

# **AVM of Inverter Module**

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- **Features**
  - Include conduction losses
  - Ignore switching losses
  - Based on sine-triangle with 3<sup>rd</sup> harmonic modulation

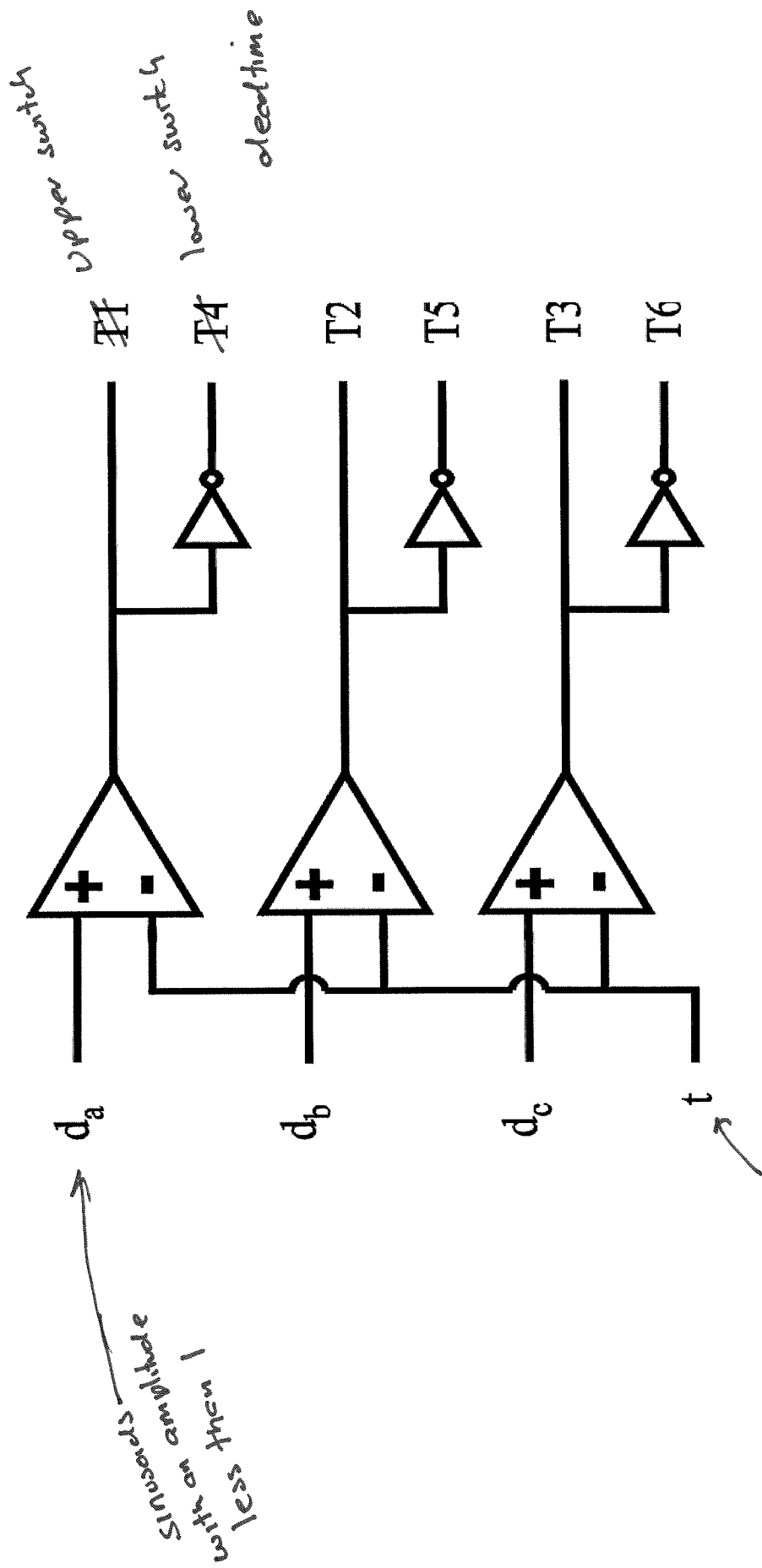
# Sine-Triangle Modulation

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- Features
  - Adjustable voltage magnitude
  - Adjustable frequency
  - Low low-frequency harmonic content
- Comments
  - Originally meant for analog implementation
  - Digital equivalents exist

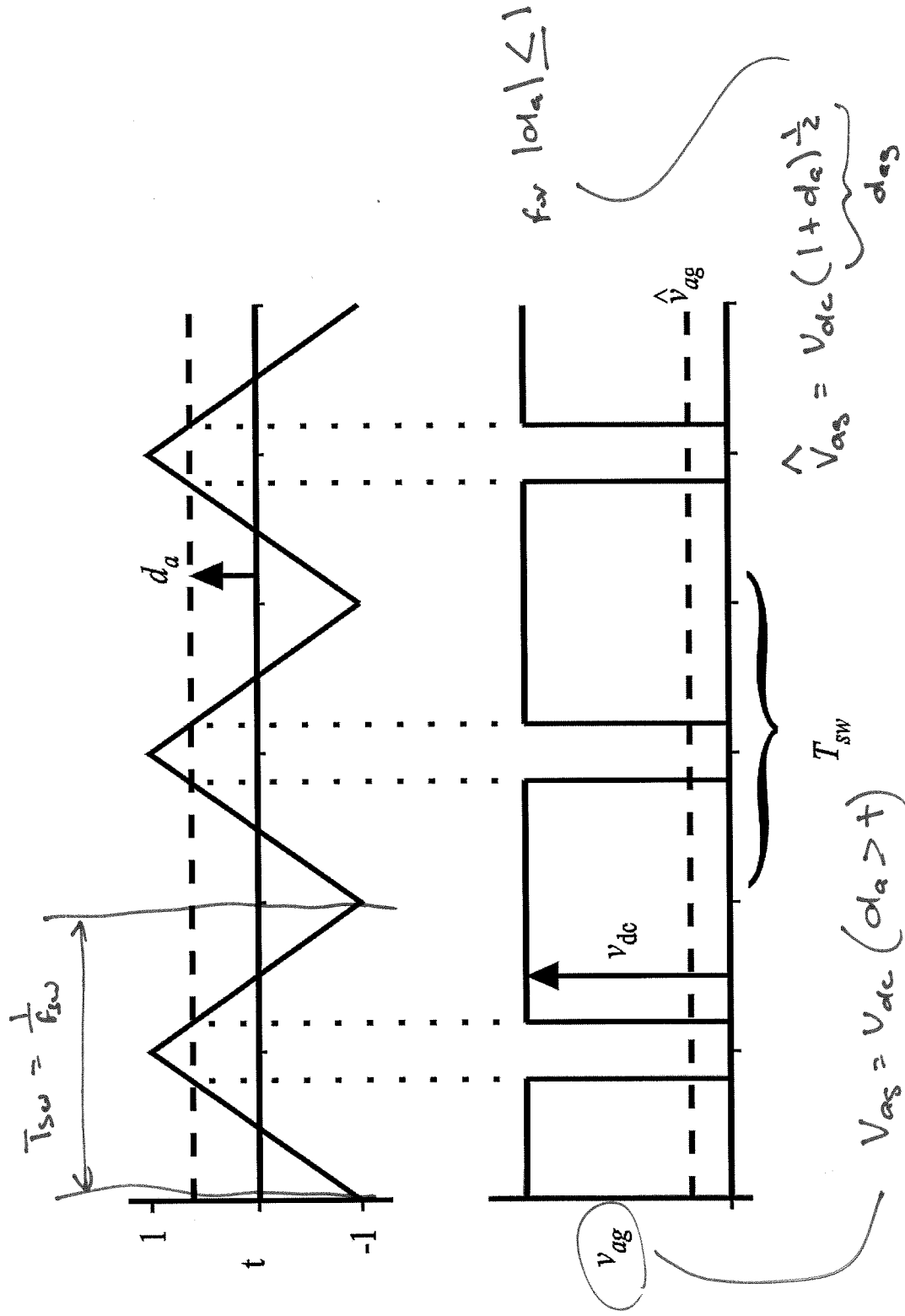
# Gate Signal Controls

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triangle wave

# Operation of A-Phase Leg



# Analysis

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- Recall the fast average

$$- \quad \hat{x}(t) = \frac{1}{T_{\text{SW}}} \int_{t-T_{\text{SW}}}^t x(t) dt \quad (13.5-1)$$

- We can show that

$$- \quad \hat{v}_{ag} = \frac{1}{2}(1+d_a)v_{dc} \quad (13.5-2)$$

$$- \quad \hat{v}_{bg} = \frac{1}{2}(1+d_b)v_{dc} \quad (13.5-3)$$

$$- \quad \hat{v}_{cg} = \frac{1}{2}(1+d_c)v_{dc} \quad (13.5-4)$$

## Analysis (2)

- Lets specify duty cycles as

$$- \quad d_a = d \cos \theta_c \quad (13.5-5)$$

$$- \quad d_b = d \cos\left(\theta_c - \frac{2\pi}{3}\right) \quad (13.5-6)$$

$$- \quad d_c = d \cos\left(\theta_c + \frac{2\pi}{3}\right) \quad (13.5-7)$$

→ converter angle

if the  $\Theta = \Theta_c$  reference frame, all the converter voltage is in the  $\beta$ -axis

$$V_{\beta}^{ca} = \underline{\quad}$$

$$V_d^{ca} = 0$$

# Analysis (3)

• Thus

$$- \hat{v}_{qi}^c = \frac{1}{2} dv_{dc} \quad (13.5-14)$$

$$- \hat{v}_{di}^c = 0 \quad (13.5-15)$$

$$\hat{V}_{gdi}^c = \frac{2}{3} \begin{bmatrix} C & C^- & C^+ \\ S & S^- & S^+ \end{bmatrix} \begin{bmatrix} \hat{V}_{as} \\ \hat{V}_{bs} \\ \hat{V}_{cs} \end{bmatrix}$$

$$= \frac{2}{3} \begin{bmatrix} C & C^- & C^+ \\ S & S^- & S^+ \end{bmatrix} \begin{bmatrix} V_{dc} \frac{1}{2} (1 + dc) \\ V_{dc} \frac{1}{2} (1 + dc) \\ V_{dc} \frac{1}{2} (1 + dc) \end{bmatrix}$$

$$= \begin{bmatrix} \frac{2}{3} V_{dc} \\ \phi \end{bmatrix}$$

Not including switch drops

## **AVM: Conduction Loss**

- Develop an Average Value Model for the DC/AC Converter
- Features
  - Include conduction losses
  - Ignore switching losses
  - Based on sine-triangle with 3<sup>rd</sup> harmonic modulation



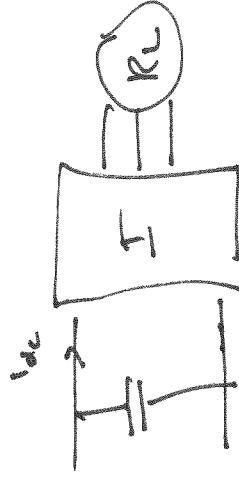
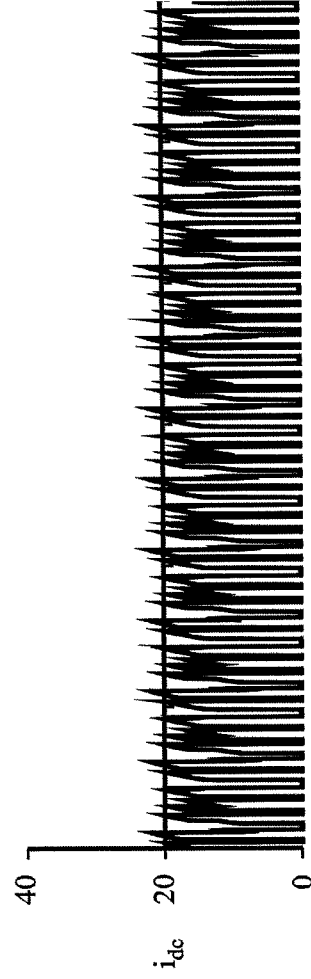
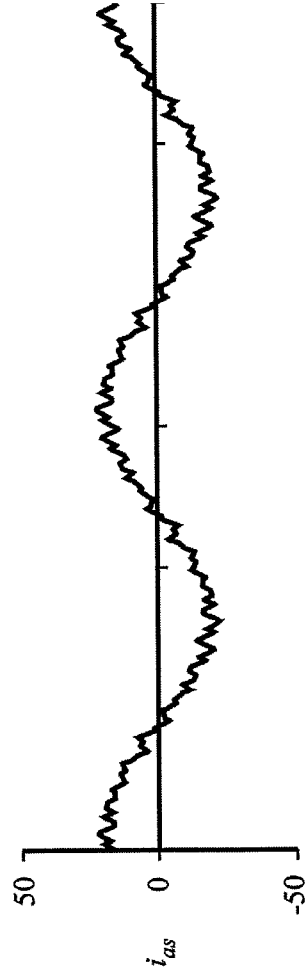
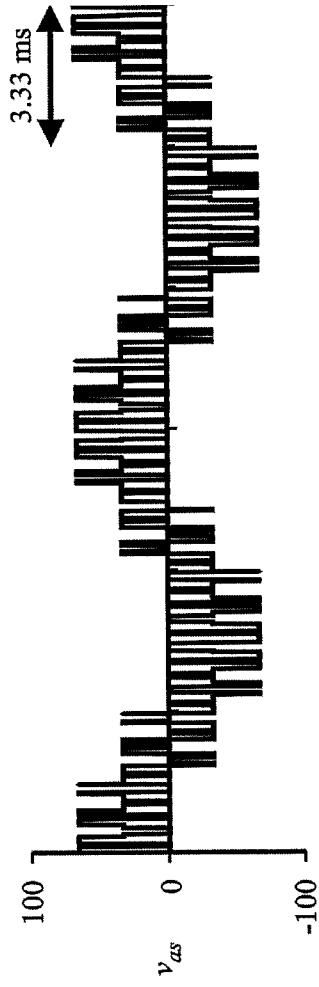
## An Example

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- Load: Balanced, wye-connected, series RL
  - $R = 2 \Omega$
  - $L = 1 \text{ mH}$
- DC Voltage: 100 V
- Fundamental Frequency: 100 Hz
- Duty Cycle:  $0.4 = \alpha$
- Switching Frequency: 3000 Hz

# Sine-Triangle Modulation

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# Limitations of Sine-Triangle Modulation

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- Sine Triangle Modulation

– Range for duty cycle:  $0 \leq \alpha \leq 1$

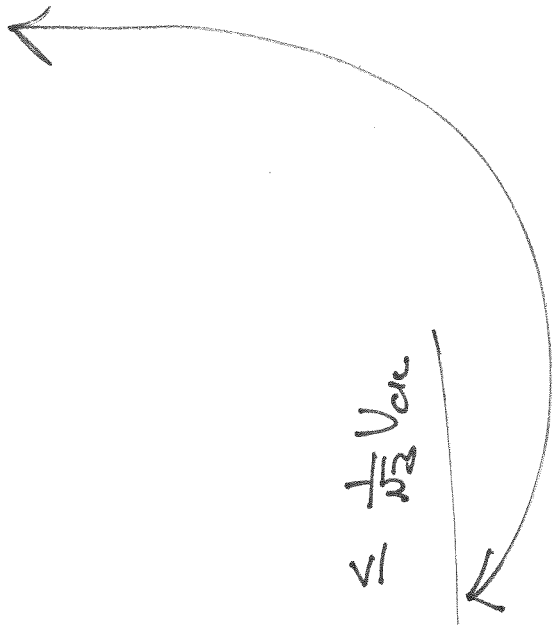
– Range for peak voltage (of fund):  ~~$0 \leq V_{pk} \leq V_{dc}$~~   $[0 \leq V_{pk} \leq \frac{1}{2} V_{dc}]$

peak value of fund.

$$V_s \leq \frac{1}{\sqrt{6}} V_{dc}$$

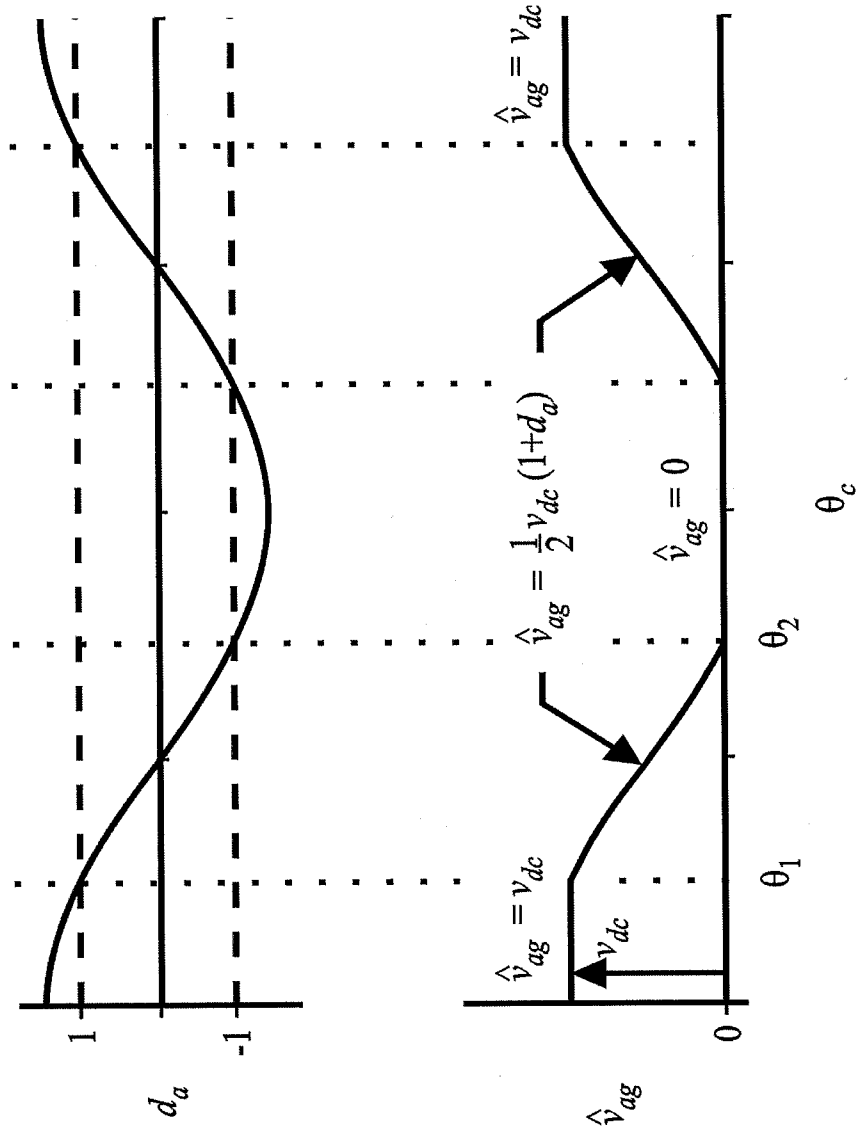
$$\sqrt{2} V_s \leq \frac{1}{\sqrt{2}} V_{dc}$$

peak value of fund  $\leq \frac{1}{\sqrt{2}} V_{dc}$



# Overmodulation

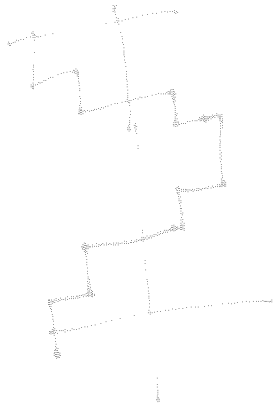
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# Analysis of Overmodulation

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- Line-to-ground voltage



$$\bar{v}_{ag} = \begin{cases} v_{dc} & d_a > 1 \\ \frac{1}{2}(1+d_a)v_{dc} & -1 < d_a < 1 \\ 0 & d_a < -1 \end{cases} \quad (13.5-16)$$

$$|v_{ag}|_{avg+fund} = \frac{v_{dc}}{2} + \frac{2v_{dc}}{\pi} f(d) \cos \theta_c \quad (13.5-17)$$

$$f(d) = \frac{1}{2} \sqrt{1 - \left(\frac{1}{d}\right)^2} + \frac{1}{4} d \left( \pi - 2 \arccos \left( \frac{1}{d} \right) \right) \quad (13.5-18)$$

$f(1) = \frac{\pi}{4}$  if  $d \rightarrow \infty$   
 $f(\infty) = 1$   $V_{D1} = \frac{2}{\pi} V_{dc}$

## Analysis of Overmodulation (2)

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- Thus we have

$$- \quad \bar{v}_{qs}^c = \frac{2v_{dc}}{\pi} f(d) \quad d \geq 1$$

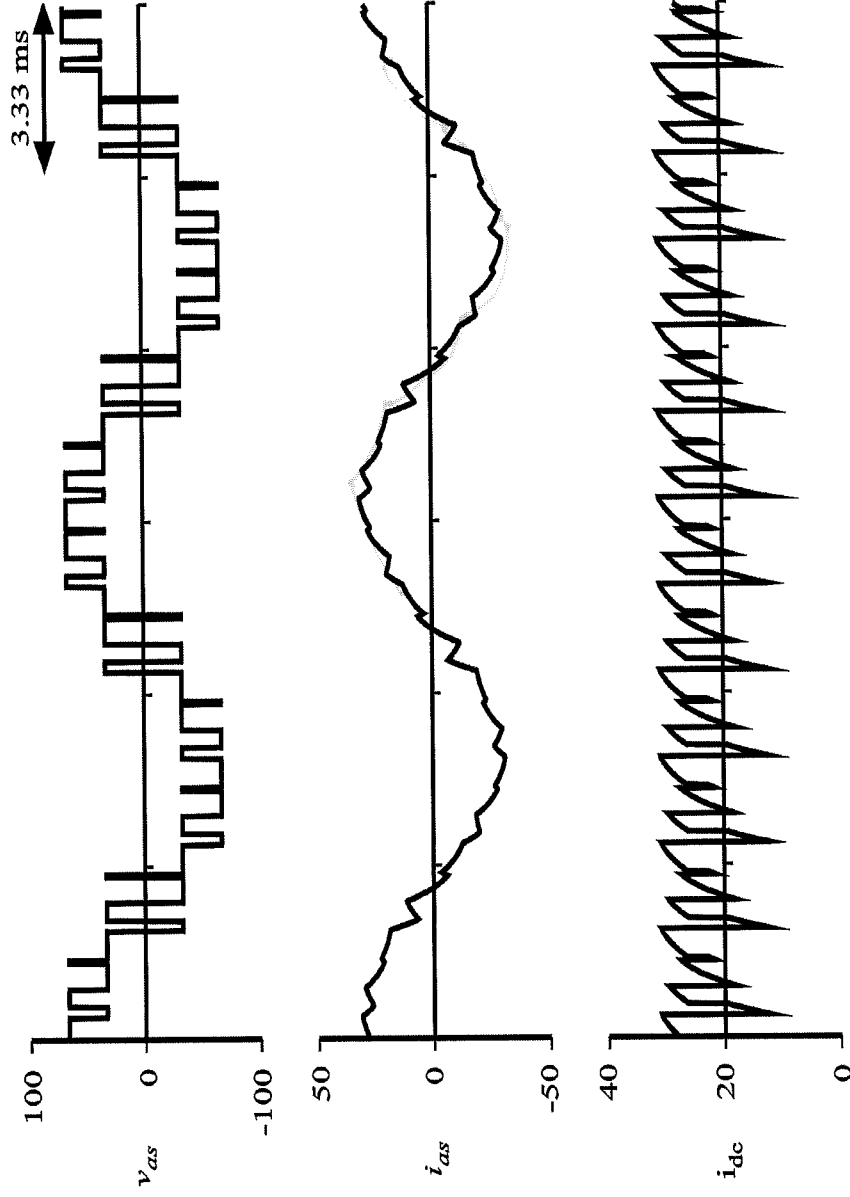
(13.5-20)

$$- \quad \bar{v}_{ds}^c = 0 \quad d \geq 0$$

(13.5-21)

# Overmodulation (d=2)

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## 13.6 Third-Harmonic Injection

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- Objective ...
  - strategy for increasing voltage w/o introducing low-frequency harmonics



# The Plan

- Suppose

$$d_a = d \cos(\theta_c) - d_3 \cos(3\theta_c) \quad (13.6-1)$$

$$d_b = d \cos\left(\theta_c - \frac{2\pi}{3}\right) - d_3 \cos(3\theta_c) \quad (13.6-2)$$

$$d_c = d \cos\left(\theta_c + \frac{2\pi}{3}\right) - d_3 \cos(3\theta_c) \quad (13.6-3)$$

$$V_{gdi}^c = \frac{2}{3} \begin{bmatrix} c & c^- & c^+ \\ s & s^- & s^+ \end{bmatrix} \begin{bmatrix} v_{cs} \\ v_{bs} \\ v_{cs} \end{bmatrix}$$

$$= \frac{2}{3} \begin{bmatrix} c & c^- & c^+ \\ s & s^- & s^+ \end{bmatrix} \frac{V_{dc}}{2} \begin{bmatrix} 1 + d_c - d_3 \cos(3\theta_c) \\ 1 + d_c^- - d_3 \cos(3\theta_c) \\ 1 + d_c^+ - d_3 \cos(3\theta_c) \end{bmatrix}$$

$$= \frac{1}{3} V_{dc} \begin{bmatrix} d \\ 0 \end{bmatrix}$$

*Assume 120° phase duty cycles*

## Results

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- Working for a little bit ...

- Therefore

$$- \hat{v}_{qs}^c = \frac{1}{2} dv_{dc}$$

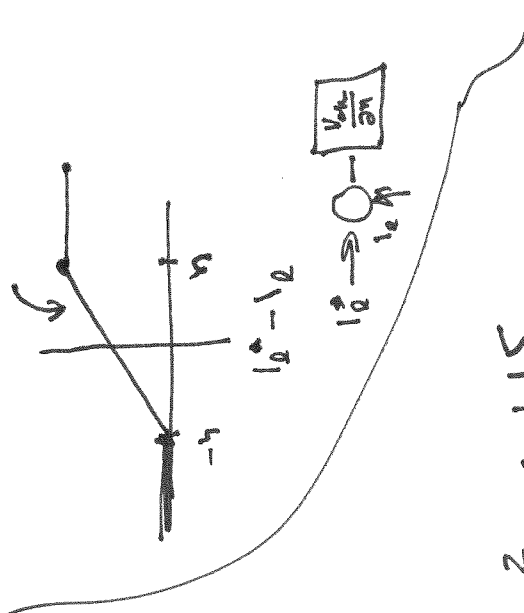
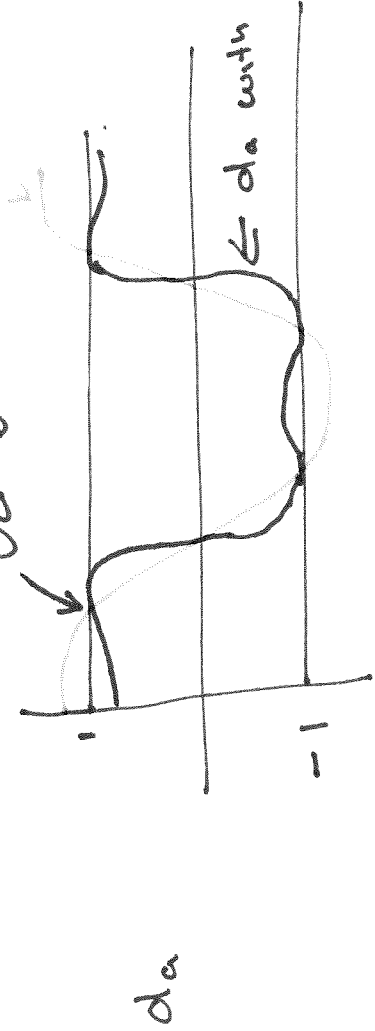
(13.5-14)

$$- \hat{v}_{ds}^c = 0$$

(13.5-15)

# So What?

- Consider



$$\frac{2}{\sqrt{3}} \approx 1.15$$

$$\cos\left(3\frac{\pi}{6}\right) = \cos\left(\frac{\pi}{2}\right) = 0$$

⇒ we need  $d \cos\left(\frac{\pi}{6}\right) < 1$   $d \leq \frac{1}{\cos\left(\frac{\pi}{6}\right)}$

⇒ if  $\theta_c$  is to be the peak then  $\frac{dd_a}{d\theta_c} = 0$  at  $\pi/6$

$$d_a = d \cos \theta_c - d_3 \cos 3\theta_c$$

$$\frac{dd_a}{d\theta_c} = -d \sin \theta_c + 3d_3 \sin(3\theta_c) = 0$$

$$-d \sin\left(\frac{\pi}{6}\right) + 3d_3 = 0$$

$$d_3 = \frac{1}{3} d \sin\left(\frac{\pi}{6}\right) = \frac{d}{6}$$

## So What ?

- Thus
  - $d \leq \frac{2}{\sqrt{3}}$
- Result
  - 15% Increase in Available Voltage

# Semiconductor Model

- Transistor

$$v = v_{sw} + r_{sw} i$$

- Diode

$$v = v_d + r_d i$$

What we want to do

Given  $I_g$  &  $I_a$  on the side  
we want the dc current

Given  $V_{dc}$  on the dc side  
we want the g- and d-axis  
voltages

Easy for voltage source strategies

Complications

① saturation at modulation  
commands

② hysteresis modulator

First Goal: DC current

## AVM - DC Current

- Consider the converter current reference frame

reference frame where  
all the ~~ac~~ ac side  
current is in the  $\delta$ -axis.

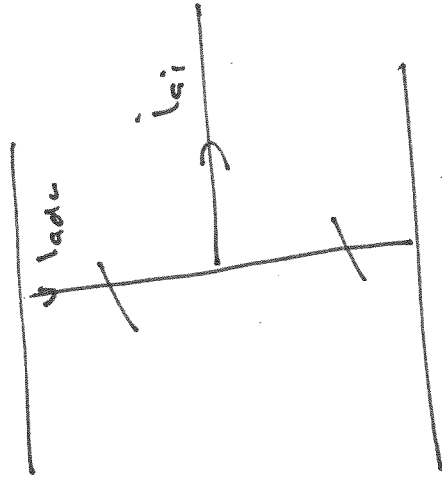
$$i_{ai} = i_{qi}^{ci} \cos \theta_{ci}$$

$$\begin{bmatrix} i_{ai} \\ i_{bi} \\ i_{ci} \end{bmatrix} = \begin{bmatrix} c & s & 1 \\ 0^- & s^- & 1 \\ c^+ & s^+ & 1 \end{bmatrix} \begin{bmatrix} i_{qi}^{ci} \\ 0 \\ 0 \end{bmatrix}$$

$$i_{ai} = i_{qi}^{ci} \cos \theta_{ci}$$

# AVM - DC Current

- Sine-Triangle Modulation with 3<sup>rd</sup> Harmonic



Upper switch on  
 $i_{dc} = i_{ai}$  (d<sub>ag</sub> of time)

Lower switch on  
 $i_{dc} = 0$  (1-d<sub>ag</sub>) of the time

$i_{dc} = i_{ai} d_{ag}$

# AVM - DC Current

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- We have

$$d_{ag} = \frac{1}{2}(1 + d_{as})$$

$$d_{as} = d \cos(\underbrace{\theta_{ci} - \phi}_{\theta_c}) - d_3 \cos(\underbrace{3(\theta_{ci} - \phi)}_{3\theta_c})$$

$$\theta_c = \theta_{ci} - \phi$$

$$\phi = \theta_{ci} - \theta_c$$

By definition, the angular displacement between the two reference frames.



# AVM - DC Current

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- We have

$$\hat{i}_{a,dc} = i_{ai} d_{ag}$$

$$\bar{i}_{a,dc} = \frac{1}{2\pi} \int_{-\pi/2}^{3\pi/2} \hat{i}_{a,dc}(\theta_{ci}) d\theta_{ci}$$

$$\begin{aligned}
 &= \frac{1}{2\pi} \int_{-\pi/2}^{3\pi/2} i_{ci} \cos \theta_{ci} \frac{1}{2} (1 + d \cos(\theta_{ci} - \phi) - d_3 \cos(3(\theta_{ci} - \phi))) d\theta_{ci} \\
 &= \frac{i_{ci}}{4\pi} \int_{-\pi/2}^{3\pi/2} \cos \theta_{ci} + \frac{1}{2} \cos(-\phi) + \frac{1}{2} \cos(2\theta_{ci} - \phi) - \frac{d_3}{2} \cos(4\theta_{ci} - 3\phi) \\
 &\quad - \frac{d_3}{2} \cos(2\theta_{ci} - 2\phi) d\theta_{ci}
 \end{aligned}$$

# AVM - DC Current

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$$\begin{aligned} I_{a,dc} &= \frac{I_{ci}}{4\pi} \int \cos(\phi) d\pi \\ &= \frac{1}{4} I_{ci} \cos\phi \end{aligned}$$

# **AVM – DC Current**

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## AVM – DC Current

- Thus we have for the a-phase

$$\bar{i}_{a,dc} = \frac{1}{4} d i_{qi}^{ci} \cos(\phi)$$

- The total dc current must be given by


$$i_{dc} = \frac{3}{4} d i_{qi}^{ci} \cos(\phi)$$

# AVM - Voltage for Positive Current

Assume  $i_{ai} \geq 0$

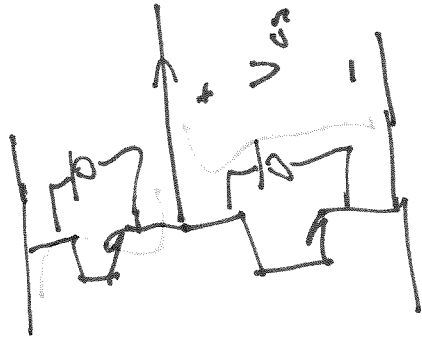
$$-\frac{\pi}{2} \leq \theta_{ci} \leq \frac{\pi}{2}$$

if upper switch on  $(d_{as})$  of the time  $T$

$$V_{as} = V_{dc} - V_{su} - r_{su} i_{ai}$$

if lower switch on  $(1-d_{as})$  of the time  $T$

$$V_{as} = -V_d - r_{al} i_{ai}$$

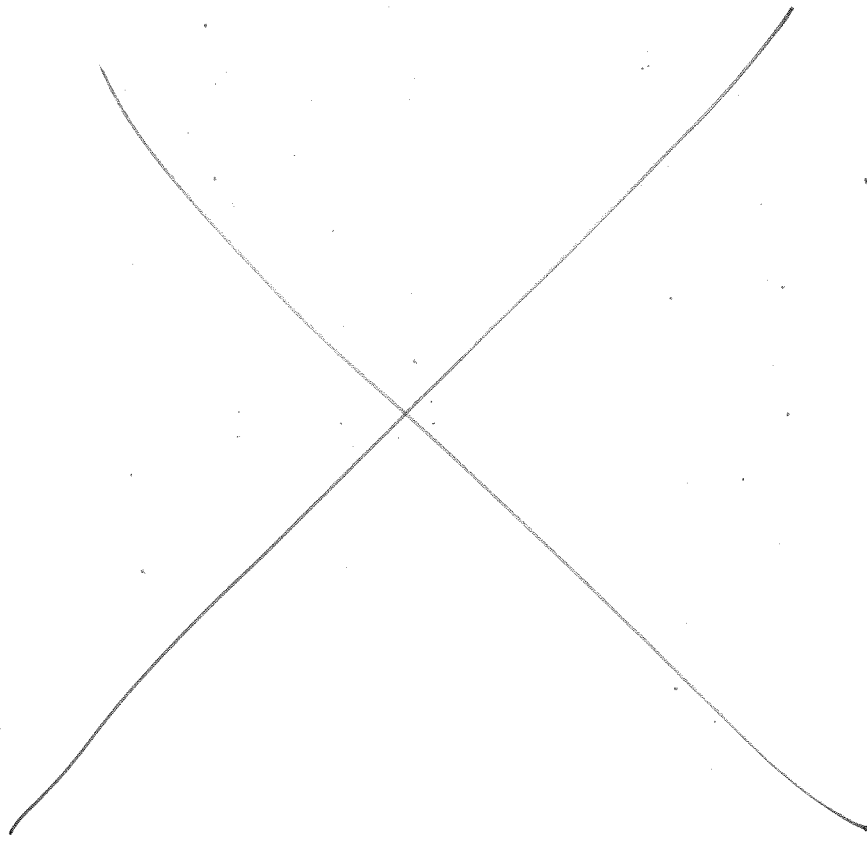


$$\hat{V}_{as+} = (V_{dc} - V_{fsu} - r_{su} i_{ai}) d_{as} - (V_d + r_{al} i_{ai}) (1 - d_{as})$$

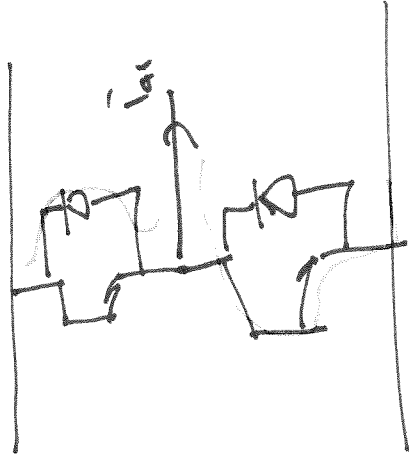
Fast decrease of  $V_{as}$  when the current is positive at  $-\frac{\pi}{2} \leq \theta_{ci} \leq \frac{\pi}{2}$

# **AVM – Voltage for Positive Current**

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# AVM - Voltage for Negative Current



Assume  $i_{ai} < 0$

if upper switch on

$$V_{as} = V_{dc} + V_d - r_{di} i_{ai}$$

if lower switch on

$$V_{as} = V_{sw} - r_{sw} i_{ai}$$

$$\therefore \hat{V}_{as} = (V_{dc} + V_d - r_{di} i_{ai}) d_{lag} + (V_{sw} - r_{sw} i_{ai})(1 - d_{lag})$$

fast average of  $V_{as}$  while  $i_{ai} < 0$

$$\text{Or } \frac{\pi}{2} \leq \theta_{ci} \leq \frac{3\pi}{2}$$

# AVM - Voltage

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- Thus the fast average voltages may be expressed

$$\hat{v}_{ag} = \begin{cases} \hat{v}_{ag+} & i_{ai} > 0 \\ \hat{v}_{ag-} & i_{ai} < 0 \end{cases}$$

$$\hat{v}_{ag+} = (v_{dc} - v_{sw} - r_{sw}i_{ai})d_{ag} + (-v_d - r_d i_{ai})(1 - d_{ag})$$

$$\hat{v}_{ag-} = (v_{dc} + v_d - r_d i_{ai})d_{ag} + (v_{sw} - r_{sw}i_{ai})(1 - d_{ag})$$



## **AVM - Voltage**

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- The fundamental component of the line-to-ground voltage may be expressed

$$\hat{v}_{ag} \Big|_{fund} = a_1 \cos \theta_{ci} + b_1 \sin \theta_{ci}$$

$$a_1 = \frac{1}{\pi} \int_{-\pi/2}^{\pi/2} \hat{v}_{ag+} \cos(\theta_{ci}) d\theta_{ci} + \frac{1}{\pi} \int_{\pi/2}^{3\pi/2} \hat{v}_{ag-} \cos(\theta_{ci}) d\theta_{ci}$$

$$b_1 = \frac{1}{\pi} \int_{-\pi/2}^{\pi/2} \hat{v}_{ag+} \sin(\theta_{ci}) d\theta_{ci} + \frac{1}{\pi} \int_{\pi/2}^{3\pi/2} \hat{v}_{ag-} \sin(\theta_{ci}) d\theta_{ci}$$

# AVM - Voltage

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- After substantial manipulation

$$a_1 = \frac{1}{2}(v_{dc} - v_{sw} + v_d)d \cos \phi - \frac{2}{\pi}(v_d + v_{sw}) - \dots$$
$$\left( \frac{1}{2}(r_{sw} + r_d) + \frac{4}{3\pi} \left( d \cos(\phi) - \frac{1}{5} d_3 \cos(3\phi) \right) (r_{sw} - r_d) \right) i_{qc}^{ci}$$

$$b_1 = \frac{1}{2}(v_{dc} + v_d - v_{sw})d \sin(\phi) - \dots$$
$$\frac{2(r_{sw} - r_d)}{3\pi} \left( d \sin(\phi) - \frac{3}{5} d_3 \sin(3\phi) \right) i_{qc}^{ci}$$

## AVM - Voltage

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- After a little more work, we have

$$\bar{v}_{qi}^{ci} = a_1$$

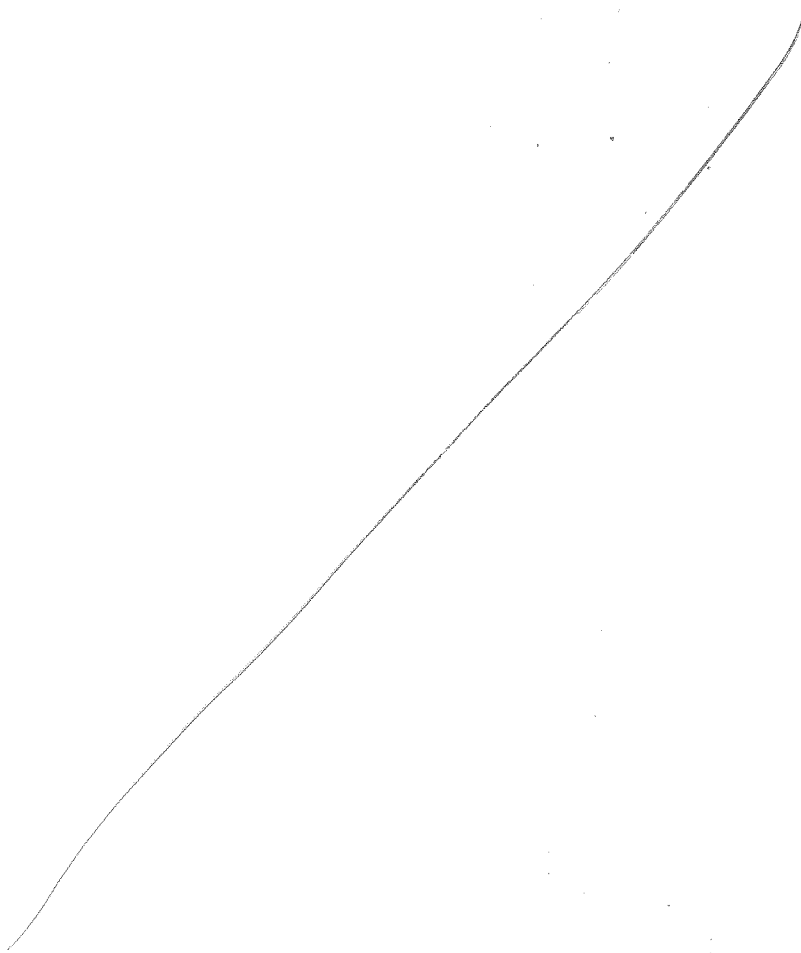
$$\bar{v}_{di}^{ci} = b_1$$

- To show this

$$\begin{bmatrix} v_{d1}^{ci} \\ v_{q1}^{ci} \\ v_{d1}^{ei} \end{bmatrix} = \frac{2}{3} \begin{bmatrix} c & c^- & c^r \\ s & s^- & s^r \end{bmatrix} \begin{bmatrix} a_1 c + b_1 s \\ a_1 c^- + b_1 s^- \\ a_1 c^r + b_1 s^r \end{bmatrix} = \begin{bmatrix} a_1 \\ b_1 \end{bmatrix}$$

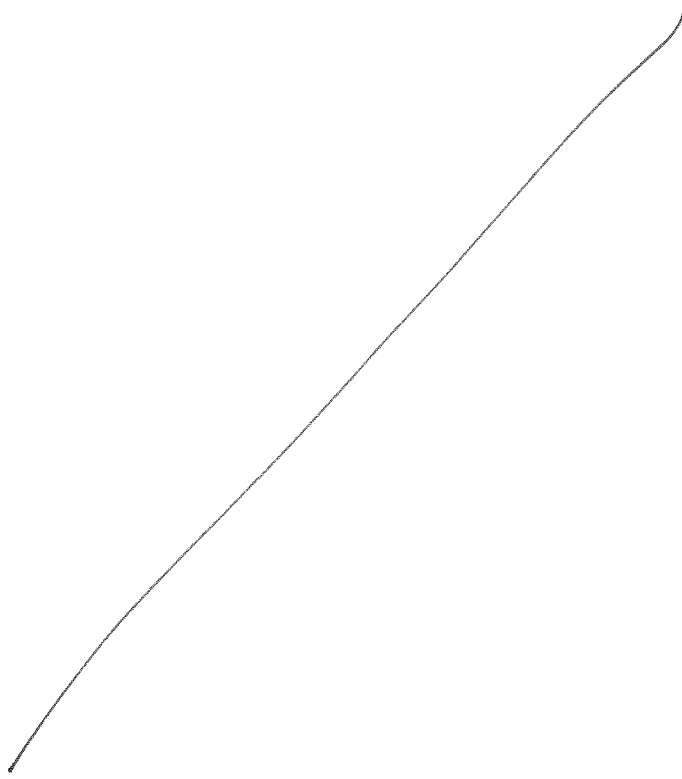
# **AVM - Voltage**

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# **AVM - Voltage**

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# **AVM – Modulation Signal**

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- Problem: we need to know  $d$ ,  $d_3$ ,  $\phi$
- Starting point: modulation indices

$$m_q^* = \frac{v_q^*}{v_{dc}}$$

$$m_d^* = \frac{v_d^*}{v_{dc}}$$

# AVM – Modulation Signal

- We will need the modulation signal in the current reference frame

$$\begin{matrix} & a_{K_{ci}} \\ & \underbrace{\hspace{10em}} \\ \begin{bmatrix} m_q^{ci*} \\ m_d^{ci*} \end{bmatrix} & = & \begin{bmatrix} \cos(\theta_{ci} - \theta) & -\sin(\theta_{ci} - \theta) \\ \sin(\theta_{ci} - \theta) & \cos(\theta_{ci} - \theta) \end{bmatrix} \begin{bmatrix} m_q^* \\ m_d^* \end{bmatrix} \end{matrix}$$

# AVM – Modulation Signal

- It can be shown that

$$\theta_{ci} - \theta = \text{angle}(i_{qi} - j i_{di})$$

- To show this

$$\begin{bmatrix} i_{qi} \\ 0 \end{bmatrix} = \underbrace{\begin{bmatrix} c & -s \\ s & c \end{bmatrix}}_{aK_{ci}} \begin{bmatrix} i_{qi} \\ i_{di} \end{bmatrix} \xrightarrow{\cos(\theta_{ci} - \theta)}$$
$$\begin{bmatrix} i_{qi} \\ i_{di} \end{bmatrix} = \begin{bmatrix} c & s \\ -s & c \end{bmatrix} \begin{bmatrix} i_{qi} \\ 0 \end{bmatrix} \quad s_i K_a$$



# AVM – Modulation Signal

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$$I_{gi} = I_{gi}^{ci} \cos(\theta_{ci} - \theta)$$

$$I_{di} = -I_{gi}^{ci} \sin(\theta_{ci} - \theta)$$

$$I_{gi} - j I_{di} = I_{gi}^{ci} e^{j(\theta_{ci} - \theta)}$$

$$\theta_{ci} - \theta = \text{angle}(I_{gi} - j I_{di})$$

$$I_{gi}^{ci} = \sqrt{(I_{gi})^2 + (I_{di})^2}$$

# **AVM – Modulation Signal**

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## AVM – Modulation Signal

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- In converter voltage reference frame

$$d_{as} = d^* \cos(\theta_c) - d_3^* \cos(3\theta_c)$$

- In this frame

$$\theta_c - \theta = \text{angle}(m_q^* - jm_d^*)$$

$$m_q^{c*} = \sqrt{m_q^{*2} + m_d^{*2}}$$

$$m_d^{c*} = 0$$

# AVM - Modulation Signal

- To show this

$$\begin{aligned}
 & \begin{bmatrix} m_q^{cv*} \\ 0 \end{bmatrix} = \underbrace{\begin{bmatrix} \cos(\theta_{cv}-\theta) & -s(\cdot) \\ s(\cdot) & \cos(\theta_{cv}-\theta) \end{bmatrix}}_{a \text{ } K^{ev}} \begin{bmatrix} m_q^* \\ m_d^* \end{bmatrix} \\
 & \begin{bmatrix} m_q^* \\ m_d^* \end{bmatrix} = \underbrace{\begin{bmatrix} \cos(\theta_{cv}-\theta) & s(\cdot) \\ -s(\cdot) & \cos(\theta_{cv}-\theta) \end{bmatrix}}_{K^{ev*}} \begin{bmatrix} m_q^* \\ m_d^* \end{bmatrix} \quad c' = cv' \\
 & m_q^* = m_q^{cv*} \cos(\theta_{cv}-\theta) \quad \text{same as } m_q^{c*} \\
 & m_d^* = -m_q^{cv*} s(\theta_{cv}-\theta) \\
 & m_q^* - jm_d^* = m_q^{cv*} e^{-j(\theta_{cv}-\theta)} \\
 & \theta_{cv}-\theta = \angle \left( \frac{m_q^* - jm_d^*}{m_q^{cv*}} \right) \\
 & m_q^{cv*} = \sqrt{(m_q^*)^2 + (m_d^*)^2}
 \end{aligned}$$

# AVM – Modulation Signal

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- Since we have

$$\theta_{ci} - \theta = \text{angle}(i_{qi} - j i_{di}) \quad d_{as} = d \cos(\theta_{ci} - \phi) - d_3 \cos(3(\theta_{ci} - \phi))$$

$$\theta_{cv} - \theta = \text{angle}(m_q^* - j m_d^*) \quad d_{as} = d^* \cos(\theta_c) - d_3^* \cos(3\theta_c)$$

$$\phi = \theta_{ci} - \theta_{cv} = (\theta_{ci} - \theta) - (\theta_{cv} - \theta)$$

- We therefore have

$$\phi = \text{angle}(i_{qi} - j i_{di}) - \text{angle}(m_q^* - j m_d^*)$$

$$\phi, d, d_3$$

# AVM Modulation Signal

- Desired magnitudes

$$d^* = 2m_q^{cv*}$$

$$d_3^* = \frac{1}{6}d^*$$

- For unsaturated operation  $d^* < \frac{2}{\sqrt{3}}$

$$d = d^*$$

$$d_3 = d_3^*$$

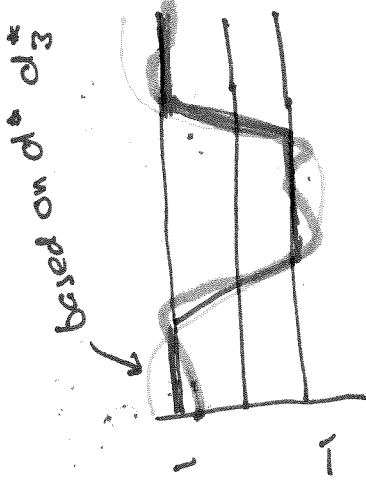
$$V_{q0}^{cv} = \frac{1}{2}d V_{dc}$$

$$V_{q0}^{cv} = m_q^{cv} V_{dc}$$

$$\frac{1}{2}d = m_q^{cv}$$

# AVM - Modulation

- Analysis plan for saturated operation



$$d_{a,aprx} = d \cos(\theta_{cv}) - d_3 \cos(3\theta_{cv})$$

$$f(d, d_3) =$$

$$\int_0^{\pi/2} (\text{bound}(-1, 1, d_a(\theta_{cv})) - d_{a,aprx}(\theta_{cv}))^2 d\theta_{cv}$$

// find  $d$  &  $d_3$   
that minimize  $f$

$$\text{bound}(a, b, x) \equiv \begin{cases} a & x < a \\ x & a \leq x \leq b \\ b & x > b \end{cases}$$

# AVM Modulation

## • Results

$$d = d^* + \frac{4}{\pi} \sin \theta_{cv1} + \frac{1}{\pi} \sin(2\theta_{cv1})(d_3^* - d^*) +$$

$$\frac{1}{2\pi} d_3^* \sin(4\theta_{cv1}) - \frac{2}{\pi} d^* \theta_{cv1}$$

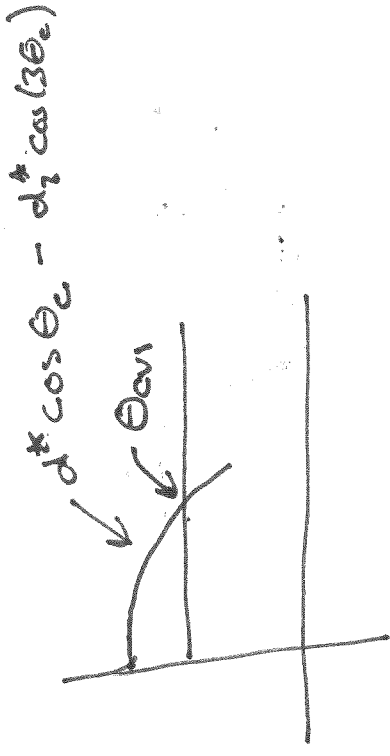
$$d_3 = d_3^* - \frac{2}{\pi} d_3^* \theta_{cv1} + \dots$$

$$\frac{1}{3\pi} \left( (9d^* - 2d_3^*) \cos \theta_{cv1} + (3d^* - 2d_3^*) \cos(3\theta_{cv1}) - \dots \right) \sin \theta_{cv1}$$

$$d^* \cos(\theta_{cv1}) - d_3^* \cos(3\theta_{cv1}) = 1$$

$$f = 1 - d^* \cos(\theta_{cv1}) + d_3^* \cos(3\theta_{cv1})$$

$$\frac{df}{d\theta_{cv1}} = d^* \sin \theta_{cv1} - 3d_3^* \sin(3\theta_{cv1})$$



To get  $\theta_{cv1}$

① Initialize

$$\theta_{cv1} = \arccos\left(\frac{1}{d^*}\right)$$

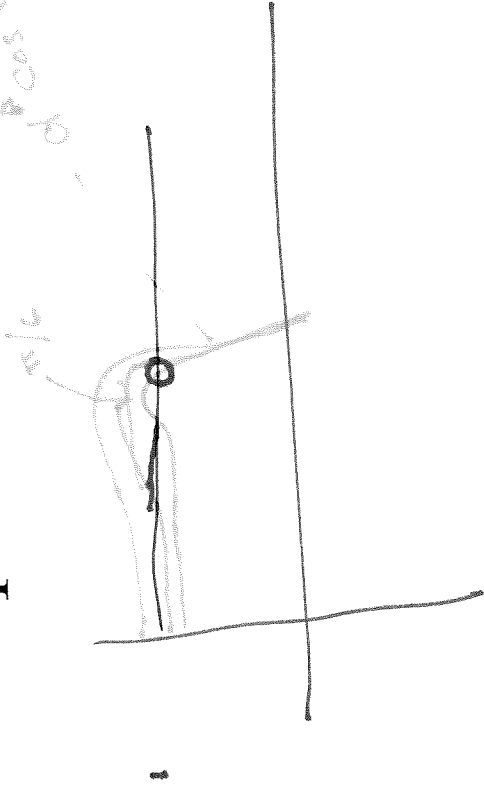
② Iterate using Newton's method

$$\theta_{cv1} = \theta_{cv1} - \frac{f}{\frac{df}{d\theta_{cv1}}}$$



# AVM Modulation

- A subtle point



- This occurs when

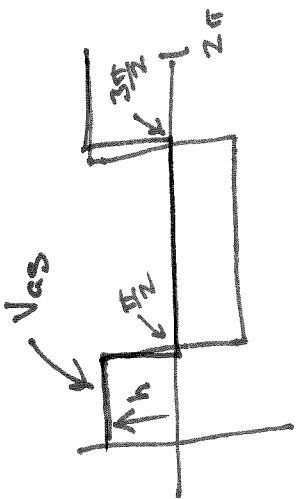
$$\frac{2}{\sqrt{3}} < d < \frac{6}{5} \quad 1.15 \dots 1.2$$

# AVM - Hysteresis Modulator

$$i_{gde} = i_{gdL} - i_{gdL}$$

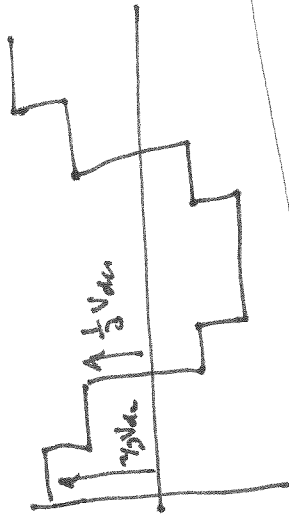
$$m_g^* = K i_{gde}$$

→ Unsaturation voltage is in phase with the current error



$i_{gde}$   
 α-phase current error

$$\text{fundamental} = \frac{4}{\pi} h \quad i_{ge} = \frac{4}{\pi} h$$



$$\text{fundamental} = \frac{2}{\pi} V_{dc} \quad V_g = \frac{2}{\pi} V_{dc}$$

$$m_g = \frac{2}{\pi}$$

$$m_g = K i_{ge}$$

$$\frac{2}{\pi} = K \frac{4}{\pi} h$$

$$K = \frac{1}{2h}$$

# AVM – Hysteresis Modulator

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# AVM - Summary

$$\left. \begin{aligned} (1) \quad |g_{de}| &= |g_{dL} - |g_{dL} \\ (2) \quad m_{gd}^* &= \frac{1}{2h} |g_{dL} \end{aligned} \right\}$$

$$(3) \quad m_{gd}^{ev*} = \sqrt{(m_g^*)^2 + (m_{dL}^*)^2}$$

$$(4) \quad d_1^* = 2 m_g^* \\ d_3^* = \frac{2}{\sqrt{3}} d_1^* / 6$$

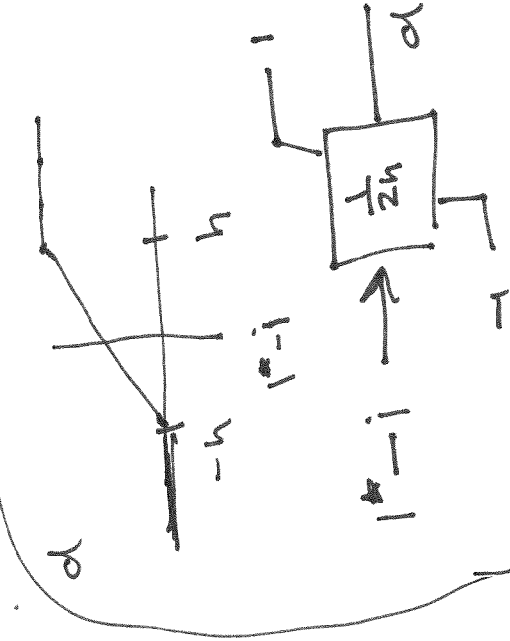
$$(5) \quad \text{if } d_1^* < \frac{2}{\sqrt{3}}$$

$$d = d_1^* \\ d_3 = d_3^*$$

else solve for  $\theta_{ev}$ ,  $d_1$ ,  $d_3$

$$(6) \quad \phi = \text{angle}(|g_i - j|d_i) - \text{angle}(m_g^* - j m_{dL}^*)$$

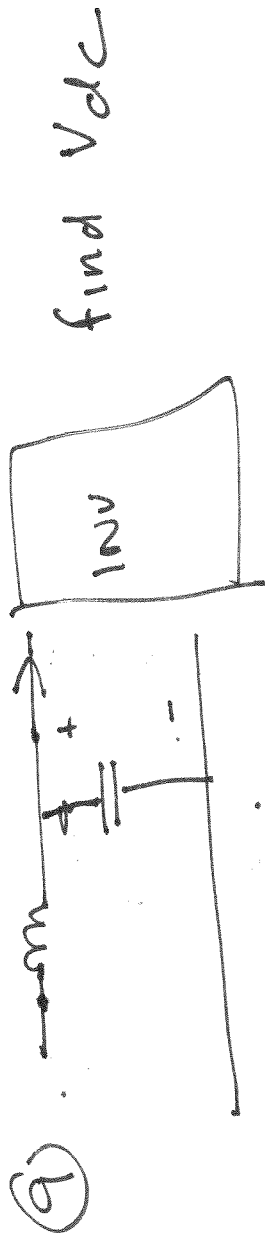
representation of hysteresis



# AVM - Summary

$$(7) \quad I_{q_i}^{ci} = \sqrt{(I_{q_i})^2 + (I_{d_i})^2}$$

$$(8) \quad I_{dc} = \frac{3}{4} I_{q_i}^{ci} \cos \phi$$



(10) find  $a_1, b_1$

$$(11) \quad V_{q_i}^{ci} = a_1$$
$$V_{d_i}^{ci} = b_1$$