

Prob. 1.20 (change of notation)

Given: system is linear and

$$x_1(t) = e^{j2t} \rightarrow \boxed{S} \rightarrow y_1(t) = e^{j3t}$$

$$x_2(t) = e^{-j2t} \rightarrow \boxed{S} \rightarrow y_2(t) = e^{-j3t}$$

$$\begin{aligned} \text{(a) } x(t) &= \cos(2t) \\ &= \underbrace{\frac{1}{2}}_{a_1} \underbrace{e^{j2t}}_{x_1(t)} + \underbrace{\frac{1}{2}}_{a_2} \underbrace{e^{-j2t}}_{x_2(t)} \rightarrow \boxed{S} \rightarrow y(t) = ? \end{aligned}$$

$$\begin{aligned} \text{(b) } x(t - \frac{1}{2}) &= \cos(2(t - \frac{1}{2})) \\ &= \underbrace{\frac{1}{2}}_{a_1} \underbrace{e^{-j}}_{x_1(t)} \underbrace{e^{j2t}}_{x_1(t)} + \underbrace{\frac{1}{2}}_{a_2} \underbrace{e^j}_{x_2(t)} \underbrace{e^{-j2t}}_{x_2(t)} \rightarrow \boxed{S} \rightarrow z(t) = ? \end{aligned}$$

If you were told system was TI: $z(t) = y(t - \frac{1}{2})$
but it turns out system is not TI