Application-Level Scheduling with Probabilistic Deadline Constraints

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Abstract-Opportunistic scheduling of delay-tolerant traffic has been shown to substantially improve spectrum efficiency. To encourage users to adopt delay-tolerant scheduling for capacityimprovement, it is critical to provide guarantees in terms of completion time. In this paper, we study application-level scheduling with deadline constraints, where the deadline is prespecified by users/applications and is associated with a deadline violation probability. To address the exponentially-high complexity due to temporally-varying channel conditions and deadline constraints, we develop a novel asymptotic approach that exploits the largeness of the network to our advantage. Specifically, we identify a lower bound on the deadline violation probability, and propose simple policies that achieve the lower bound in the large-system regime. The results in this paper thus provide a rigorous analytical framework to develop and analyze policies for application-level scheduling under very general settings of channel models and deadline requirements. Further, based on the asymptotic approach, we propose the notion of Application-Level Effective Capacity region, i.e., the throughput region that can be supported subject to deadline constraints, which allows us to quantify the potential gain of application-level scheduling. Simulation results show that application-level scheduling can improve the system capacity significantly while guaranteeing the deadline constraints.

Index Terms—Wireless scheduling, deadline constraints, asymptotically optimal policies.

I. INTRODUCTION

T ODAY'S mobile Internet is facing a grand challenge to meet the exponentially increasing demand for mobile broadband services. However, *not all traffic is created equal*. While some applications require instant access, many other applications may be willing to tolerate delay from minutes to hours [2, 3]. By opportunistically scheduling delay-tolerant transmission when the network condition is more favorable, we can significantly improve network utilization.

In this context, delay is a key performance metric that is directly tied to the users' overall experience. Unless the network can set a clear expectation for the completion time, users may fear that their traffic could be delayed for too long. Therefore, providing predictable completion time is critical for encouraging users to adopt delay-tolerant scheduling for capacity improvement. In this paper, we consider a model where each transmission task is associated with a pre-specified

This paper is published in IEEE/ACM TRANSACTIONS ON NETWORKING. Published version is available online at http://ieeexplore.ieee.org/xpl/articleDetails.jsp?arnumber=7081791.

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When there is a single base-station (BS), the above problem can be viewed as a single-server job scheduling problem with deadlines. If there is no channel variation, it is well-known that simple policies such as Earliest-Deadline-First (EDF) are optimal in underloaded systems [7]. Unfortunately, when there are channel variations, such a deadline-constrained scheduling problem is known to be extremely challenging because of the difficult trade-off between serving more urgent users and serving users with better channel conditions. In the special case with two-state channels, variants of EDF have been proposed to deal with this trade-off [8,9]. Specifically, in [8], a Feasible-Earlier-Due-Date (FEDD) policy was shown to be optimal for certain restricted arrival processes, such as periodic processes. A more recent work [9] proposed an optimal policy called Earliest Positive-Debt Deadline First (EPDF) for scheduling live video streams. In contrast, for multistate channels, existing results usually require more restrictive assumptions [10–12]. For example, [11] makes a non-causal assumption that the scheduler knows the channel states in the future, which is unrealistic in practice. [12] requires that the arrivals and deadlines follow a periodic structure. For more general systems with causal multi-state channels and without a periodic structure, however, we are not aware of a tractable methodology to find optimal scheduling policies subject to deadline constraints.

Under general multi-state channels and arrival models, although recently-developed optimization-based approaches to wireless control have been very successful for maximizing long-term throughput and stability [13–15], they are of limited capability in maximizing capacity or network utility subject to deadline constraints. For instance, the Delay-driven MaxWeight [15] policy was shown to be throughput optimal for flow-level scheduling, but may perform poorly in the case with deadline constraints, as will be demonstrated by simulations later. Similarly, even though the Lyapunov-function based method developed in [16] approximately maximizes the network utility with worst-case-delay guarantees, the attainable utility at a finite deadline constraint could still be far from optimum. Finally, stochastic decision theory can be used to solve the optimal decision subject to deadline constraints. For example, [17, 18] and [19] proposed dynamic-programming (DP) based policies for minimizing the energy in single-user systems. However, as the number of users increases, such a

A preliminary version of this paper has appeared in IEEE INFOCOM 2014 [1].

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stochastic decision problem is known to incur exponentiallyhigh complexity.

In this paper, we develop a novel approach to this open problem. Our key idea is that when the system is large, significant simplicity arises, which enables us to develop simple policies that are close-to-optimal. In other words, instead of suffering from the curse-of-dimensionality in a large-sized system, we exploit the largeness of the system to our advantage. Specially, we consider the large-system regime where both the arrival rate and the capacity increase proportionally to infinity. We show that when the system size is large, the interactions between users can be captured by the resource constraints and the deadline violation probability of each user is mainly determined by its own channel conditions. Based on such insights, we can then decouple the system and design policies that are not only provably optimal in the large-system regime, but also perform very well for medium-sized systems.

For readers familiar with the large-system asymptotics [20], the intuition that the competition between users becomes less dominant in the large-system regime may seem somewhat natural. However, as we will elaborate later, when there is channel variation, it is non-trivial to design scheduling policies that correctly exploit this intuition. Specifically, if one simply generalizes policies from the case of no channel variations (e.g., EDF), these policies may in fact perform poorly even if the system size is large. In contrast, the results in this paper provide a rigorous analytical framework to develop and analyze the correct scheduling policies in such settings.

In summary, the main contributions of this paper are:

- We first present a lower bound on the deadline violation probability for application-level scheduling with deadline constraints under a given network capacity (Section III-A). Moreover, we show that this lower bound is tight in the large-system regime as it can be achieved by appropriately designed scheduling schemes. We note that this result holds under very general channel models that may have multiple transmission rates and even temporal correlation patterns.
- We then develop new scheduling policies, called Maximum-Total-On-users (MTO) and its workconserving enhancement (MTO-WCE) (Sections III-B to III-C). They are not only asymptotically optimal in the large-system regime, but also achieve superior performance for medium-sized systems. We demonstrate that it is non-trivial to design good policies, e.g., the variants of traditional EDF and MaxWeight policies may perform poorly even when the system size is large.
- We generalize these results from single-class systems (Section III) to multi-class systems (Section IV), where the performance requirements of different classes can differ significantly. Further, based on the above asymptotic approach, we study the Application-Level Effective Capacity (ALEC), i.e., the maximum throughput that can be supported by the system with given requirements on the deadline violation probability (Section IV). We show that our proposed policies asymptotically achieve the optimal ALEC region. By evaluating the ALEC, we demonstrate the significant potential for capacity improvement thanks to application-level opportunistic control.

The remainder of this paper is organized as follows. We first

describe the application-level scheduling model in Section II. Then, we focus on the case with unit file size and study the scheduling problems for single-class systems in Section III and for multi-class systems in Section IV. We generalize the results to systems with random file size in Section V. We evaluate the scheduling policies through numerical simulations in Section VI and finally conclude our work in Section VII.

II. SYSTEM MODEL

We consider a wireless network with a single BS serving a sequence of mobile users. The system operates in a timeslotted fashion, i.e., $t \in \{0, 1, 2, ...\}$. The time-slot length considered throughout this paper is typically much larger than that in the conventional opportunistic-scheduling schemes that leverage small-time-scale fading [4, 5]. There, each time-slot is on the order of milliseconds. In contrast, since the deadlines in application-level scheduling usually range from minutes to hours [21], we will use time-slot length of tens of seconds to a few minutes.

A. Traffic Models

We focus on the downlink of the BS in this paper although the uplink can be studied similarly. The BS serves K classes of users. We assume that the arrival processes are stationary and ergodic, and are independent across classes. Let $A_k(t)$ (k = 1, 2, ..., K) represent the number of class-k users that arrive during time-slot t. For ease of exposition, we assume that $A_k(t)$ is a Poisson random variable with mean value $\lambda_k = \mathbb{E}\{A_k(t)\}$. However, we note that the results obtained in this paper can also be extended to more general arrival processes that satisfy certain conditions, e.g., traffic generated by i.i.d. sources. Denote λ as the aggregated arrival rate, i.e, $\lambda = \sum_{k=1}^{K} \lambda_k$, and let α_k be the ratio of the load contributed by class-k users, i.e, $\alpha_k = \lambda_k/\lambda$.

Let $\mathcal{I} = \{1, 2, ...\}$ be the index set of all users that enter the system. Each user $i \in \mathcal{I}$ requests to download a file of size F_i . We assume that the file size F_i is known as soon as the task is created. For ease of exposition, we first study scheduling policies assuming unit-size files, i.e., $F_i = 1$, in Sections III and IV. In Section V, we extend the results to the scenario where users from the same class can request files with i.i.d. random size, provided that the file sizes are independent of arrival processes and channel processes.

Associated with each class-k user is a (relative) deadline D_k , which is the maximum waiting time that a class-k user can tolerate. For example, for a class-k user arriving in timeslot t, its transmission task should be completed before $t + D_k$ (absolute deadline). However, due to the uncertainty of channel conditions and the limitation of available resource, it may not be possible to complete all tasks before expiration. Users that violate their deadlines will give up the task and depart the system. The deadline violation probability is a main concern of this paper, as will be defined shortly.

B. Channel Model

We aim at designing scheduling policies that exploit channel variations in the coarse time-scale due to shadowing and user mobility. The measurements in [22] show that "the channel has a dominant slow-fading component on which the fastfading component is overlaid", and the slow-fading component remains roughly constant on the order of seconds to minutes depending on the mobility. In our analysis, we mainly consider the slow-fading component by averaging out the fast-fading component within each time-slot, and thus assume that the channel condition stays unchanged within one time-slot.

For each $i \in \mathcal{I}$, let the channel state $S_i(t)$ represent the transmission rate (in the unit of bits/slot per unit of radio resource) available to user i in time-slot t. As suggested in [23], we model $S_i(t)$ as a finite-state Markov chain, i.e., $S_i(t) \in \{r_1, r_2, \ldots, r_J\}$, where J is the number of possible rates, and $0 \leq r_1 < r_2 < \ldots < r_J$ are the possible values of transmission rates. We assume that each user can estimate the current channel state $S_i(t)$, e.g., based on the measurement of the pilot signal broadcast by the BS. Further, the user can report its state $S_i(t)$ to the BS through the control channel if necessary.

We assume that channel processes are independent across users, and users from the same class have the same transition probability matrix, which is given by

$$\mathbf{P}^{(k)} = \left[p_{j_1 j_2}^{(k)} \right]_{J \times J}, k = 1, 2, \dots, K,$$

where $p_{j_1j_2}^{(k)} \in [0,1]$, $1 \leq j_1, j_2 \leq J$, is the transition probability from state j_1 to state j_2 for class-k users. We assume that each user can learn these transition probabilities based on historical measurements, as in [24, 25]. Further, denote the stationary distribution for the Markov chain of class-k as

$$\boldsymbol{\pi}^{(k)} = [\pi_1^{(k)}, \pi_2^{(k)}, \dots, \pi_J^{(k)}], \tag{1}$$

where $\pi_j^{(k)}$ $(1 \le j \le J)$ is the stationary probability of state j. We assume that the channel processes have reached the steady state, i.e., with the stationary distribution $\pi^{(k)}$, when transmission tasks are created.

C. Scheduling Model and Performance Objectives

At the beginning of each time-slot t, the BS makes scheduling decisions based on the network status and transfers data with available resource. We assume that users are allocated with orthogonal resource (e.g., resource blocks in OFDMA systems) and the total amount of radio resource consumed is limited. Under this model, we assume no other interference among users. Define the system capacity C as the amount of available radio resource, which is the product of bandwidth and slot-length. Assume that when a user i is selected to transmit in time-slot t, its download task can be completed within the given time-slot using $F_i/S_i(t)$ units of resource. This assumption is reasonable since the time-slot length is much larger than that in packet-level scheduling. For example, if we take a time-slot of 30 seconds, as many as 3 Gbits (when the bandwidth is 20 MHz and the spectrum efficiency is 5 bps/Hz [26]) can be transferred in a time-slot. Hence, for a medium file size of a few MBytes, these files can be easily completed in one time-slot provided that the channel condition is good.

Let $Q_k(t)$ represent the amount of class-k data (in the unit of bits) waiting for transmission at the beginning of timeslot t. Note that in time-slot t, the users departing the system include the users being scheduled and the users violating their deadlines. Then, for each $k \in \{1, 2, ..., K\}$, the queue length $Q_k(t)$ evolves as follows

$$Q_k(t+1) = Q_k(t) - Z_k(t) - V_k(t) + A_k(t),$$
(2)

where $Z_k(t)$ and $V_k(t)$ represent the total amount of data of completed users and expired users in time-slot t, respectively. Let Γ be the set of all possible policies. For each policy $\gamma \in \Gamma$, the deadline violation probability of class k is defined as

$$v_{k,\gamma}(\boldsymbol{\lambda}, C) = \limsup_{T \to \infty} \frac{1}{\lambda_k T} \sum_{t=0}^{T-1} \mathbb{E}[V_k(t)],$$
(3)

where $\boldsymbol{\lambda} = [\lambda_1, \lambda_2, \dots, \lambda_K]$ is the arrival rate vector.

In a single-class system, we omit the class index for simplicity and denote the deadline violation probability by $v_{\gamma}(\lambda, C)$. The objective of the BS is to minimize the deadline violation probability subject to a given load level, i.e.,

$$\min_{\gamma\in\Gamma} v_{\gamma}(\lambda,C).$$

In a multi-class system, the deadline violation probabilities across different classes are coupled and the BS needs to tradeoff the performance of different classes. In this case, we are interested in the optimal region of the deadline violation probability, which is defined as follows.

Definition 1 (Optimal DVP region) Given λ and C, the optimal region for the Deadline Violation Probability (optimal DVP region) is defined as the set of probability vectors that can be achieved under certain scheduling policy, i.e.,

$$\mathcal{V}(\boldsymbol{\lambda}, C) = \{ \boldsymbol{v} \in [0, 1]^K : \exists \gamma \in \Gamma, \\ \text{ich that } v_{k, \gamma}(\boldsymbol{\lambda}, C) \le v_k \text{ for all classes } k \}.$$
(4)

We are then interested in identifying the optimal DVP region and designing policies that can achieve any point in this region.

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Remark: We note that application-level scheduling studied in this paper differs from typical packet-level and flow-level scheduling problems in literature. Our model differs from packet-level scheduling [4,5] due to two reasons. First, the user population is dynamic due to user arrivals and departures/expirations. Second, there is a difference in the time-scale that we are interested in. Specifically, packet-level scheduling focuses on the small-time-scale channel variations typically due to multi-path fading. In contrast, our application-level scheduling focuses on exploiting larger time-scale variations, which are typically due to shadowing and/or users mobility. We note that, by averaging out the fast-fading component in each time-slot, the analysis in this paper does not account for the packet-level scheduling gain. Thus, it is conservative in nature. In reality, the BS can still apply a packet-level scheduling algorithm within each time-slot. In that case, we expect that the actual performance of the system (in terms of the deadline violation probability) will only be better. We leave it for future work to study how the analysis can be extended to account for the fast-fading component. Our model also differs from flow-level scheduling. In typical flowlevel scheduling studies [14, 15, 27-30], flow-level dynamics and packet-level dynamics are mixed together, i.e., packetlevel scheduling decisions must take into account flow-level statistics (e.g., delay or residual file size [15]). In contrast, our model can be viewed as a simplification that decouples flowlevel scheduling from packet-level scheduling. The benefit of such simplification is that we can provide rigorous delay guarantees (in comparison, existing flow-level studies focus only on stability and throughput optimality [14, 15, 27]).

III. SCHEDULING IN SINGLE-CLASS SYSTEMS

In this section, we study the single-class case, i.e., K = 1, and omit the class index for simplicity. Recall that the BS aims to minimize the deadline violation probability for a given system capacity C and arrival rate λ . We first identify a lower bound on the deadline violation probability by studying an individual decision problem. Then, we propose asymptotically optimal policies, called MTO and MTO-WCE, which achieve the lower bound in the large-system regime, i.e., when C and λ proportionally grow to infinity.

A. A Lower Bound on the Deadline Violation Probability

To obtain a lower bound on the deadline violation probability, we first focus on the decision problem for an individual user: the user decides whether or not to request transmission in each time-slot based on its *waiting time* and *channel condition*.

Let $w \in \{0, 1, ..., D-1\}$ be the waiting time of the user, i.e., the number of time-slots that the user has waited in the system. Then, a request decision policy for the user can be represented by an *individual decision matrix* $\boldsymbol{x} = [x_{w,j}]_{D \times J}$, where $x_{w,j} \in [0,1]$ (w = 0, 1, ..., D-1; j = 1, 2, ..., J) is the probability that the user requests transmission when its waiting time is w and its channel state is j. Let \mathcal{X} be the set of all possible decision matrices. Corresponding to each $\boldsymbol{x} \in \mathcal{X}$, we define the following two metrics:

- Silent probability $p_0(x)$: the probability that the user does not request transmission within D slots.
- Expected consumed resource c(x): the expected amount of resource consumed by the user if it ever requests transmission in some time-slot.

The above two metrics (as functions of x) can be calculated as follows. Let $\pi'_{w,j}(x)$ be the probability that a user has waited for w slots and its channel condition is j. We can first calculate $\pi'_{w,j}(x)$'s iteratively. First, for w = 0, we have $\pi'_{0,j}(x) = \pi_j$ for j = 1, 2, ..., J. For w > 0, we have the following iterations:

$$\pi'_{w,j}(\boldsymbol{x}) = \sum_{j'=1}^{J} (1 - x_{w-1,j'}) \pi'_{w-1,j'}(\boldsymbol{x}) p_{j'j}, \quad j = 1, 2, \dots, J.$$

Then, we can calculate $p_0(x)$ and c(x) as:

$$p_0(\boldsymbol{x}) = \sum_{j=1}^J \pi'_{D,j}(\boldsymbol{x}), \text{ and, } c(\boldsymbol{x}) = \sum_{w=0}^{D-1} \sum_{j=1}^J \frac{x_{w,j} \pi'_{w,j}(\boldsymbol{x})}{r_j}.$$

Let p_0^* be the optimal value of the following resourceconstrained individual decision problem:

$$p_0^* = \min_{\boldsymbol{x} \in \mathcal{X}} \quad p_0(\boldsymbol{x})$$

subject to $c(\boldsymbol{x}) \le \frac{C}{\lambda}$. (5)

The above problem (5) can be viewed as a constrained MDP as follows. The state is $\hat{S} \in \{Completed\} \cup \{1, 2, \dots, J\}$.

The action is "*Request*" or "*Wait*". The state \hat{S} transits to "Completed" if the user requests to transmit, or transits from j to j' with probability $p_{jj'}$ if the user decides to wait. One unit of cost incurs if $\hat{S} \neq$ "Completed" at time-slot D, and $1/r_i$ units of resource is consumed if the user requests to transmit under channel condition j. This constrained MDP can be solved by a Lagrangian relaxation approach as in [31]. By introducing a Lagrangian multiplier, we can convert the constrained MDP problem into a non-constrained MDP, and then solve it by dynamic programming iteratively. In particular, when the channel process is independent across time, the optimal solution can be shown to follow a threshold structure, i.e., for each given w, there exists a j_0 such that $x_{w,i} = 0$ for $j < j_0, x_{w,j} = 1$ for $j > j_0$, and $x_{w,j_0} \in [0, 1]$. In other words, a user with waiting time w only requests transmission when its data rate exceeds a certain threshold j_0 . If $x_{w,j_0} \neq 0$ or 1, it corresponds to some randomization at the state j_0 , which may be necessary to guarantee the equality of resource constraint in (5). This threshold j_0 may depend on the waiting time w. In the case where the channel is i.i.d. across time, the user will use larger threshold j_0 when w is small, and use a smaller threshold j_0 when w is large, i.e., when it is close to expiration. We refer readers to [31] for the details of solving this constrained MDP problem. We note that when we use the Lagrangian relaxation approach to solve such an individual decision problem, it involves iterations of solving a dynamic programming problem with J + 1 states and horizon D. The corresponding complexity is on the order of $O(J^2D)$ and is much lower than the complexity of solving the network-scale scheduling problem as an MDP.

Next, the following proposition states that p_0^* is a lower bound of the deadline violation probability.

Proposition 1 Given system capacity C and arrival rate λ , the deadline violation probability under any scheduling policy γ satisfies $v_{\gamma}(\lambda, C) \geq p_0^*$.

Remark: Note that in general, a multi-user system is complicated to analyze due to the coupling across users. In other words, when one user requests transmission, the system may not have the capacity to accommodate it if there are many other users requesting transmission at the same time. However, a key insight from Proposition 1 is that, the deadline violation probability is bounded by each user's own channel characteristics, while the coupling across users is captured only through the *average* resource consumption $c(\mathbf{x})$. Intuitively, there are on average λ users that should be served in each time-slot, and hence the expected resource consumption of each user should not be larger than C/λ . Proposition 1 then shows that the minimum violation probability subject to the resource constraint but without considering the coupling effect indeed gives a lower bound on the minimum deadline violation probability of the entire network.

Sketch of Proof: The scheduling problem of the whole system can be viewed as an MDP. Specifically, we refine the queue evolution equation (2). In time-slot t, corresponding to waiting time w and channel condition j, let $Q_{w,j}(t)$ be the number of users waiting at the beginning of the time-slot, $Z_{w,j}(t)$ be the number of served users, $A_j(t)$ be the number of users arriving at channel state j. Viewing $Q_{w,j}(t)$ as the system state and $Z_{w,j}(t)$ as the action, we can verify that the

system state in the next time-slot only depends on the state and action in the current slot: for w = 0, $Q_{w,j}(t+1) = A_j(t)$; for $1 \le w \le D-1$, $Q_{w+1,j}(t+1) = Q_{w,j}(t) - Z_{w,j}(t)$; and the cost is $V(t) = \sum_{j=1}^{J} Q_{D,j}(t)$. Then, the scheduling problem becomes an MDP with a countable state-space. Solving this network-scale MDP is extremely challenging as we discussed before, but we know that there exists an optimal stationary policy for this problem. Then, we bound its performance by showing that any network-scale stationary policy can be mapped to an individual decision policy subject to the resource constraint in (5). Details are available in Appendix A.

B. Achieving the Lower Bound in the Large-System Regime

In this section, we study scheduling policies that are asymptotically optimal in the large-system regime where the system capacity and arrival rate grow proportionally to infinity.

We consider the following semi-distributed framework. At the mobile-side, each user makes its own decision on whether or not to request transmission. As discussed in Section III-A, an individual decision policy is represented by a decision matrix $\boldsymbol{x} = [x_{w,i}]_{D \times J}$. Let $\mathcal{Q}_{w,i}(t)$ be the users that have waiting time w and channel condition j in time-slot t. Then each user $i \in \mathcal{Q}_{w,i}(t)$ sends the transmission request with probability $x_{w,j}$. A user is referred to as an "ON" user when it sends its transmission request, and an "OFF" user, otherwise (Note that the notion of ON-OFF users is different from the notion of ON-OFF channels in [8]: the channel in this paper may still have multiple rate levels). Again, note that not all ON users can be served if there are too many of them requesting transmission at the same time. Hence, at the network-side, the scheduler needs to make decision for serving the "ON" users. Next, we show that the Maximum-Total-On-users (MTO) policy presented in Algorithm 1 performs very well when the system size is large and all users use appropriate x.

Algorithm 1 MTO policy
Input: $\boldsymbol{x} = [x_{w,j}]_{D \times J}, C;$
for $t = 0$ to ∞ do
User $i \in \mathcal{Q}_{w,j}(t)$ becomes ON with probability $x_{w,j}$;
BS sorts all ON users in ascending order of $F_i/S_i(t)$; then
serves the users sequentially until the sum of $F_i/S_i(t)$
over all served users reaches C ;
end for

We represent the MTO policy as MTO(x), since it depends on the individual decision matrix x for each user. We note that the MTO(x) policy exhibits a number of highly desirable features for ease of implementation. First, each user determines its own individual decision matrix x, possibly based on its future channel characteristics. The BS does not need to know the channel characteristics of each individual user. Second, to schedule which users should be served, the BS only needs to know the current channel conditions of those users who request transmission. The BS does not need to track the state of all other users. Both features significantly reduce the amount of signalling overhead between the users and the BS.

Let x^* be the optimal solution to problem (5), we next show that MTO(x^*) (i.e., using x^* as the individual decision matrix) is asymptotically optimal in the large-system regime.

Proposition 2 Fix $\bar{c} = C/\lambda$ and let \mathbf{x}^* be the optimal solution of problem (5). Then, $MTO(\mathbf{x}^*)$ is asymptotically optimal in the large-system regime, i.e.,

$$\lim_{C \to \infty} v_{\mathrm{MTO}(\boldsymbol{x}^*)}(C/\bar{c}, C) = p_0^*,\tag{6}$$

and the convergence speed is at least $1/\sqrt{C}$.

The proposition indicates that, as the system capacity and the arrival rate grow proportionally to infinity, the deadline violation probability under $MTO(x^*)$ approaches the lower bound. We note that this result is non-trivial because the lower bound in Proposition 1 implicitly assumes that all users requesting transmission can be served immediately. However, due to randomness, not all ON users can be served even when the *average* total consumed resource is no greater than C. Fortunately, when the system size is large, this "fluctuation" effect becomes less critical. The proof is divided into two parts. First, we consider an even simpler policy, called FOO, that also has the same asymptotic properties. Then, we show that the MTO policy dominates the FOO policy with the same individual decision matrix, and thus has better performance.

1) A Baseline Policy: FOO

We first consider a policy that only serves those users requesting transmission for the first time after they arrive. Such a user is referred to as a "First-ON" user, and the corresponding policy presented in Algorithm 2 is referred to as *First-On-Only (FOO)* policy.

Similar to MTO(x), we represent the FOO policy as FOO(x), since it also depends on the individual decision matrix x for each user. We first consider a general individual decision matrix x. Let $\rho(x) = \lambda c(x)/C$ be the offered load level under x. For a fixed offered load $\rho(x) \leq 1$, we can show that in the large-system regime, almost all "First-ON" users can be served and the deadline violation probability under FOO(x) approaches the silent probability $p_0(x)$.

Lemma 1 Fix the decision matrix x such that the load level satisfies $\rho(x) \leq 1$. Under the FOO policy, the deadline violation probability approaches the silent probability as C grows to infinity, i.e.,

$$\lim_{C \to \infty} v_{\text{FOO}(\boldsymbol{x})}(C\rho(\boldsymbol{x})/c(\boldsymbol{x}), C) = p_0(\boldsymbol{x}), \tag{7}$$

and the convergence speed is at least $1/\sqrt{C}$.

Sketch of Proof: We prove the lemma by exploiting two critical properties of FOO. First, since each user is considered to be scheduled only when it is "First-ON", the candidate set for scheduling in each time-slot only depends on each user's own channel characteristics. Second, FOO fully utilizes the

resource to serve "First-ON" users in each time-slot. Using these two properties, we can show that as the system size increases, the probability that a user is "First-ON" but can not be served becomes negligible, with the convergence speed of at least $1/\sqrt{C}$. Details are available in Appendix B.

2) Dominance of MTO and Proof of Proposition 2

The FOO policy only allows each user to request transmission *once* before its deadline. However, the proposed MTO policy removes this restriction and we can show that with the same individual decision matrix x, the proposed MTO policy dominates FOO in any time-slot. Specifically, the candidate set of MTO is a superset of that of FOO in each time-slot, and thus the number of served users under MTO is no less than that under FOO in any time-slot. Therefore, Eq. (7) also holds for MTO(x). As a special case, when the individual decision matrix is x^* , we have $\rho(x^*) \leq 1$, and the conclusion of Proposition 2 then follows.

C. Work-Conserving Enhancement of MTO

Under MTO, resource may still be wasted if after serving all ON users, there is still capacity remaining. In this case, if we allow the BS to serve some of the OFF users, the MTO policy should perform even better. For example, consider the following policy called MTO with Work-Conserving Enhancement (MTO-WCE). We consider another version of problem (5) where the constraint is relaxed to $c(\mathbf{x}) < (1+\xi)C/\lambda$, where $\xi > 0$ is a control factor that can be used for tradingoff between the resource utilization and signaling overhead. We let $x^{(\xi)}$ be the optimal solution to the relaxed individual decision problem (5). The users who request transmission based on x^* are still called ON users, and the users who request transmission based on $x^{(\xi)}$ are called "secondary-ON" users. The MTO-WCE policy will serve the ON users first. If there is remaining capacity, the BS then serves the "secondary-ON" users. Clearly, MTO-WCE must achieve even better performance than MTO because we always serve the ON users first.

D. Comparison and Discussions

We briefly compare and discuss the above policies before studying scheduling policies for more general cases. The simulation setting is the same as that presented in Section VI, which will also include more numerical results. Fig. 1 shows the deadline violation probability versus the system scale Cin a single-class setting with fixed λ/C . As we can observe from the figure, FOO, MTO, MTO-WCE approach the lower bound when the system size is large. However, FOO leads to a much larger violation probability in medium-sized system due to the restriction that we discussed earlier. Further, MTO-WCE outperforms MTO and reduces the violation probability even further. Next, we compare the above policies with other policies (i.e., Delay-MW, EDOF-WCE, and HRF, which will be defined later), and discuss the implications of the observations.

1) Achieving asymptotic optimality is not trivial: Readers may have the impression that, since even a policy as simple as FOO achieves the same asymptotic optimality when the system size is large, perhaps any reasonable policy will be as good as MTO/MTO-WCE. This apparent triviality could

be quite misleading. For example, consider a variation of the EDF policy that is often used for systems with fixed or twostate channels [7,8]. Specifically, in each time-slot, the BS serves ON users according to the EDF discipline (we call it the Earliest-Deadline-ON-user-First (EDOF) policy). As shown in Fig. 1, even for EDOF with work-conserving-enhancement (EDOF-WCE), the deadline violation probability is still larger than that under FOO and may not approach the lower bound p_0^* even when the system is large. What happens is that the EDOF policy does not dominate FOO in each sample path. In general, when the waiting time w is larger, a user will tend to request transmission even if its channel is poor (because it is already approaching its deadline). Under EDOF, since an ON user closer to the deadline gets a higher priority to be served, the system will be more likely to serve a user when its channel is poor. This deficiency reduces the overall system performance. Another well-known policy, Delay-driven MaxWeight [15], does not approach the lower bound either when the system size is large, as shown in Fig. 1 (which is not surprising because Delay-driven MaxWeight is only throughput optimal but does not guarantee deadline performance). The above examples therefore illustrate that, even when the system size is large, we must carefully design efficient scheduling policies based on rigorous theoretical principles, in particular, by choosing policies that dominate FOO.

2) Serving only the ON users (or secondary-ON users) is *important*: In the single-class case, one may envision other policies that do not rely on individual decision matrices x^* or $x^{(\xi)}$. For example, consider the following Higher-Rate-First (HRF) policy: all users are eligible for service and in each time-slot, the BS gives priorities to the users that have higher data rate ¹. One can show that the HRF policy also dominates FOO and hence is asymptotically optimal in the single-class case. However, there are two reasons why MTO/MTO-WCE are more preferable than HRF. First, as we will see later in Section VI, it is difficult to extend the HRF policy to the multiclass case because it is unable to balance the performance across different classes. In contrast, the MTO/MTO-WCE policies using the optimal individual decision matrices can be shown to be optimal in the multi-class case as well. Second, for HRF the BS needs to know the channel conditions of all users. In contrast, MTO and MTO-WCE incur much lower signalling overhead because only the ON (or secondary-ON) users need to report the channel state to the BS. As shown in Fig. 2, the ON-ratio under MTO-WCE is higher with a larger ξ , because a larger ξ results in a looser resource constraint $c(\boldsymbol{x}) \leq (1+\xi)C/\lambda$ and reduces the threshold for becoming ON/secondary-ON, i.e., each user will be more aggressive in becoming an ON/secondary-ON user. With an appropriate relaxation factor, the ON-ratio is low, e.g., only about onethird of users need to report to the BS when $\xi = 0.15$ and the ratio becomes less at high arrival rate since the resource

¹We acknowledge that the Less-Resource-First (LRF) defined in our earlier work [1] may be not asymptotically optimal in the case with random file size, although it is equivalent to HRF in the case with identical file size.



Fig. 1. Convergence of deadline violation probability $(D = 10, \lambda/C = 12(\text{MHz} \cdot \text{Slot})^{-1})$.

constraint becomes tighter². Hence, there are both analytical and practical advantages to use MTO/MTO-WCE.

3) Impact of Correlation Among Users: We have shown the asymptotic optimality of MTO/MTO-WCE based on the assumption that the channel processes for all tasks are independent. In practice, a user may request multiple transmission tasks either in the same or different time-slots. Hence, these tasks experience the same channel conditions. Here, we investigate the impact of correlations and show that the proposed approaches are still applicable for such a more general setting in the large-system regime. Let N be the total number of users in the system. For each new task, the user that requests the task is uniformly chosen from 1 to N. Hence, the ratio λ/N represents the average number of transmission tasks generated by each user in one slot and the correlation of channel-state processes becomes larger as λ/N increases. We assume that each user does not combine tasks and thus makes decision for each task separately. Fig. 3 shows the convergence of deadline violation probability for different values of λ/N . From the figure, we can see that under MTO-WCE, the deadline violation probability increases as the correlation of channelstate processes becomes stronger, especially when the system scale is small. However, the difference becomes negligible as the system scale becomes larger. Hence, the proposed approaches can be applied to approximately minimize the deadline violation probability in the systems where the channel processes may be correlated.

IV. SCHEDULING IN MULTI-CLASS SYSTEMS

In the previous section, we have shown that, when there is a single class, simple MTO and MTO-WCE policies are not only asymptotically optimal when the system size is large, but also perform well in medium-sized systems. In this section, we extend the results to multi-class systems.

In multi-class systems, the design of scheduling policies must be even more careful because we need to balance the performance across different classes. Since the resource shared among different classes is limited, it is impossible to



Fig. 2. ON-ratio under different arrival rates (C = 10 MHz, D = 10).



Fig. 3. Impact of correlations $(D = 10, \lambda/C = 12(\text{MHz} \cdot \text{Slot})^{-1}).$

simultaneously minimize the deadline violation probability of all classes. Thus, we turn to study the optimal DVP region (see Definition 1). We will identify an outer bound for the optimal DVP region and show that MTO/MTO-WCE can asymptotically attain any point strictly inside the outer bound in the large-system regime. Further, we quantify the maximum throughput that can be supported for given requirement on the deadline violation probabilities, which will show the benefit of application-level scheduling.

A. Optimal DVP Region

For given system capacity C and arrival rate vector λ , we define the optimal DVP region $\mathcal{V}(\lambda, C)$ by Eq. (4). However, obtaining the accurate region of $\mathcal{V}(\lambda, C)$ is difficult. Next, we will establish a simple outer bound for $\mathcal{V}(\lambda, C)$, and show that an appropriately-designed MTO policy will attain this bound when the system size is large.

In order to obtain an outer bound for $\mathcal{V}(\boldsymbol{\lambda}, C)$, we first consider the scenario where each class is separately served with a certain proportion of the resource. Such separation allows us to use the results obtained in the single-class case. Specifically, let $\boldsymbol{\zeta} \in [0, 1]^K$ satisfy $\sum_{k=1}^K \zeta_k = 1$, and let $\zeta_k C$ be the resource allocated to class k. By Proposition 1, we know that the lower bound on the deadline violation probability for each class is given by the optimal value $p_{0,k}^*(\zeta_k)$ of the following optimization problem:

$$p_{0,k}^*(\zeta_k) = \min_{\boldsymbol{x}_k \in \mathcal{X}_k} p_{0,k}(\boldsymbol{x}_k)$$

subject to $c_k(\boldsymbol{x}_k) \le \zeta_k C / \lambda_k.$ (8)

As a result, separating the resource according to ζ should allow us to achieve any vector of deadline violation probability in $\{v \in [0,1]^K : p_{0,k}^*(\zeta_k) \le v_k \le 1\}$. Taking the union of all possible ζ , we then obtain the following region:

$$\hat{\mathcal{V}}(\boldsymbol{\lambda}, C) = \bigcup_{\boldsymbol{\zeta} \in [0,1]^K : \sum_{k=1}^K \zeta_k = 1} \{ \boldsymbol{v} \in [0,1]^K : p_{0,k}^*(\zeta_k) \le v_k \le 1 \}$$

Next, we will show that $\hat{\mathcal{V}}(\boldsymbol{\lambda}, C)$ is an outer bound for the optimal DVP region $\mathcal{V}(\boldsymbol{\lambda}, C)$. Further, we will show that the MTO policy with appropriately chosen individual decision matrices is asymptotically optimal in attaining any vector of deadline violation probabilities in this outer bound when the system size is large. Specifically, suppose that we are given a vector $\boldsymbol{v} = [v_1, v_2, \dots, v_k] \in \hat{\mathcal{V}}(\boldsymbol{\lambda}, C)$. Let $\boldsymbol{x}_k^{\sharp}(v_k)$ be the optimal solution to the following individual decision problem:

$$\min_{\boldsymbol{x}_k \in \mathcal{X}_k} \quad c_k(\boldsymbol{x}_k)$$
subject to $p_{0,k}(\boldsymbol{x}_k) \le v_k.$

$$(9)$$

²When the traffic load is low ($\lambda \leq 90$), the ON-ratio remains roughly constant as ξ or λ increases because in this range, the constraint in (5) is not binding yet (i.e., resource is plentiful). For a fixed and strictly-positive $\xi > 0$, there is a medium range of λ where the ON-ratio increases with λ . This is because, in this range the relaxed constraint tends to make the BS oversubscribed with secondary-ON users. As a result, more secondary-ON users must be declined service and these users will then become ON or secondary-ON again later with a higher probability (because they are closer to the deadline). Thus, the overall ON-ratio in fact increases. We choose $\xi = 0.15$ in our simulations later as it provides a low deadline violation probability without causing too much additional signaling overhead.

Further, let $x^{\sharp}(v) = \{x_1^{\sharp}(v_1), x_2^{\sharp}(v_2), \ldots, x_K^{\sharp}(v_K)\}$. We represent the MTO policy with individual matrices $x^{\sharp}(v)$ as MTO($x^{\sharp}(v)$). In other words, under MTO($x^{\sharp}(v)$), classk users request transmission using matrix $x_k^{\sharp}(v_k)$, and those users from each class requesting transmission are called ON users. As in Section III, in each time-slot, the MTO policy serves as many ON users as possible, regardless of which class they are from.

The following proposition states that the optimal DVP region is outer-bounded by $\hat{\mathcal{V}}(\boldsymbol{\lambda}, C)$ and the MTO policy is asymptotically optimal in the sense that it can achieve any violation probability vectors in $\hat{\mathcal{V}}(\boldsymbol{\lambda}, C)$, including the frontier, in the large-system regime.

Proposition 3 For given system capacity C and arrival rate vector λ , the optimal DVP region satisfies $\mathcal{V}(\lambda, C) \subseteq \hat{\mathcal{V}}(\lambda, C)$. In addition, for a fixed amount of average resource $\bar{c} = C/\lambda$, arrival proportion vector α , and any $v \in \hat{\mathcal{V}}(\lambda, C)$, we have

$$\lim_{C \to \infty} v_{k,\text{MTO}(\boldsymbol{x}^{\sharp}(\boldsymbol{v}))}(C\boldsymbol{\alpha}/\bar{c},C) \le v_k, \tag{10}$$

Sketch of Proof: The proof for the outer bound is similar to the proof of Proposition 1. To show the asymptotic optimality of $MTO(x^{\sharp}(v))$, we first show that the conclusion holds for $FOO(x^{\sharp}(v))$ by the similar approach as in Lemma 1, and then extend the results to $MTO(x^{\sharp}(v))$. However, the extension is trickier than the single-class case, because even though $MTO(x^{\sharp}(v))$ dominates $FOO(x^{\sharp}(v))$ in terms of *total number* of served ON users, it does not dominate $FOO(x^{\sharp}(v))$ in terms of number of served ON users for each class. We deal with this issue by upper bounding the expected number of served users from each class and then show that the deadline violation probability of each class under MTO will approach a value no greater than v_k . The details are available in Appendix C.

Remark: As discussed earlier in the single-class case, a highly desirable feature of the MTO policy is that each user computes independently its decision matrix x_k , and decides whether it should be ON or OFF in each time-slot. Then, the BS only needs to schedule as many ON users as possible. Note that the BS needs not to know the channel characteristics of each user, nor its targeted deadline violation probability. Hence, the MTO policy is easy to implement in a distributed manner. In addition, we also note that the individual decision matrices x_k 's play a crucial role in balancing the performance requirements of different classes of users. Without such control, it would have been much more difficult for the BS to decide who should be served. As we will see in the simulation results in Section VI, this difficulty is precisely why policies such as HRF, which performs well for single-class systems, fail in multi-class systems. In HRF (or in other weightbased policies such as Delay-driven MaxWeight), although one can introduce and adjust weights to control the priority of different classes, it is difficult to predict the achieved deadline violation probabilities in advance, without actually running the policy. Hence, they are ineffective in guaranteeing the delay performance in the deadline-constrained scenarios that we are interested in.

We also note that, similar to the single-class case, we can use work-conserving enhancement to further improve the performance. Specifically, we can solve the problem (5) with relaxed resource constraint $c_k(x) \leq (1 + \xi)c_k(x^{\sharp}(v_k))$, and use the solution to decide the "secondary-ON" users as in Section III-C.

B. Application-Level Effective Capacity Region

Instead of minimizing the deadline violation probability subject to given offered load, a dual problem would be to maximize the offered load subject to given deadline violation probabilities. Let η_k be the maximum deadline violation probability for class-k users. Then, in the single-class system, the objective of the BS is to maximize the throughput while guaranteeing that the deadline violation probability does not exceed η . We refer to this maximum throughput as *Application-Level Effective Capacity (ALEC)*, to differentiate it from the Effective Capacity concept proposed in [32]. In a multi-class system, the ALECs are again coupled across different classes. Therefore, with given requirement $\eta = [\eta_1, \eta_2, \dots, \eta_K]$, we define the ALEC region as follows.

Definition 2 (ALEC region) Given system capacity C and required value η of deadline violation probabilities, the ALEC region is defined as follows,

$$\Lambda(\boldsymbol{\eta}, C) = \left\{ \boldsymbol{\lambda} \in [0, \infty)^{K} : \exists \text{ policy } \gamma \in \Gamma, \\ \text{such that } v_{k,\gamma}(\boldsymbol{\lambda}, C) \le \eta_{k} \text{ for all classes } k \right\}$$
(11)

Similar to the analysis of the optimal DVP region, we consider the outer bound for $\Lambda(\eta, C)$. Define the following region:

$$\hat{\Lambda}(\boldsymbol{\eta}, C) = \left\{ \boldsymbol{\lambda} \in [0, \infty]^K, \sum_{k=1}^K c_k^{\sharp}(\eta_k) \lambda_k \le C \right\},\$$

where $c_k^{\sharp}(\eta_k)$ is the optimal value of the constrained optimization problem (9), with the deadline violation probability v_k replaced by η_k . Clearly, $\hat{\Lambda}(\boldsymbol{\eta}, C)$ increases linearly in C. Using the approach in Section IV-A, we can show that $\hat{\Lambda}(\boldsymbol{\eta}, C)$ is an outer bound for $\Lambda(\boldsymbol{\eta}, C)$ and is tight in the large-system regime.

Proposition 4 Given the system capacity C and the required values η of deadline violation probabilities, the ALEC region satisfies $\Lambda(\eta, C) \subseteq \hat{\Lambda}(\eta, C)$. In addition, for any λ that is in the interior of $\hat{\Lambda}(\eta, 1)$, we have

$$\lim_{C \to \infty} v_{k,\text{MTO}(\boldsymbol{x}^{\sharp}(\boldsymbol{\eta}))}(\boldsymbol{\lambda} C, C) \le \eta_k.$$
(12)

As a special case of Proposition 4, we conclude that for the single-class case (i.e., K = 1), the ALEC is upper bounded by $C/c^{\sharp}(\eta)$ and it approaches this upper bound as C grows to infinity under MTO/MTO-WCE. By evaluating this ALEC in Section VI, we will demonstrate the benefit of application-level scheduling.

V. SCHEDULING WITH RANDOM FILE SIZES

For simplicity, in the previous sections, we have studied asymptotically optimal policies with the assumption of unit file size. In this section, we discuss the extension of the results to the case of random file size.

A. Adjustments of System Models and Performance Metrics

We assume that the file sizes F_i 's of users from the same class are i.i.d. and are independent of the arrival and channel condition. Let $\mu_{F,k}$ and $\sigma_{F,k}^2$ be the expectation and variance of the file size for class-k users, i.e., $\mathbb{E}[F_i] = \mu_{F,k}$ and $\operatorname{Var}(F_i) = \sigma_{F,k}^2$ if user *i* is from class *k*.

Since the file size of each user is different, we define the metrics based on the amount of data (rather than the amount of users). Note that in Section II, we have already defined the queue length $Q_k(t)$, the amount of data completion $Z_k(t)$ and the amount of violations $V_k(t)$ based on the amount of data (although for unit-size files, their definitions are the same if we defined them based on the number of users). Thus, here we only need to replace the number of arrivals $A_k(t)$ in Eq. (2) by $B_k(t)$, which is defined as the amount of data requested by the new arrivals from class k. Let N(t) be the total number of users entering the system up to time-slot t, i.e., $N(t) = \sum_{t'=0}^{t} \sum_{k=1}^{K} A_k(t')$, and $\mathcal{I}_k \subseteq \mathcal{I}$ be the index set of class-k users. Then the total amount of class-k data arriving in time-slot t can be represented by

$$B_k(t) = \sum_{i=N(t-1)+1}^{N(t)} \mathbf{1}_{i \in \mathcal{I}_k} F_i$$

where $\mathbf{1}_{i \in \mathcal{I}_k}$ is the indicator function of the event $\{i \in \mathcal{I}_k\}$. Then, the expectation of $B_k(t)$ is $\mathbb{E}[B_k(t)] = \lambda_k \mu_{F,k}$ [33].

We also take the utility of file download to be proportional to the amount of successfully transferred data. Hence, the deadline violation probability should also be defined as the ratio of the amount of expired data to the amount of total data, i.e., Eq. (3) should be rewritten as

$$v_{k,\gamma}(\boldsymbol{\lambda}, C) = \limsup_{T \to \infty} \frac{1}{\lambda_k \mu_{F,k} T} \sum_{t=0}^{T-1} \mathbb{E}[V_k(t)].$$

With the above definition of the violation probability, the definitions of optimal DVP region and ALEC need no changes.

B. Adjustments of Design and Analysis

We only discuss the design and analysis for single-class systems. The results can be easily generalized to multi-class systems as in Section IV.

In the individual decision stage, because the silent probability and expected consumed resource are obtained by averaging over all possible file sizes, each user can apply an identical policy for different-size files without loss of optimality. In other words, each user only needs to obtain the optimal individual decision policy assuming unit file size subject to a per-bit resource constraint, i.e.,

$$p_0^* = \min_{oldsymbol{x} \in \mathcal{X}} p_0(oldsymbol{x})$$

subject to $c(oldsymbol{x}) \leq rac{C}{\lambda \mu_F}$

With the optimal individual solution, we can show that the lower bound property, i.e., Proposition 1, still holds for the case of random file sizes. The proof is quite similar to that in Appendix A with the per-user resource constraint replaced by the per-bit resource constraint. Further, the policies used by the BS should also be interpreted in terms of the amount of data. For example, the proposed MTO policy can be interpreted as Maximum-Total-bits-of-On-users rather than Maximum-Total-On-users. Then, using the property of compound Poisson random variable [33] presented in Lemma 2 in Appendix B and taking the average file size into account, we can show that the asymptical optimality, e.g., Proposition 2, still holds in the case of random file size.

VI. SIMULATION RESULTS

A. Simulation Setup

We evaluate the performance of the proposed mechanism with typical LTE parameters [11, 26], which are summarized in Table I. Since we consider application-level scheduling, we focus on a large time-scale and set the time-slot length to be 30 seconds. The file size of each user follows truncated lognormal distribution with mean 2 Mbytes, standard deviation 0.72 Mbytes, and maximum size 5 Mbytes [34]. The results for unit file size seem to be even better and have similar trends, and hence are omitted here. We generate the channel processes based on the random waypoint (RWP) mobility model [35]. Specifically, we estimate the 1-step transition probabilities of the channel process for the users traveling in the cell with RWP model with a velocity of 3 Km/h. Then, the transition probabilities are used to drive a Markov model that simulates channel realizations.

TABLE I System Parameters

Property	Setting
Carrier frequency	2 GHz
System bandwidth	1.25, 2.5, 5, 7.5, 10, 15, 20 MHz
BS Tx power	46 dBm for 10 MHz
Coverage radius	500 m
Path loss	$128.1 + 37.6 \log_{10}(d[\text{km}]) \text{ dB},$
Penetration loss	20 dB
Shadowing	Lognormal, standard deviation 8 dB
Noise power density	-170 dBm/Hz
Link adaption	Shannon's equation, clipped at -10 dB and 20 dB

We evaluate the deadline violation probability and ALEC under application-level scheduling with different disciplines. We use the optimal individual decision matrices for FOO, EDOF-WCE, and MTO/MTO-WCE. For the work-conserving enhancement, i.e., MTO-WCE and EDOF-WCE, the control factor is set to $\xi = 0.15$ (see the definition of ξ in Section III). We also compare the proposed policies with the HRF (see Section III-C) and Delay-driven MaxWeight (Delay-MW) [15] policies. In the multi-class case, weight vector is introduced in HRF and Delay-driven MaxWeight to trade-off between different classes. Specifically, the HRF policy prioritizes users according to $\zeta_k S_i(t)$, and Delay-driven MaxWeight prioritizes users according to $\zeta_k w_i S_i(t)$, where $0 \le \zeta_k \le 1$ reflects the additional weight of class-k users and $\sum_{k=1}^{K} \zeta_k = 1$.

B. Deadline Violation Probability

Recall that we have evaluated the deadline violation probability versus the system size C in Fig. 1, when the relative load λ/C is fixed. Next, we evaluate the deadline violation probability with fixed C in Figs. 4 and 5. In the single-class case, Fig. 4(a) shows the deadline violation probability as a function of the arrival rate, and Fig. 4(b) zooms in a portion of it to show more details. The minimum silent probability





Fig. 4. Deadline violation probability in single-class scenarios (C = 10 MHz), (a) global view for different arrival rates (D = 10), (b) partial view for different arrival rates (D = 10), (c) different deadlines ($\lambda = 80$), (d) different velocities ($\lambda = 80$, and D = 10).

Fig. 5. Deadline violation probability region in 2class scenarios (C = 10 MHz, D = [5, 15], and $\lambda = [15, 20]$), (a) global view, (b) partial view.

given by (5) serves as a lower bound of the system, as stated in Proposition 1. We can observe that the deadline violation probability of MTO-WCE is very close to the lower bound and dominates all other policies in the whole range presented. When the load is light (e.g., $\lambda \leq 70$), all work-conserving policies achieve similar performance because the contention is low. However, as the load increases, the performance of different scheduling policies starts to differ. The MTO, MTO-WCE, and HRF policies perform very well, while Delaydriven MaxWeight and EDOF-WCE can perform significantly worse. For example, the deadline violation probability under Delay-driven MaxWeight can be much larger than that under MTO-WCE (by two times when $\lambda = 120$). For EDOF-WCE, the deadline violation probability is close to MTO-WCE when the load is very heavy ($\lambda \ge 125$) because users with different waiting time will become "ON" only under the best channel condition. However, the deadline violation probability of EDOF-WCE is rather high in the medium range $(85 < \lambda < 125)$. This is because in this range, a user with larger waiting time will request transmission even if its channel is poor (because it is already approaching its deadline). EDOF-WCE prioritizes "ON" users close to the deadline and tends to serve these close-to-expiration users whose channel conditions are probably unfavorable.

Fig. 4(c) shows the deadline violation probability versus the deadline for fixed values of C and λ . As the deadline increases, users have more opportunities to request transmission and the deadline violation probability decreases under most policies except EDOF-WCE and FOO. EDOF-WCE can result in severe deadline violations for certain deadlines (e.g., $6 \le D \le 13$) because of the same reasons as in the analysis of Fig. 4(a). Similar trends can be observed in Fig. 4(d), which shows the deadline violation probability versus the velocity. As the velocity increases, the channel conditions vary faster and provide more opportunity to improve the system throughput. Hence, the deadline violation probability can be reduced under properly designed polices such as MTO/MTO-WCE.

Fig. 5 shows the deadline violation probabilities for the 2class scenario, where Fig. 5(a) presents a global view and Fig. 5(b) zooms in to show a part of the region in more detail. For HRF and Delay-driven MaxWeight, each pair of deadline violation probabilities corresponds to a weight vector ζ . From the figure, we can see that the proposed MTO-WCE policy achieves close-to-optimal deadline violation probabilities. The deadline violation probability under HRF and Delay-MW is greater than that under MTO-WCE. Moreover, the exact impact of weight vector is unpredictable and difficult to tune in practice.

In summary, designing the optimal scheduling policies is non-trivial and some heuristic policies, e.g., EDOF, may perform rather poorly in certain range. The rigorous theoretical framework in this paper provides a principled approach to design and analyze the scheduling policies. Under this framework, the proposed MTO/MTO-WCE policies not only achieve the optimal bound in the large-system regime, but also perform well in medium-sized systems.

C. Application-Level Effective Capacity

In this section, we evaluate ALEC under different system sizes and requirements. The ALEC is normalized by the bandwidth and shown as spectrum efficiency (bps/Hz). Because MTO-WCE consistently outperforms FOO, MTO, and EDOF-WCE in earlier simulations, we will mainly use MTO-WCE in the rest of the simulations. Fig. 6 shows the convergence of ALEC in a single-class system as the system size increases. We can see that under MTO-WCE, the supportable traffic load approaches the upper bound stated in Proposition 4 (the dashed line). The gap from the upper bound is negligible when $C \ge 10$ MHz, which is a typical value of the bandwidth in cellular networks. Hence, we use C = 10 MHz for the rest of the simulation.



Fig. 6. Convergence of ALEC for different deadlines (C=10 MHz and $\eta=0.05).$

Fig. 7(a) shows the ALEC in a single-class system as a function of deadline. It clearly demonstrates the benefit of exploiting the delay tolerance of the traffic. Namely, the capacity can be significantly improved if the users can tolerate certain delay. For example, if users require to finish the transmission task within 1 slot (30 seconds), the spectrum efficiency is about 1 bps/Hz. However, with application-level scheduling, this efficiency can be increased to more than 6 bps/Hz if the users can tolerate a delay of 10 slots (5 minutes). Comparing with Delay-driven MaxWeight, we see that although MTO-WCE performs similarly to Delay-driven MaxWeight when the deadline is small, it clearly outperforms Delay-driven MaxWeight for larger deadlines. Comparing with the upper bound, we can see that the room for further improvement over the proposed MTO-WCE policy is very small. Similar trends can be seen in Fig. 7(b), which shows the ALEC as a function of the velocity. The ALEC increases as the velocity becomes large but the gain becomes smaller when the velocity is larger than a certain threshold. Again, the proposed MTO-WCE policy performs best and achieves ALEC that is quite close to the upper bound.

Fig. 7(c) shows the ALEC region for a 2-class system. We can see that MTO-WCE achieves an ALEC region that is quite close to the outer bound. In contrast, for a given weight vector ζ , the ALEC regions under Delay-driven MaxWeight and HRF are smaller than that achieved by MTO-WCE. It is interesting to observe that, if we take the union of the ALEC region under HRF or Delay-driven MaxWeight over different choices of ζ , the union becomes closer to the optimal. However, in practice, it is difficult to predict the delay performance of HRF or Delay-driven MaxWeight in advance. As a result, it is difficult to tune the parameter ζ for these algorithms under a given mixture of deadline-constrained traffic, without actually running the algorithms. Therefore, we believe that the theoretical results and our proposed MTO/MTO-WCE policies are particularly useful for multi-class systems with different deadline constraints.

VII. CONCLUSIONS AND FUTURE WORK

In this paper, we study application-level scheduling mechanisms for delay-tolerant traffic with deadline requirements. The objective of the network is to minimize the deadline violation probability for given arrival traffic. We present a lower bound on the deadline violation probability, and develop simple threshold-based policies, MTO and MTO-WCE, that achieve the lower bound in the large-system regime, under general channel models and multiple classes. These schemes also perform well in medium-size systems. We note the insights from the analysis are important in the design of scheduling policies as some commonly studied policies may not perform well in certain regimes. Further, based on the asymptotic approach, we propose estimation approach for the ALEC region. Numerical results show that under applicationlevel scheduling, if users can tolerate certain delay, the capacity can be improved significantly. For example, the capacity can be increased by about 6 times if the users can tolerate a delay of 10 time-slots (e.g., 5 minutes).

Although the results in the paper focus on the single-cell system with stationary arrivals and channels, we believe that the key insights are applicable to more general settings. For future work, we will study how to generalize the algorithms and insights into the multi-cell cases with time-dependent arrivals and/or channels.

APPENDIX A

PROOF OF PROPOSITION 1

As discussed in Section III-A, the scheduling problem of the whole system can be viewed as an MDP with $Q_{w,j}(t)$ being the system state. For such an MDP, there exists a stationary policy that minimizes the deadline violation probability. Note that corresponding to each stationary policy II, there is a stationary distribution matrix,

$$\mathbf{\Phi} = [\phi_{w,j}]_{D \times J},$$

where $\phi_{w,j} \in [0,1]$ represents the probability that a user is served when its waiting time is w and channel state is j. Hence, the deadline violation probability is $v(\lambda, C) =$ $1 - \sum_{w=0}^{D-1} \sum_{j=1}^{J} \phi_{w,j}$. In addition, because of the resource constraint, we must have $\lambda \sum_{w=0}^{D-1} \sum_{j=1}^{J} \frac{\phi_{w,j}}{r_j} \leq C$ ($\phi_{w,1} = 0$ if $r_1 = 0$).

On the other hand, by considering a scenario with infinite available resource, each feasible Φ can be uniquely mapped to an individual decision matrix x as follows.

 $\Phi \rightarrow x$ mapping: Consider a scenario where all users use an identical individual decision matrix x. In addition, the available resource is infinite and any user sending the request can be served immediately. Let $\pi'_{w,j}$ be the ratio of users that still stay in the system after waiting w slots and is in channel state j. For w = 0, we know that this ratio is equal to the stationary distribution of the channel process, i.e., $\pi'_{0,j} = \pi_j$ (j = 1, 2, ..., J). Then, we can decide $x_{0,j}$ by solving $\pi'_{0,j}x_{0,j} = \phi_{0,j}$ (for $\pi'_{0,j} = 0$, we let $x_{0,j} = 0$, which will not affect the value of other variables). For w > 0, we can decide $x_{w,j}$ in an iterative manner. Specifically, after obtaining $x_{w-1,j}$, we can calculate $\pi'_{w,j}$ as

$$\pi'_{w,j} = \sum_{j'=1}^{J} (1 - x_{w-1,j'}) \pi'_{w-1,j'} p_{j'j},$$



Fig. 7. Evaluation of ALEC, (a) ALEC for single-class system with different deadlines (C = 10 MHz and $\eta = 0.05$), (b) ALEC for single-class system with different velocities (C = 10 MHz, D = 10, and $\eta = 0.05$), (c) ALEC region for 2-class system (C = 10 MHz, D = [5, 15], and $\eta = [0.05, 0.05]$).

and obtain $x_{w,j}$ by solving $\pi'_{w,j}x_{w,j} = \phi_{w,j}$.

Then, under individual decision matrix \boldsymbol{x} , the expected consumed resource and the silent probability are equal to their corresponding values under II. Therefore, the expected consumed resource must satisfy $c(\boldsymbol{x}) = \sum_{w=0}^{D-1} \sum_{j=1}^{J} \frac{\phi_{w,j}}{r_j} \leq C/\lambda$ and the deadline violation probability satisfies $v(\lambda, C) = p_0(\boldsymbol{x}) \geq p_0^*$. Note that these expressions precisely correspond to the constraint and objective of problem (5). Hence, we conclude that $v(\lambda, C)$ must be greater than p_0^* .

APPENDIX B Proof of Lemma 1

The proof of Lemma 1 will use a property of compound Poisson random variable (i.e., sum of Poisson number of i.i.d. random variables [33]), which is described as follow. We use the notation for asymptotic upper bounds as in [36]: for two functions $g_1(\lambda)$ and $g_2(\lambda)$, we say $g_1(\lambda) = O(g_2(\lambda))$ if there exists constants $\kappa > 0$ and $\lambda_0 > 0$ so that for all $\lambda > \lambda_0$, we have $g_1(\lambda) \le \kappa g_2(\lambda)$. Moreover, we focus on the case where $r_1 > 0$ here while the case of $r_1 = 0$ can be proved with slight modifications.

Lemma 2 Let N be a Poisson random variable with mean value λ , and X_1, X_2, \ldots, X_N be i.i.d. random variables that are independent of N with $\mathbb{E}[X_i] = \mu_X$ and $\operatorname{Var}(X_i) = \sigma_X^2$. Let $Y^{(\lambda)} = \sum_{i=1}^N X_i$ be the sum of the i.i.d. sequence and $[Y - \lambda \mu_X]^+ = \max\{Y - \lambda \mu_X, 0\}$. Then, we have

$$\mathbb{E}\left\{ [Y^{(\lambda)} - \lambda \mu_X]^+ \right\} = O(\sqrt{\lambda}). \tag{14}$$

Proof: Using the results of Examples 3.11 and 3.19 in [33], we know that the expectation and variance of $Y^{(\lambda)}$ are $\mathbb{E}[Y^{(\lambda)}] = \lambda \mu_X$ and $\operatorname{Var}\{Y^{(\lambda)}\} = \lambda(\sigma_X^2 + \mu_X^2)$, respectively. Hence, $\mathbb{E}\{Y^{(\lambda)} - \lambda \mu_X\} = 0$, $\operatorname{Var}\{Y^{(\lambda)} - \lambda \mu_X\} = \lambda(\sigma_X^2 + \mu_X^2)$, and $\mathbb{E}\{[Y^{(\lambda)} - \lambda \mu_X]^2\} = \lambda(\sigma_X^2 + \mu_X^2)$. Therefore,

$$\left\{ \mathbb{E}\left\{ [Y^{(\lambda)} - \lambda \mu_X]^+ \right\} \right\}^2 \leq \mathbb{E}\left\{ [Y^{(\lambda)} - \lambda \mu_X]^2 \right\}$$
$$= \lambda(\sigma_X^2 + \mu_X^2).$$

The conclusion of the lemma then follows.

Now, consider FOO(x), i.e., the FOO policy with individual decision matrix x. Note that number of arrivals A(t) are i.i.d. over time. From the process of FOO (Algorithm 2), we also note a critical property of FOO: since each user is considered to be scheduled only when it is "First-ON", the candidate set

for scheduling in each time-slot only depends on each user's own channel conditions, which is independent across users. Hence, the system behaviors are identical in statistics and we only need to focus on an arbitrary time-slot. We omit the slot index for simplicity.

Let Y_j (j = 1, 2, ..., J) be the number of "First-ON" users with channel state j for a given individual decision matrix x. Further, let $\phi_{w,j} \in [0, 1]$ represent the probability that a user is served in channel state j at w slots after their arrivals. Note that the "First-ON" users evolve from the users arriving in the past D slots. Using the property of Poisson variables, we know that Y_j is a Poisson random variable with mean value $\pi_j^{\sharp}\lambda$, where $\pi_j^{\sharp} = \sum_{w=0}^{D-1} \phi_{w,j}$ is the probability that a user is "First-ON" at channel state j within D slots. In addition, the expected required resource for all "First-ON" users is $\lambda c(x) =$ $\lambda \sum_{j=1}^{J} \pi_j^{\sharp}/r_j$, and the offered load level $\rho(x) = \lambda c(x)/C \leq$ 1. Note that the summation is calculated from j = 2 if $r_1 = 0$ since a user cannot request transmission with zero data rate.

Next we show that since $\rho(x) \leq 1$, the probability that a "First-ON" user is unserved due to overflow tends to 0 as λ and C grow proportionally to infinity, with the convergence speed at least $1/\sqrt{\lambda}$.

Let $L(Y_1, Y_2, ..., Y_J)$ be the number of ON users that are unserved due to overflow when the number of ON users at channel state j is Y_j . Note that the total amount of resource exceeding the system capacity satisfies $\left[\sum_{j=1}^J r_j^{-1} Y_j - C\right]^+ \leq \sum_{j=1}^J r_j^{-1} [Y_j - \pi_j^{\sharp} \lambda]^+$. Thus, the number of drop users satisfies

$$L(Y_{1}, Y_{2}, \dots, Y_{J}) \leq \frac{\sum_{j=1}^{J} r_{j}^{-1} [Y_{j} - \pi_{j}^{\sharp} \lambda]^{+}}{r_{J}^{-1}} \leq \frac{r_{J}}{r_{1}} \sum_{j=1}^{J} [Y_{j} - \pi_{j}^{\sharp} \lambda]^{+}.$$
(15)

On the other hand, when overflow occurs, i.e., $\sum_{j=1}^{J} r_j^{-1} Y_j > C$, then $\sum_{j=1}^{J} Y_j > Cr_1$. Thus, we can bound the probability that a "First-ON" user is unserved as follows

$$p_{\text{unserved}}(C) = \mathbb{E}\left\{\frac{L(Y_1, Y_2, \dots, Y_J)}{\sum_{j=1}^J Y_j}\right\}$$
$$\leq \frac{r_J}{r_1^2} \mathbb{E}\left\{\frac{\sum_{j=1}^J [Y_j - \pi_j^{\sharp}\lambda]^+}{C}\right\} \quad (16)$$

Because Y_j is a Poisson random variable with mean value $\mathbb{E}[Y_j] = \pi_j^{\sharp} \lambda$, Y_j can be viewed as the sum of λ i.i.d. Poisson variables with mean value π_j^{\sharp} . From Lemma 2, we have

$$\mathbb{E}[Y_j - \pi_j^{\sharp} \lambda]^+ = O(\sqrt{\lambda}) = O(\sqrt{C}).$$

Hence,

$$p_{\text{unserved}}(C) \leq \frac{r_J}{r_1^2} \mathbb{E}\left\{\frac{\sum_{j=1}^J [Y_j - \pi_j^{\sharp} \lambda]^+}{C}\right\} = O\left(\frac{1}{\sqrt{C}}\right).$$

This implies that as C grows to infinity, $p_{\text{unserved}}(C)$ converges to 0, with convergence speed of at least $1/\sqrt{C}$. The conclusion of Lemma 1 then follows.

APPENDIX C PROOF OF PROPOSITION 3

A. Outer bound on the optimal DVP region

The proof for the outer bound is similar to the proof of Proposition 1. Consider any deadline violation probability v that is achievable, i.e., $v \in \mathcal{V}(\lambda, C)$. Using the similar approach as in Appendix A, we can map v to individual decision matrices $x_k(v_k)$ (k = 1, 2, ..., K) and the silent probability under $x_k(v_k)$ is v_k . Also, corresponding to each $x_k(v_k)$, there is an expected consumed resource $c_k(x_k(v_k))$. Because the achievability of v, we know that the total expected consumed resource satisfies the resource constraint, i.e., $\sum_{k=1}^{K} \lambda_k c_k(x_k(v_k)) \leq C$. Next, let $\rho(v) =$ $\sum_{k=1}^{K} \lambda_k c_k(x_k(v_k))/C$ and $\zeta_k = \frac{\lambda_k c_k(x_k(v_k))}{C\rho(v)}$. Then, we have $\sum_{k=1}^{K} \zeta_k = 1$, and the solution of Problem (8) satisfies $p_{0,k}^*(\zeta_k) \leq v_k \leq 1$ because $\zeta_k C/\lambda \geq c_k(x_k(v_k))$. Therefore, the vector v belongs to $\hat{\mathcal{V}}(\lambda, C)$ and hence $\mathcal{V}(\lambda, C) \subseteq$ $\hat{\mathcal{V}}(\lambda, C)$

B. Asymptotic optimality of MTO

To show the asymptotic optimality of $MTO(x^{\sharp}(v))$, we first show that with individual decision matrices $x^{\sharp}(v)$, the offered load level must satisfies $\rho(x^{\sharp}(v)) = \frac{1}{C} \sum_{k=1}^{K} \lambda_k c_k^{\sharp}(v_k) \leq 1$, where $c_k^{\sharp}(v_k)$ is the optimal value of problem (9). Otherwise, the vector \boldsymbol{v} cannot be in $\mathcal{V}(\boldsymbol{\lambda}, C)$. Thus, we can show that the conclusion holds for FOO($x^{\sharp}(v)$) by the similar approach as in Lemma 1. Then we need to extend the results to $MTO(x^{\sharp}(v))$. However, the extension is trickier than the single-class case, because even though MTO($x^{\sharp}(v)$) dominates FOO($x^{\sharp}(v)$) in terms of total number of served ON users, it does not dominate $FOO(x^{\sharp}(v))$ in terms of number of served ON users for each class. We need to prove the conclusion by further examining the upper bound of the number of served ON users for each class. Specifically, we note that the expected number of served users in each time-slot should not exceed an upper bound given by the expected number of ON users. Using this upper bound, we can then show that the deadline violation probability of each class under MTO will approach a value no greater than v_k .

Specifically, let \overline{Z}_k be the expected number of class-k users receiving service before expiration, i.e.,

$$\bar{Z}_k = \lim_{T \to \infty} \frac{1}{T} \sum_{t=0}^{T-1} \mathbb{E}[Z_k(t)]$$

Note that for any $\boldsymbol{\zeta} \in [0,1]^K$ satisfying $\sum_{k=1}^K \zeta_k = 1$, we know that $\rho(\boldsymbol{x}^*(\boldsymbol{\zeta})) \leq 1$. Using the similar argument in the proof of Lemma 1, we know that

$$\lim_{C \to \infty} \frac{Z_{k,\text{FOO}}}{\lambda} = \alpha_k [1 - p_{0,k}^*(\zeta_k)],$$
$$\lim_{C \to \infty} \frac{\bar{Z}_{\text{FOO}}}{\lambda} = \sum_{k=1}^K \alpha_k [1 - p_{0,k}^*(\zeta_k)],$$

where $\bar{Z}_{\text{FOO}} = \sum_{k=1}^{K} \bar{Z}_{k,\text{FOO}}$ is the expected total number of users being served under FOO.

Now we take the performance of FOO as a benchmark for analyzing MTO. Because the candidate user set of FOO is a subset of that for MTO in each time-slot, the total number of users being served under MTO is no less than FOO. Hence,

$$\lim_{C \to \infty} \frac{\bar{Z}_{\text{MTO}}}{\lambda} \ge \lim_{C \to \infty} \frac{\bar{Z}_{\text{FOO}}}{\lambda} = \sum_{k=1}^{K} \alpha_k [1 - p_{0,k}^*(\zeta_k)],$$

where $\bar{Z}_{MTO} = \sum_{k=1}^{K} \bar{Z}_{k,MTO}$ is the expected total number of users being served under MTO. Hence, we have

$$\lim_{L \to \infty} \frac{\bar{Z}_{\text{MTO}}}{\lambda} = \lim_{C \to \infty} \frac{\sum_{k=1}^{K} \bar{Z}_{k,\text{MTO}}}{\lambda}.$$

On the other hand, the expected number of served users from each class is bounded by the ON probability, i.e.,

$$\lim_{C \to \infty} \frac{Z_{k,\text{MTO}}}{\lambda} \le \alpha_k [1 - p_{0,k}^*(\zeta_k)].$$

Combining with the bound of the expected total served users, we have

$$\lim_{C \to \infty} \frac{Z_{k,\text{MTO}}}{\lambda} = \alpha_k [1 - p_{0,k}^*(\zeta_k)].$$

Equation (10) then follows.

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