Loop optimizations

Monday, November 30, 15

Loop optimization

- · Low level optimization
 - Moving code around in a single loop
 - Examples: loop invariant code motion, strength reduction, loop unrolling
- High level optimization
 - Restructuring loops, often affects multiple loops
 - Examples: loop fusion, loop interchange, loop tiling

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Identifying loops

- First, we must identify dominators
 - Node a dominates node b if every possible execution path that gets to b must pass through a
- Many different algorithms to calculate dominators we will not cover how this is calculated
- A back edge is an edge from b to a when a dominates b
- The target of a back edge is a loop header

Agenda

- Low level loop optimizations
 - Code motion
 - Strength reduction
 - Unrolling
- High level loop optimizations
 - Loop fusion
 - Loop interchange
 - Loop tiling

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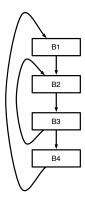
Low level loop optimizations

- Affect a single loop
- Usually performed at three-address code stage or later in compiler
- First problem: identifying loops
 - Low level representation doesn't have loop statements!

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Natural loops

- Will focus on <u>natural loops</u> loops that arise in structured programs
- For a node n to be in a loop with header h
 - n must be dominated by h
 - There must be a path in the CFG from n to h through a back-edge to h
- What are the back edges in the example to the right? The loop headers? The natural loops?



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Loop invariant code motion

- Idea: some expressions evaluated in a loop never change; they are loop invariant
 - Can move loop invariant expressions outside the loop, store result in temporary and just use the temporary in each iteration
 - Why is this useful?

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Identifying loop invariant code

· To determine if a statement

```
s:a = b op c
```

is loop invariant, find all definitions of b and c that reach s

- A statement t defining b reaches s if there is a path from t to s where b is not re-defined
- s is loop invariant if both b and c satisfy one of the following
 - it is constant
 - all definitions that reach it are from outside the loop
 - only one definition reaches it and that definition is also loop invariant

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Moving loop invariant code

Just because code is loop invariant doesn't mean we can move it!

- We can move a loop invariant statement a = b op c if
 - The statement dominates all loop exits where a is live
 - There is only one definition of a in the loop
 - a is not live before the loop
- Move instruction to a <u>preheader</u>, a new block put right before loop header

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Strength reduction

- Like strength reduction peephole optimization
- Peephole: replace expensive instruction like a * 2 with a << 1
- Replace expensive instruction, multiply, with a cheap one, addition
 - Applies to uses of an induction variable
 - Opportunity: array indexing

```
for (i = 0; i < 100; i++)
A[i] = 0;

i = 0;
L2:if (i >= 100) goto L1
    j = 4 * i + &A
    *j = 0;
    i = i + 1;
    goto L2
L1:
```

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Strength reduction

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- Replace expensive instruction, multiply, with a cheap one, addition
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 - Opportunity: array indexing

```
for (i = 0; i < 100; i++)
A[i] = 0;

i = 0; k = &A;
L2:if (i >= 100) goto L1
    j = k;
    *j = 0;
    i = i + 1; k = k + 4;
    goto L2
L1:
```

Induction variables

- A basic induction variable is a variable i
 - whose only definition within the loop is an assignment of the form i = i ± c, where c is loop invariant
 - Intuition: the variable which determines number of iterations is usually an induction variable
- A mutual induction variable j may be
 - defined once within the loop, and its value is a linear function of some other induction variable i such that

```
j = c1 * i \pm c2 \text{ or } j = i/c1 \pm c2
```

where c1, c2 are loop invariant

 A family of induction variables include a basic induction variable and any related mutual induction variables

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Strength reduction algorithm

- Let j be an induction variable in the family of the basic induction variable i, such that j = c1 * i + c2
 - Create a new variable j'
 - Initialize in preheader

$$i' = c1 * i + c2$$

Track value of i. After i = i + c3, perform

$$j' = j' + (c1 * c3)$$

Replace definition of i with

j = j'

 Key: c1, c2, c3 are all loop invariant (or constant), so computations like (c1 * c3) can be moved outside loop

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Linear test replacement

- After strength reduction, the loop test may be the only use of the basic induction variable
- Can now eliminate induction variable altogether
- Algorithm
 - If only use of an induction variable is the loop test and its increment, and if the test is always computed
 - Can replace the test with an equivalent one using one of the mutual induction variables

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Loop unrolling

- Modifying induction variable in each iteration can be expensive
- Can instead unroll loops and perform multiple iterations for each increment of the induction variable
- What are the advantages and disadvantages?

```
for (i = 0; i < N; i++)
A[i] = ...
```

Unroll by factor of 4

for (i = 0; i < N; i += 4)

A[i] = ...A[i+1] = ...

 $A[i+2] = \dots$

 $A[i+3] = \dots$

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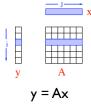
High level loop optimizations

- Many useful compiler optimizations require restructuring loops or sets of loops
 - Combining two loops together (loop fusion)
 - Switching the order of a nested loop (loop interchange)
 - Completely changing the traversal order of a loop (loop tiling)
- These sorts of high level loop optimizations usually take place at the AST level (where loop structure is obvious)

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Cache behavior

- Most loop transformations target cache performance
 - Attempt to increase spatial or temporal locality
 - Locality can be exploited when there is reuse of data (for temporal locality) or recent access of nearby data (for spatial locality)
- Loops are a good opportunity for this: many loops iterate through matrices or arrays
- Consider matrix-vector multiply example
 - Multiple traversals of vector: opportunity for spatial and temporal locality
- Regular access to array: opportunity for spatial locality

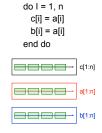


Loop fusion

do I = 1, n c[i] = a[i] end do do I = 1, n b[i] = a[i] end do



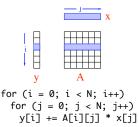
- Combine two loops together into a single loop
- Why is this useful?
- Is this always legal?



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Loop interchange

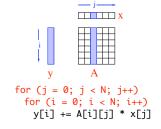
- Change the order of a nested loop
- This is not always legal it changes the order that elements are accessed!
- Why is this useful?
 - Consider matrix-matrix multiply when A is stored in column-major order (i.e., each column is stored in contiguous memory)



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Loop interchange

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- Why is this useful?
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Loop tiling

- Also called "loop blocking"
- for (i = 0; i < N; i++)for (j = 0; j < N; j++)y[i] += A[i][j] * x[j]
- One of the more complex loop transformations
 - Goal: break loop up into for (ii = 0; ii < N; ii += B)
- smaller pieces to get spatial and temporal locality
 - Create new inner loops so that data accessed in inner loops fit in cache
- Also changes iteration order, so may not be legal

for (jj = 0; jj < N; jj += B)for (i = ii; i < ii+B; i++) for (j = jj; j < jj+B; j++)y[i] += A[i][j] * x[j]



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Loop tiling

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- and temporal locality Create new inner loops so that data accessed in inner loops fit in cache

Also changes iteration

order, so may not be legal

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for (i = 0; i < N; i++)

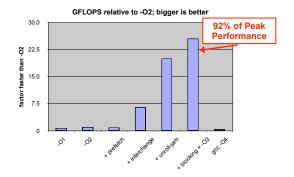
for (j = 0; j < N; j++)

y[i] += A[i][j] * x[j]



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In a real (Itanium) compiler



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Loop transformations

- Loop transformations can have dramatic effects on performance
- Doing this legally and automatically is very difficult!
- Researchers have developed techniques to determine legality of loop transformations and automatically transform the loop
 - Techniques like unimodular transform framework and polyhedral
 - These approaches will get covered in more detail in advanced compilers course
 - In this class, we will see some simple techniques to reason about high-level loop optimizations

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