

Homework 1

Due at the beginning of your scheduled lab period

E-mail: _____ @purdue.edu Signature: _____

Lab Div: _____ Printed Name: SOLUTION KEY

Printed copies of these pages along with your original (**hand-annotated**, **not photocopied**) written solution in the space provided (unless otherwise indicated) are required in order to receive credit. NOTE: The purpose of homework is to provide an opportunity for practicing the kinds of problems you will be asked to solve on quizzes and exams – **copying the work of someone else does not accomplish this.**

1. [4 pts] Unsigned base conversions (LO 1-1). Grading: 1 pt each, no partial credit

(a) $(7A2C)_{16}$ to base 2

7 A 2 C
0111 1010 0010 1100₂

(b) $(10010110)_2$ to base 10

150₁₀

$$\begin{aligned} 1 * 2 + 0 &= 2 \\ 2 * 2 + 0 &= 4 \\ 4 * 2 + 1 &= 9 \\ 9 * 2 + 0 &= 18 \\ 18 * 2 + 1 &= 37 \\ 37 * 2 + 1 &= 75 \\ 75 * 2 + 0 &= 150 \end{aligned}$$

(c) $(1001111100101010)_2$ to base 16

9 F 2 A₁₆

(d) $(9274)_{10}$ to base 16

$$\begin{array}{r} 579 \\ 16 \overline{) 9274} \\ \underline{9264} \\ 10 \end{array} \quad \begin{array}{r} 36 \\ 16 \overline{) 579} \\ \underline{576} \\ 3 \end{array} \quad \begin{array}{r} 2 \\ 16 \overline{) 36} \\ \underline{-32} \\ 4 \end{array} \quad \begin{array}{r} 0 \\ 16 \overline{) 2} \\ \underline{-0} \\ 2 \end{array}$$

(243A)₁₆

2. [4 pts] For the function $F(X,Y,Z) = X \cdot Y' + Y' \cdot Z$, fill in the truth table, below, along with its dual (F^D) and complement (F') functions (LO 1-4 & 1-5).

| X | Y | Z | $F(X,Y,Z)$ | $F^D(X,Y,Z)$ | $F'(X,Y,Z)$ |
|---|---|---|------------|--------------|-------------|
| 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 1 | 0 | 1 | 1 |

2 pts

1 pt

1 pt

no partial credit

3. [4 pts] Prove T13 (DeMorgan's Law) for $n=3$ using perfect induction (LO 1-6).

| X1 | X2 | X3 | $X1 \cdot X2 \cdot X3$ | $(X1 \cdot X2 \cdot X3)'$ | X1' | X2' | X3' | $X1' + X2' + X3'$ |
|----|----|----|------------------------|---------------------------|-----|-----|-----|-------------------|
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 |
| 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 1 |
| 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |

all columns
must be shown
for full credit

Score: 12 / 12