2.62 Determine the autocorrelation sequences of the following signals.

(a)
$$x(n) = \{1, 2, 1, 1\}$$

(b)
$$y(n) = \{1, 1, 2, 1\}$$

What is your conclusion?

2.63 What is the normalized autocorrelation sequence of the signal x(n) given by

$$x(n) = \begin{cases} 1, & -N \le n \le N \\ 0, & \text{otherwise} \end{cases}$$

2.64 An audio signal s(t) generated by a loudspeaker is reflected at two different walls with reflection coefficients r_1 and r_2 . The signal x(t) recorded by a microphone close to the loudspeaker, after sampling, is

$$x(n) = s(n) + r_1 s(n - k_1) + r_2 s(n - k_2)$$

where k_1 and k_2 are the delays of the two echoes.

- (a) Determine the autocorrelation $r_{xx}(l)$ of the signal x(n).
- **(b)** Can we obtain r_1 , r_2 , k_1 , and k_2 by observing $r_{xx}(l)$?
- (c) What happens if $r_2 = 0$?
- **2.65** Time-delay estimation in radar Let $x_a(t)$ be the transmitted signal and $y_a(t)$ be the received signal in a radar system, where

$$y_a(t) = ax_a(t - t_d) + v_a(t)$$

and $v_a(t)$ is additive random noise. The signals $x_a(t)$ and $y_a(t)$ are sampled in the receiver, according to the sampling theorem, and are processed digitally to determine the time delay and hence the distance of the object. The resulting discrete-time signals are

$$x(n) = x_a(nT)$$

$$y(n) = y_a(nT) = ax_a(nT - DT) + v_a(nT)$$

$$\stackrel{\triangle}{=} ax(n - D) + v(n)$$

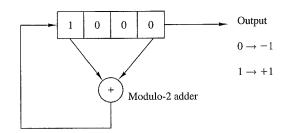


Figure P2.65 Linear feedback shift register.



(b) Le

an W D

- (c) Co
- (d) R
- (e) R

fe (f) R fi to

N

(a) Explain how we can measure the delay D by computing the crosscorrelation $r_{xy}(l)$.

(b) Let x(n) be the 13-point Barker sequence

$$x(n) = \{+1, +1, +1, +1, +1, -1, -1, +1, +1, -1, +1, -1, +1\}$$

and v(n) be a Gaussian random sequence with zero mean and variance $\sigma^2 = 0.01$. Write a program that generates the sequence y(n), $0 \le n \le 199$ for a = 0.9 and D = 20. Plot the signals x(n), y(n), $0 \le n \le 199$.

(c) Compute and plot the crosscorrelation $r_{xy}(l)$, $0 \le l \le 59$. Use the plot to estimate the value of the delay D.

(d) Repeat parts (b) and (c) for $\sigma^2 = 0.1$ and $\sigma^2 = 1$.

(e) Repeat parts (b) and (c) for the signal sequence

$$x(n) = \{-1, -1, -1, +1, +1, +1, +1, -1, +1, -1, +1, +1, -1, -1, +1\}$$

which is obtained from the four-stage feedback shift register shown in Fig. P2.65. Note that x(n) is just one period of the periodic sequence obtained from the feedback shift register.

(f) Repeat parts (b) and (c) for a sequence of period $N = 2^7 - 1$, which is obtained from a seven-stage feedback shift register. Table 2.2 gives the stages connected to the modulo-2 adder for (maximal-length) shift-register sequences of length $N = 2^m - 1$.

TABLE 2.2 Shift-Register Connections for Generating Maximal-Length Sequences

uting munimum Zongm bodwones	
m	Stages Connected to Modulo-2 Adder
1	1
2	1, 2
3	1, 3
4	1, 4
5 6	1, 4
6	1, 6
7	1, 7
8	1, 5, 6, 7
9	1, 6
10	1, 8
11	1, 10
12	1, 7, 9, 12
13	1, 10, 11, 13
14	1, 5, 9, 14
15	1, 15
16	1, 5, 14, 16
17	1, 15

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different walls rophone close

nd $y_a(t)$ be the

sampled in the itally to deterg discrete-time

utput

→ -

 $\rightarrow +1$