

$$h[n] = \left(\frac{1}{5}\right)^n u[n]$$

Prob 2.28

a) - Causal since $h[n] = 0$ for $n < 0$ - stable since $\sum_{n=0}^{\infty} \left(\frac{1}{5}\right)^n = \frac{1}{1 - \frac{1}{5}} = \frac{5}{4} < \infty$ b) - Not Causal since $h[n] \neq 0$ for $n < 0$ - stable since $\sum_{n=-2}^{\infty} (0.8)^n = \frac{1}{1 - 0.8} = \frac{1}{0.2} = 5 < \infty$

$$h[n] = (0.8)^n u[n+2]$$

c) - Not Causal since $h[n] \neq 0$ for $n < 0$ - Unstable since $\sum_{n=-\infty}^0 \left(\frac{1}{2}\right)^n = \infty$

$$h[n] = \left(\frac{1}{2}\right)^n u[-n]$$

$$d) h[n] = (5)^n u[3-n]$$

- Not Causal

- Stable

since $h[n] \neq 0$ for $n < 0$

$$\begin{aligned} \text{since } \sum_{n=-\infty}^3 5^n &= \sum_{n=-3}^{\infty} \left(\frac{1}{5}\right)^n = \left(\frac{1}{5}\right)^{-3} \sum_{n=0}^{\infty} \left(\frac{1}{5}\right)^n \\ &= 5^3 \frac{1}{1 - \frac{1}{5}} = 5^3 \cdot \frac{5}{4} = \frac{625}{4} < \infty \end{aligned}$$

$$e) h[n] = \left(-\frac{1}{2}\right)^n u[n] + (1.01)^n u[n-1]$$

- Causal since $h[n] = 0$ for $n < 0$ - Unstable because $\sum_{n=1}^{\infty} (1.01)^n = \infty$

$$f) h[n] = \left(-\frac{1}{2}\right)^n u[n] + (1.01)^n u[1-n]$$

- Not Causal since $h[n] \neq 0$ for $n < 0$ - Stable since $\sum_{n=-\infty}^{\infty} |h[n]| = \frac{30.5}{3} < \infty$

$$g) h[n] = n \left(\frac{1}{3}\right)^n u[n-1]$$

- Causal since $h[n] = 0$ for $n < 0$ - Stable since $\sum_{n=1}^{\infty} |h[n]| = 1 < \infty$