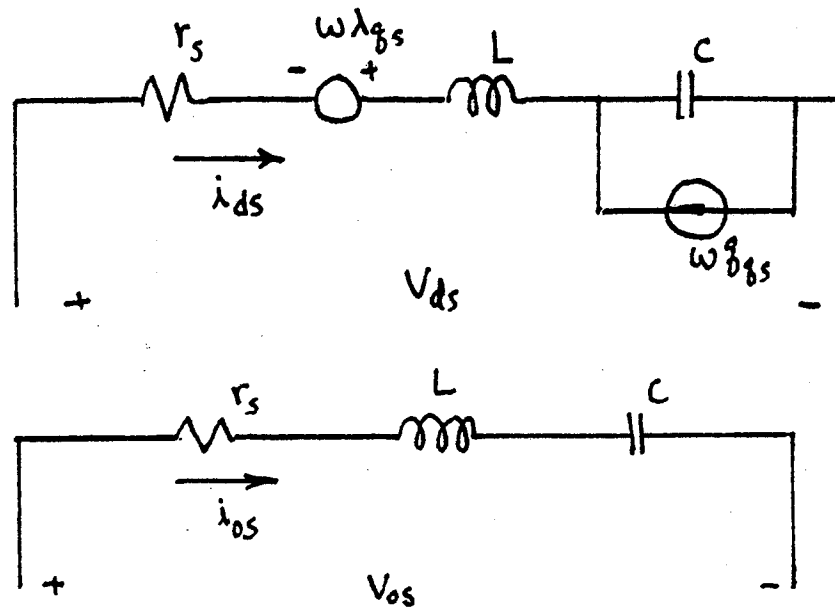
$$\begin{aligned} \bar{V}_{gds} &= \bar{K}_{2s} \bar{V}_{abs} = \bar{K}_{2s} P \bar{\lambda}_{abs} = \bar{K}_{2s} P [(\bar{K}_{2s})^{-1} \bar{\lambda}_{gds}] \\ &= \bar{K}_{2s} (\bar{K}_{2s})^{-1} P \bar{\lambda}_{gds} + \bar{K}_{2s} [P (\bar{K}_{2s})^{-1}] \bar{\lambda}_{gds} \\ &= P \bar{\lambda}_{gds} + \bar{K}_{2s} \begin{bmatrix} -\sin \theta & \cos \theta \\ \cos \theta & \sin \theta \end{bmatrix} \frac{d\theta}{dt} \bar{\lambda}_{gds} \\ &= \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \omega \bar{\lambda}_{gds} + P \bar{\lambda}_{gds} \end{aligned}$$

$$\text{That is } v_{gs} = \omega \lambda_{ds} + p \lambda_{gs}, \quad v_{ds} = -\omega \lambda_{gs} + p \lambda_{ds}$$

3-4. According to equations (3.4-2), (3.4-3), (3.4-9), (3.4-16)

(3.4-22) and (3.4-28), the equivalent circuit can be drawn as follows.





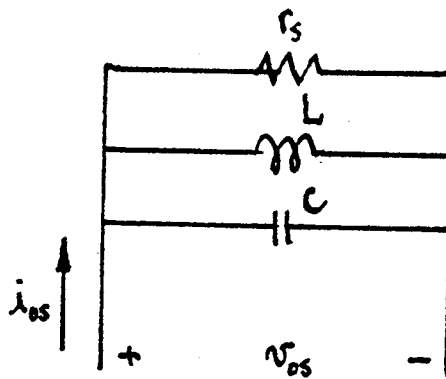
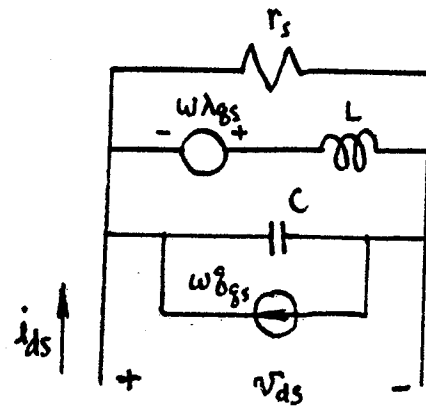
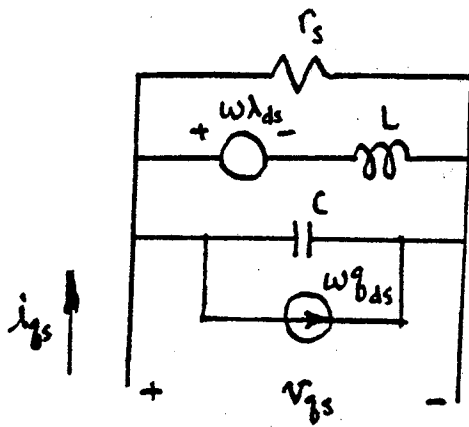
The current sources  $\omega \delta_{gs}$  and  $\omega \delta_{ds}$  can be replaced by equivalent voltage sources. Then the voltage equations in arbitrary reference frame are easily obtained.

$$V_{gs} = (r_s + pL + \frac{1}{Cp}) i_{gs} + \omega \lambda_{ds} - \frac{\omega}{Cp} \delta_{ds}$$

$$V_{ds} = (r_s + pL + \frac{1}{Cp}) i_{ds} - \omega \lambda_{gs} + \frac{\omega}{Cp} \delta_{gs}$$

$$V_{os} = (r_s + pL + \frac{1}{Cp}) i_{os}$$

3-5 The equivalent circuit .



$$i_{gs} = \left( \frac{1}{r_s} + \frac{1}{pL} + pC \right) v_{gs} + \omega g_{ds} - \frac{\omega}{pL} \lambda_{ds}$$

$$i_{ds} = \left( \frac{1}{r_s} + \frac{1}{pL} + pC \right) v_{ds} - \omega g_{gs} + \frac{\omega}{pL} \lambda_{gs}$$

$$i_{os} = \left( \frac{1}{r_s} + \frac{1}{pL} + pC \right) v_{os}$$

3-9

See formulas (5.2-8), (5.2-11), (5.2-12) and (5.5-5) of Chapter 5.

3-10.

$$\begin{aligned}
 {}^B_K{}^A &= \begin{bmatrix} \cos(\theta_A - \theta_B) & -\sin(\theta_A - \theta_B) & 0 \\ \sin(\theta_A - \theta_B) & \cos(\theta_A - \theta_B) & 0 \\ 0 & 0 & 1 \end{bmatrix} \\
 &= \begin{bmatrix} \cos(\theta_B - \theta_A) & \sin(\theta_B - \theta_A) & 0 \\ -\sin(\theta_B - \theta_A) & \cos(\theta_B - \theta_A) & 0 \\ 0 & 0 & 1 \end{bmatrix} \\
 &= \begin{bmatrix} \cos(\theta_B - \theta_A) & -\sin(\theta_B - \theta_A) & 0 \\ \sin(\theta_B - \theta_A) & \cos(\theta_B - \theta_A) & 0 \\ 0 & 0 & 1 \end{bmatrix}^{-1} = ({}^{A-B}_K)^{-1}
 \end{aligned}$$

3-14

$$\begin{aligned}
& \frac{3}{2} (V_{gs} I_{gs} + V_{ds} I_{ds}) \\
&= 3V_s I_s \cos [(\omega_e - \omega)t + \theta_{ev}(0) - \theta(0)] \cos [(\omega_e - \omega)t + \theta_{ei}(0) - \theta(0)] \\
&\quad + 3V_s I_s \sin [(\omega_e - \omega)t + \theta_{ev}(0) - \theta(0)] \sin [(\omega_e - \omega)t + \theta_{ei}(0) - \theta(0)] \\
&= 3V_s I_s \cos [\theta_{ev}(0) - \theta_{ei}(0)] = P_e
\end{aligned}$$

$$\begin{aligned}
& \frac{3}{2} (\overset{+}{V_{gs} I_{ds}} + \overset{-}{V_{ds} I_{gs}}) \\
&= \overset{+}{3V_s I_s} \cos [(\omega_e - \omega)t + \theta_{ev}(0) - \theta(0)] \sin [(\omega_e - \omega)t + \theta_{ei}(0) - \theta(0)] \\
&\quad + \overset{-}{3V_s I_s} \sin [(\omega_e - \omega)t + \theta_{ev}(0) - \theta(0)] \cos [(\omega_e - \omega)t + \theta_{ei}(0) - \theta(0)] \\
&= 3V_s I_s \sin [\theta_{ev}(0) - \theta_{ei}(0)] = Q_e
\end{aligned}$$