Agenda

Parsers

- Terminology
- LL(I) Parsers
- Overview of LR Parsing

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Terminology

- Grammar $G = (V_t, V_n, S, P)$
 - V_t is the set of terminals
 - V_n is the set of non-terminals
 - S is the start symbol
 - P is the set of productions
 - Each production takes the form: $V_n \rightarrow \lambda \mid (V_n \mid V_t) +$
 - Grammar is context-free (why?)
- A simple grammar:

 $G = (\{a,b\}, \{S,A,B\}, \{S \rightarrow A \ B \ \$,A \rightarrow A \ a,A \rightarrow a,B \rightarrow B \ b,B \rightarrow b\},S)$

Terminology

- $\bullet \quad \mbox{V is the } \begin{subarray}{ll} V \mbox{is the } \begin{subarray}{ll} V \mbox{on sisting of terminal } (V_t) \\ \mbox{and non-terminal } (V_n) \mbox{ symbols} \\ \end{subarray}$
- For our sample grammar
 - $V_n = \{S, A, B\}$
 - Non-terminals are symbols on the LHS of a production
 - Non-terminals are constructs in the language that are recognized during parsing
 - $\bullet \quad V_t = \{a,b\}$
 - Terminals are the tokens recognized by the scanner
 - They correspond to symbols in the text of the program

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Terminology

- Productions (rewrite rules) tell us how to derive strings in the language
 - Apply productions to rewrite strings into other strings
- We will use the standard BNF form
- $P = \{$ $S \rightarrow A B \$$ $A \rightarrow A a$ $A \rightarrow a$ $B \rightarrow B b$ $B \rightarrow b$

Generating strings

 $S \rightarrow A B$ \$

 $A \rightarrow A a$

 $A \rightarrow a$

 $B \rightarrow B b$

 $B \rightarrow b$

 Given a start rule, productions tell us how to rewrite a non-terminal into a different set of symbols

 By convention, first production applied has the start symbol on the left, and there is only one such production

To derive the string "a a b b b" we can do the following rewrites:

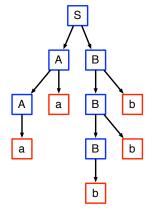
```
S \Rightarrow A B \$ \Rightarrow A a B \$ \Rightarrow a a B b \$ \Rightarrow a a B b \$ \Rightarrow a a B b b \$ \Rightarrow a a b b b \$
```

Terminology

- Strings are composed of symbols
 - AAaaBbbAais a string
 - We will use Greek letters to represent strings composed of both terminals and non-terminals
- L(G) is the language produced by the grammar G
 - All strings consisting of only terminals that can be produced by G
 - In our example, L(G) = a+b+\$
 - All regular expressions can be expressed as grammars for context-free languages, but not vice-versa
 - Consider: ai bi \$ (what is the grammar for this?)

Parse trees

- Tree which shows how a string was produced by a language
 - Interior nodes of tree: nonterminals
 - Children: the terminals and non-terminals generated by applying a production rule
 - Leaf nodes: terminals



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Leftmost derivation

- Rewriting of a given string starts with the leftmost symbol
- Exercise: do a leftmost derivation of the input program

$$F(V + V)$$

using the following grammar:

E	→	Prefix (E)
E	→	V Tail
Prefix	→	F
Prefix	→	λ
Tail	→	+ E
Tail	→	λ

What does the parse tree look like?

Rightmost derivation

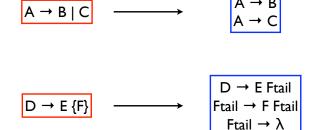
- Rewrite using the rightmost non-terminal, instead of the left
- What is the rightmost derivation of this string?

$$F(V + V)$$

E	\rightarrow	Prefix (E)
E	→	V Tail
Prefix	\rightarrow	F
Prefix	\rightarrow	λ
Tail	\rightarrow	+ E
Tail	\rightarrow	λ

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Simple conversions



Top-down vs. Bottom-up parsers

- Top-down parsers use left-most derivation
- Bottom-up parsers use right-looking parse
- Notation:
 - LL(I): Leftmost derivation with I symbol lookahead
 - LL(k): Leftmost derivation with k symbols lookahead
 - LR(I): Right-looking derivation with I symbol lookahead

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What is parsing

- Parsing is recognizing members in a language specified/ defined/generated by a grammar
- When a construct (corresponding to a production in a grammar) is recognized, a typical parser will take some action
 - In a compiler, this action generates an intermediate representation of the program construct
 - In an interpreter, this action might be to perform the action specified by the construct. Thus, if a+b is recognized, the value of a and b would be added and placed in a temporary variable

Another simple grammar

```
PROGRAM → begin STMTLIST $

STMTLIST → STMT; STMTLIST

STMTLIST → end

STMT → id

STMT → if (id) STMTLIST
```

- A sentence in the grammar:
 begin if (id) if (id) id; end; end; end; \$
- What are the terminals and non-terminals of this grammar?

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Parsing this grammar

PROGRAM \rightarrow begin STMTLIST \$
STMTLIST \rightarrow STMT; STMTLIST
STMTLIST \rightarrow end
STMT \rightarrow id
STMT \rightarrow if (id) STMTLIST

- Note
 - To parse STMT in STMTLIST → STMT; STMTLIST, it is necessary to choose between either STMT → id or STMT → if ...
 - Choose the production to parse by finding out if next token is if or id
 - i.e., which production the next input token matches
 - This is the *first* set of the production

Another example

 $S \rightarrow A B$ \$ $A \rightarrow x a A$ $A \rightarrow y a A$ $A \rightarrow \lambda$ $B \rightarrow b$

- Consider $S \Rightarrow A B \$ \Rightarrow x a A B \$ \Rightarrow x a B \$ \Rightarrow x a b \$$
- When parsing x a b \$ we know from the goal production we need to match an A.The next token is x, so we apply $A \to x$ a A
- The parser matches x, matches a and now needs to parse A again
- How do we know which A to use? We need to use A $\rightarrow \lambda$
 - When matching the right hand side of A \to λ , the next token comes from a non-terminal that follows A (i.e., it must be b)
 - Tokens that can follow A are called the follow set of A

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First and follow sets

 First(α): the set of terminals that begin all strings that can be derived from α

First(A) = {x, y}First(xaA) = {x}

• First (AB) = {x, y, b}

 $A \rightarrow y a A$ $A \rightarrow \lambda$

 $S \rightarrow A B \$$

 $A \rightarrow x a A$

 Follow(A): the set of terminals that can appear immediately after A in some partial derivation

 $B \rightarrow b$

• Follow(A) = {b}

First and follow sets

- First(α) = { $a \in V_t \mid \alpha \Rightarrow^* a\beta$ } \cup { $\lambda \mid \text{if } \alpha \Rightarrow^* \lambda$ }
- Follow(A) = $\{a \in V_t \mid S \Rightarrow^+ ... Aa ...\} \cup \{\$ \mid \text{if } S \Rightarrow^+ ... A \$\}$

start symbol

a: a terminal symbol

a non-terminal symbol

x,β: a string composed of terminals and non-terminals (typically, α is the RHS of a production

derived in 1 step

 \Rightarrow^* : derived in 0 or more steps

⇒+: derived in I or more steps

Computing first sets

- Terminal: First(a) = {a}
- Non-terminal: First(A)
 - Look at all productions for A

$$A \rightarrow X_1 X_2 ... X_k$$

- First(A) \supseteq (First(X₁) λ)
- If $\lambda \in First(X_1)$, $First(A) \supseteq (First(X_2) \lambda)$
- If λ is in First(X_i) for all i, then $\lambda \in First(A)$
- Computing First(α): similar procedure to computing First(A)

Exercise

 What are the first sets for all the non-terminals in following grammar:

$$S \rightarrow A B$$
\$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow \lambda$

 $B \rightarrow b$

 $B \rightarrow A$

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Computing follow sets

- Follow(S) = {\$}
- To compute Follow(A):
 - Find productions which have A on rhs. Three rules:

1.
$$X \rightarrow \alpha A \beta$$
: Follow(A) \supseteq (First(β) - λ)

2.
$$X \rightarrow \alpha A \beta$$
: If $\lambda \in First(\beta)$, Follow(A) \supseteq Follow(X)

- 3. $X \rightarrow \alpha A$: Follow(A) \supseteq Follow(X)
- Note: Follow(X) never has λ in it.

Exercise

• What are the follow sets for

 $S \rightarrow A B$ \$

 $A \rightarrow x a A$

 $A \rightarrow y a A$

 $A \rightarrow \lambda$

 $B \rightarrow b$

 $B \rightarrow A$

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Towards parser generators

- Key problem: as we read the source program, we need to decide what productions to use
- Step I: find the tokens that can tell which production P (of the form $A \to X_1 X_2 ... X_m$) applies

$$Predict(P) =$$

$$\begin{cases} \operatorname{First}(X_1 \dots X_m) & \text{if } \lambda \not\in \operatorname{First}(X_1 \dots X_m) \\ (\operatorname{First}(X_1 \dots X_m) - \lambda) \cup \operatorname{Follow}(A) & \text{otherwise} \end{cases}$$

 If next token is in Predict(P), then we should choose this production

Parse tables

- Step 2: build a parse table
 - Given some non-terminal V_n (the non-terminal we are currently processing) and a terminal V_t (the lookahead symbol), the parse table tells us which production P to use (or that we have an error
 - More formally:

$$T:V_n \times V_t \rightarrow P \cup \{Error\}$$

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Building the parse table

 Start:T[A][t] = //initialize all fields to "error" foreach A:

foreach P with A on its lhs:

foreach t in Predict(P): T[A][t] = P

 $2.A \rightarrow x a A$

• Exercise: build parse table for our toy grammar

3. $A \rightarrow y a A$ 4. $A \rightarrow \lambda$

 $I.S \rightarrow AB$ \$

5.B → b

э. Б 🖰

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Stack-based parser for LL(I)

- Given the parse table, a stack-based algorithm is much simpler to generate than a recursive descent parser
- Basic algorithm:
 - I. Push the RHS of a production onto the stack
 - 2. Pop a symbol, if it is a terminal, match it
 - 3. If it is a non-terminal, take its production according to the parse table and go to I
- Algorithm on page 121
- Note: always start with start state

An example

Recursive-descent parsers

Given the parse table, we can create a program which

Remember the recursive descent parser we saw for

If the choice of production is not unique, the parse table

generates recursive descent parsers

tells us which one to take

However, there is an easier method!

MICRO

1. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. $A \rightarrow y a A$

• How would a stack-based parser parse:

xayab

4. $A \rightarrow \lambda$ 5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	xayab\$	predict I

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An example

A → x a A
 A → y a A
 A → λ

5. B → b

I. $S \rightarrow A B \$$

• How would a stack-based parser parse:

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict l
A B \$	xayab\$	predict 2

An example

1. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. $A \rightarrow y a A$ 4. $A \rightarrow \lambda$ 5. $B \rightarrow b$

How would a stack-based parser parse:

xayab

Parse stack Remaining input Parser action

S xayab\$ predict I

AB\$ xayab\$ predict 2

xaAB\$ xayab\$ match(x)

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An example

A → x a A
 A → y a A

I. $S \rightarrow A B$ \$

• How would a stack-based parser parse:

4. A → λ5. B → b

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict l
A B \$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	avab\$	match(a)

An example

S → A B \$
 A → x a A
 A → y a A

• How would a stack-based parser parse:

4. A → λ5. B → b

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict I
AB\$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
A B \$	yab\$	predict 3

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An example

1. $S \rightarrow A B \$$ 2. $A \rightarrow \times a A$ 3. $A \rightarrow y a A$ 4. $A \rightarrow \lambda$

• How would a stack-based parser parse:

5. B → b

x a y a b

Parse stack	Remaining input	Parser action
S	xayab\$	predict l
A B \$	xayab\$	predict 2
×aAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
A B \$	yab\$	predict 3
y a A B \$	yab\$	match(y)

An example

S → A B \$
 A → x a A
 A → y a A

How would a stack-based parser parse:

xayab

4. $A \rightarrow \lambda$ 5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	xayab\$	predict l
AB\$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
AB\$	yab\$	predict 3
yaAB\$	yab\$	match(y)
a A B \$	a b \$	match(a)

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An example

1. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. $A \rightarrow y a A$ 4. $A \rightarrow \lambda$ 5. $B \rightarrow b$

• How would a stack-based parser parse:

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict I
A B \$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
A B \$	yab\$	predict 3
уаАВ\$	yab\$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4

An example

1. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. $A \rightarrow y a A$ 4. $A \rightarrow \lambda$ 5. $B \rightarrow b$

• How would a stack-based parser parse:

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict l
A B \$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
A B \$	yab\$	predict 3
уаАВ\$	yab\$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
В\$	b\$	predict 5

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An example

I. $S \rightarrow A B \$$ 2. $A \rightarrow x a A$ 3. A → y a A 4. A → λ

• How would a stack-based parser parse:

5. B → b

xayab

Parse stack	Remaining input	Parser action
S	xayab\$	predict I
AB\$	xayab\$	predict 2
xaAB\$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
AB\$	yab\$	predict 3
уа АВ\$	yab\$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
В\$	b\$	predict 5
b \$	b \$	match(b)

An example

I. $S \rightarrow A B \$$ 2. A → x a A 3. A → y a A 4. A → λ

• How would a stack-based parser parse:

xayab

5. B → b
Parser action
predict I
predict 2
match(x)
match(a)
predict 3
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Parse stack	Remaining input	Parser action
S	xayab\$	predict I
A B \$	xayab\$	predict 2
x a A B \$	xayab\$	match(x)
a A B \$	ayab\$	match(a)
A B \$	yab\$	predict 3
y a A B \$	yab\$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
В\$	b \$	predict 5
b \$	b \$	match(b)
\$	\$	Done!

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LL(k) parsers

• Can use similar techniques for LL(k) parsers

- Use more than one symbol of look-ahead to distinguish productions
- Why might this be bad?

Dealing with semantic actions

- Recall: we can annotate a grammar with action symbols
 - Tell the parser to invoke a semantic action routine
- Can simply push action symbols onto stack as well
- When popped, the semantic action routine is called

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Non-LL(I) grammars

- Not all grammars are LL(1)!
- Consider

<stmt> → if <expr> then <stmt list> endif

<stmt> → if <expr> then <stmt list> else <stmt list> endif

- This is not LL(I) (why?)
- We can turn this in to

<stmt $> \rightarrow$ if <expr> then <stmt list> <if suffix>

<if suffix> → endif

<if suffix> → else <stmt list> endif

Left recursion

- Left recursion is a problem for LL(1) parsers
 - LHS is also the first symbol of the RHS
- Consider:

 $E \rightarrow E + T$

What would happen with the stack-based algorithm?

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Removing left recursion



Algorithm on page 125

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Are all grammars LL(k)?

• No! Consider the following grammar:

$$\begin{array}{ccc} S & \rightarrow E \\ E & \rightarrow (E+E) \\ E & \rightarrow (E-E) \\ E & \rightarrow x \end{array}$$

- When parsing E, how do we know whether to use rule 2 or 3?
 - Potentially unbounded number of characters before the distinguishing '+' or '-' is found
 - No amount of lookahead will help!

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In real languages?

- Consider the if-then-else problem
- if x then y else z
- Problem: else is optional
- if a then if b then c else d
 - Which if does the else belong to?
- This is analogous to a "bracket language": $[i]^j$ ($i \ge j$)

$$\begin{array}{lll} S & \rightarrow [\ S \ C \\ S & \rightarrow \lambda \end{array} & \hbox{ [[] can be parsed: SS\LC or SSC\Lambda} \\ C & \rightarrow] & \hbox{ (it's ambiguous!)} \end{array}$$

Solving the if-then-else problem

- The ambiguity exists at the language level. To fix, we need to define the semantics properly
 - "] matches nearest unmatched ["
 - This is the rule C uses for if-then-else
 - What if we try this?

$$S \rightarrow [S \\ S \rightarrow SI \\ SI \rightarrow [SI]$$
$$SI \rightarrow \lambda$$

This grammar is still not LL(I) (or LL(k) for any k!)

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Two possible fixes

- If there is an ambiguity, prioritize one production over another
 - e.g., if C is on the stack, always match "]" before matching "λ"

$$\begin{array}{ccc} c & \rightarrow j \\ c & \rightarrow j \\ c & \rightarrow [c & c \\ c & c \\ c & \rightarrow [c & c \\ c &$$

- Another option: change the language!
 - e.g., all if-statements need to be closed with an endif

$$S \rightarrow \text{if } S E$$
 $S \rightarrow \text{other}$
 $E \rightarrow \text{else } S \text{ endif}$
 $E \rightarrow \text{endif}$

Parsing if-then-else

- What if we don't want to change the language?
 - C does not require { } to delimit single-statement blocks
- To parse if-then-else, we need to be able to look ahead at the entire rhs of a production before deciding which production to use
 - In other words, we need to determine how many "]" to match before we start matching "["s
- LR parsers can do this!

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LR Parsers

- Parser which does a Left-to-right, Right-most derivation
 - Rather than parse top-down, like LL parsers do, parse bottom-up, starting from leaves
- Basic idea: put tokens on a stack until an entire production is found
- Issues:
 - Recognizing the endpoint of a production
 - Finding the length of a production (RHS)
 - Finding the corresponding nonterminal (the LHS of the production)

Data structures

- At each state, given the next token,
 - A goto table defines the successor state
 - An action table defines whether to
 - shift put the next state and token on the stack
 - reduce an RHS is found; process the production
 - terminate parsing is complete

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Example

• Consider the simple grammar:

oprogram> → begin <stmts> end \$

<stmts> → SimpleStmt; <stmts>

<stmts> → begin <stmts> end ; <stmts>

 $\langle stmts \rangle \rightarrow \lambda$

• Shift-reduce driver algorithm on page 142

Action and goto tables

	begin	end	;	SimpleStmt	\$	<pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre>	<stmts></stmts>
0	S/I						
I	S / 4	R4		S / 5			S / 2
2		S / 3					
3					Α		
4	S / 4	R4		S / 5			S / 7
5			S / 6				
6	S / 4	R4		S / 5			S / 10
7		S / 8					
8			S / 9				
9	S / 4	R4		S / 6			S / II
10		R2					
П	·	R3			•		

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Example

• Parse: begin SimpleStmt; SimpleStmt; end \$

Step	Parse Stack	Remaining Input	Parser Action
I	0	begin S;S;end\$	Shift I
2	0 1	S;S;end\$	Shift 5
3	0 5	; S ; end \$	Shift 6
4	0 5 6	S ; end \$	Shift 5
5	0 1 5 6 5	; end \$	Shift 6
6	015656	end \$	Reduce 4 (goto 10)
7	0 5 6 5 6 10	end \$	Reduce 2 (goto 10)
8	0 5 6 0	end \$	Reduce 2 (goto 2)
9	0 2	end \$	Shift 3
10	0 1 2 3	\$	Accept

LR Parsers

- Basic idea:
 - shift tokens onto the stack. At any step, keep the set of productions that could generate the read-in tokens
 - reduce the RHS of recognized productions to the corresponding non-terminal on the LHS of the production. Replace the RHS tokens on the stack with the LHS non-terminal.

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LR(k) parsers

- LR(0) parsers
 - No lookahead
 - Predict which action to take by looking only at the symbols currently on the stack
- LR(k) parsers
 - Can look ahead k symbols
 - Most powerful class of deterministic bottom-up parsers
 - LR(I) and variants are the most common parsers

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Terminology for LR parsers

• Configuration: a production augmented with a "•"

$$A \rightarrow X_1 \dots X_i \bullet X_{i+1} \dots X_i$$

- The "•" marks the point to which the production has been recognized. In this case, we have recognized X₁ ... X_i
- Configuration set: all the configurations that can apply at a given point during the parse:

$$A \rightarrow B \cdot CD$$

$$A \rightarrow B \cdot GH$$

$$T \rightarrow B \cdot Z$$

 Idea: every configuration in a configuration set is a production that can possibly be matched

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Configuration closure set

 Include all the configurations necessary to recognize the next symbol after the •

closure0(configuration set) defined on page 146

• Example:



closure0($(S \rightarrow \cdot E \$)$) = { $S \rightarrow \cdot E \$$ $E \rightarrow \cdot E + T$ $E \rightarrow \cdot T$ $T \rightarrow \cdot |D$ $T \rightarrow \cdot (E)$

Successor configuration set

Starting with the initial configuration set

$$s0 = closure0(\{S \rightarrow \bullet \alpha \$\})$$

an LR(0) parser will find the successor given the next symbol \boldsymbol{X}

- X can be either a terminal (the next token from the scanner) or a non-terminal (the result of applying a reduction)
- Determining the successor s' = go_to0(s, X):
 - For each configuration in s of the form A \rightarrow B X γ add A \rightarrow B X γ to t
 - s' = closure0(t)

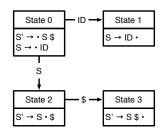
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CFSM

- CFSM = Characteristic Finite State Machine
- Nodes are configuration sets (starting from s0)
- Arcs are go_to relationships





Building the goto table

• We can just read this off from the CFSM

		Symbol		
		ID	\$	S
State	0	- 1		2
	- 1			
	2		3	
	3			

Building the action table

- Given the configuration set s:
 - We shift if the next token matches a terminal after the in some configuration

$$A \rightarrow \alpha \cdot a \ \beta \in s \ and \ a \in V_t$$
, else error

• We reduce production P if the • is at the end of a production

$$B \to \alpha \bullet \in s$$
 where production P is $B \to \alpha$

- Extra actions:
 - shift if goto table transitions between states on a nonterminal
 - accept if we are about to shift \$

Action table

		Symbol		
		D	\$	S
	0	S		S
State	1	R2	R2	R2
	2		Α	
	3			

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Conflicts in action table

- For LR(0) grammars, the action table entries are unique: from each state, can only shift or reduce
- But other grammars may have conflicts
 - Reduce/reduce conflicts: multiple reductions possible from the given configuration
 - Shift/reduce conflicts: we can either shift or reduce from the given configuration

Shift/reduce example

• Consider the following grammar:

$$S \rightarrow A y$$

$$A \rightarrow \lambda \mid x$$

This leads to the following initial configuration set:

$$S \rightarrow \bullet A y$$

$$A \rightarrow \cdot x$$

$$A \rightarrow \lambda$$

• Can shift or reduce here

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Lookahead

- Can resolve reduce/reduce conflicts and shift/reduce conflicts by employing lookahead
 - Looking ahead one (or more) tokens allows us to determine whether to shift or reduce
 - (cf how we resolved ambiguity in LL(1) parsers by looking ahead one token)

Semantic actions

- Recall: in LL parsers, we could integrate the semantic actions with the parser
 - Why? Because the parser was predictive
- Why doesn't that work for LR parsers?
 - Don't know which production is matched until parser reduces
- For LR parsers, we put semantic actions at the end of productions
 - May have to rewrite grammar to support all necessary semantic actions

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Parsers with lookahead

- Adding lookahead creates an LR(I) parser
 - Built using similar techniques as LR(0) parsers, but uses lookahead to distinguish states
 - LR(I) machines can be much larger than LR(0) machines, but resolve many shift/reduce and reduce/ reduce conflicts
 - Other types of LR parsers are SLR(I) and LALR(I)
 - · Differ in how they resolve ambiguities
 - yacc and bison produce LALR(I) parsers

LR(I) parsing

 Configurations in LR(1) look similar to LR(0), but they are extended to include a lookahead symbol

$$A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_j$$
, I (where $I \in V_t \cup \lambda$)

 If two configurations differ only in their lookahead component, we combine them

$$A \rightarrow X_1 \dots X_i \bullet X_{i+1} \dots X_j$$
, $\{I_1 \dots I_m\}$

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Building configuration sets

• To close a configuration

$$B \rightarrow \alpha \cdot A \beta, I$$

- Add all configurations of the form $A \rightarrow \bullet \gamma$, u where $u \in First(\beta I)$
- Intuition: the parse could apply the production for A, and the lookahead after we apply the production should match the next token that would be produced by B



closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$



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Example

closure I ({S
$$\rightarrow$$
 • E \$, { λ }}) = S \rightarrow • E \$, { λ }





Example

closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$	
S → • E \$, {λ}	
E → • E + T, {\$	

Example

closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$	
	$S \rightarrow \bullet E \$, \{\lambda\}$
	E → • E + T, {\$}
	E → • T, {\$}





closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$	
	$S \rightarrow \bullet E \$, \{\lambda\}$
	E → • E + T, {\$}
	E → • T, {\$}
	T → • ID, {\$}

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Example



closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$
S → • E \$, {λ}
E → • E + T, {\$}
E → • T, {\$}
T → • ID, {\$}
T → • (E), {\$}



Example

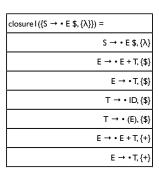
closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$		
	$S \rightarrow \bullet E \$, \{\lambda\}$	
	E → • E + T, {\$}	
	E → • T, {\$}	
	T → • ID, {\$}	
	T → • (E), {\$}	
	E → • E + T, {+}	

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Example







Example

closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}\) =$		
	$S \rightarrow \bullet E \$, \{\lambda\}$	
	E → • E + T, {\$}	
	E → • T, {\$}	
	T → • ID, {\$}	
	T → • (E), {\$}	
	E → • E + T, {+}	
	E → • T, {+}	
	T → • ID, {+}	

Example



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closure I ($\{S \rightarrow \bullet E \$, \{\lambda\}\}$	}) =
	$S \rightarrow \bullet E \$, \{\lambda\}$
	E → • E + T, {\$}
	E → • T, {\$}
	T → • ID, {\$}
	T → • (E), {\$}
	E → • E + T, {+}
	E → • T, {+}
	T → • ID, {+}
	T → • (E), {+}
	·

Building goto and action tables

- The function gotol (configuration-set, symbol) is analogous to gotol(configuration-set, symbol) for LR(0)
 - Build goto table in the same way as for LR(0)
- Key difference: the action table.

action[s][x] =

 reduce when • is at end of configuration and x ∈ lookahead set of configuration

$$A \rightarrow \alpha \bullet, \{... \times ...\} \in s$$

• shift when • is before x

$$A \rightarrow \beta \cdot x \gamma \in s$$

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Problems with LR(I) parsers

- LR(I) parsers are very powerful ...
 - But the table size is much larger than LR(0) as much as a factor of $|V_t|$ (why?)
 - Example: Algol 60 (a simple language) includes several thousand states!
- Storage efficient representations of tables are an important issue

Solutions to the size problem

- Different parser schemes
 - SLR (simple LR): build an CFSM for a language, then add lookahead wherever necessary (i.e., add lookahead to resolve shift/reduce conflicts)
 - What should the lookahead symbol be?
 - To decide whether to reduce using production A → α, use Follow(A)
 - LALR: merge LR states in certain cases (we won't discuss this)

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