

# Lec10

Thursday, February 6, 2020 8:43 AM

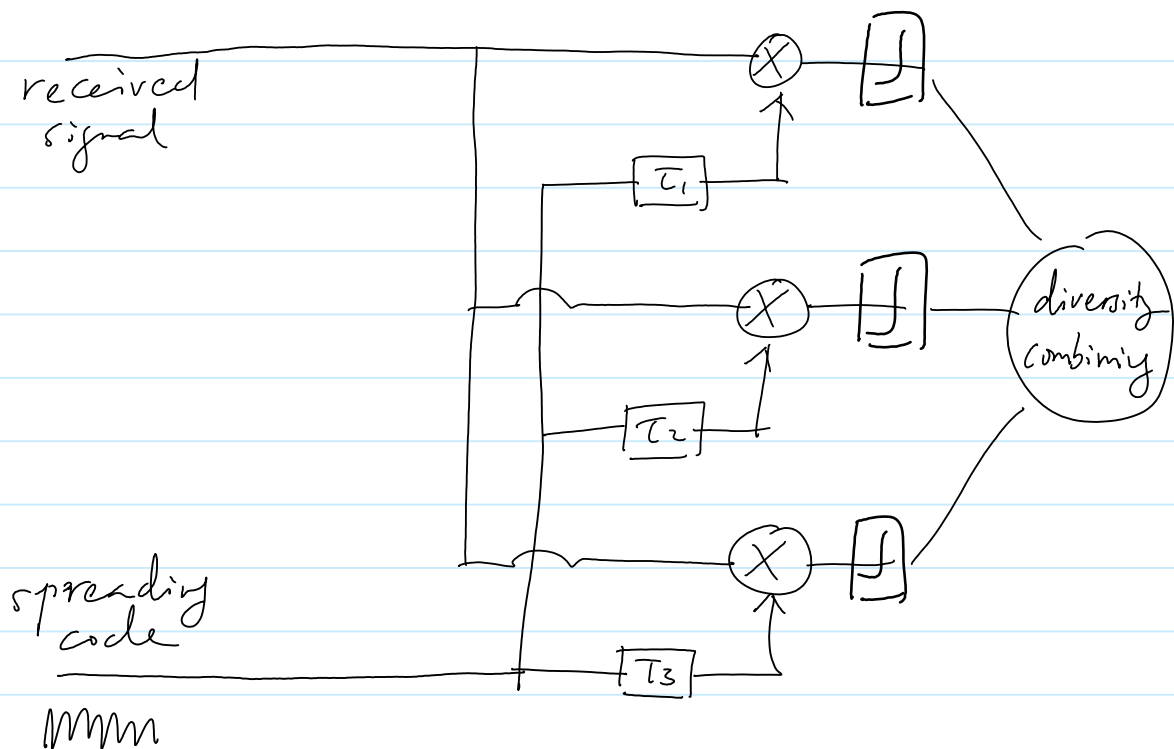
HW2 is assigned.  
Bring CDMA handout

## Rake receiver - 10min

Wednesday, January 16, 2008

3:42 PM

In CDMA, when bandwidth of the signal is much larger than the coherent bw, different paths can be separately detected. Multiple detected paths can be combined to achieve higher SINR.



Each individually resolvable path of the signal will have maximum correlation with the spreading code at a particular delay.

Diversity combining can pick either the max path, or some weighted sum. that

maximizes the SNR.

(35)

## Single cell - 15min

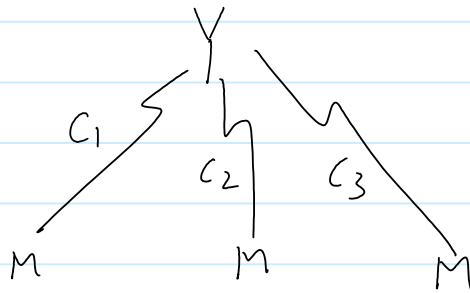
Saturday, March 15, 2008 10:42 AM

Given a particular modulation scheme (before spreading), a certain SNR for the received signal  $\tilde{s}(t)$  is required for correct detection.

$\frac{E_b}{I_0}$  — energy of signal  
— energy of noise/interference

7 dB ( $=5$ ) typical.

## Single Cell, No fading



## Assumptions:

- There are  $K$  users in one cell.
- Focus on the uplink of the cell.
- All users in the cell has power control, so that the same received power  $P_R$  is received at BS.

— No noise, no fading

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In order to decode the signal from a particular receiver:

$$\text{Energy: } E_b = P_R \cdot T_s$$

Interference due to  $(k-1)$  interfering users

$$I_0 = \frac{P_R}{W} \cdot (k-1) \cdot T_s$$

$$\therefore \frac{E_b}{I_0} = \frac{P_R \cdot T_s}{\frac{P_R}{W} (k-1) \cdot T_s} = \frac{W}{k-1}$$

The requirement on  $\frac{E_b}{I_0}$  limits the maximum number of users the cell can support:

$$K = \frac{W}{E_b/I_0} + 1.$$

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Example: IS-95

- Information bit rate  $1/T_s = 9.6 \text{ kbps}$
- Transmission bandwidth  $1/T_c = 1.2288 \text{ Mbps}$

$$W = T_s/T_c = 128$$

$$- E_b/I_0 = 5 \quad (\text{or } 7\text{dB})$$

$$\therefore K = 26 \text{ users/cell for } 1.25 \text{ MHz}$$

For a 25 MHz band, we have

$$\frac{25 \text{ MHz}}{1.25 \text{ MHz}} \times 13 = 520 \text{ users/cell}$$

compared to 248 users/cell in the GSM example. (4-reuse)

$$\frac{25 \text{ M}}{200} \times \frac{8}{4} = 250$$

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Caveats:

- We have not taken into account the interference from other cells
  - Fading
- 

Note: In the above derivation, we have assumed perfect power control.

Power control is critical to CDMA systems.

Consider the case w/o power control

- If users transmit at the same power

- If users transmit at the same power
- The received power  $P_i$  at the BS will be different
- close-in users have a larger received power than far-away users

$$\text{SNR for user } i = \frac{P_i}{\sum_{j \neq i} \frac{P_j}{W}}$$

⇒ The close-in users would have a higher SNR than far-away users, making the signal of far-away users difficult to decode.

- We will discuss power-control techniques later.

(60)

## Multicell case with shadow fading

### Assumptions:

- Focus again on uplink
- Power control is executed in each cell, such that the same average receiving power  $P_R$  is received from the mobiles in the cell.
- The channel gain changes slowly due to shadow fading.

X Due to power control, the transmitted power of the mobile must be adjusted according to the fading gain, in order to maintain the same received power.

We assume that power control is fast enough to compensate the changes in channel gain due to shadow fading.

- Assume that shadow fading & path-loss parameters are the same across cells.

$$P_R = P_T \cdot r^{-\alpha} 10^{z/10}, \quad z \sim N(0, \sigma^2)$$



To model the distance  $r$ :

- Mobiles are uniformly distributed in each cell. The average # of users in each cell is  $K$ .
- Hard-handoff: a mobile communicates with the BS in the geometric cell only.

(This is versus the soft-handoff we will discuss later: a mobile communicates with the BS with the smallest propagation loss.)

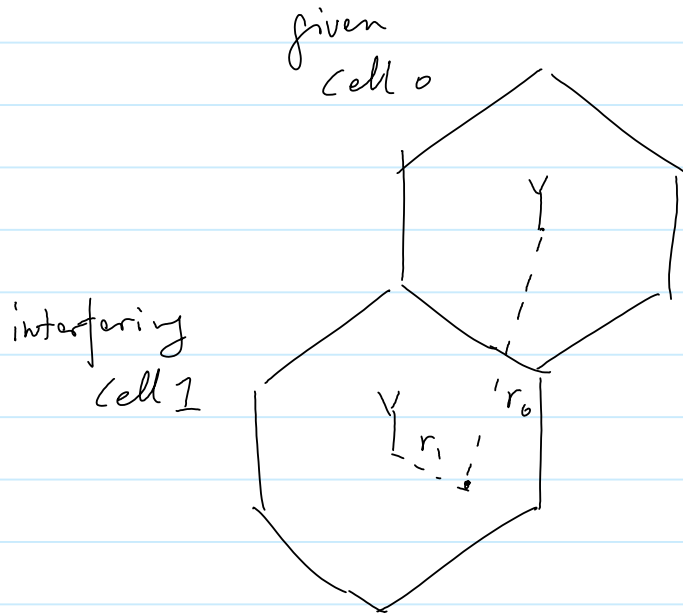
- Ignore multipath fading: Assume it is taken into account in the SINR threshold.

(65)

## Interfering cells - 15min

Saturday, March 15, 2008 11:16 AM

We need to derive the interference from other cells.



Consider a given mobile in interfering cell 1.

Let  $r_i$  be its distance to its own BS,  
let  $r_o$  be its distance to the BS in the cell  
of interest (cell 0).

Let us calculate the interference caused by  
this mobile at the BS of cell 0.

At the interfering cell, since we assume  
perfect power control:

$$P_R = P_{T_i} \cdot r_i^{-n} 10^{3/10}$$

⇒ Transmission power

$$P_{T_i} = P_R \cdot r_i^{-n} 10^{-\alpha_i/10}$$

At cell 0, interference created by this mobile is given by

$$P_{T_i} \cdot r_0^{-n} \cdot 10^{-\alpha_0/10}$$

$$= P_R \cdot \left(\frac{r_i}{r_0}\right)^n 10^{-(\alpha_0 - \alpha_i)/10}$$

Note that the density of the mobile is

$$\rho = \frac{2k}{3\sqrt{3} R^2}$$

↑ radius of cell.

Hence, the total average interference power at  $BS_0$  from mobiles outside  $S_0$  is given by

$$I_{S_0}^* = \frac{2k}{3\sqrt{3} R^2} P_R \cdot$$

Why is expected value enough?

$$\cdot E \left\{ \iint_{S_0^*} \left[ \left(\frac{r_i}{r_0}\right)^n \cdot 10^{-(\alpha_i - \alpha_0)/10} \right] dA \right\}$$

↑

areas outside cell 0.

Assume that shadow fading is independent of the location.

$$I_{S_0^*} = \frac{2k}{2\sqrt{3} R^2} \cdot P_R \cdot \underbrace{E \left[ 10^{(\beta_1 - \beta_0)/10} \right]}_{\text{due to shadow fading}} \cdot \underbrace{\iint_{S_0^*} \left( \frac{r_1}{r_0} \right)^n dA}_{\text{due to mobile location}}$$

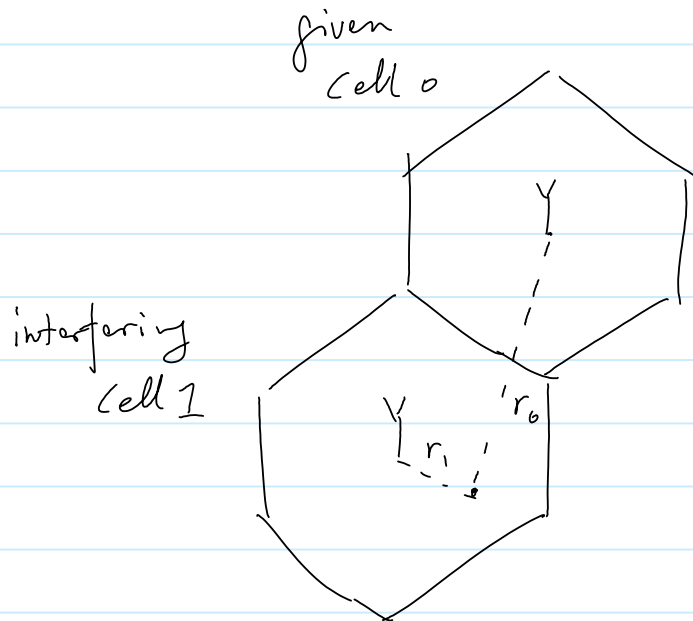
- When there is  
no fading  
 $\Rightarrow 1$

- With fading  
 $> 1$ .

## Interfering cells - handout

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Let  $r_1$  be its distance to its own BS,  
let  $r_0$  be its distance to the BS in the cell  
of interest (cell 0).

Let us calculate the interference caused by  
this mobile at the BS of cell 0.

At the interfering cell, since we assume  
perfect power control:

$$P_R = P_{T_1} \cdot r_1^{-n} 10^{3.1/10}$$

⇒ Transmission power  
 $P_{T_i} =$

At cell 0, interference created by this mobile is given by

$$P_{T_i} \cdot r_0^{-n} \cdot 10^{\delta_0/10}$$

=

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Why is expected value enough?

Assume that shadow fading is independent of the location.

$$I_{S_0}^* = .$$

## Effect of shadow fading - 10min

Saturday, March 15, 2008

11:30 AM

Let us first derive

$$\bar{E} \left[ 10^{(z_1 - z_0)/10} \right]$$

$$z_1, z_0 \sim N(0, \sigma^2)$$

In general,  $z_1$  &  $z_0$  may be correlated because  $BS_0$  &  $BS_1$  are close to each other.

Assume in addition that

$$z_i = ah + b h_i, \quad i=1,2$$

where

$h, h_i$ 's are Gaussian r.v.'s  $N(0, \sigma^2)$

$h$  represents the fading term common to  $z_1$  &  $z_0$

$h_i$ 's represent the independent fading terms.

$a, b$  are coefficients,  $a^2 + b^2 = 1$

Then

$$y \triangleq z_1 - z_0 = b(h_1 - h_0)$$

is a Gaussian r.v. with variance  $2b^2\sigma^2 \triangleq \sigma_y^2$

Knowing  $\sigma_y^2$ , we can then calculate

$$\bar{E} \left[ 10^{(z_1 - z_0)/10} \right] \triangleq \bar{E} \left[ 10^{y/10} \right]$$



$$E[10^{y - \frac{\ln 10}{10}}] = E[10^{y/10}]$$

$$= \int e^{y \cdot \frac{\ln 10}{10}} \cdot \frac{1}{\sqrt{2\pi} \sigma_y} e^{-y^2/2\sigma_y^2} dy$$

$$= \frac{1}{\sqrt{2\pi} \sigma_y} \int e^{-\frac{1}{2\sigma_y^2} (y - \sigma_y^2 \frac{\ln 10}{10})^2} \cdot e^{\frac{1}{2} \sigma_y^2 (\frac{\ln 10}{10})^2} dy$$

$$= e^{\frac{1}{2} \sigma_y^2 (\frac{\ln 10}{10})^2}$$

30

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$$= 1 \quad \text{if} \quad \sigma_y = 0$$

$$> 1 \quad \text{in general}$$

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30

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