

Announcements

- You may optionally work with a partner on the project
 - Must work with the partner for the entire project
- Let me know by next Thursday who you are working with (if anyone), and under which username you will be submitting
- I'm trying to get the lectures posted online at least a day before class (some days I'm more successful than others!)

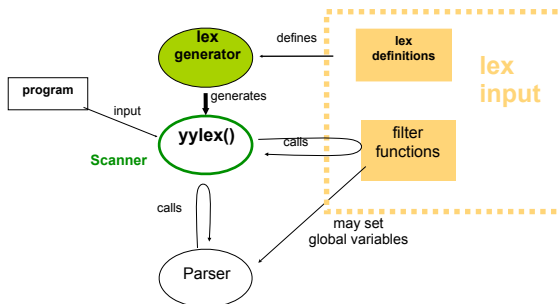
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From last time: Lex (Flex)

- Commonly used Unix scanner generator (superseded by Flex)
- Has character classes and regular expressions like ScanGen but some key differences:
 - After each token is matched, calls user-defined "filter" function, which processes identified token before returning it to parser
 - Hence, no "Toss" facility (why?)
- No exception list
- Instead, supports matching multiple regexps.
 - Matches longest token (i.e., doesn't think `if` is `IF` `ID(a)`)
 - In case of tie, returns earliest-defined regexp
 - To treat `if` as a reserved word instead of an identifier, define token `IF` before defining identifiers.

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Lex operation



Example of Lex input on page 67 of textbook

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Parsers

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Agenda

- Terminology
- LL(1) Parsers
- Overview of LR Parsing

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Terminology

- Grammar $G = (V_t, V_n, S, P)$
 - V_t is the set of **terminals**
 - V_n is the set of **non-terminals**
 - S is the **start symbol**
 - P is the set of **productions**
 - Each production takes the form: $V_n \rightarrow \lambda \mid (V_n \mid V_t)^+$
 - Grammar is **context-free** (why?)
- A simple grammar:
 $G = (\{a, b\}, \{S, A, B\}, \{S \rightarrow A B \$, A \rightarrow A a, A \rightarrow a, B \rightarrow B b, B \rightarrow b\}, S)$

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Terminology

- V is the *vocabulary* of a grammar, consisting of terminal (V_t) and non-terminal (V_n) symbols
- For our sample grammar
 - $V_n = \{S, A, B\}$
 - Non-terminals are symbols on the LHS of a production
 - Non-terminals are constructs in the language that are recognized during parsing
 - $V_t = \{a, b\}$
 - Terminals are the tokens recognized by the scanner
 - They correspond to symbols in the text of the program

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Terminology

- Productions (rewrite rules) tell us how to derive strings in the language
 - Apply productions to rewrite strings into other strings
- We will use the standard BNF form
- $P = \{$
 - $S \rightarrow A B \$$
 - $A \rightarrow A a$
 - $A \rightarrow a$
 - $B \rightarrow B b$
 - $B \rightarrow b$
- $\}$

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Generating strings

$S \rightarrow A B \$$

$A \rightarrow A a$

$A \rightarrow a$

$B \rightarrow B b$

$B \rightarrow b$

- Given a start rule, productions tell us how to rewrite a non-terminal into a different set of symbols
- By convention, first production applied has the start symbol on the left, and there is only one such production

To derive the string "a a b b b" we can do the following rewrites:

$S \Rightarrow A B \$ \Rightarrow A a B \$ \Rightarrow a a B \$ \Rightarrow a a B b \$ \Rightarrow a a B b b \$ \Rightarrow a a b b b \$$

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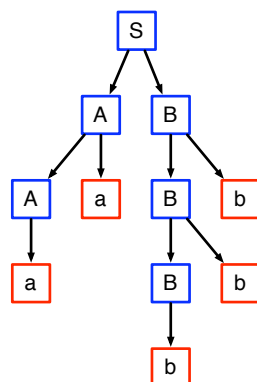
Terminology

- *Strings* are composed of symbols
 - $A A a a B b b A a$ is a string
 - We will use Greek letters to represent strings composed of both terminals and non-terminals
- $L(G)$ is the language produced by the grammar G
 - All strings consisting of only terminals that can be produced by G
 - In our example, $L(G) = a^+b^+ \$$
 - All regular expressions can be expressed as grammars for context-free languages, but not vice-versa
 - Consider: $a^i b^j \$$ (what is the grammar for this?)

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Parse trees

- Tree which shows how a string was produced by a language
- Interior nodes of tree: non-terminals
 - Children: the terminals and non-terminals generated by applying a production rule
- Leaf nodes: terminals



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Leftmost derivation

- Rewriting of a given string starts with the leftmost symbol
- Exercise: do a leftmost derivation of the input program

$F(V + V)$

using the following grammar:

E	\rightarrow	Prefix (E)
E	\rightarrow	V Tail
Prefix	\rightarrow	F
Prefix	\rightarrow	λ
Tail	\rightarrow	$+ E$
Tail	\rightarrow	λ

- What does the parse tree look like?

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Rightmost derivation

- Rewrite using the rightmost non-terminal, instead of the left
- What is the rightmost derivation of this string?

$F(V + V)$

E	→ Prefix (E)
E	→ V Tail
Prefix	→ F
Prefix	→ λ
Tail	→ + E
Tail	→ λ

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Top-down vs. Bottom-up parsers

- Top-down parsers use left-most derivation
- Bottom-up parsers use right-looking parse
- Notation:
 - LL(1): Leftmost derivation with 1 symbol lookahead
 - LL(k): Leftmost derivation with k symbols lookahead
 - LR(1): Right-looking derivation with 1 symbol lookahead

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Micro in standard BNF

```

1 Program      ::= BEGIN Statement-list END
2 Statement-list ::= Statement StatementTail
3 StatementTail ::= Statement StatementTail
4 StatementTail ::=  $\lambda$ 
5 Statement    ::= ID := Expression ;
6 Statement    ::= READ ( Id-list ) ;
7 Statement    ::= WRITE ( Expr-list ) ;
8 Id-list      ::= ID IdTail
9 IdTail       ::= , ID IdTail
10 IdTail      ::=  $\lambda$ 
11 Expr-list   ::= Expression ExprTail
12 ExprTail    ::= , Expression ExprTail
13 ExprTail    ::=  $\lambda$ 
14 Expression  ::= Primary PrimaryTail
15 PrimaryTail ::= Add-op Primary PrimaryTail
16 PrimaryTail ::=  $\lambda$ 
17 Primary     ::= ( Expression )
18 Primary     ::= ID
19 Primary     ::= INTLITERAL
20 Add-op      ::= PLUSOP
21 Add-op      ::= MINUSOP
22 System-goal ::= Program SCANEOP
    
```

Compare this to grammar
in lecture 2

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Micro in standard BNF

```

1 Program      ::= BEGIN Statement-list END
2 Statement-list ::= Statement StatementTail
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11 Expr-list   ::= Expression ExprTail
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20 Add-op      ::= PLUSOP
21 Add-op      ::= MINUSOP
22 System-goal ::= Program SCANEOP
    
```

$A ::= B \mid C$
 \downarrow
 $A ::= B$
 $A ::= C$

Compare this to grammar
in lecture 2

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Micro in standard BNF

```

1 Program      ::= BEGIN Statement-list END
2 Statement-list ::= Statement StatementTail
3 StatementTail ::= Statement StatementTail
4 StatementTail ::=  $\lambda$ 
5 Statement    ::= ID := Expression ;
6 Statement    ::= READ ( Id-list ) ;
7 Statement    ::= WRITE ( Expr-list ) ;
8 Id-list      ::= ID IdTail
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10 IdTail      ::=  $\lambda$ 
11 Expr-list   ::= Expression ExprTail
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16 PrimaryTail ::=  $\lambda$ 
17 Primary     ::= ( Expression )
18 Primary     ::= ID
19 Primary     ::= INTLITERAL
20 Add-op      ::= PLUSOP
21 Add-op      ::= MINUSOP
22 System-goal ::= Program SCANEOP
    
```

$A ::= B \mid C$
 \downarrow
 $A ::= B$
 $A ::= C$

$A ::= B \{C\}$
 \downarrow
 $A ::= B \text{ tail}$
 $\text{tail} ::= C \text{ tail}$
 $\text{tail} ::= \lambda$

Compare this to grammar
in lecture 2

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What is parsing

- Parsing is recognizing members in a language specified/defined/generated by a grammar
- When a construct (corresponding to a production in a grammar) is recognized, a typical parser will take some action
 - In a compiler, this action generates an intermediate representation of the program construct
 - In an interpreter, this action might be to perform the action specified by the construct. Thus, if $a+b$ is recognized, the value of a and b would be added and placed in a temporary variable

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Another simple grammar

PROGRAM \rightarrow **begin** STMTLIST \$

STMTLIST \rightarrow STMT ; STMTLIST

STMTLIST \rightarrow **end**

STMT \rightarrow **id**

STMT \rightarrow **if (id)** STMTLIST

- A sentence in the grammar:
begin if (id) if (id) id ; end; end; end; \$
- What are the terminals and non-terminals of this grammar?

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Parsing this grammar

PROGRAM \rightarrow **begin** STMTLIST \$

STMTLIST \rightarrow STMT ; STMTLIST

STMTLIST \rightarrow **end**

STMT \rightarrow **id**

STMT \rightarrow **if (id)** STMTLIST

- Note
 - To parse STMT in STMTLIST \rightarrow STMT ; STMTLIST, it is necessary to parse either STMT \rightarrow **id** or STMT \rightarrow **if ...**
 - Choose the production to parse by finding out if next token is **if** or **id**
 - i.e., which production the next input token matches
 - This is the **first** set of the production

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Another example

$S \rightarrow A B \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow \lambda$

$B \rightarrow b$

- Consider $S \Rightarrow A B \$ \Rightarrow x a A B \$ \Rightarrow x a B \$ \Rightarrow x a b \$$
- When parsing $x a b \$$ we know from the goal production we need to match an A. The next token is **x**, so we apply $A \rightarrow x a A$
- The parser matches **x**, matches **a** and now needs to parse A again
- How do we know which A to use? We need to use $A \rightarrow \lambda$
 - When matching the right hand side of $A \rightarrow \lambda$, the next token comes from a non-terminal that follows A (i.e., it must be **b**)
 - Tokens that can follow A are called the **follow** set of A

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First and follow sets

- First(α): the set of terminals that begin all strings that can be derived from α

• First(A) = {x, y}

• First(xaA) = {x}

• First(AB) = {x, y, b}

- Follow(A): the set of terminals that can appear immediately after A in some partial derivation

• Follow(A) = {b}

$S \rightarrow A B \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow \lambda$

$B \rightarrow b$

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First and follow sets

- First(α) = $\{a \in V_t \mid \alpha \Rightarrow^* a\beta\} \cup \{\lambda \mid \text{if } \alpha \Rightarrow^* \lambda\}$
- Follow(A) = $\{a \in V_t \mid S \Rightarrow^+ \dots Aa \dots\} \cup \{\$ \mid \text{if } S \Rightarrow^+ \dots A \$\}$

S: start symbol
a: a terminal symbol
A: a non-terminal symbol
 α, β : a string composed of terminals and non-terminals (typically, α is the RHS of a production)

\Rightarrow : derived in 1 step

\Rightarrow^* : derived in 0 or more steps

\Rightarrow^+ : derived in 1 or more steps

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Computing first sets

- Terminal: First(a) = {a}
- Non-terminal: First(A)
 - Look at all productions for A
 $A \rightarrow X_1 X_2 \dots X_k$
 - First(A) \supseteq (First(X_1) - λ)
 - If $\lambda \in \text{First}(X_1)$, First(A) \supseteq (First(X_2) - λ)
 - If λ is in First(X_i) for all i, then $\lambda \in \text{First}(A)$
- Computing First(α): similar procedure to computing First(A)

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Exercise

- What are the first sets for all the non-terminals in following grammar:

$S \rightarrow A B \$$
 $A \rightarrow x a A$
 $A \rightarrow y a A$
 $A \rightarrow \lambda$
 $B \rightarrow b$

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Computing follow sets

- $\text{Follow}(S) = \{\$ \}$
- To compute $\text{Follow}(A)$:
 - Find productions which have A on rhs. Three rules:
 - $X \rightarrow \alpha A \beta$: $\text{Follow}(A) \supseteq (\text{First}(\beta) - \lambda)$
 - $X \rightarrow \alpha A \beta$: If $\lambda \in \text{First}(\beta)$, $\text{Follow}(A) \supseteq \text{Follow}(X)$
 - $X \rightarrow \alpha A$: $\text{Follow}(A) \supseteq \text{Follow}(X)$
- Note: $\text{Follow}(X)$ never has λ in it.

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Exercise

- What are the follow sets for

$S \rightarrow A B \$$
 $A \rightarrow x a A$
 $A \rightarrow y a A$
 $A \rightarrow \lambda$
 $B \rightarrow b$

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Towards parser generators

- Key problem: as we read the source program, we need to decide what productions to use
- Step 1: find the tokens that can tell which production P (of the form $A \rightarrow X_1 X_2 \dots X_m$) applies

$\text{Predict}(P) =$

$$\begin{cases} \text{First}(X_1 \dots X_m) & \text{if } \lambda \notin \text{First}(X_1 \dots X_m) \\ (\text{First}(X_1 \dots X_m) - \lambda) \cup \text{Follow}(A) & \text{otherwise} \end{cases}$$

- If next token is in $\text{Predict}(P)$, then we should choose this production

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Parse tables

- Step 2: build a parse table
 - Given some non-terminal V_n (the non-terminal we are currently processing) and a terminal V_t (the lookahead symbol), the parse table tells us which production P to use (or that we have an error)
- More formally:
 $T: V_n \times V_t \rightarrow P \cup \{\text{Error}\}$

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Building the parse table

- Start: $T[A][t] = \text{//initialize all fields to "error"}$
foreach A:
 foreach P with A on its lhs:
 foreach t in $\text{Predict}(P)$:
 $T[A][t] = P$
- Exercise: build parse table for our toy grammar

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

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Recursive-descent parsers

- Given the parse table, we can create a program which generates recursive descent parsers
- Remember the recursive descent parser we saw for MICRO
- If the choice of production is not unique, the parse table tells us which one to take
- However, there is an easier method!

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Stack-based parser for LL(1)

- Given the parse table, a stack-based algorithm is much simpler to generate than a recursive descent parser

- Basic algorithm:

1. Push the RHS of a production onto the stack
2. Pop a symbol, if it is a terminal, match it
3. If it is a non-terminal, take its production according to the parse table and go to 1

- Algorithm on page 121
- Note: always start with start state

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An example

- How would a stack-based parser parse:

x a y a b

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	x a y a b \$	predict 1

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An example

- How would a stack-based parser parse:

x a y a b

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	x a y a b \$	predict 1
A B \$	x a y a b \$	predict 2

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An example

- How would a stack-based parser parse:

x a y a b

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	x a y a b \$	predict 1
A B \$	x a y a b \$	predict 2
x a A B \$	x a y a b \$	match(x)

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An example

- How would a stack-based parser parse:

x a y a b

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	x a y a b \$	predict 1
A B \$	x a y a b \$	predict 2
x a A B \$	x a y a b \$	match(x)
a A B \$	a y a b \$	match(a)

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3
$y a A B \$$	$y a b \$$	match(y)

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3
$y a A B \$$	$y a b \$$	match(y)
a A B \$	a b \$	match(a)

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3
$y a A B \$$	$y a b \$$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3
$y a A B \$$	$y a b \$$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
B \$	b \$	predict 5

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An example

- How would a stack-based parser parse:

$x a y a b$

1. $S \rightarrow A B \$$
2. $A \rightarrow x a A$
3. $A \rightarrow y a A$
4. $A \rightarrow \lambda$
5. $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	$x a y a b \$$	predict 1
A B \$	$x a y a b \$$	predict 2
$x a A B \$$	$x a y a b \$$	match(x)
$a A B \$$	$a y a b \$$	match(a)
A B \$	$y a b \$$	predict 3
$y a A B \$$	$y a b \$$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
B \$	b \$	predict 5
b \$	b \$	match(b)

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An example

- How would a stack-based parser parse:

$x a y a b$

- $S \rightarrow A B \$$
- $A \rightarrow x a A$
- $A \rightarrow y a A$
- $A \rightarrow \lambda$
- $B \rightarrow b$

Parse stack	Remaining input	Parser action
S	x a y a b \$	predict 1
A B \$	x a y a b \$	predict 2
x a A B \$	x a y a b \$	match(x)
a A B \$	a y a b \$	match(a)
A B \$	y a b \$	predict 3
y a A B \$	y a b \$	match(y)
a A B \$	a b \$	match(a)
A B \$	b \$	predict 4
B \$	b \$	predict 5
b \$	b \$	match(b)
\$	\$	Done!

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LL(k) parsers

- Can use similar techniques for LL(k) parsers
- Use more than one symbol of look-ahead to distinguish productions
- Why might this be bad?

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Dealing with semantic actions

- Recall: we can annotate a grammar with *action symbols*
 - Tell the parser to invoke a semantic action routine
- Can simply push action symbols onto stack as well
- When popped, the semantic action routine is called

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Non-LL(1) grammars

- Not all grammars are LL(1)!
- Consider
 - $\langle \text{stmt} \rangle \rightarrow \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt list} \rangle \text{ endif}$
 - $\langle \text{stmt} \rangle \rightarrow \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt list} \rangle \text{ else } \langle \text{stmt list} \rangle \text{ endif}$
- This is not LL(1) (why?)
- We can turn this in to
 - $\langle \text{stmt} \rangle \rightarrow \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt list} \rangle \langle \text{if suffix} \rangle$
 - $\langle \text{if suffix} \rangle \rightarrow \text{endif}$
 - $\langle \text{if suffix} \rangle \rightarrow \text{else } \langle \text{stmt list} \rangle \text{ endif}$

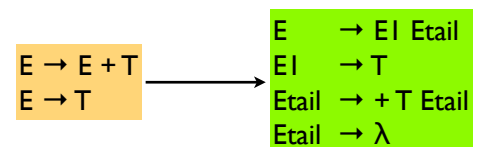
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Left recursion

- Left recursion** is a problem for LL(1) parsers
 - LHS is also the first symbol of the RHS
- Consider:
 - $E \rightarrow E + T$
- What would happen with the stack-based algorithm?

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Removing left recursion



Algorithm on page 125

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Are all grammars LL(1)?

- No! Consider the if-then-else problem
- if x then y else z
- Problem: else is optional
- if a then if b then c else d
 - Which if does the else belong to?
- This is analogous to a “bracket language”: “[]” ($i \geq j$)

$S \rightarrow [S C$
 $S \rightarrow \lambda$
 $C \rightarrow]$
 $C \rightarrow \lambda$

[] can be parsed: $SS\lambda C$ or $SSC\lambda$
(it's ambiguous!)

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Solving the if-then-else problem

- The ambiguity exists at the language level. To fix, we need to define the semantics properly
- “[]” matches nearest unmatched “[”
- This is the rule C uses for if-then-else
- What if we try this?

$S \rightarrow [S$
 $S \rightarrow S I$
 $S I \rightarrow [S I]$
 $S I \rightarrow \lambda$

This grammar is still not LL(1)
(or LL(k) for any k!)

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Two possible fixes

- If there is an ambiguity, prioritize one production over another
- e.g., if C is on the stack, always match “[” before matching “[”

$S \rightarrow [S C$
 $S \rightarrow \lambda$
 $C \rightarrow]$
 $C \rightarrow \lambda$

- Another option: change the language!
- e.g., all if-statements need to be closed with an endif

$S \rightarrow \text{if } S E$
 $S \rightarrow \text{other}$
 $E \rightarrow \text{else } S \text{ endif}$
 $E \rightarrow \text{endif}$

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Parsing if-then-else

- What if we don't want to change the language?
- C does not require { } to delimit single-statement blocks
- To parse if-then-else, we need to be able to look ahead at the entire rhs of a production before deciding which production to use
- In other words, we need to determine how many “[” to match before we start matching “[”s
- LR parsers can do this!

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LR Parsers

- Parser which does a Left-to-right, Right-most derivation
- Rather than parse top-down, like LL parsers do, parse bottom-up, starting from leaves
- Basic idea: put tokens on a stack until an entire production is found
- Issues:
 - Recognizing the endpoint of a production
 - Finding the length of a production (RHS)
 - Finding the corresponding nonterminal (the LHS of the production)

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Data structures

- At each state, given the next token,
 - A goto table defines the successor state
 - An action table defines whether to
 - shift – put the next state and token on the stack
 - reduce – an RHS is found; process the production
 - terminate – parsing is complete

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Example

- Consider the simple grammar:
 - `<program>` \rightarrow `begin <stmts> end $`
 - `<stmts>` \rightarrow `SimpleStmt ; <stmts>`
 - `<stmts>` \rightarrow `begin <stmts> end ; <stmts>`
 - `<stmts>` $\rightarrow \lambda$
- Shift-reduce driver algorithm on page 142

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Action and goto tables

	begin	end	;	SimpleStmt	\$	<program>	<stmts>
0	S / 1						
1	S / 4	R4		S / 5			S / 2
2		S / 3					
3					A		
4	S / 4	R4		S / 5			S / 7
5			S / 6				
6	S / 4	R4		S / 5			S / 10
7		S / 8					
8			S / 9				
9	S / 4	R4		S / 6			S / 11
10		R2					
11		R3					

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Example

- Parse: `begin SimpleStmt ; SimpleStmt ; end $`

Step	Parse Stack	Remaining Input	Parser Action
1	0	begin S ; S ; end \$	Shift 1
2	0 1	S ; S ; end \$	Shift 5
3	0 1 5	; S ; end \$	Shift 6
4	0 1 5 6	S ; end \$	Shift 5
5	0 1 5 6 5	; end \$	Shift 6
6	0 1 5 6 5 6	end \$	Reduce 4 (goto 10)
7	0 1 5 6 5 6 10	end \$	Reduce 2 (goto 10)
8	0 1 5 6 10	end \$	Reduce 2 (goto 2)
9	0 1 2	end \$	Shift 3
10	0 1 2 3	\$	Accept

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Announcements

- I will be out of town on Tuesday (9/15)
- Class will be covered by Professor Midkiff

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LR Parsers

- Basic idea:
 - shift** tokens onto the stack. At any step, keep the set of productions that could generate the read-in tokens
 - reduce** the RHS of recognized productions to the corresponding non-terminal on the LHS of the production. Replace the RHS tokens on the stack with the LHS non-terminal.

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LR(k) parsers

- LR(0) parsers
 - No lookahead
- Predict which action to take by looking only at the symbols currently on the stack
- LR(k) parsers
 - Can look ahead k symbols
 - Most powerful class of deterministic bottom-up parsers
 - LR(1) and variants are the most common parsers

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Terminology for LR parsers

- Configuration: a production augmented with a “•”
 $A \rightarrow X_1 \dots X_i \bullet X_{i+1} \dots X_j$
- The “•” marks the point to which the production has been recognized. In this case, we have recognized $X_1 \dots X_i$
- Configuration set: all the configurations that can apply at a given point during the parse:
 $A \rightarrow B \bullet CD$
 $A \rightarrow B \bullet GH$
 $T \rightarrow B \bullet Z$
- Idea: every configuration in a configuration set is a production that can possibly be matched

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Configuration closure set

- Include all the configurations necessary to recognize the next symbol after the •

$\text{closure0}(\text{configuration_set})$ defined on page 146

- Example:

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

$\text{closure0}(\{S \rightarrow \bullet E \$\}) = \{$
 $S \rightarrow \bullet E \$$
 $E \rightarrow \bullet E + T$
 $E \rightarrow \bullet T$
 $T \rightarrow \bullet ID$
 $T \rightarrow \bullet (E)$
 $\}$

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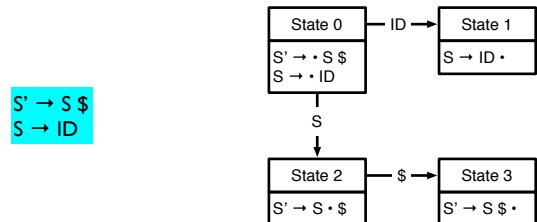
Successor configuration set

- Starting with the initial configuration set
 $s_0 = \text{closure0}(\{S \rightarrow \bullet \alpha \$\})$
 an LR(0) parser will find the successor given the next symbol X
- X can be either a terminal (the next token from the scanner) or a non-terminal (the result of applying a reduction)
- Determining the successor $s' = \text{go_to0}(s, X)$:
 - For each configuration in s of the form $A \rightarrow \beta \bullet X \gamma$ add $A \rightarrow \beta X \bullet \gamma$ to t
 - $s' = \text{closure0}(t)$

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CFSM

- CFSM = Characteristic Finite State Machine
- Nodes are configuration sets (starting from s_0)
- Arcs are go_to relationships



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Building the goto table

- We can just read this off from the CFSM

		Symbol		
		ID	\$	S
State	0	1		2
	1			
	2		3	
	3			

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Building the action table

- Given the configuration set s :
 - We **shift** if the next token matches a terminal after the • in some configuration
 $A \rightarrow \alpha \bullet a \beta$ and $a \in V_t$, else error
 - We **reduce** production P if the • is at the end of a production
 $B \rightarrow \alpha \bullet$ where production P is $B \rightarrow \alpha$
- Extra actions:
 - shift** if goto table transitions between states on a non-terminal
 - accept** if we are about to shift $\$$

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Action table

		Symbol		
		ID	\$	S
State	0	S		S
	1	R2	R2	R2
	2		A	
	3			

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Alternate representation

- Some books represent goto and action tables differently
- Action table only has columns for terminals, and consists of two kinds of actions:
 - shift + state: shift and move to a state
 - reduce + rule: reduce according to rule
- Goto table only has columns for non-terminals
- Specifies which state to go to after reducing

State	Action		Goto
	ID	\$	S
0	S1		1
1	R2	R2	
2		A	
3			

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Conflicts in action table

- For LR(0) grammars, the action table entries are unique: from each state, can only shift or reduce
- But other grammars may have conflicts
 - Reduce/reduce conflicts: multiple reductions possible from the given configuration
 - Shift/reduce conflicts: we can either shift or reduce from the given configuration

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Shift/reduce example

- Consider the following grammar:

$$S \rightarrow A y$$

$$A \rightarrow \lambda \mid x$$
- This leads to the following initial configuration set:

$$S \rightarrow \cdot A y$$

$$A \rightarrow \cdot x$$

$$A \rightarrow \lambda \cdot$$
- Can shift or reduce here

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Lookahead

- Can resolve reduce/reduce conflicts and shift/reduce conflicts by employing *lookahead*
- Looking ahead one (or more) tokens allows us to determine whether to shift or reduce
- (cf how we resolved ambiguity in LL(1) parsers by looking ahead one token)
- Note that it is possible to create an LR(0) grammar for any LR(k) grammar (as long as we can determine the end of a program), but it may be very complex!

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LR(1) parsing

- Configurations in LR(1) look similar to LR(0), but they are extended to include a lookahead symbol

$$A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_j, l \text{ (where } l \in V_t \cup \lambda \text{)}$$
- If two configurations differ only in their lookahead component, we combine them

$$A \rightarrow X_1 \dots X_i \cdot X_{i+1} \dots X_j, \{l_1 \dots l_m\}$$

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Building configuration sets

- To close a configuration
 $B \rightarrow \alpha \cdot A \beta, l$
- Add all configurations of the form $A \rightarrow \cdot \gamma, u$ where $u \in \text{First}(\beta l)$
- Intuition: the parse could apply the production for A, and the lookahead after we apply the production should match the next token that would be produced by B

Example

closure1($\{S \rightarrow \cdot E \$, \{\lambda\}\}$) =

S → E \$
E → E + T | T
T → ID | (E)

Example

closure1($\{S \rightarrow \cdot E \$, \{\lambda\}\}$) =

S → E \$, {λ}

S → E \$
E → E + T | T
T → ID | (E)

Example

closure1($\{S \rightarrow \cdot E \$, \{\lambda\}\}$) =

S → E \$, {λ}

E → E + T, {\$}

S → E \$
E → E + T | T
T → ID | (E)

Example

closure1($\{S \rightarrow \cdot E \$, \{\lambda\}\}$) =

S → E \$, {λ}

E → E + T, {\$}

E → · T, {\$}

S → E \$
E → E + T | T
T → ID | (E)

Example

closure1($\{S \rightarrow \cdot E \$, \{\lambda\}\}$) =

S → E \$, {λ}

E → E + T, {\$}

E → · T, {\$}

T → · ID, {\$}

S → E \$
E → E + T | T
T → ID | (E)

Example

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

closure($\{S \rightarrow \bullet E \$, \{\lambda\}\}$) =	
$S \rightarrow \bullet E \$, \{\lambda\}$	
$E \rightarrow \bullet E + T, \{\$\}$	
$E \rightarrow \bullet T, \{\$\}$	
$T \rightarrow \bullet ID, \{\$\}$	
$T \rightarrow \bullet (E), \{\$\}$	

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Example

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

closure($\{S \rightarrow \bullet E \$, \{\lambda\}\}$) =	
$S \rightarrow \bullet E \$, \{\lambda\}$	
$E \rightarrow \bullet E + T, \{\$\}$	
$E \rightarrow \bullet T, \{\$\}$	
$T \rightarrow \bullet ID, \{\$\}$	
$T \rightarrow \bullet (E), \{\$\}$	
$E \rightarrow \bullet E + T, \{+\}$	

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Example

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

closure($\{S \rightarrow \bullet E \$, \{\lambda\}\}$) =	
$S \rightarrow \bullet E \$, \{\lambda\}$	
$E \rightarrow \bullet E + T, \{\$\}$	
$E \rightarrow \bullet T, \{\$\}$	
$T \rightarrow \bullet ID, \{\$\}$	
$T \rightarrow \bullet (E), \{\$\}$	
$E \rightarrow \bullet E + T, \{+\}$	
$E \rightarrow \bullet T, \{+\}$	

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Example

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

closure($\{S \rightarrow \bullet E \$, \{\lambda\}\}$) =	
$S \rightarrow \bullet E \$, \{\lambda\}$	
$E \rightarrow \bullet E + T, \{\$\}$	
$E \rightarrow \bullet T, \{\$\}$	
$T \rightarrow \bullet ID, \{\$\}$	
$T \rightarrow \bullet (E), \{\$\}$	
$E \rightarrow \bullet E + T, \{+\}$	
$E \rightarrow \bullet T, \{+\}$	
$T \rightarrow \bullet ID, \{+\}$	

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Example

$S \rightarrow E \$$
 $E \rightarrow E + T \mid T$
 $T \rightarrow ID \mid (E)$

closure($\{S \rightarrow \bullet E \$, \{\lambda\}\}$) =	
$S \rightarrow \bullet E \$, \{\lambda\}$	
$E \rightarrow \bullet E + T, \{\$\}$	
$E \rightarrow \bullet T, \{\$\}$	
$T \rightarrow \bullet ID, \{\$\}$	
$T \rightarrow \bullet (E), \{\$\}$	
$E \rightarrow \bullet E + T, \{+\}$	
$E \rightarrow \bullet T, \{+\}$	
$T \rightarrow \bullet ID, \{+\}$	
$T \rightarrow \bullet (E), \{+\}$	

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Building goto and action tables

- The function **goto**(configuration-set, symbol) is analogous to **goto0**(configuration-set, symbol) for LR(0)
 - Build goto table in the same way as for LR(0)
- Key difference: the action table.
 $action[s][x] =$
 - reduce** when \bullet is at end of configuration and $x \in$ lookahead set of configuration
 $A \rightarrow \alpha \bullet, \{\dots x \dots\} \in s$
 - shift** when \bullet is before x
 $A \rightarrow \beta \bullet x \gamma \in s$

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Problems with LR(I) parsers

- LR(I) parsers are very powerful ...
 - But the table size is much larger than LR(0) — as much as a factor of $|V_t|$ (why?)
 - Example: Algol 60 (a simple language) includes several thousand states!
- Storage efficient representations of tables are an important issue

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Solutions to the size problem

- Different parser schemes
 - SLR (simple LR): build an CFSM for a language, then add lookahead wherever necessary (i.e., add lookahead to resolve shift/reduce conflicts)
 - What should the lookahead symbol be?
 - To decide whether to reduce using production $A \rightarrow \alpha$, use Follow(A)
 - LALR: merge LR states in certain cases (we won't discuss this)

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Semantic actions

- Recall: in LL parsers, we could integrate the semantic actions with the parser
 - Why? Because the parser was *predictive*
- Why doesn't that work for LR parsers?
 - Don't know which production is matched until parser reduces
- For LR parsers, we put semantic actions at the end of productions
 - May have to rewrite grammar to support all necessary semantic actions

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