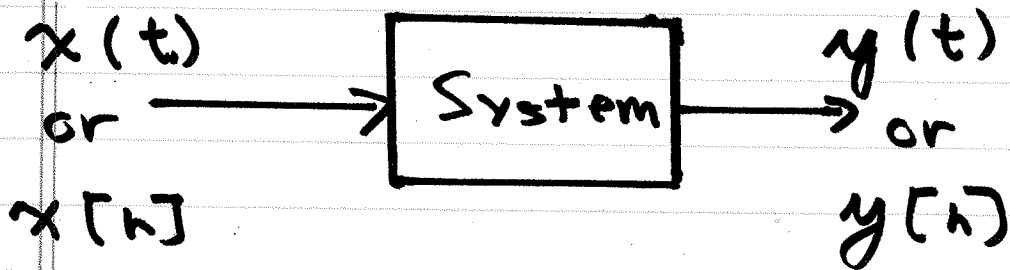
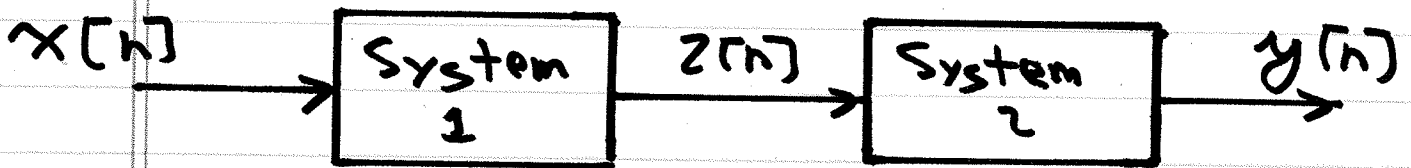


# Systems

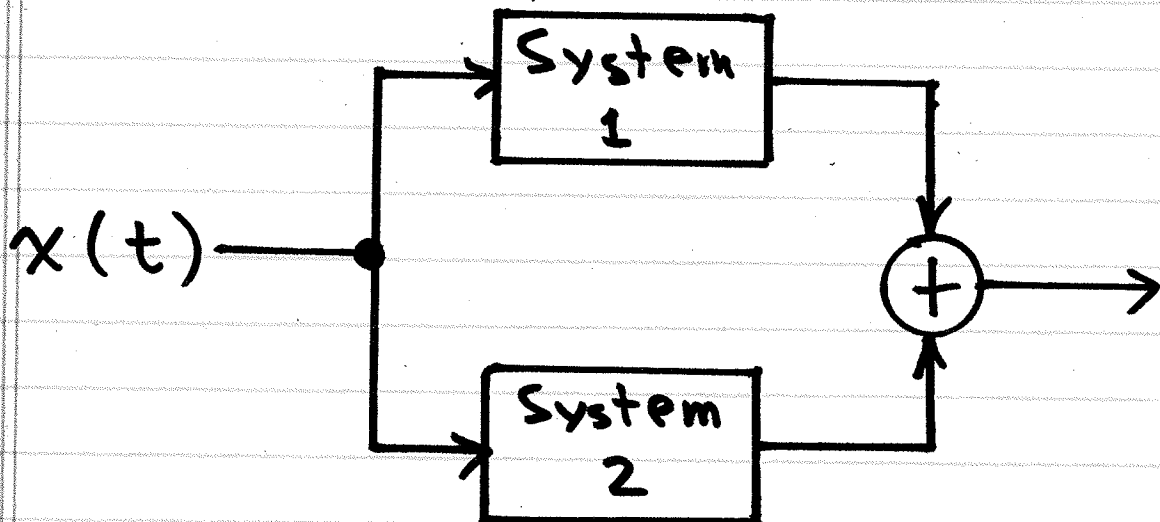
- Take "black-box" viewpoint of systems in this course



- Systems in series:



- Systems in parallel:



# Potential System Properties

Linear:

$$x_i(t) \rightarrow \boxed{S'} \rightarrow y_i(t) \\ i=1,2$$

$$a_1 x_1(t) + a_2 x_2(t) \rightarrow \boxed{S'} \rightarrow a_1 y_1(t) + a_2 y_2(t)$$

Time Invariance

$$x(t) \rightarrow \boxed{S'} \rightarrow y(t)$$

$$x(t-t_0) \rightarrow \boxed{S'} \rightarrow y_{t_0}(t)$$

$$y_{t_0}(t) \stackrel{?}{=} y(t-t_0)$$

Causal:  $y(t)$  does not depend on future (time) values of  $x(t)$ .

Stable:

$$x(t) \rightarrow \boxed{S'} \rightarrow y(t)$$

$$|x(t)| < B_{in} \quad \forall t \quad \text{guarantees} \quad |y(t)| < B_{out} \quad \forall t$$

$$B_{in} \neq \infty \quad B_{out} \neq \infty$$

Memoryless:  $y(t_0)$  only depends on  $x(t_0)$   
true for any  $t_0$

Invertible:  $x(t) \rightarrow \boxed{S'} \rightarrow \underbrace{\boxed{S'^{-1}}}_{\text{inverse system}} \rightarrow x(t)$

for any and all inputs  $x(t)$

inverse system

# CT: Common Systems Encountered in Practice

$$y(t) = \int_{-\infty}^t x(\tau) d\tau$$

Linear and TI  
LTI

or:  $y(t) = \int_{t-T_1}^{t+T_2} x(\tau) d\tau$

LTI

$$y(t) = x^2(t)$$

not L, TI  
nonlinear

$$y(t) = x(at)$$

L, not TI

$$y(t) = g(t)x(t)$$

L, not TI

$$y(t) = \frac{d}{dt} x(t)$$

LTI

$$y(t) = x(t-t_0)$$

LTI

$$y(t) = \begin{cases} x(t), & \text{if } a < x(t) < b \\ b, & \text{if } x(t) > b \\ a, & \text{if } x(t) < a \end{cases}$$

nonlinear  
TI

## DT: Common Systems Encountered in Practice

$$y[n] = \sum_{k=-\infty}^n x[k] \quad \text{LTI}$$

$$y[n] = \sum_{k=n-N_1}^{n+N_2} x[k] \quad \text{LTI}$$

$$y[n] = x^2[n] \quad \text{not L, TI}$$

$$y[n] = x[Ln] \quad \text{L, not TI}$$

$L$  integer

$$y[n] = g[n] x[n] \quad \text{L, not TI}$$

$$y[n] = x[n] - x[n-1] \quad \text{LTI}$$

$$y[n] = x[n - n_0] \quad \text{LTI}$$

Difference Equation

$$y[n] = -\sum_{k=1}^N a_k y[n-k] + \sum_{k=0}^M b_k x[n-k]$$

LTI