

Global Register Allocation

(Slides from Andrew Myers)

Monday, October 17, 2011

Main idea

- Want to replace temporary variables with some fixed set of registers
- **First**: need to know which variables are live after each instruction
 - Two simultaneously live variables cannot be allocated to the same register

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Register allocation

- For every node n in CFG, we have $out[n]$
 - Set of temporaries live out of n
- Two variables *interfere* if
 - both initially live (ie: function args), or
 - both appear in $out[n]$ for any n
- How to assign registers to variables?

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Interference graph

- **Nodes** of the graph = variables
- **Edges** connect variables that interfere with one another
- Nodes will be assigned a **color** corresponding to the register assigned to the variable
- Two colors can't be next to one another in the graph

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Interference graph

Instructions	Live vars
$b = a + 2$	
$c = b * b$	
$b = c + 1$	
return $b * a$	

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Interference graph

Instructions	Live vars
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$b = c + 1$	
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Interference graph

Instructions	Live vars
$b = a + 2$	
$c = b * b$	a,c
$b = c + 1$	b,a
return $b * a$	

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Interference graph

Instructions	Live vars
$b = a + 2$	
$c = b * b$	b,a
$b = c + 1$	a,c
return $b * a$	b,a

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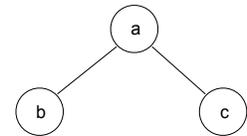
Interference graph

Instructions	Live vars
$b = a + 2$	a
$c = b * b$	b,a
$b = c + 1$	a,c
return $b * a$	b,a

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Interference graph

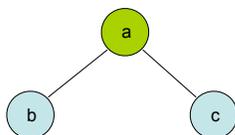
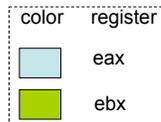
Instructions	Live vars
$b = a + 2$	a
$c = b * b$	a,b
$b = c + 1$	a,c
return $b * a$	a,b



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Interference graph

Instructions	Live vars
$b = a + 2$	a
$c = b * b$	a,b
$b = c + 1$	a,c
return $b * a$	a,b



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Graph coloring

- Questions:
 - Can we efficiently find a coloring of the graph whenever possible?
 - Can we efficiently find the optimum coloring of the graph?
 - How do we choose registers to avoid move instructions?
 - What do we do when there aren't enough colors (registers) to color the graph?

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Coloring a graph

- Kempe's algorithm [1879] for finding a K-coloring of a graph
- Assume $K=3$
- **Step 1 (simplify):** find a node with **at most $K-1$** edges and cut it out of the graph. (Remember this node on a stack for later stages.)

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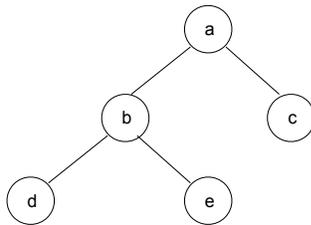
Coloring a graph

- Once a coloring is found for the simpler graph, we can always color the node we saved on the stack
- **Step 2 (color):** when the simplified subgraph has been colored, add back the node on the top of the stack and assign it a color not taken by one of the adjacent nodes

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Coloring

color	register
	eax
	ebx

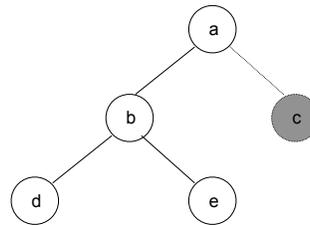


stack:

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Coloring

color	register
	eax
	ebx



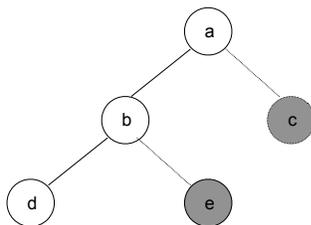
stack:

c

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Coloring

color	register
	eax
	ebx



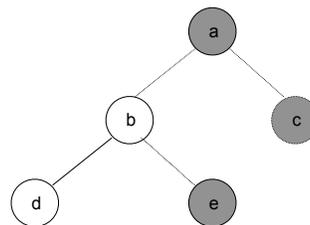
stack:

e
c

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Coloring

color	register
	eax
	ebx



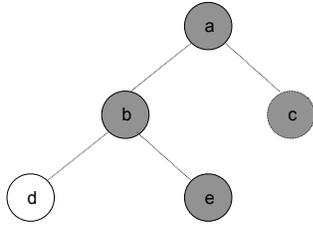
stack:

a
e
c

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Coloring

color	register
	eax
	ebx

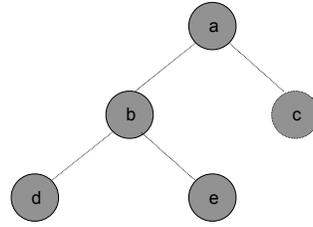


stack:
b
a
e
c

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Coloring

color	register
	eax
	ebx

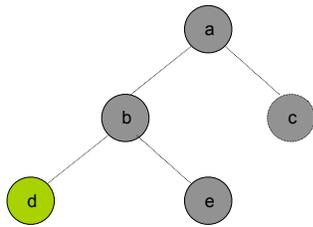


stack:
d
b
a
e
c

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Coloring

color	register
	eax
	ebx

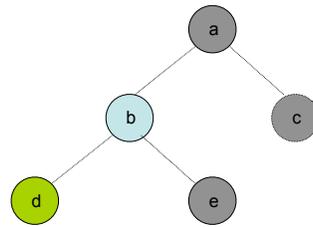


stack:
b
a
e
c

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Coloring

color	register
	eax
	ebx

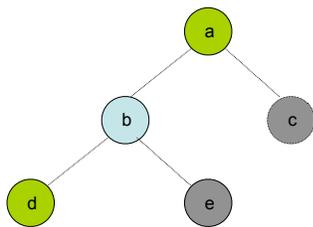


stack:
a
e
c

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Coloring

color	register
	eax
	ebx

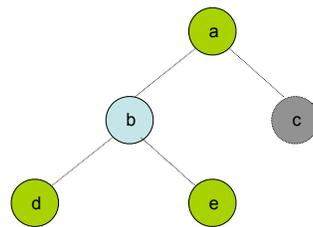


stack:
e
c

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Coloring

color	register
	eax
	ebx

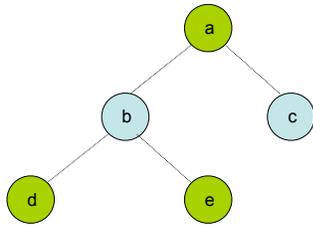


stack:
c

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Coloring

color	register
	eax
	ebx



stack:

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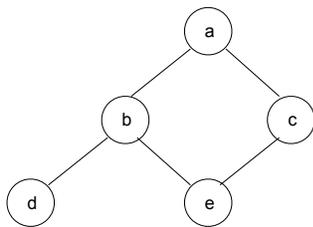
Failure

- If the graph cannot be colored, it will eventually be simplified to graph in which **every node has at least K neighbors**
- Sometimes, the graph is still K-colorable!
- Finding a K-coloring in all situations is an **NP-complete** problem
 - We will have to approximate to make register allocators fast enough

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Coloring

color	register
	eax
	ebx

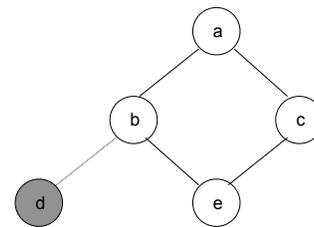


stack:

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Coloring

color	register
	eax
	ebx



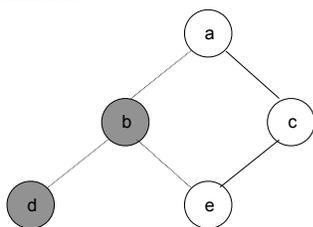
stack:
d

all nodes have
2 neighbours!

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Coloring

color	register
	eax
	ebx



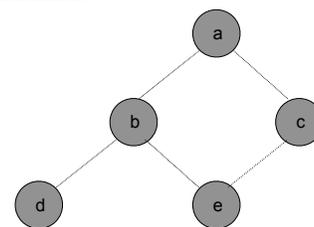
stack:

b
d

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Coloring

color	register
	eax
	ebx

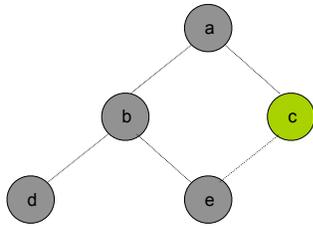


stack:
c
e
a
b
d

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Coloring

color	register
	eax
	ebx

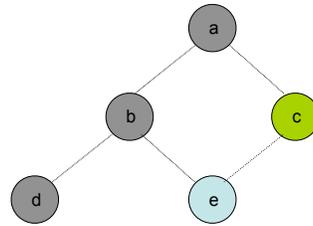


stack:
e
a
b
d

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Coloring

color	register
	eax
	ebx

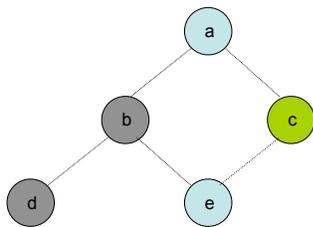


stack:
a
b
d

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Coloring

color	register
	eax
	ebx

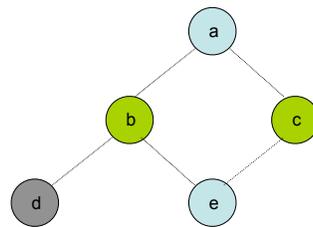


stack:
b
d

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Coloring

color	register
	eax
	ebx

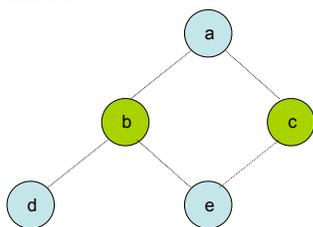


stack:
d

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Coloring

color	register
	eax
	ebx



We got lucky!

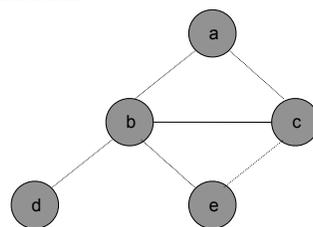
stack:
c
b
e
a
d

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Coloring

color	register
	eax
	ebx

Some graphs can't be colored in K colors:



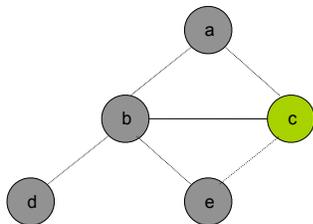
stack:
c
b
e
a
d

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Coloring

color	register
	eax
	ebx

Some graphs can't be colored in K colors:



stack:

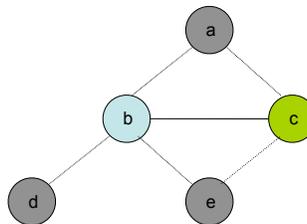
b
e
a
d

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Coloring

color	register
	eax
	ebx

Some graphs can't be colored in K colors:



stack:

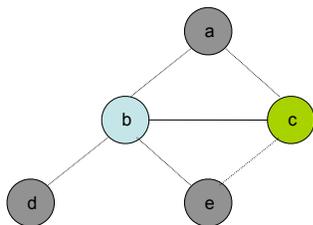
e
a
d

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Coloring

color	register
	eax
	ebx

Some graphs can't be colored in K colors:



stack:

e
a
d

no colors left for e!

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Spilling

- **Step 3 (spilling):** once all nodes have K or more neighbors, pick a node for **spilling**
 - Storage on the stack
- There are many heuristics that can be used to pick a node
 - not in an inner loop

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Spilling code

- We need to generate extra instructions to load variables from stack and store them
- These instructions use registers themselves. What to do?
 - **Stupid approach:** always keep extra registers handy for shuffling data in and out: **what a waste!**
 - **Better approach:** rewrite code introducing a new temporary; rerun liveness analysis and register allocation
 - Intuition: you were not able to assign a single register to the variable that was spilled but there may be a free register available at each spot where you need to use the value of that variable

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Rewriting code

- Consider: **add t1 t2**
 - Suppose **t2** is selected for spilling and assigned to stack location **[ebp-24]**
 - Invent new temporary **t35** for just this instruction and rewrite:
 - **mov t35, [ebp-24];**
 - **add t1, t35**
 - Advantage: **t35** has a very short live range and is much less likely to interfere.
 - Rerun the algorithm; fewer variables will spill

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Precolored Nodes

- Some variables are pre-assigned to registers
 - Eg: mul on x86/pentium
 - uses eax; defines eax, edx
 - Eg: call on x86/pentium
 - Defines (trashes) caller-save registers eax, ecx, edx
- Treat these registers as special temporaries; before beginning, **add them to the graph with their colors**

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Precolored Nodes

- Can't simplify a graph by removing a precolored node
- Precolored nodes are the starting point of the coloring process
- Once simplified down to colored nodes start adding back the other nodes as before

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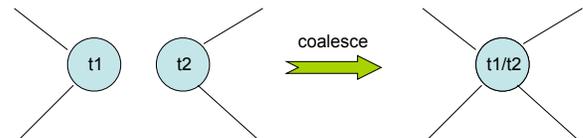
Optimizing Moves

- Code generation produces a lot of extra move instructions
 - mov t1, t2
 - If we can assign t1 and t2 to the same register, we do not have to execute the mov
 - Idea: if t1 and t2 are not connected in the interference graph, we **coalesce** into a single variable

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Coalescing

- Problem: coalescing can increase the number of interference edges and make a graph uncolorable



- Solution 1 (Briggs): avoid creation of high-degree ($\geq K$) nodes
- Solution 2 (George): a can be coalesced with b if every neighbour t of a :
 - already interferes with b , or
 - has low-degree ($< K$)

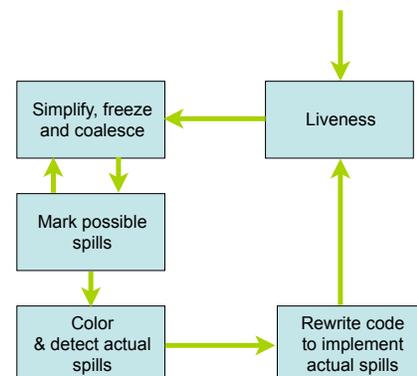
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Simplify & Coalesce

- **Step 1 (simplify)**: simplify as much as possible without removing nodes that are the source or destination of a move (**move-related nodes**)
- **Step 2 (coalesce)**: coalesce move-related nodes provided low-degree node results
- **Step 3 (freeze)**: if neither steps 1 or 2 apply, freeze a move instruction: registers involved are marked **not move-related** and try step 1 again

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Overall Algorithm



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