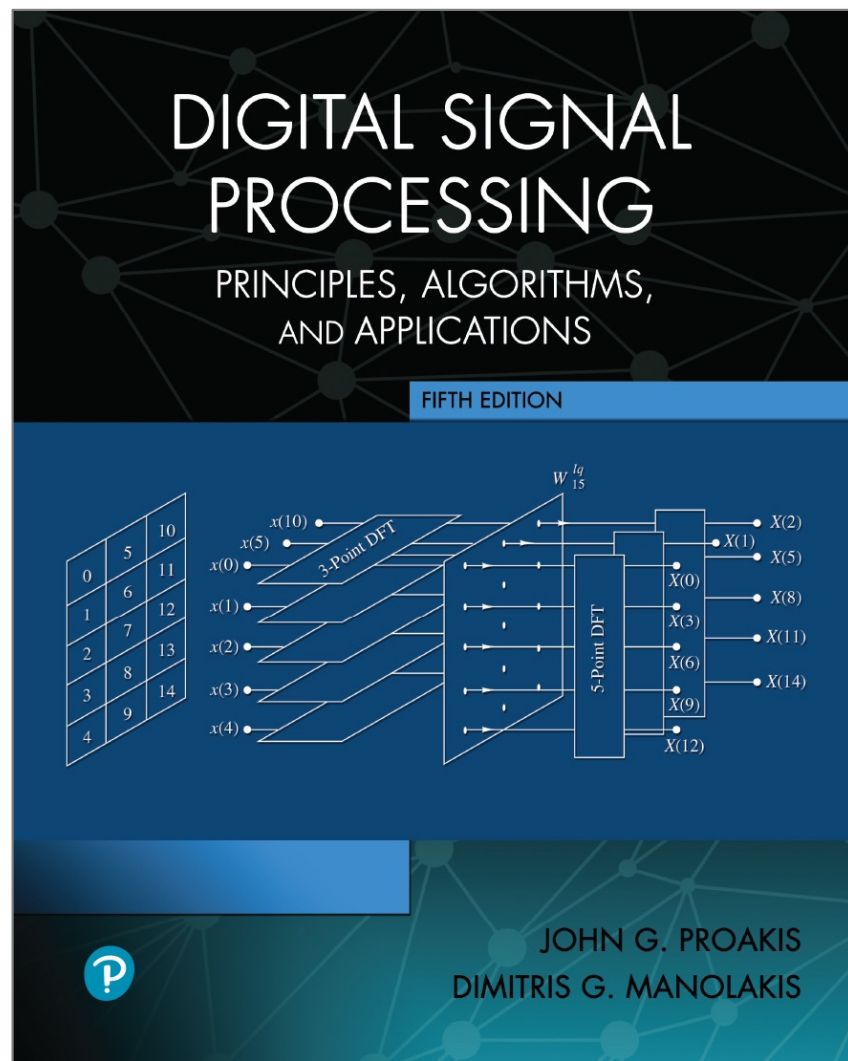


# Digital Signal Processing

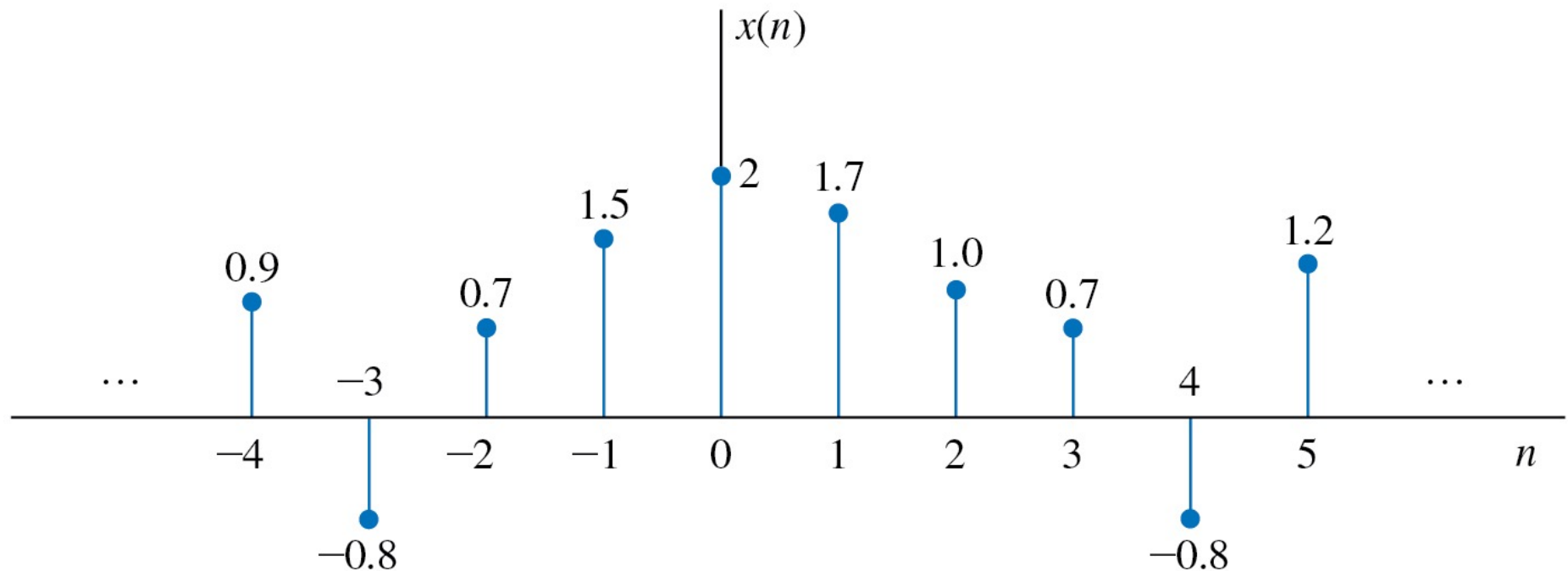
Fifth Edition



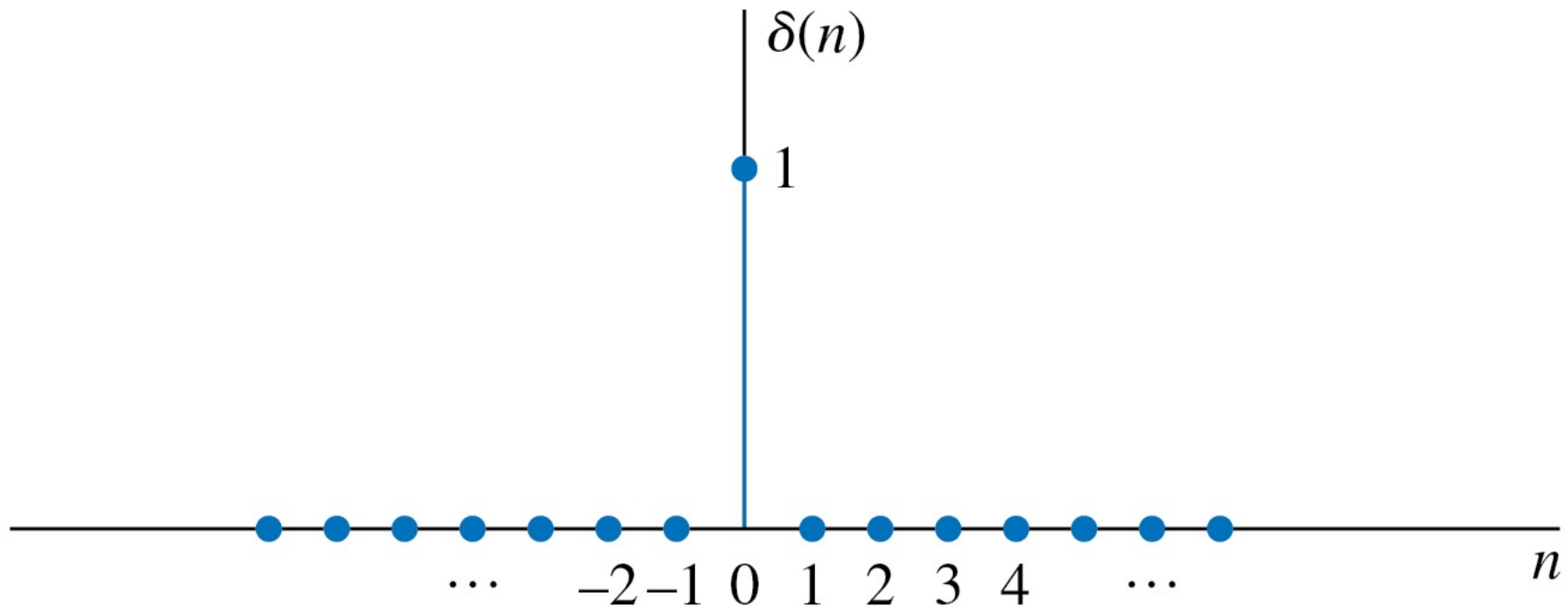
## Chapter 2

### Discrete-Time Signals and Systems

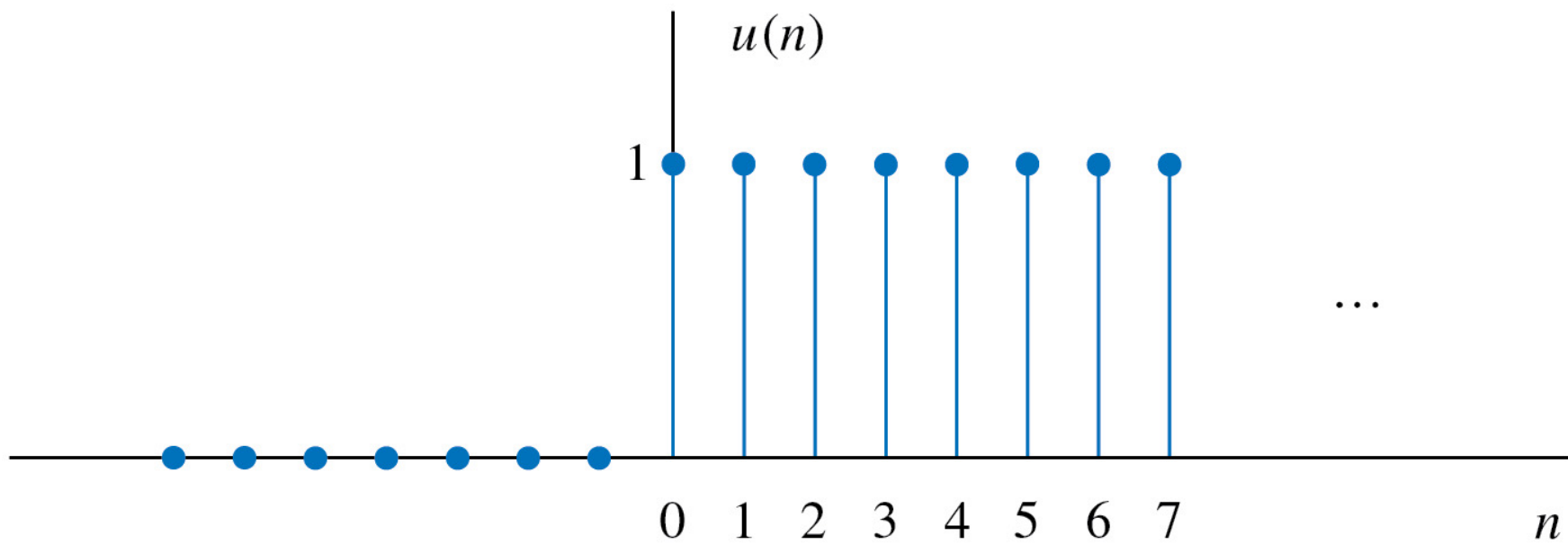
**Figure 2.1.1** Graphical representation of a discrete-time signal.



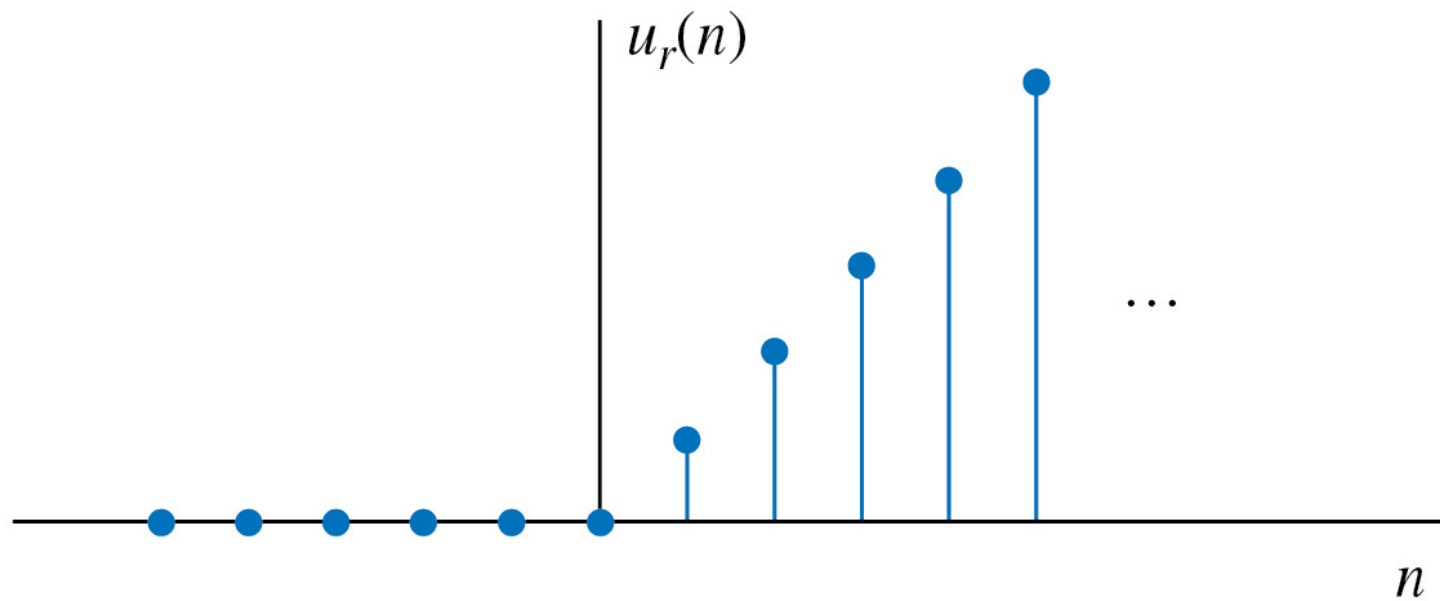
**Figure 2.1.2** Graphical representation of the unit sample signal.



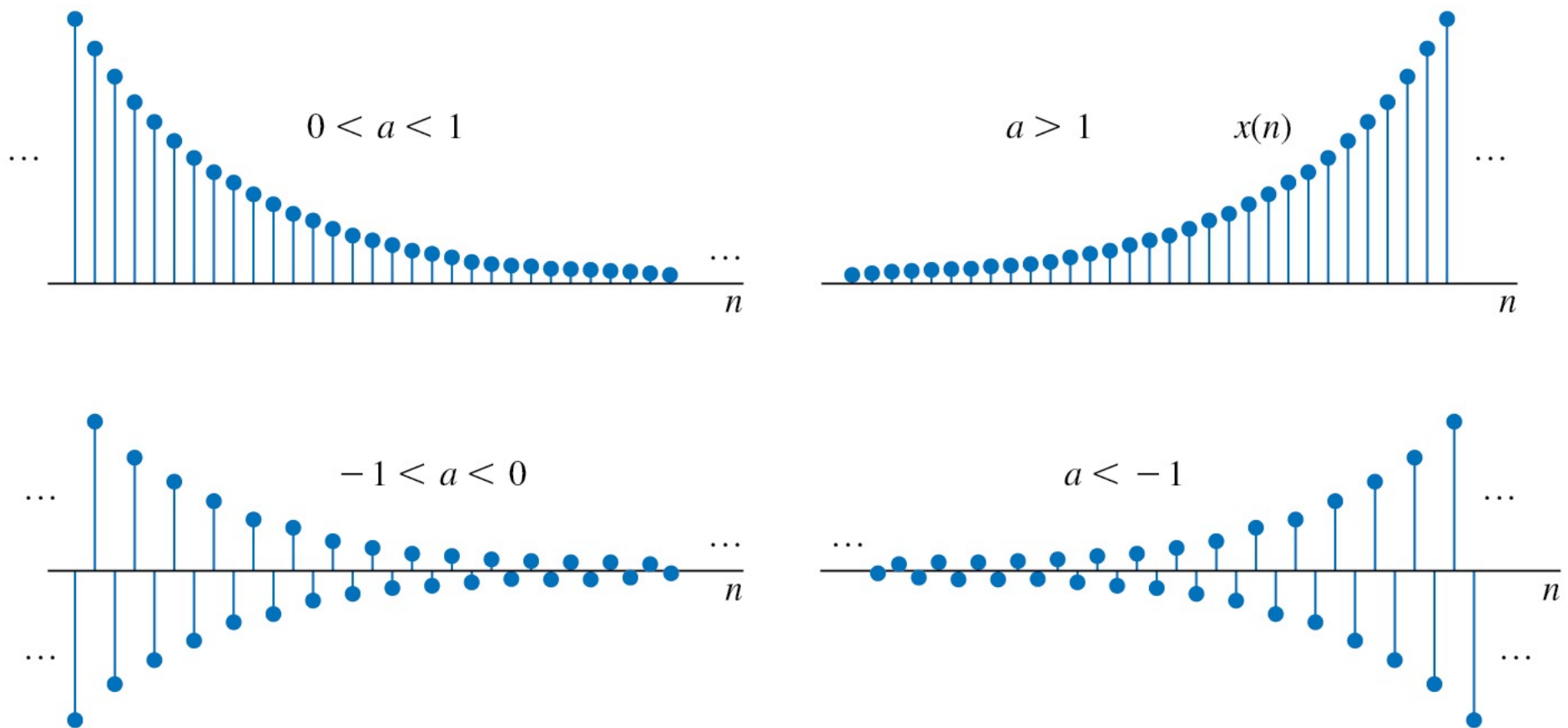
**Figure 2.1.3** Graphical representation of the unit step signal.



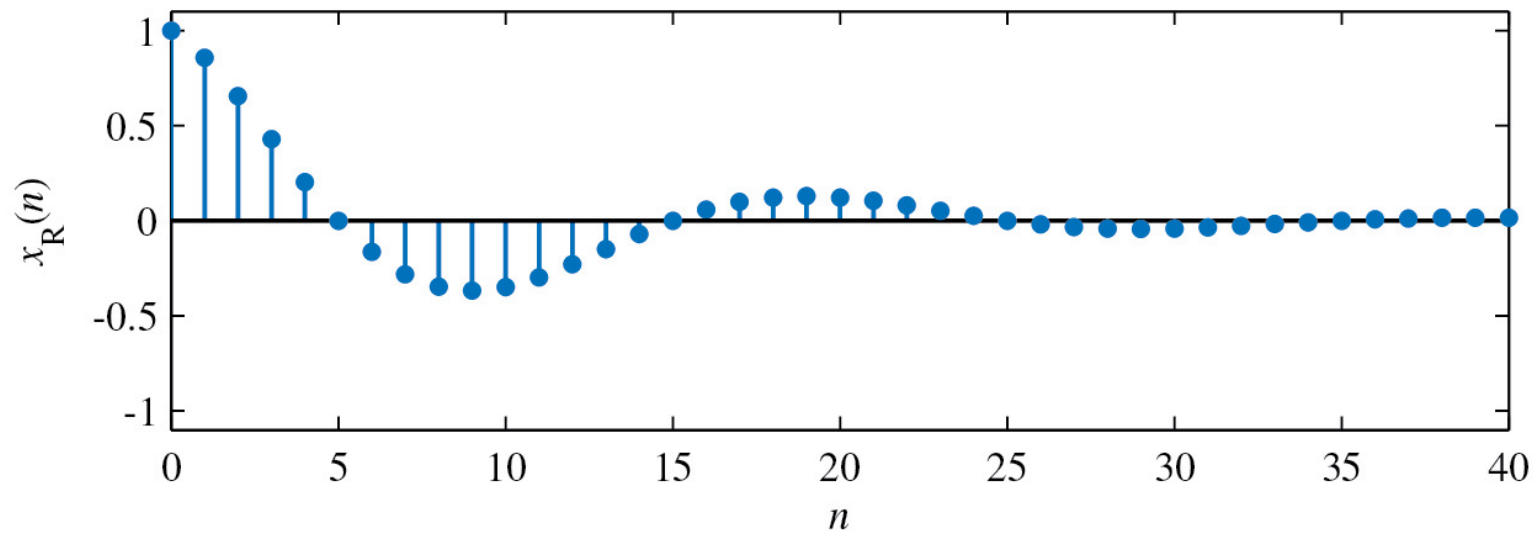
**Figure 2.1.4** Graphical representation of the unit ramp signal.



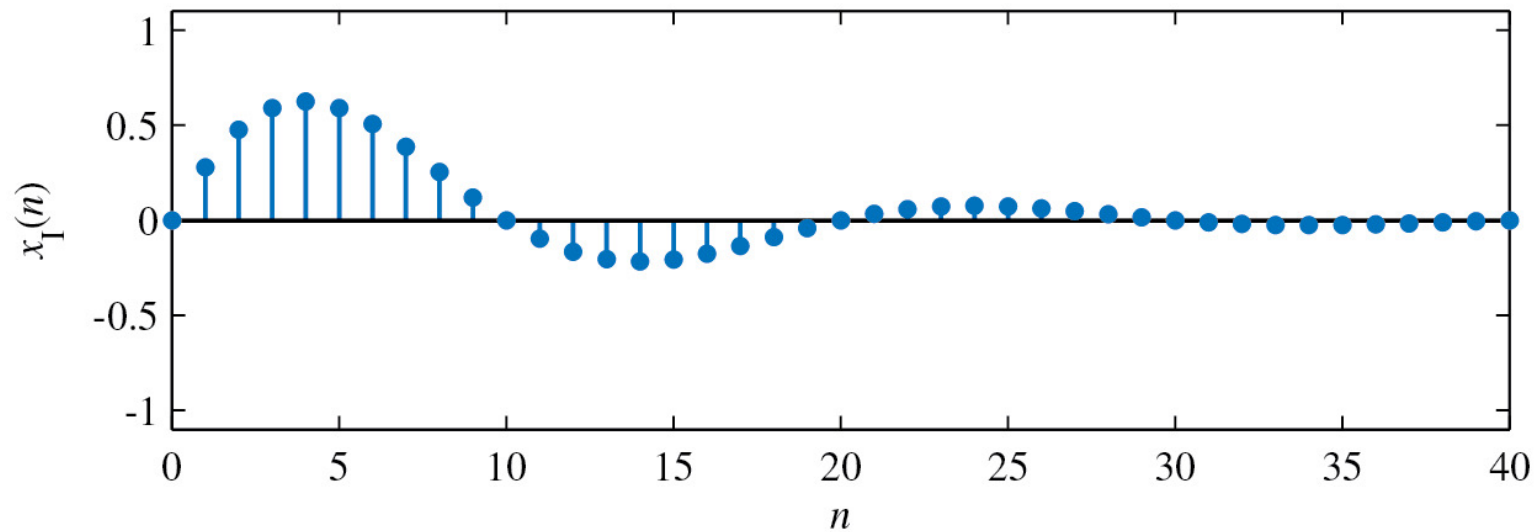
**Figure 2.1.5** Graphical representation of exponential signal.



**Figure 2.1.6** Graph of the real and imaginary components of a complex-valued exponential signal.

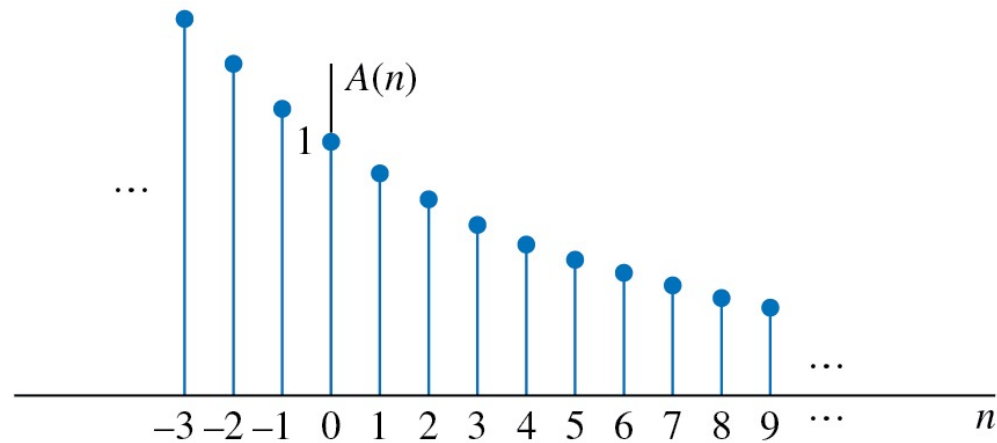


(a)

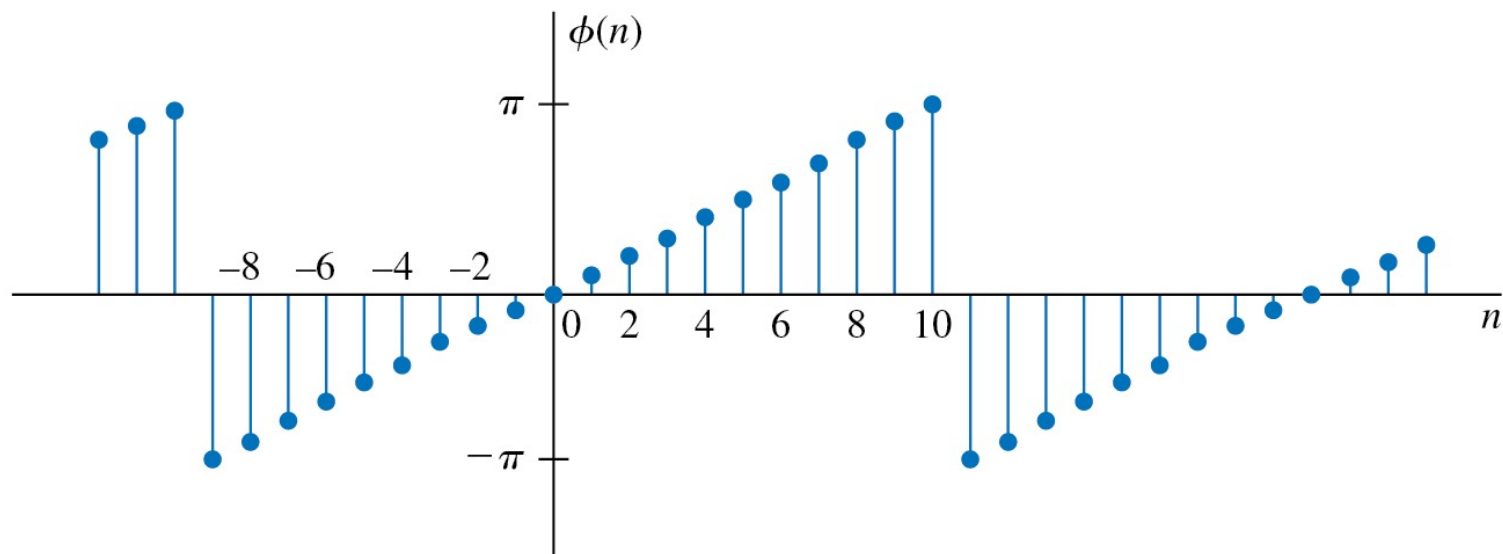


(b)

**Figure 2.1.7** Graph of amplitude and phase function of a complex-valued exponential signal: (a) graph of  $A(n) = r^n$ ,  $r = 0.9$ ; (b) graph of  $\phi(n) = (\pi/10)n$ , modulo  $2\pi$  plotted in the range  $(-\pi, \pi]$ .



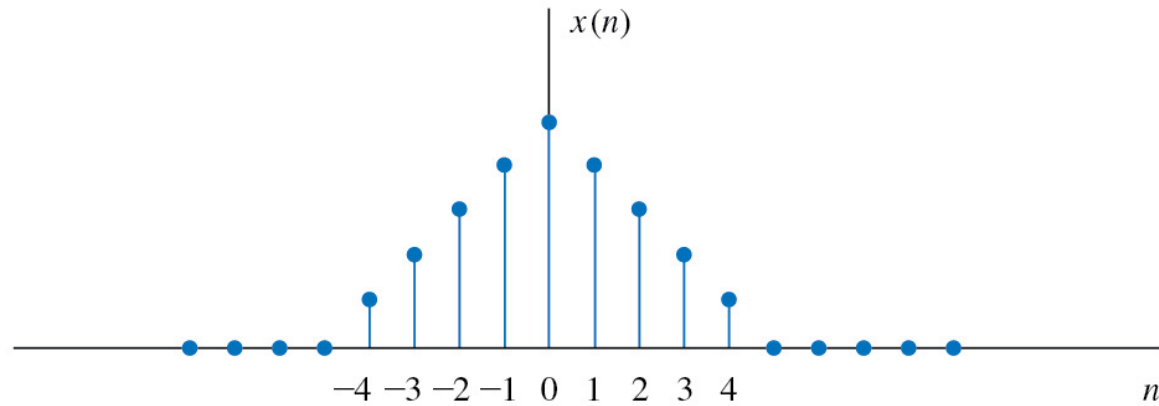
(a) Graph of  $A(n) = r^n$ ,  $r = 0.9$



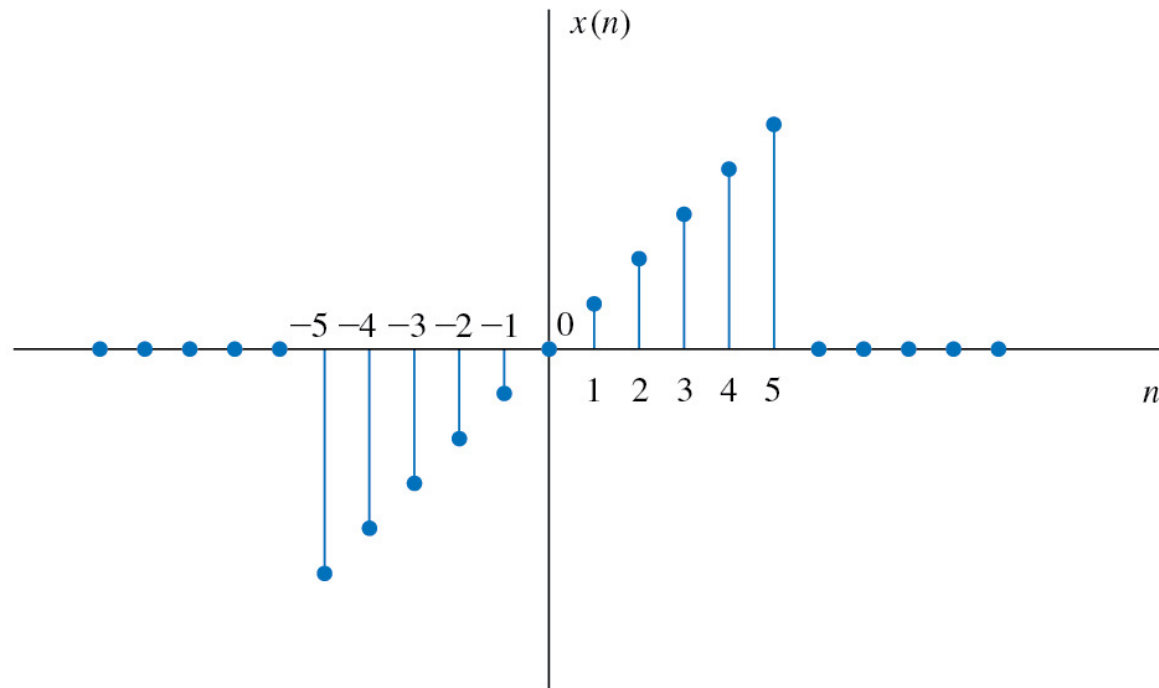
(b) Graph of  $\phi(n) = \frac{\pi}{10}n$ , modulo  $2\pi$  plotted in the range  $(-\pi, \pi]$



**Figure 2.1.8** Example of even (a) and odd (b) signals.

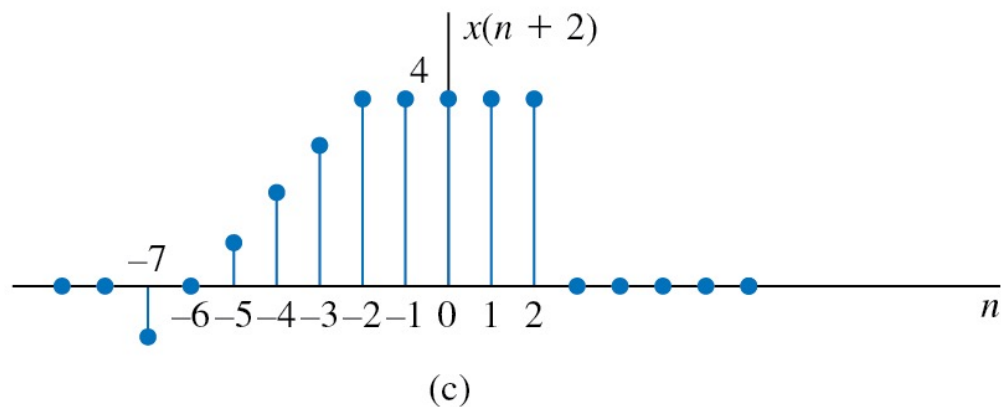
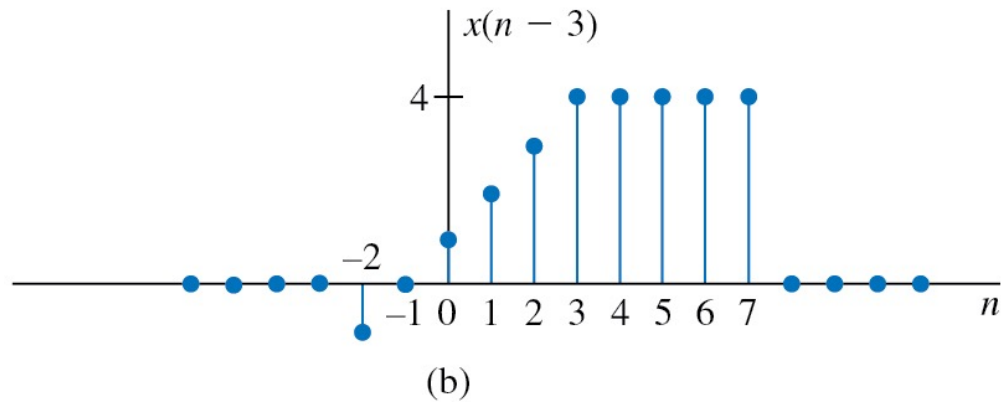
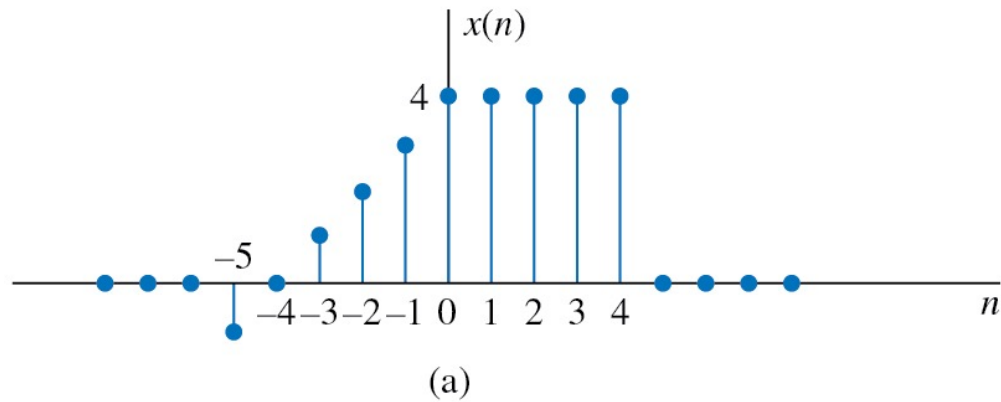


(a)

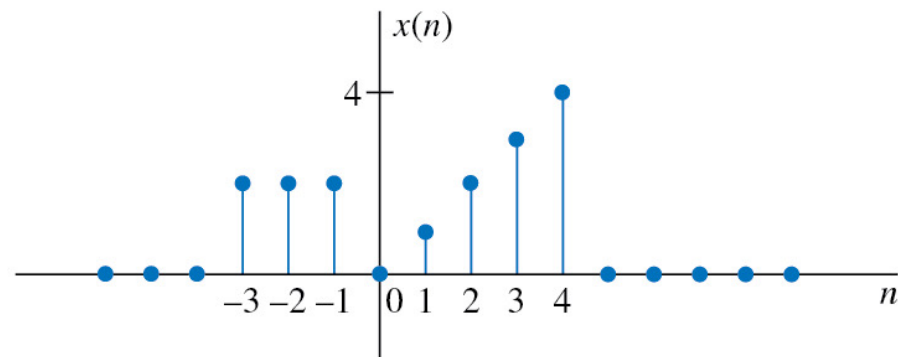


(b)

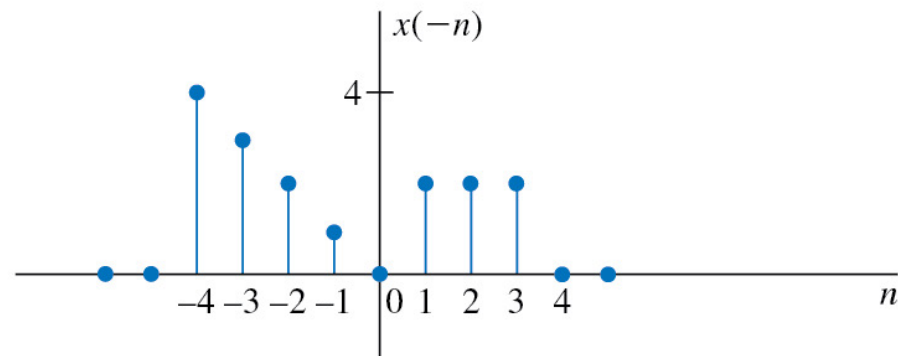
**Figure 2.1.9** Graphical representation of a signal, and its delayed and advanced versions.



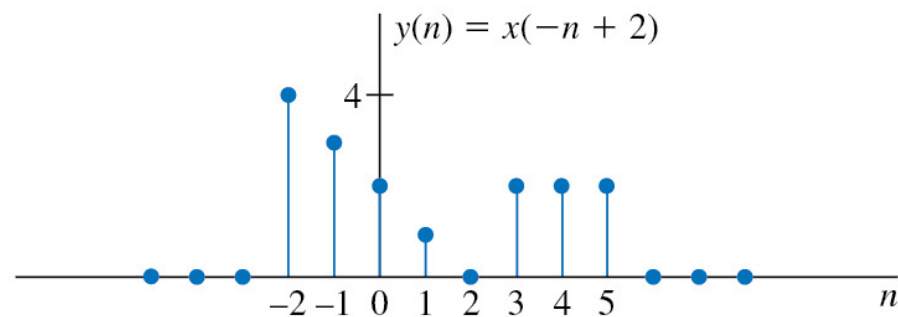
**Figure 2.1.10** Graphical illustration of the folding and shifting operations.



(a)

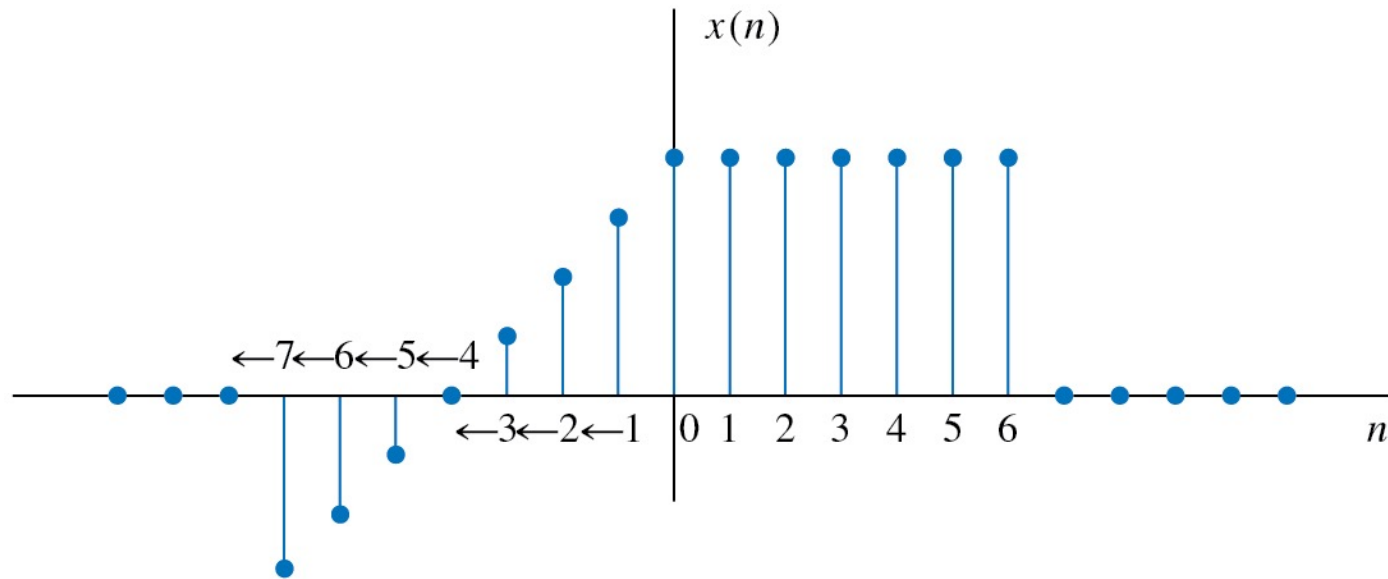


(b)

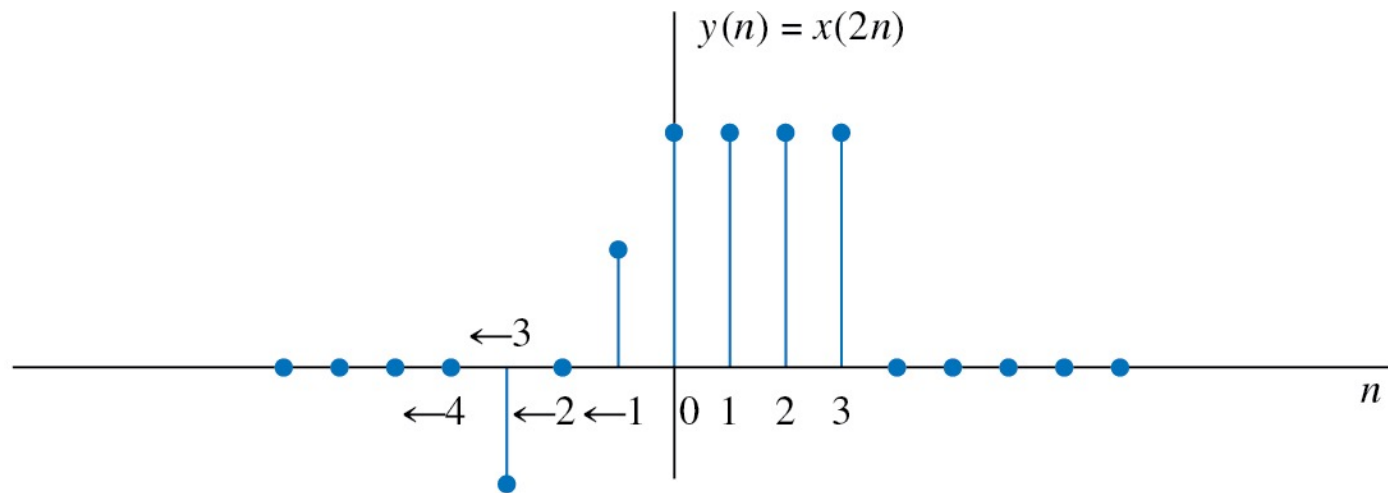


(c)

**Figure 2.1.11** Graphical illustration of down-sampling operation.

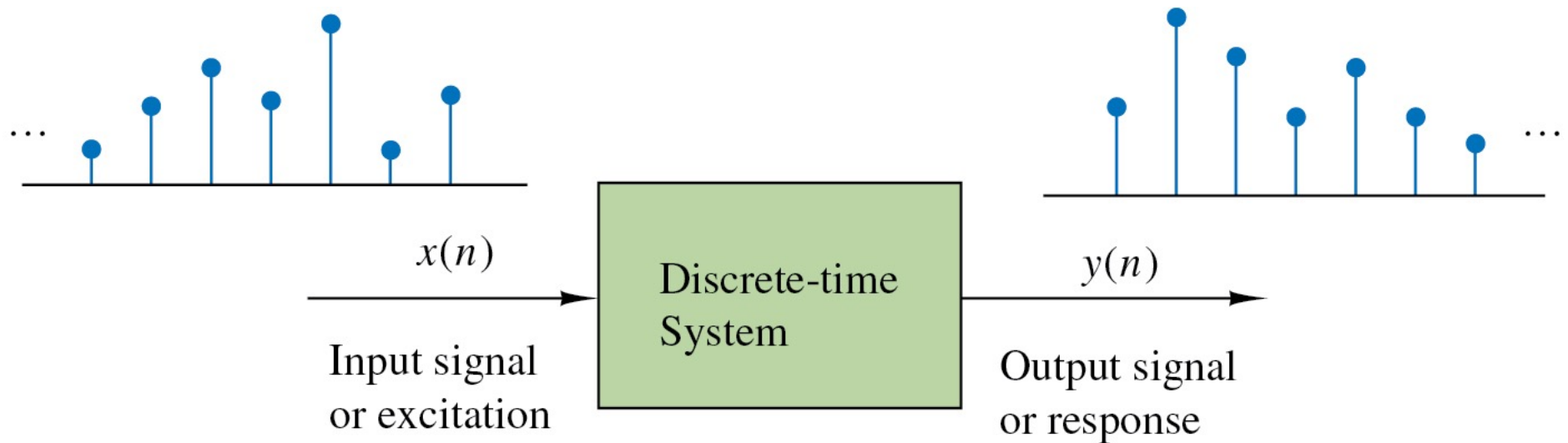


(a)

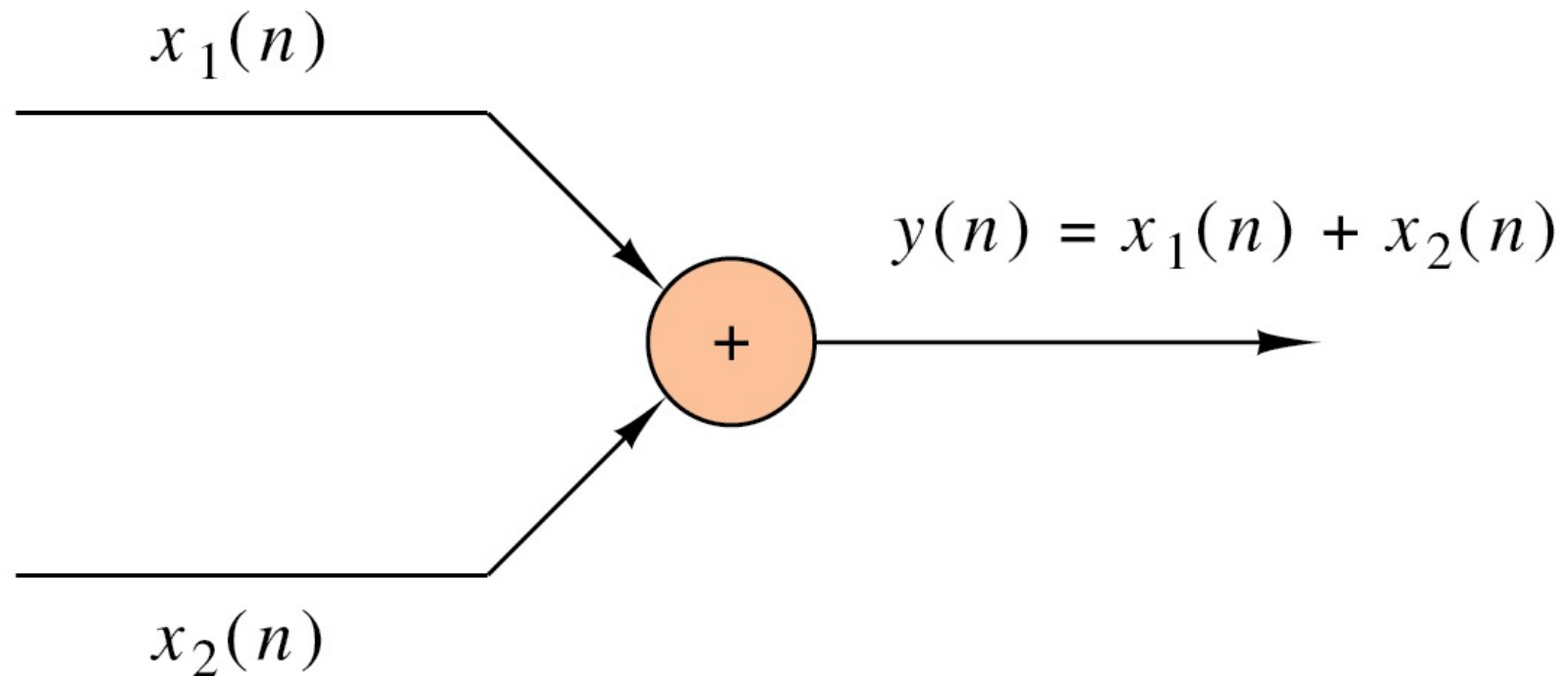


(b)

**Figure 2.2.1** Block diagram representation of a discrete-time system.



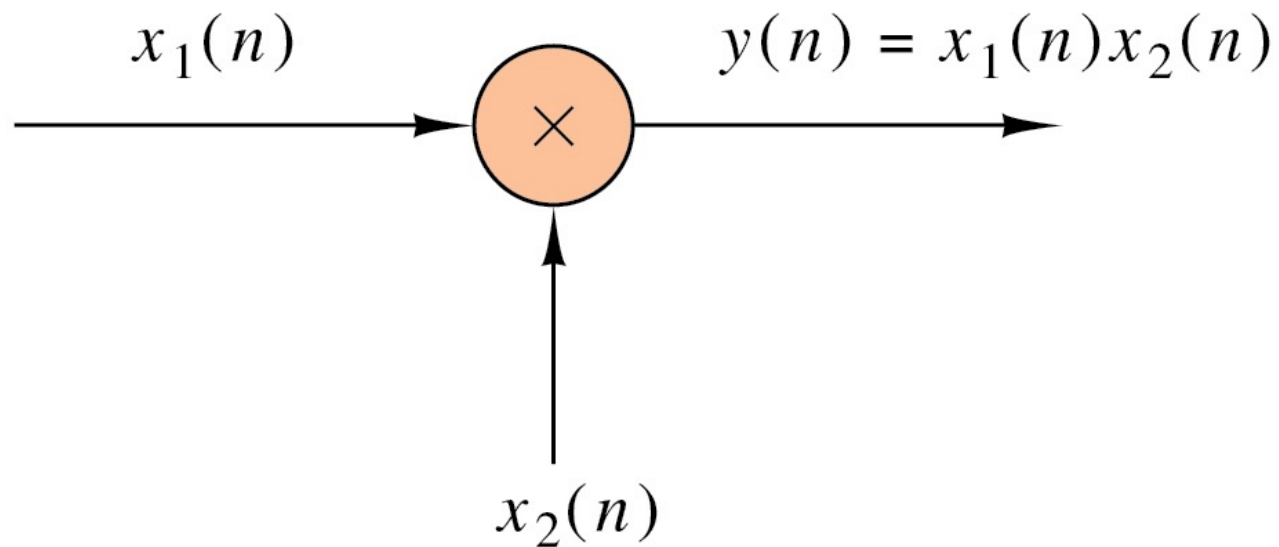
**Figure 2.2.2** Graphical representation of an adder.



**Figure 2.2.3** Graphical representation of a constant multiplier.

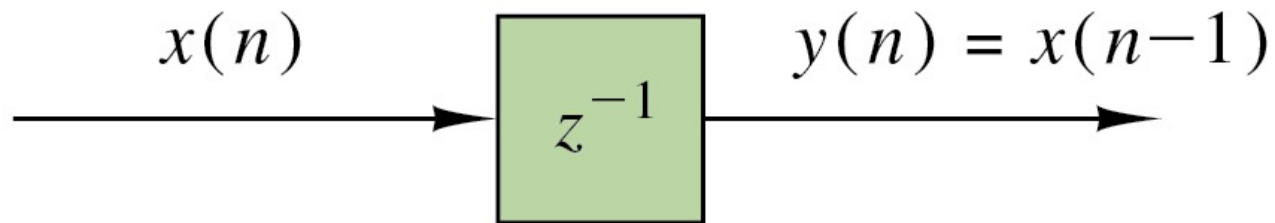


**Figure 2.2.4** Graphical representation of a signal multiplier.

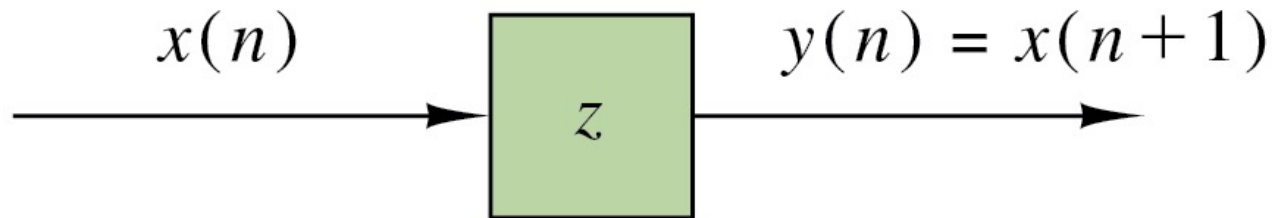




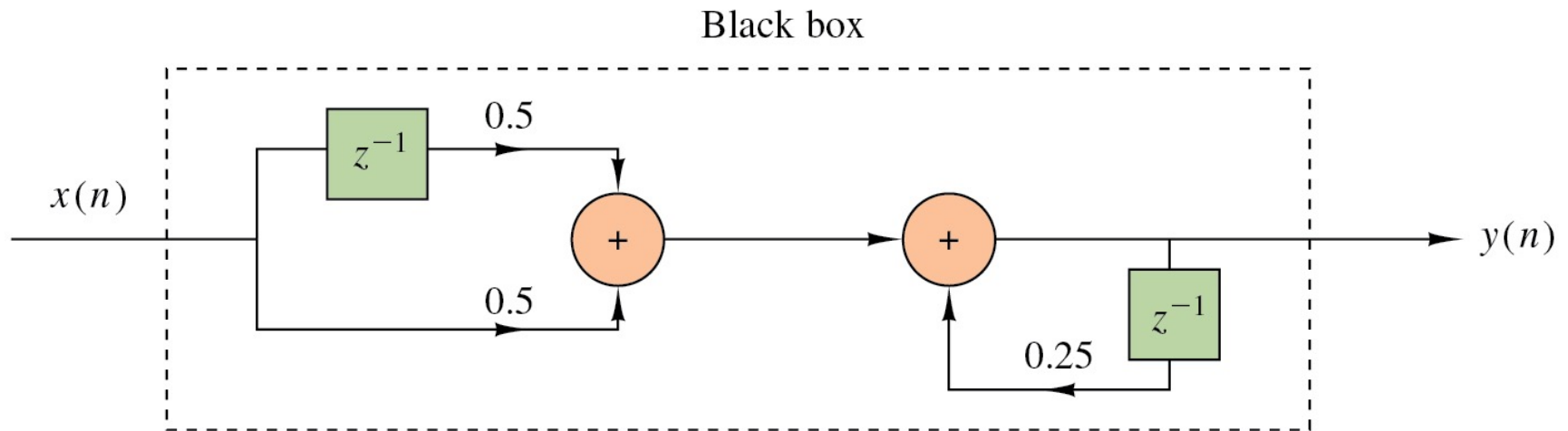
**Figure 2.2.5** Graphical representation of the unit delay element.



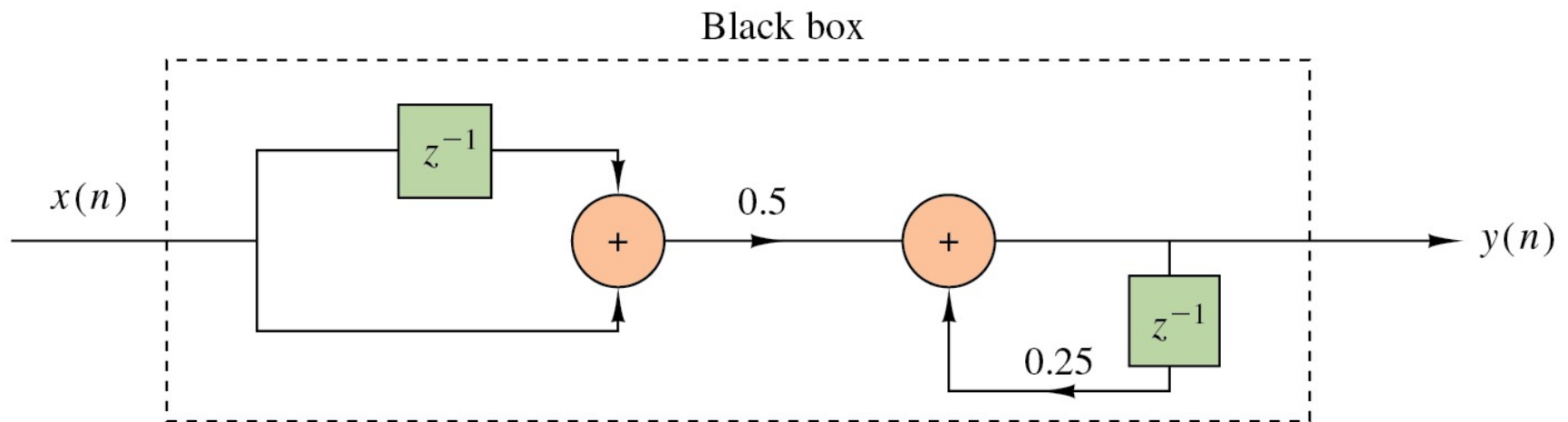
**Figure 2.2.6** Graphical representation of the unit advance element.



**Figure 2.2.7** Block diagram realizations of the system  $y(n] = 0.25y[n - 1] + 0.5x[n] + 0.5x[n - 1]$ .

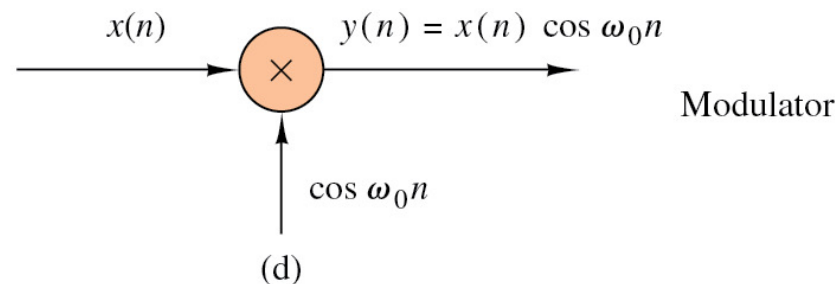
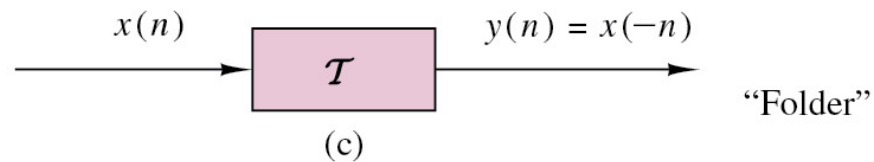
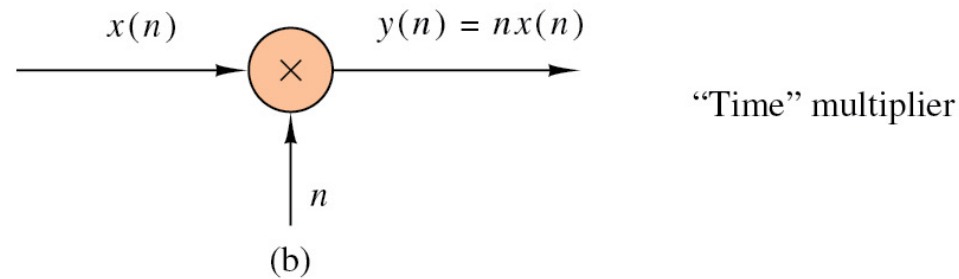
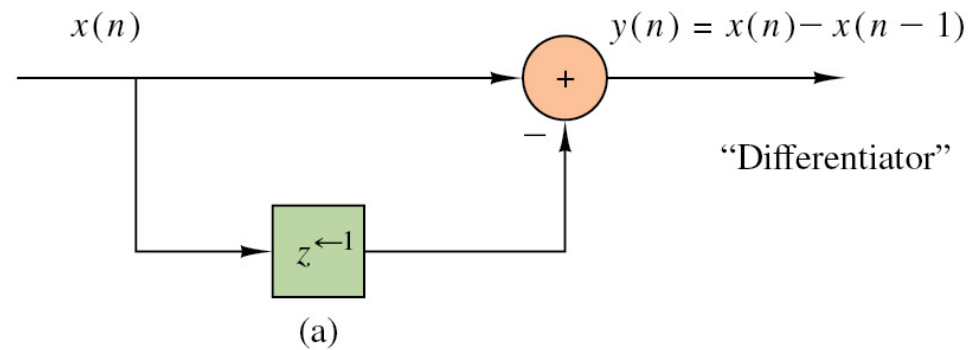


(a)

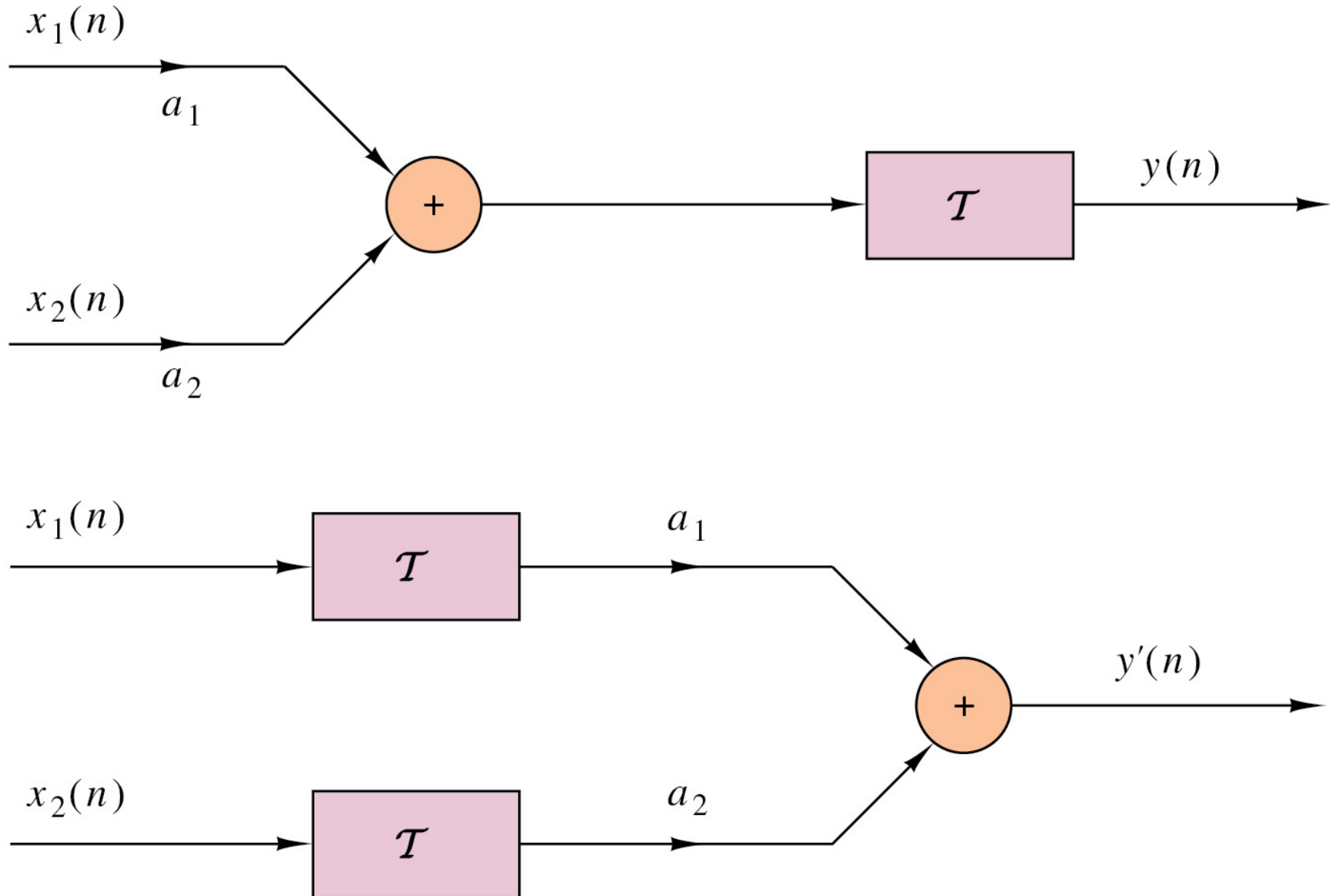


(b)

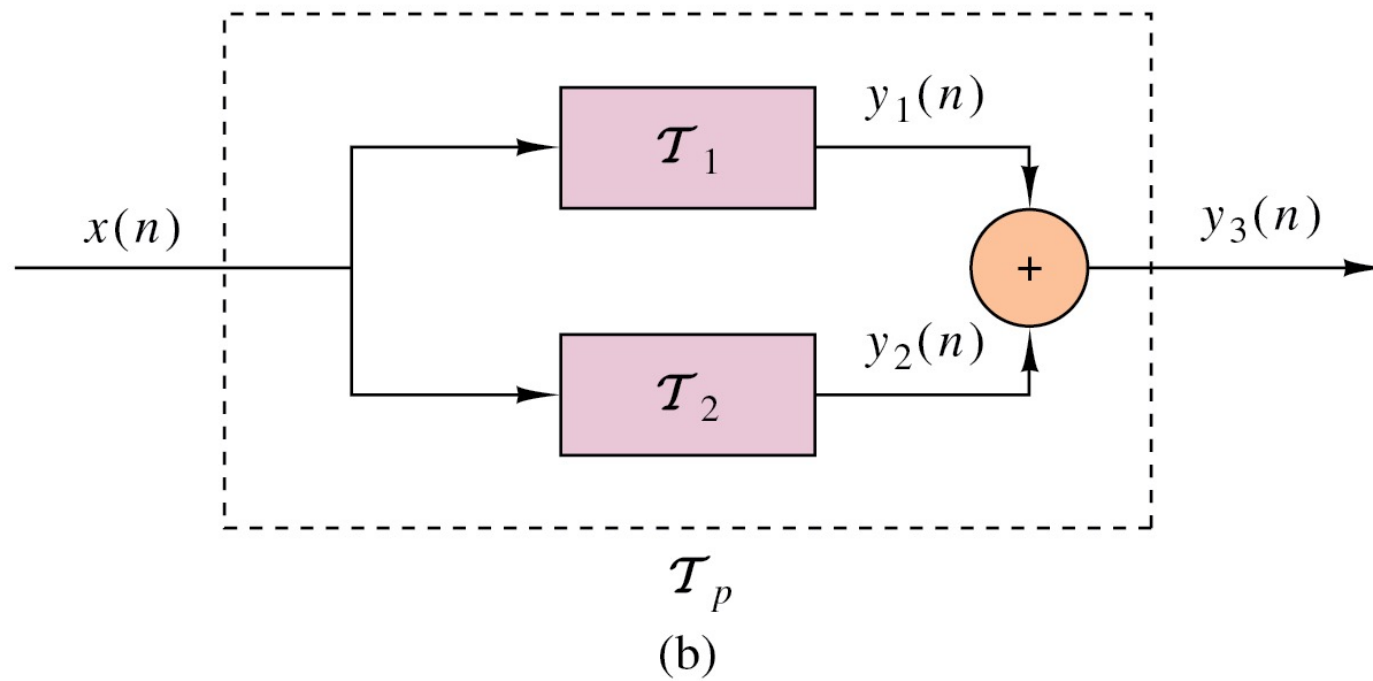
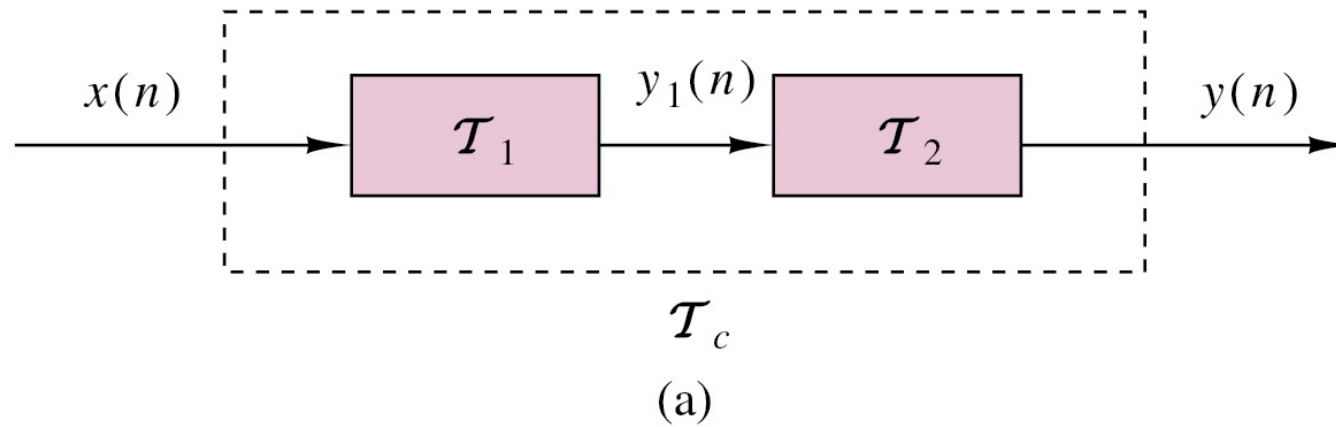
**Figure 2.2.8** Examples of a time-invariant (a) and some time-variant systems (b)–(d).



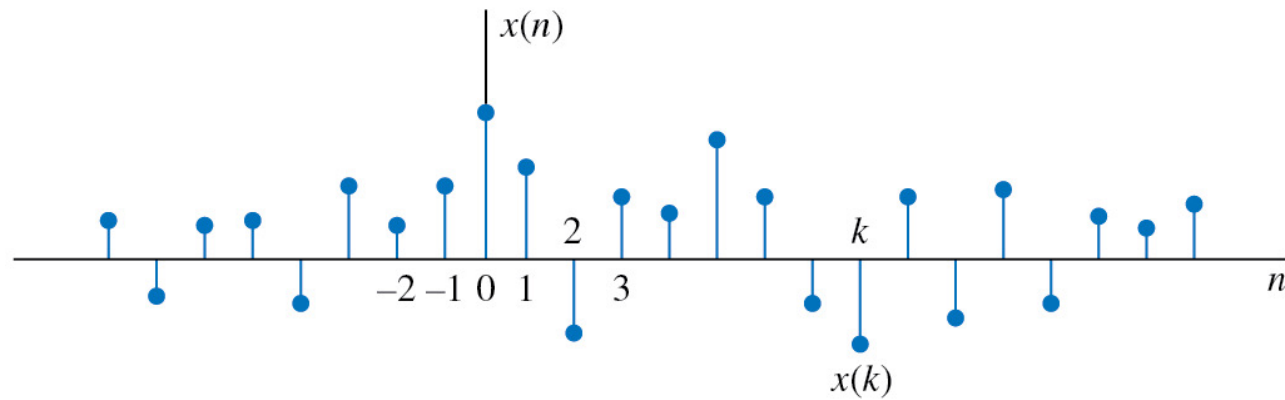
**Figure 2.2.9** Graphical representation of the superposition principle.  $T$  is linear if and only if  $y(n) = y'(n)$ .



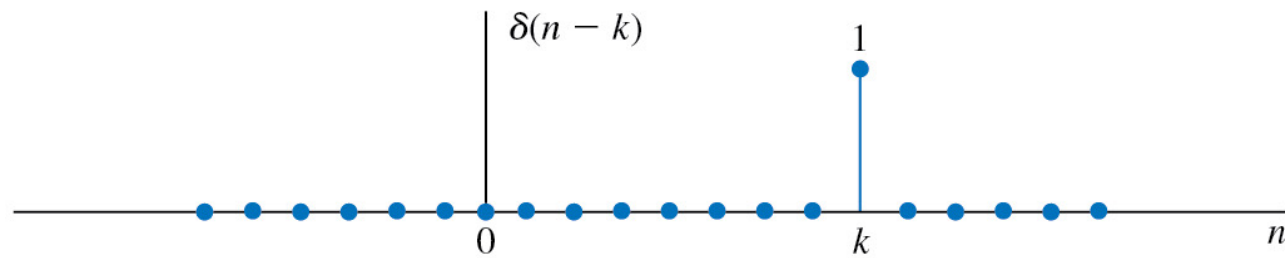
**Figure 2.2.10** Cascade (a) and parallel (b) interconnections of systems.



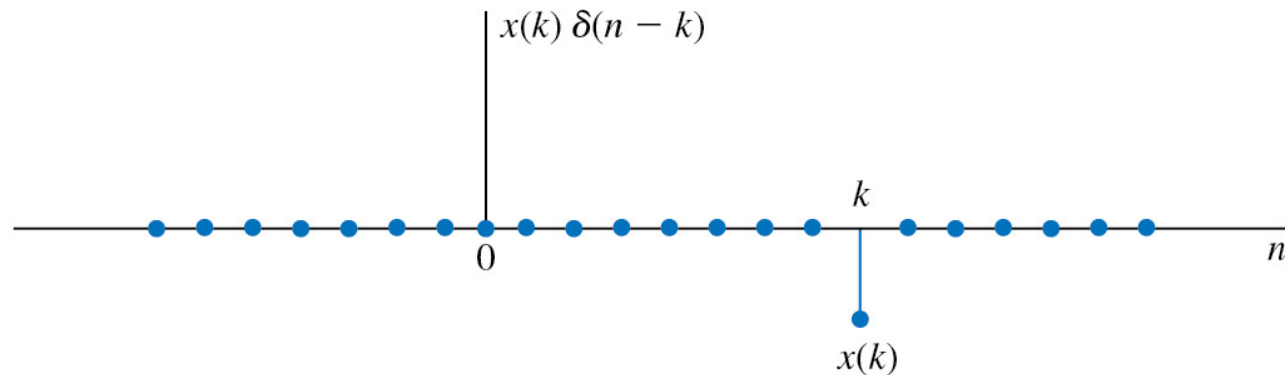
**Figure 2.3.1** Multiplication of a signal  $x(n]$  with a shifted unit sample sequence.



(a)

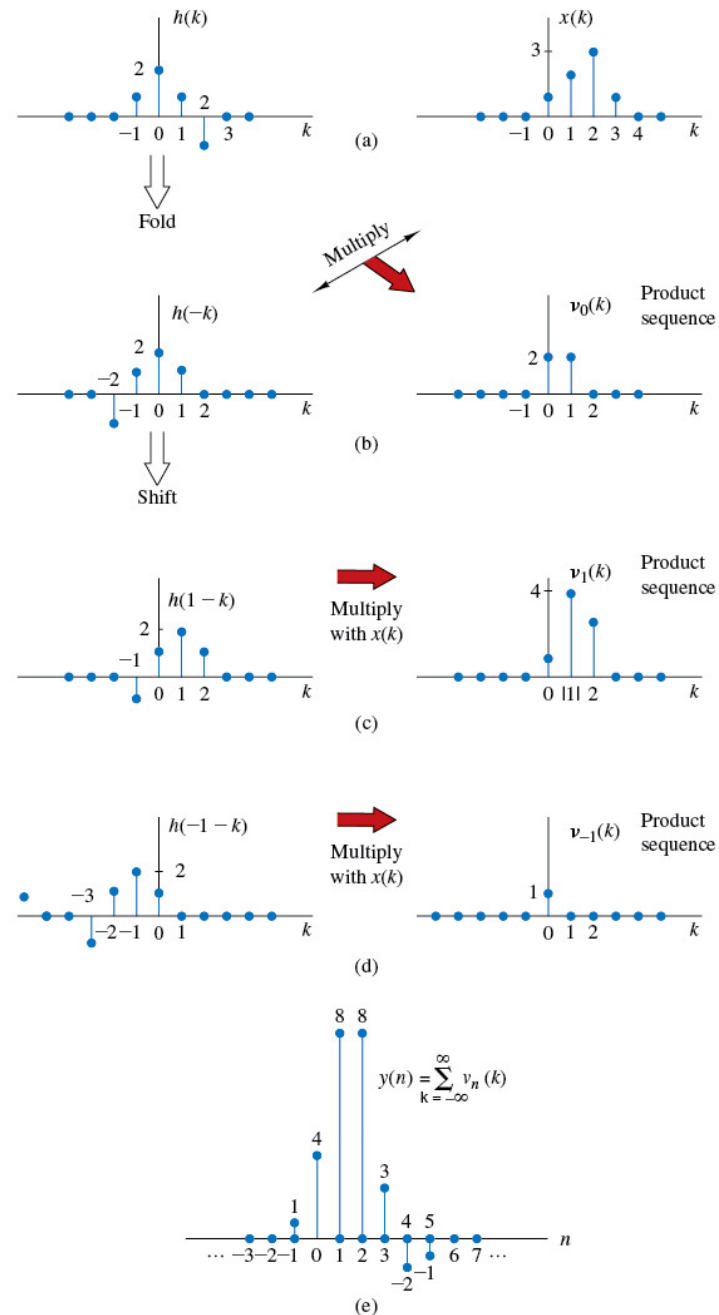


(b)



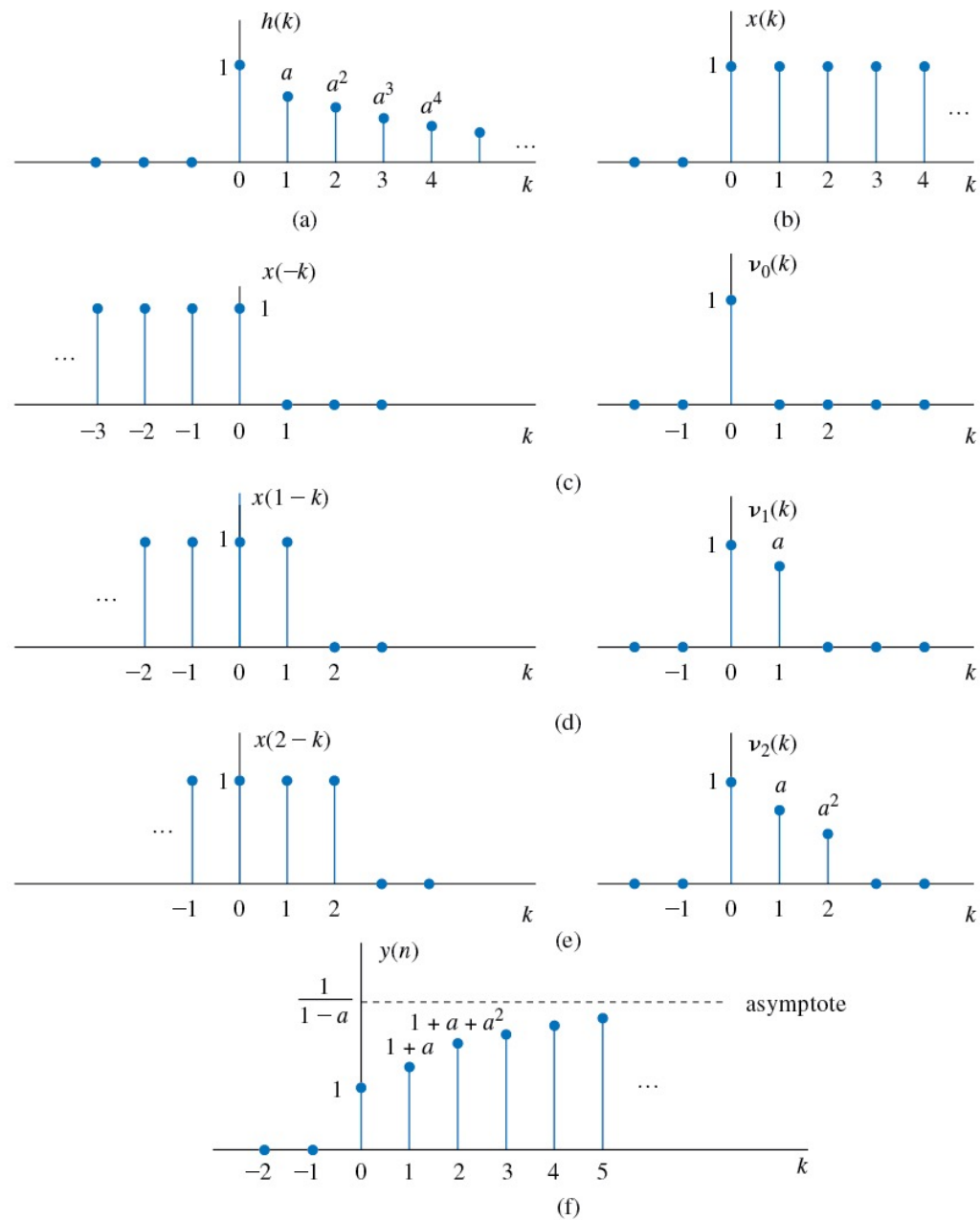
(c)

**Figure 2.3.2** Graphical computation of convolution.

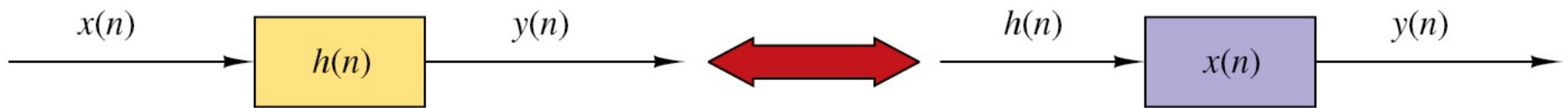




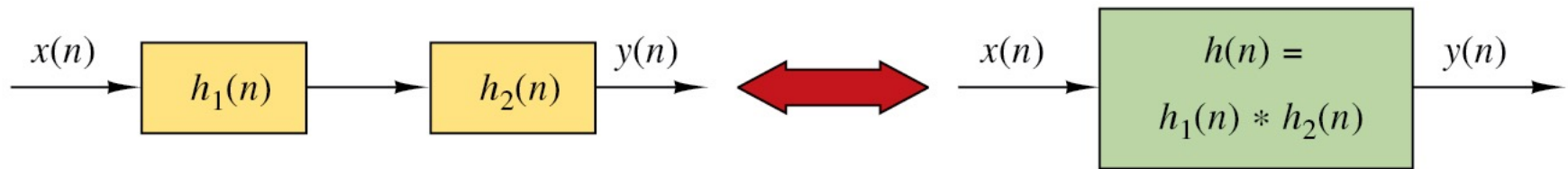
**Figure 2.3.3** Graphical computation of convolution in Example 2.3.3.



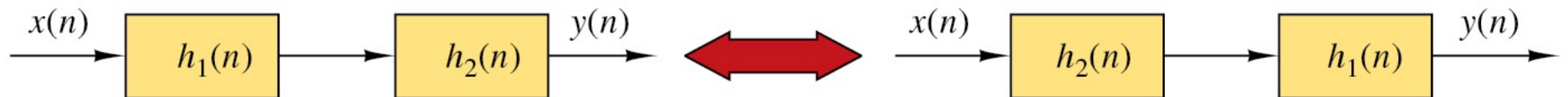
**Figure 2.3.4** Interpretation of the commutative property of convolution.



**Figure 2.3.5** Implications of the associative (a) and the associative and commutative (b) properties of convolution.

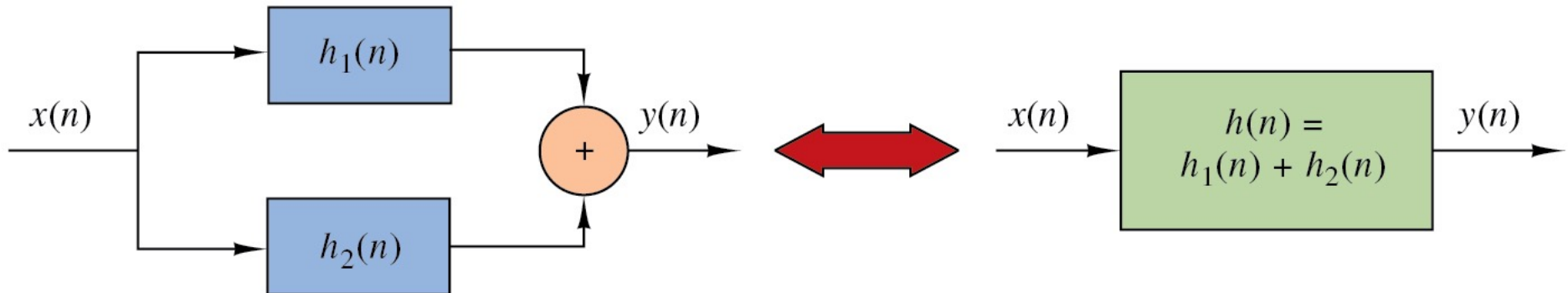


(a)

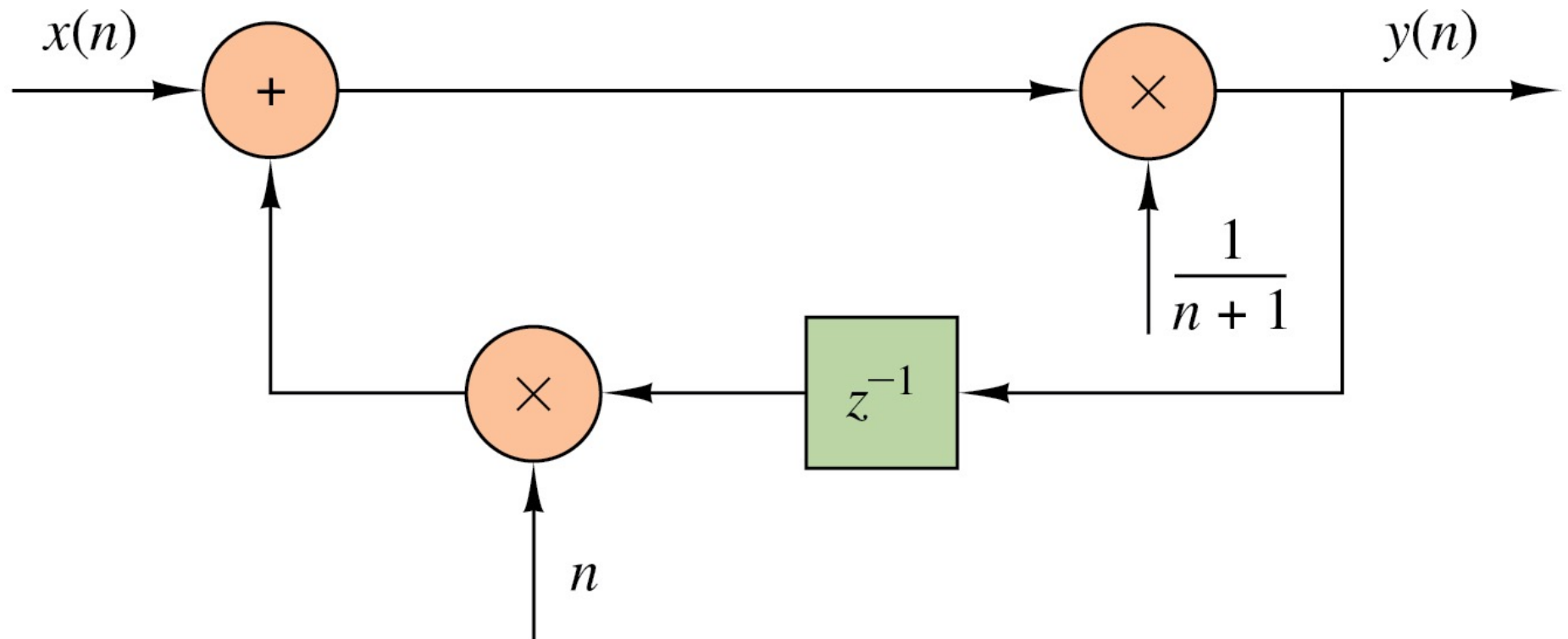


(b)

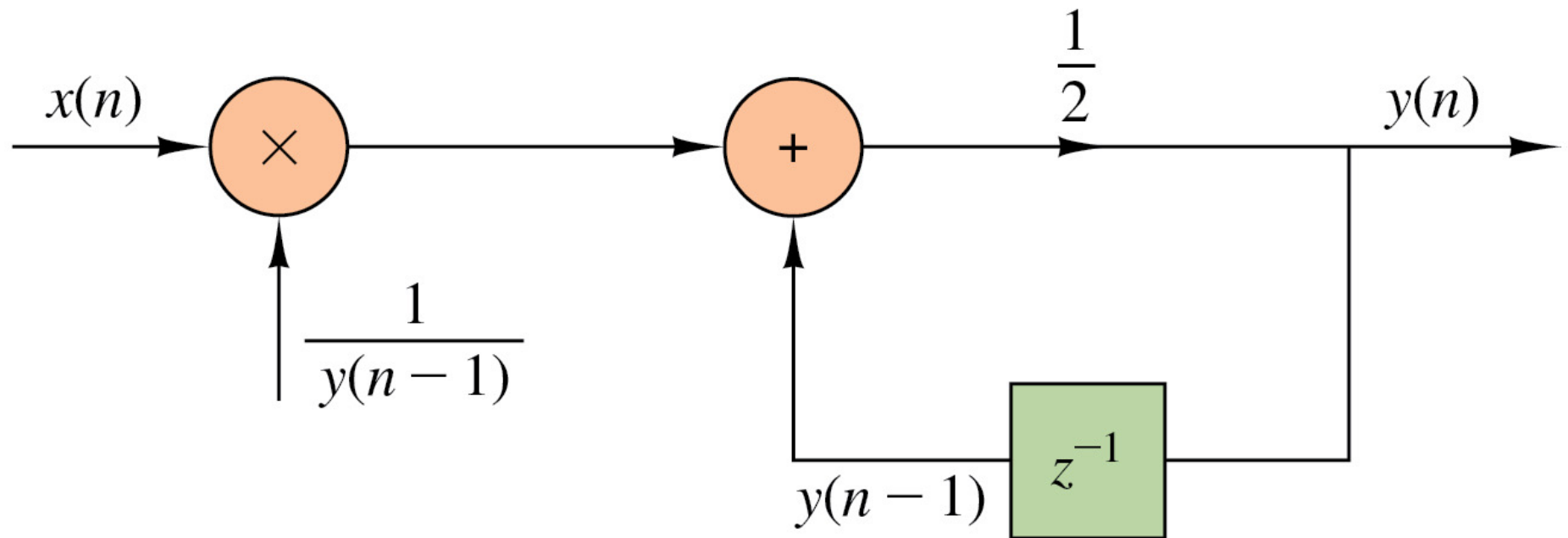
**Figure 2.3.6** Interpretation of the distributive property of convolution: two LTI systems connected in parallel can be replaced by a single system with  $h(n) = h_1(n) + h_2(n)$ .



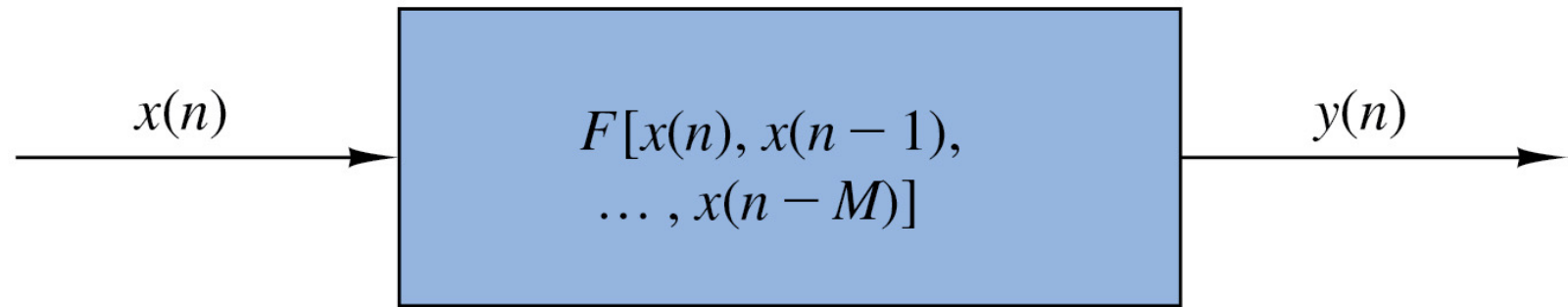
**Figure 2.4.1** Realization of a recursive cumulative averaging system.



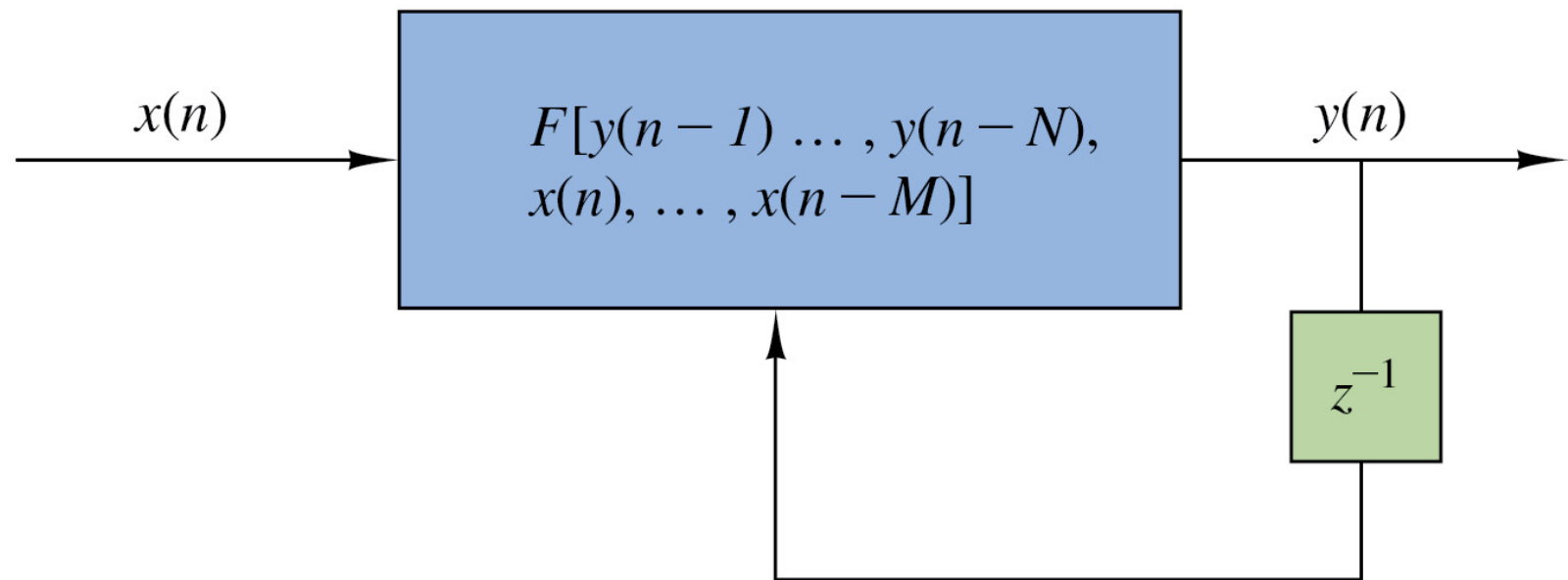
**Figure 2.4.2** Realization of the square-root system.



**Figure 2.4.3** Basic form for a casual and realizable (a) nonrecursive and (b) recursive system.

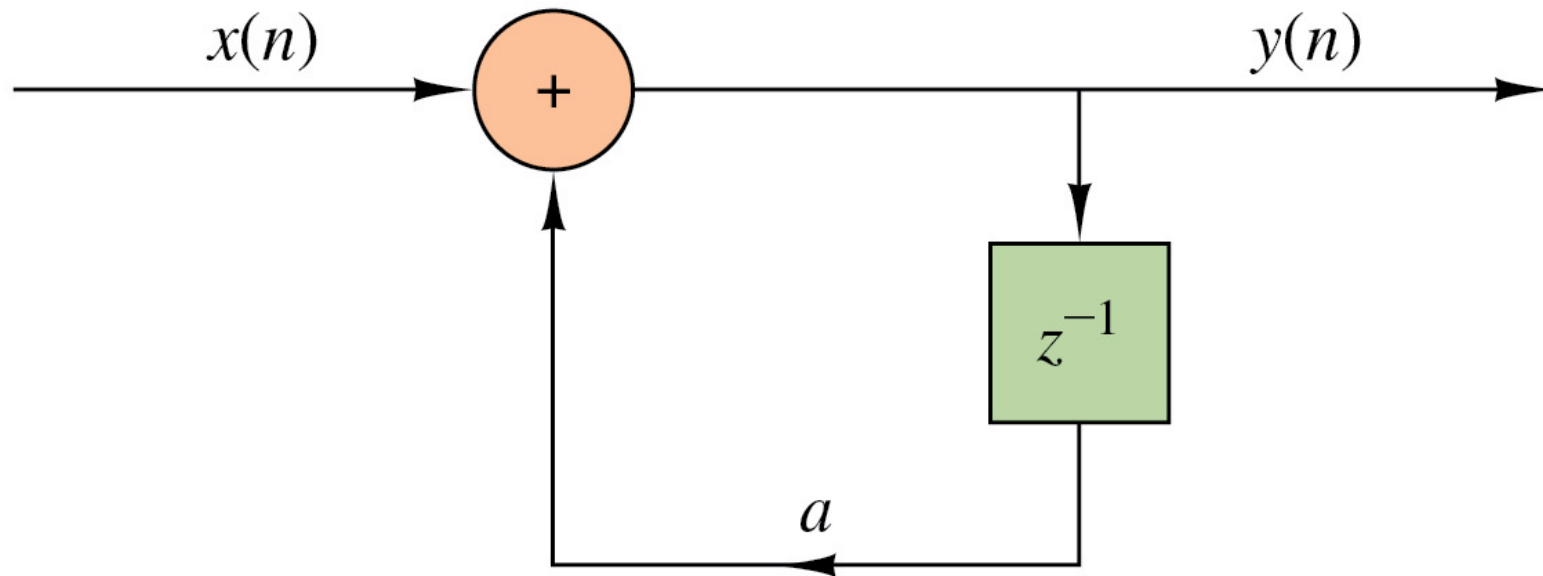


(a)



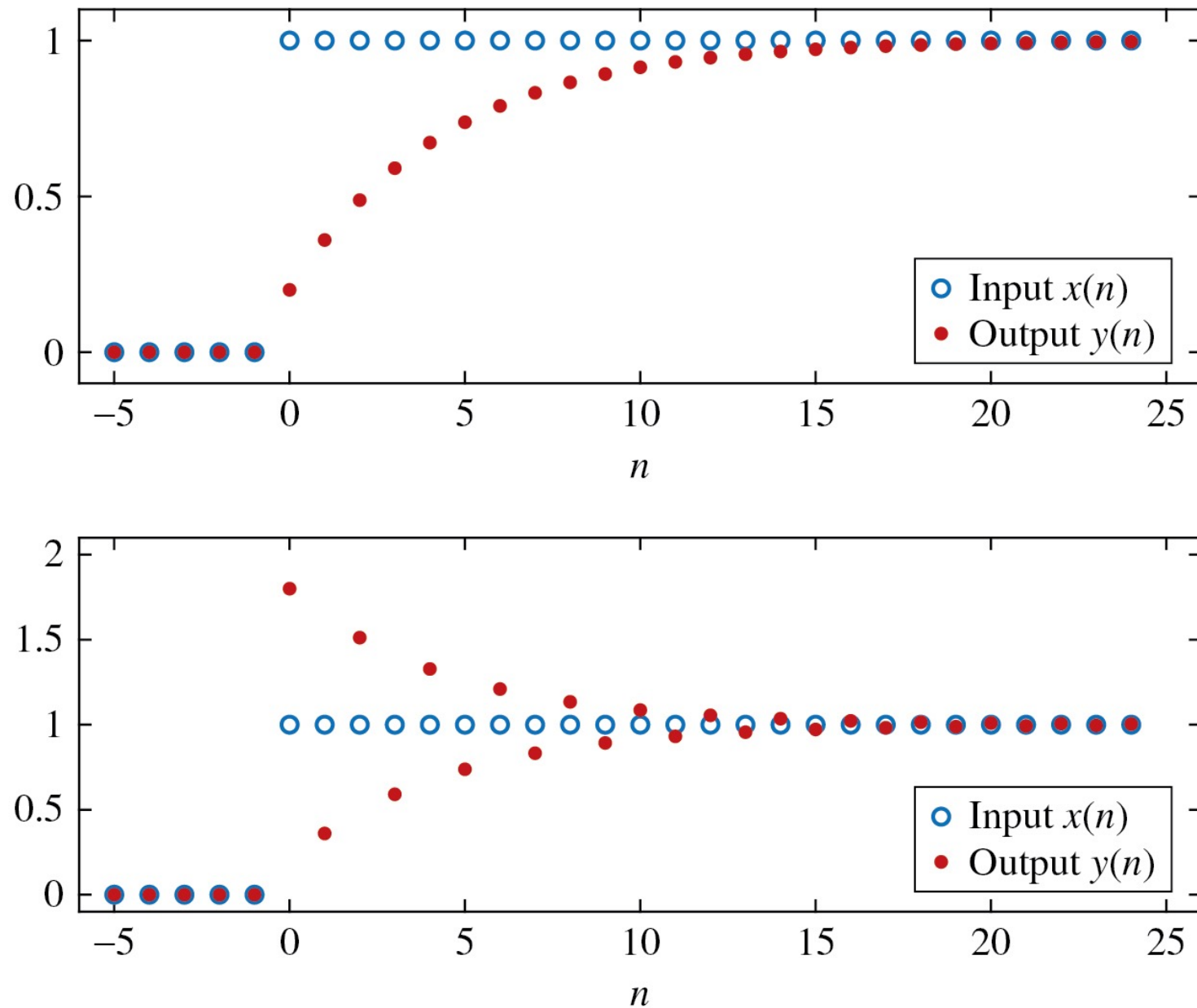
(b)

**Figure 2.4.4** Block diagram realization of a simple recursive system.

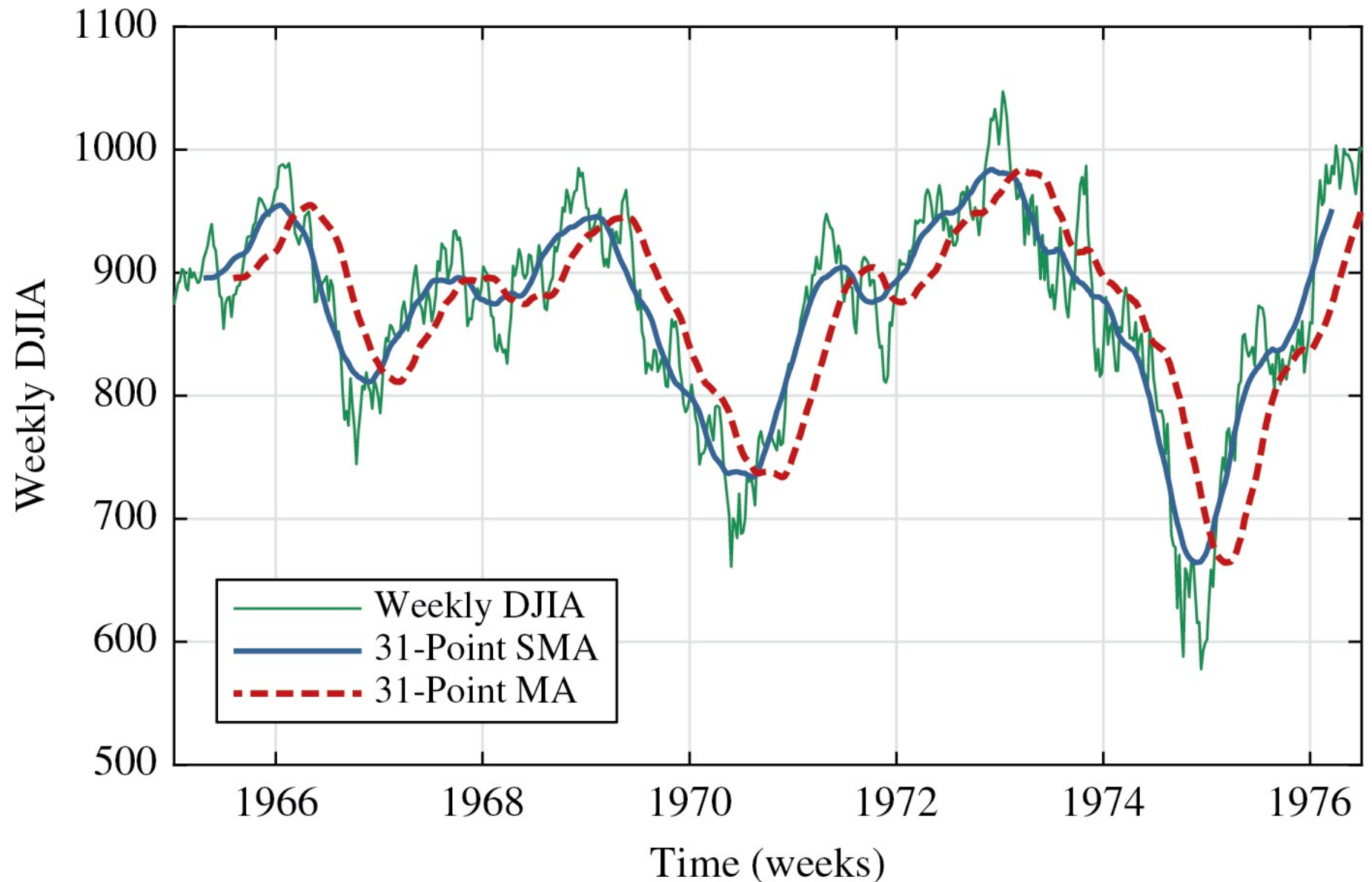




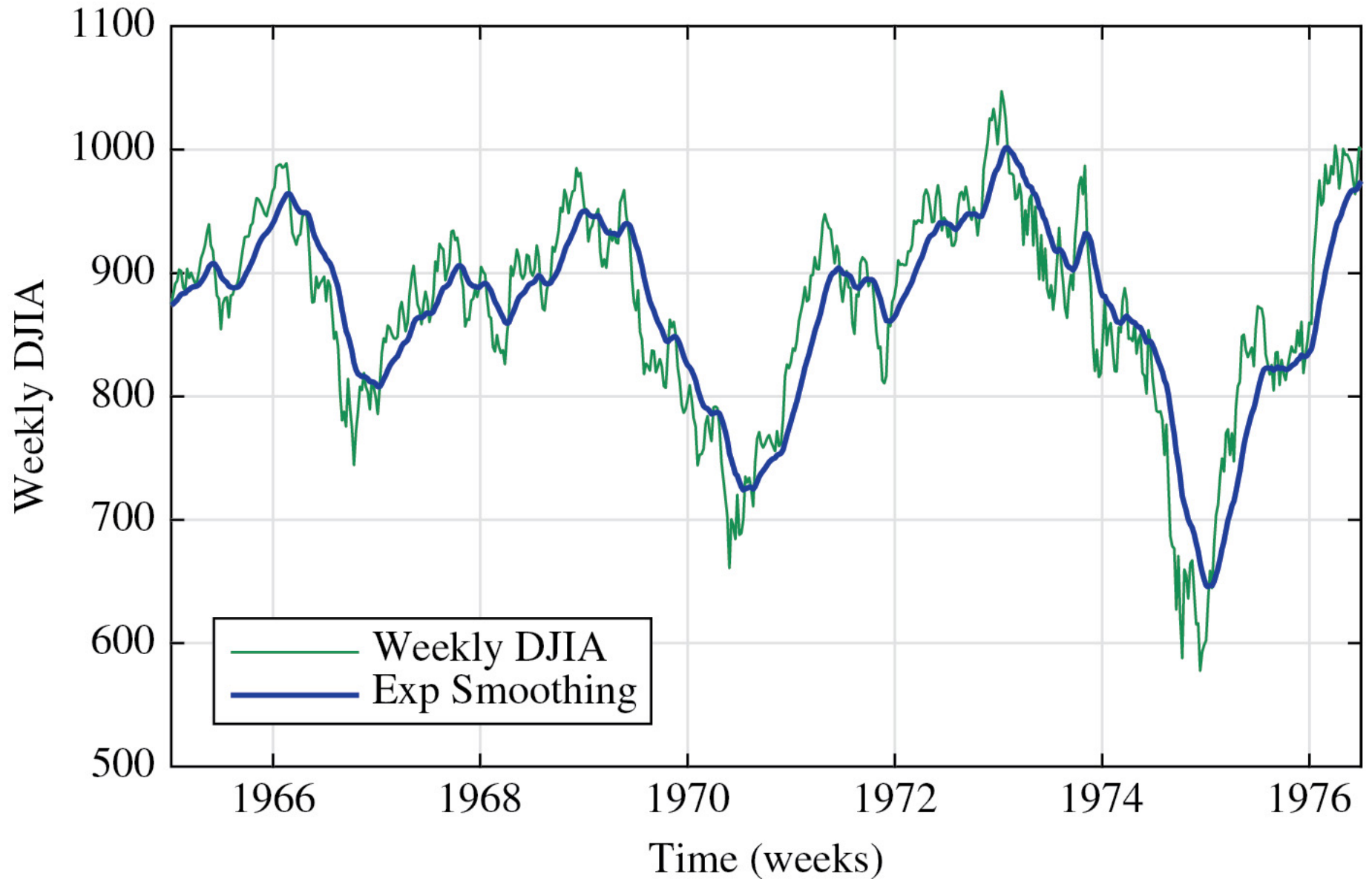
**Figure 2.4.5** Illustration of the transient and steady-state response of a first-order recursive system with  $a = 0.8$  (top) and  $a = -0.8$  (bottom).



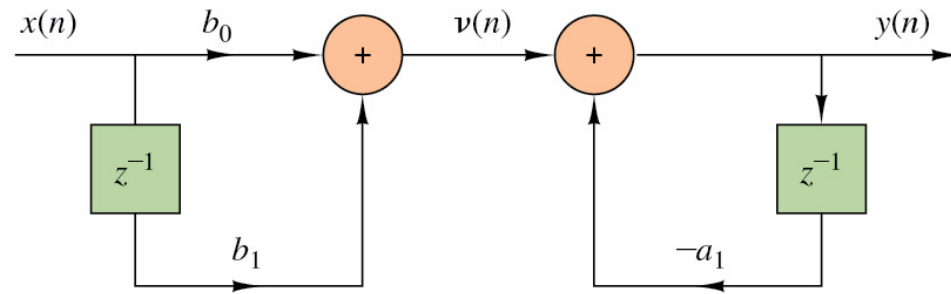
**Figure 2.4.6** The weekly Dow Jones Industrial Average index, an SMA smoothed version with  $M = 31$ , and a MA smoothed version with  $M = 31$ .



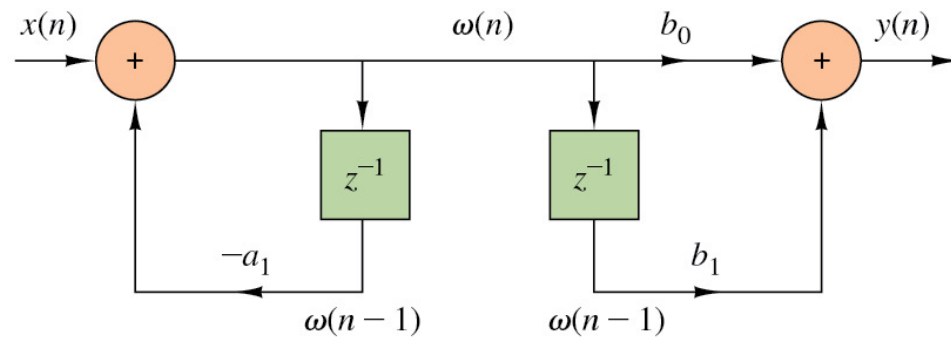
**Figure 2.4.7** The DJIA and an exponentially smoothed version with  $\lambda = 0.1$ .



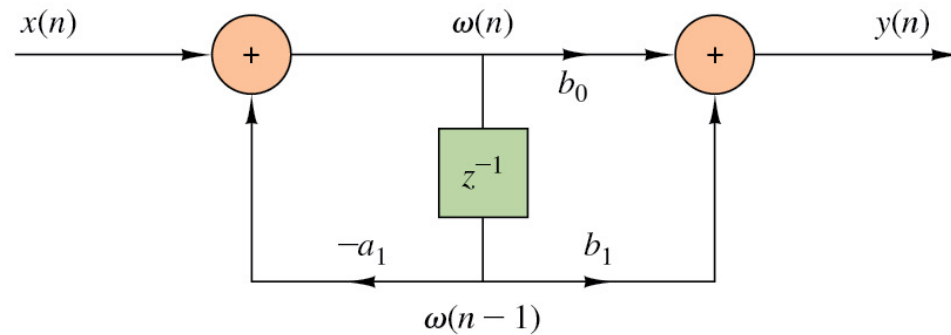
**Figure 2.5.1** Steps in converting from the direct form I realization in (a) to the direct form II realization in (c).



(a)

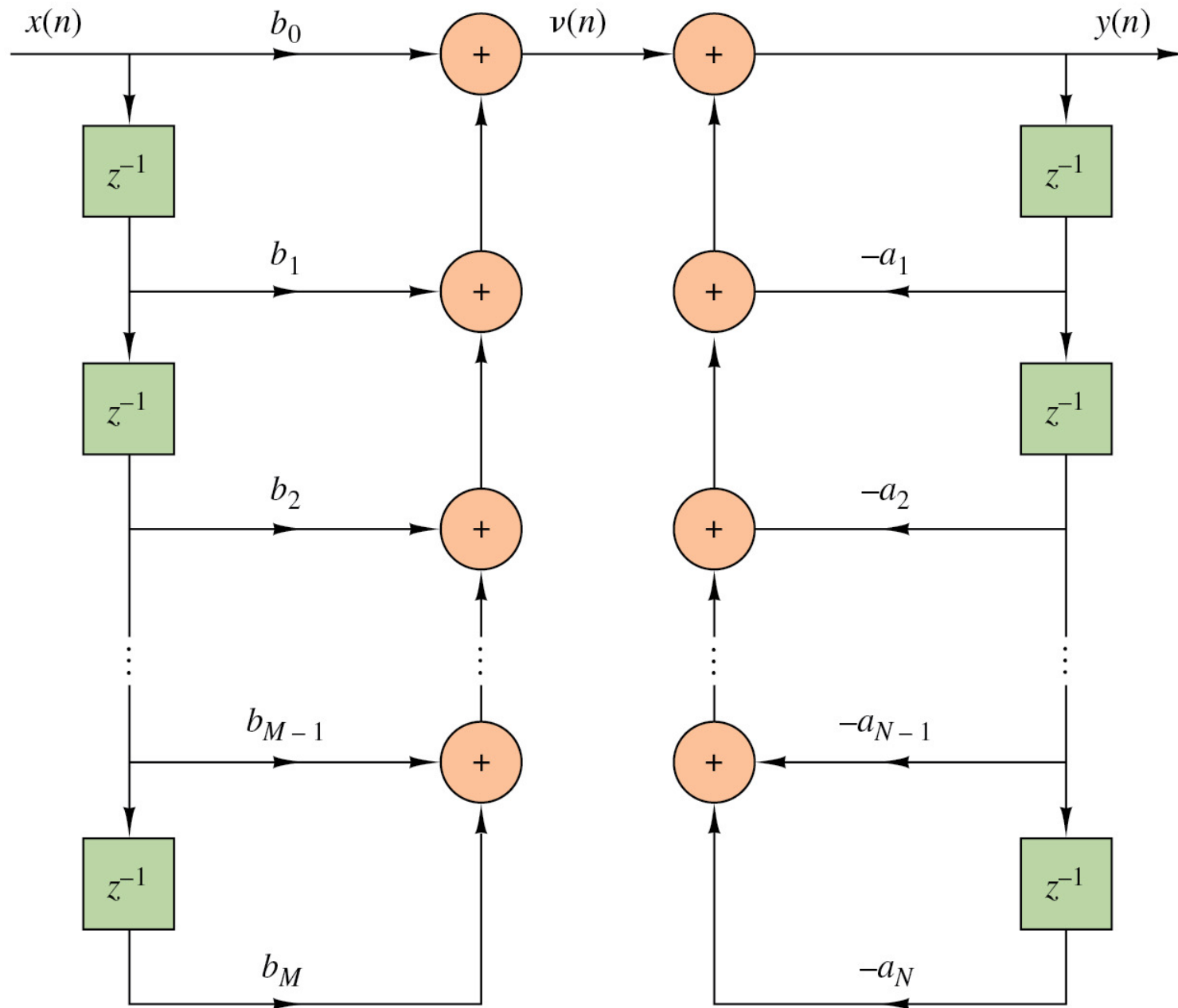


(b)

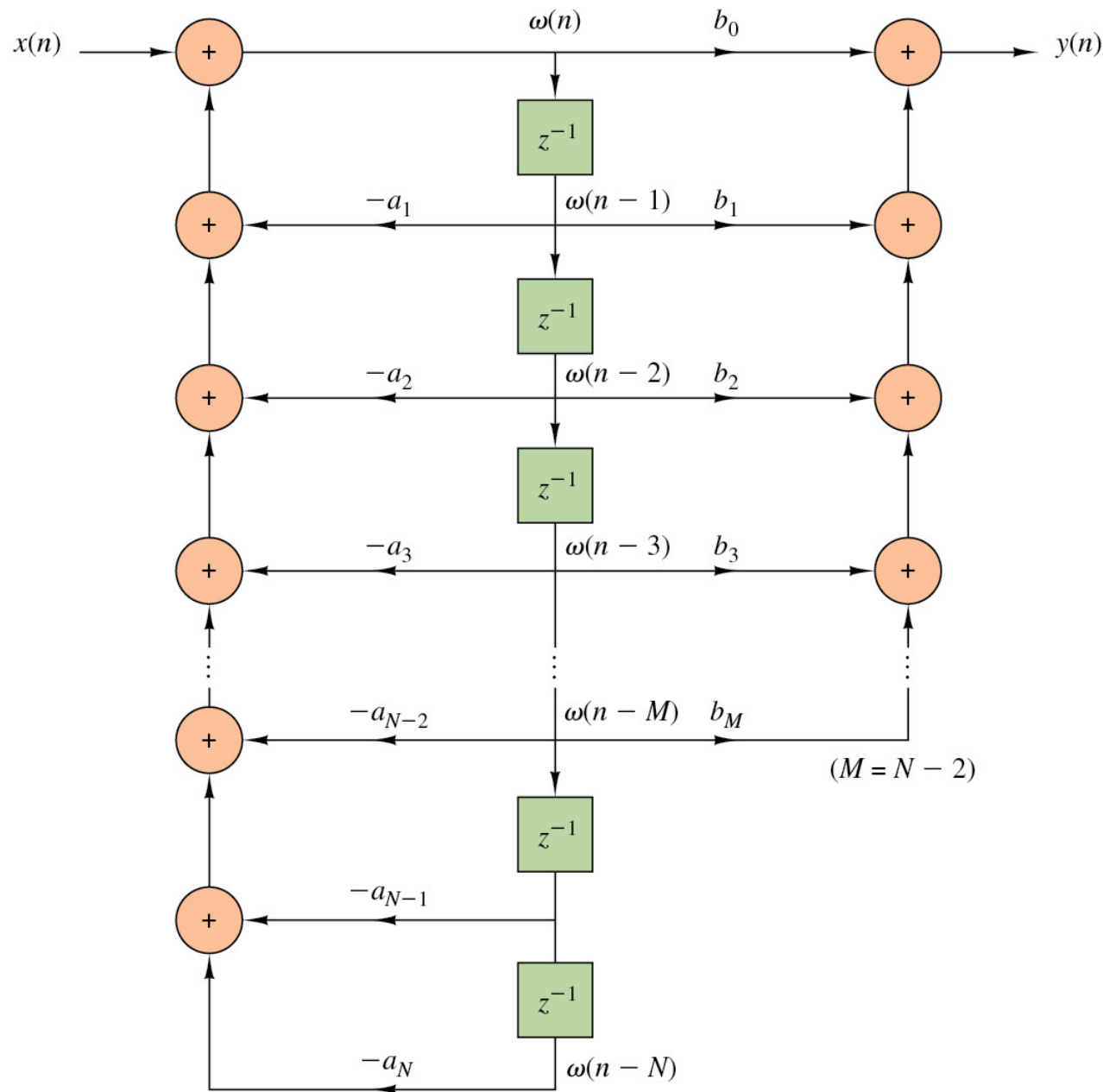


(c)

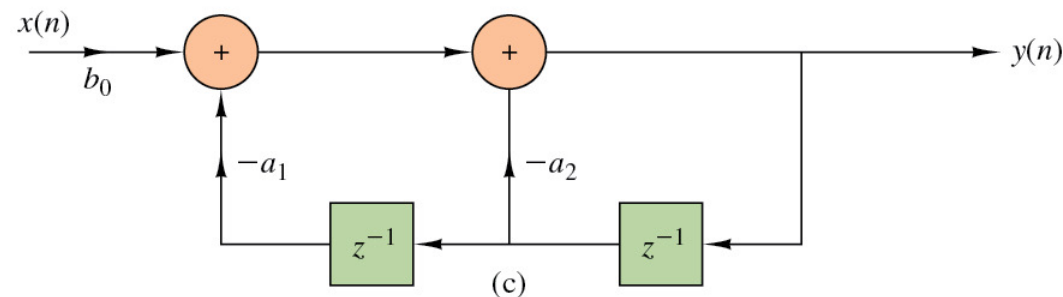
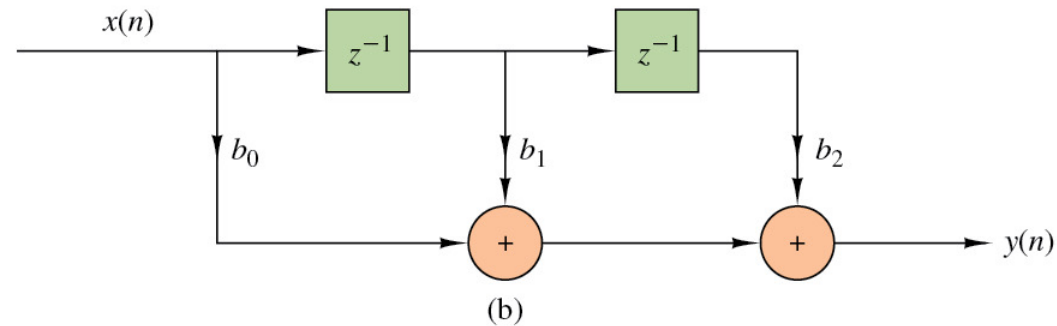
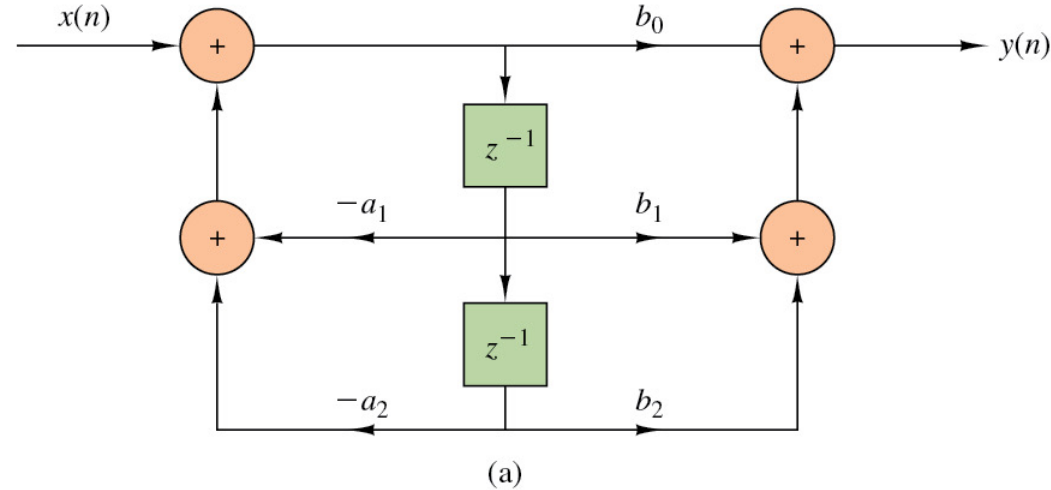
**Figure 2.5.2** Direct form I structure of the system described by (2.5.6).



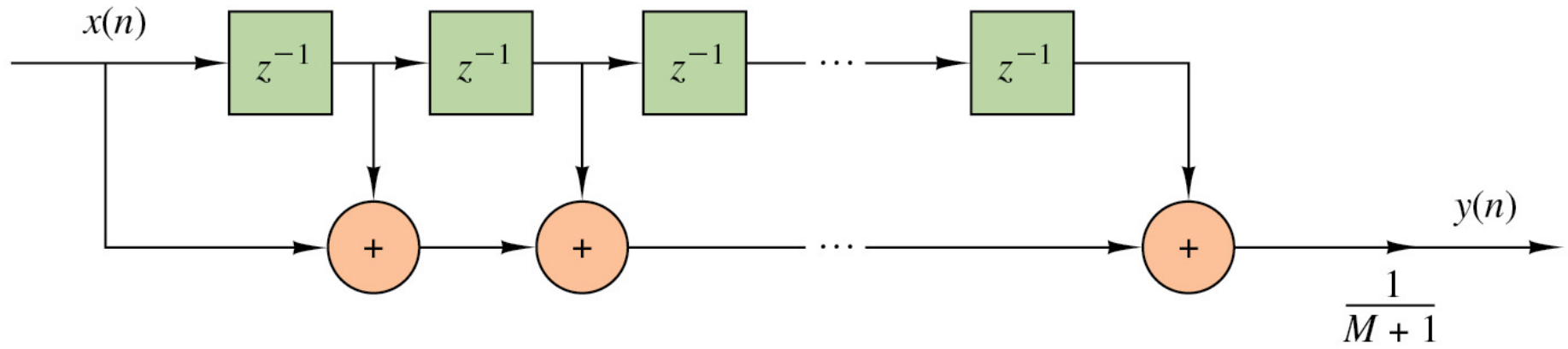
**Figure 2.5.3** Direct form II structure of the system described by (2.5.6).



**Figure 2.5.4** Structures for the realization of second-order systems: (a) general second-order system; (b) FIR system; (c) “purely recursive system.”

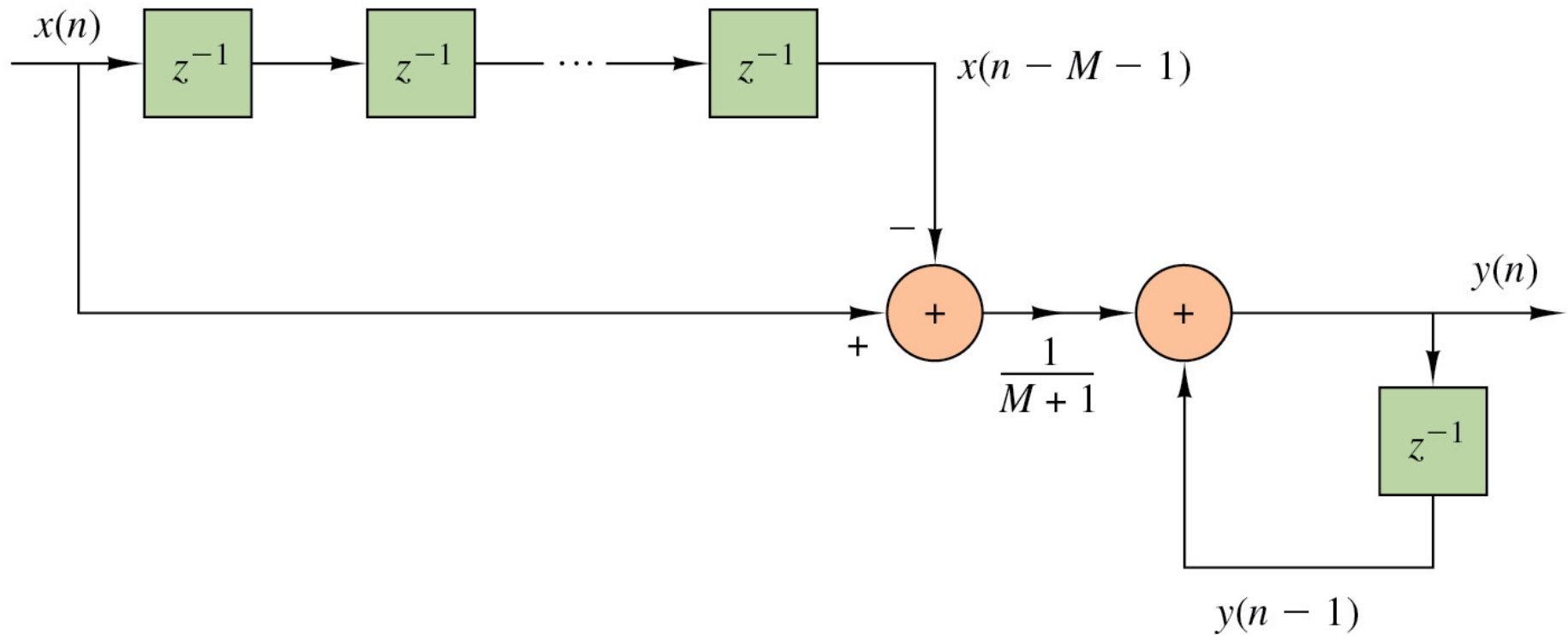


**Figure 2.5.5** Nonrecursive realization of an FIR moving average system.

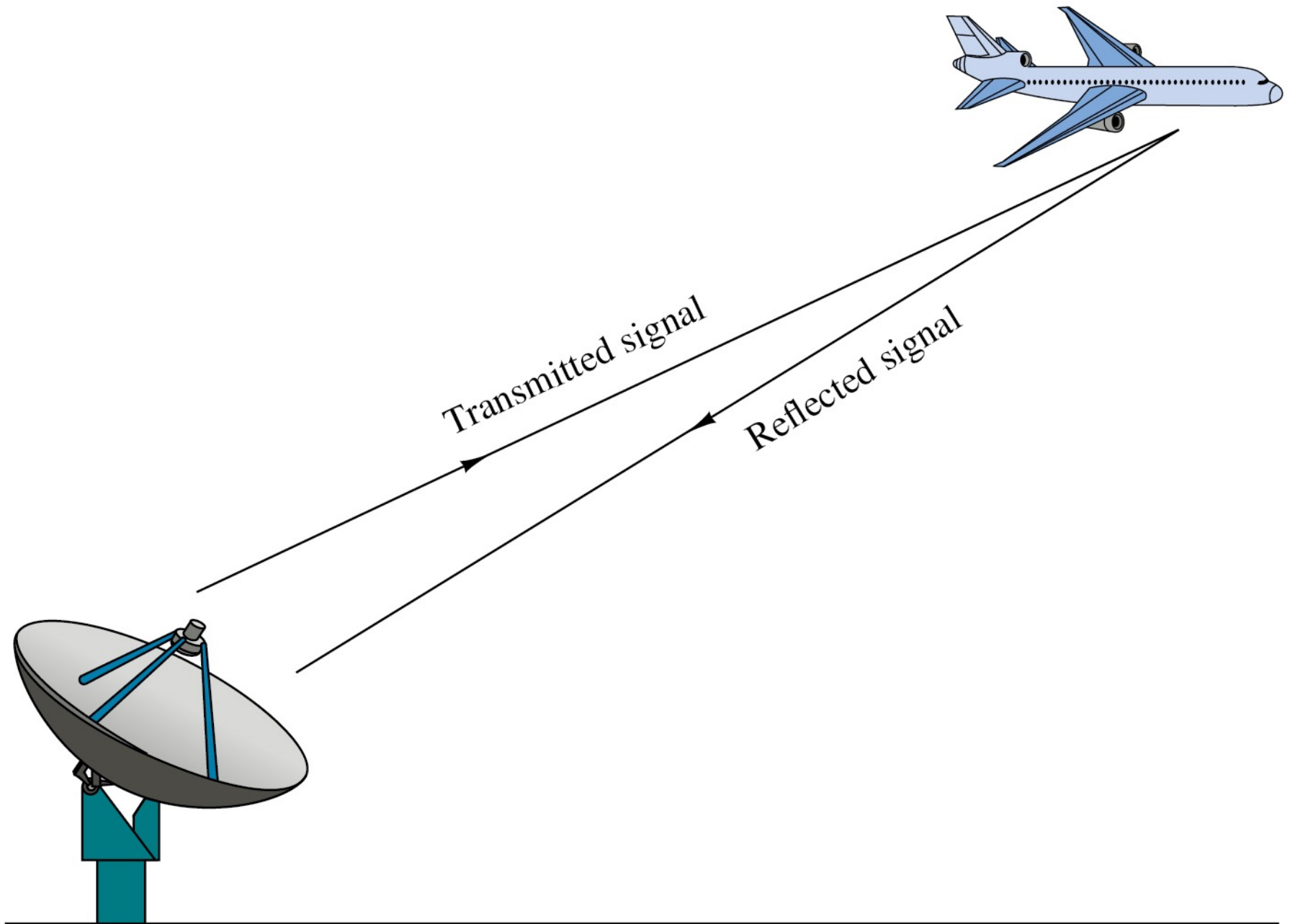




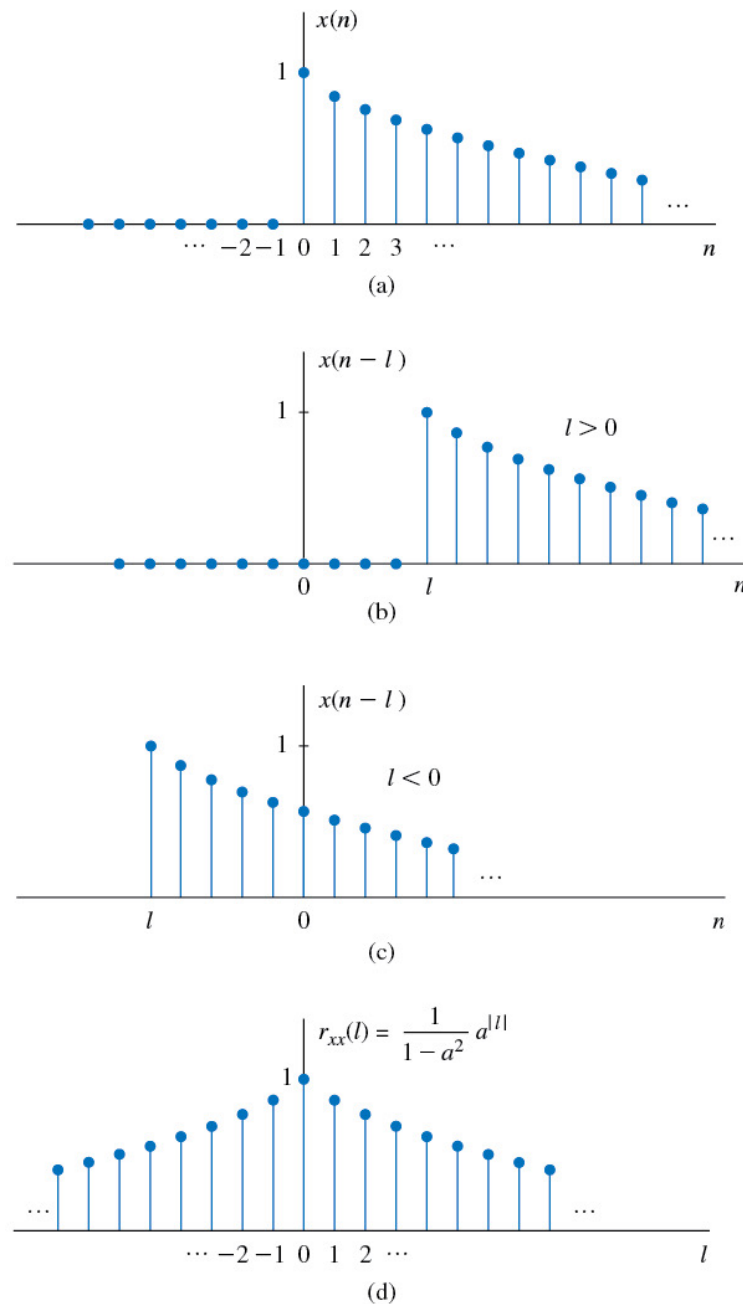
**Figure 2.5.6** Recursive realization of an FIR moving average system.



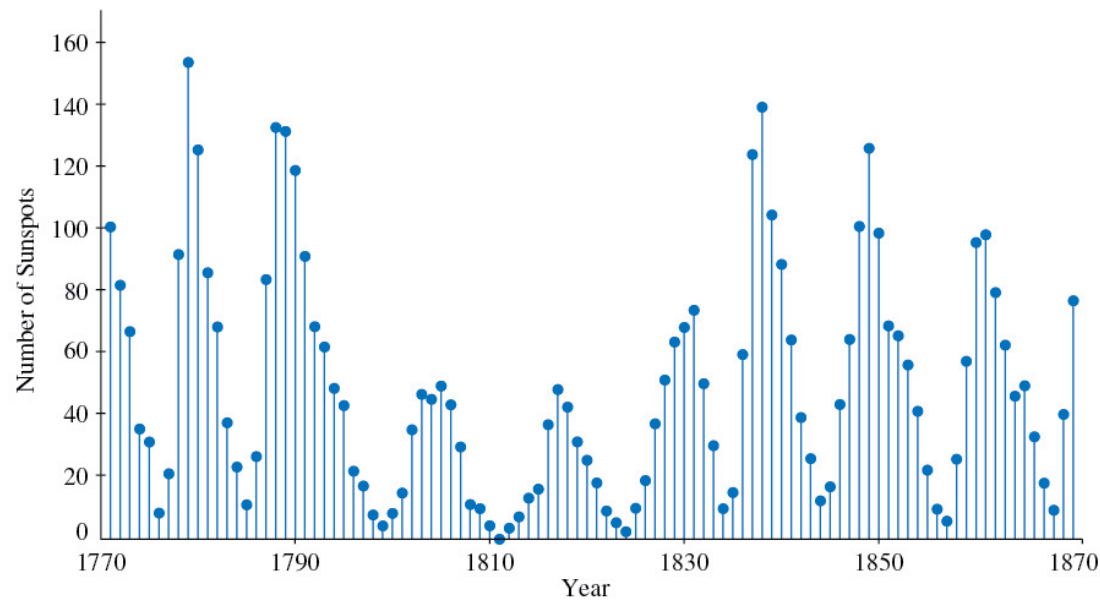
**Figure 2.6.1** Radar target detection.



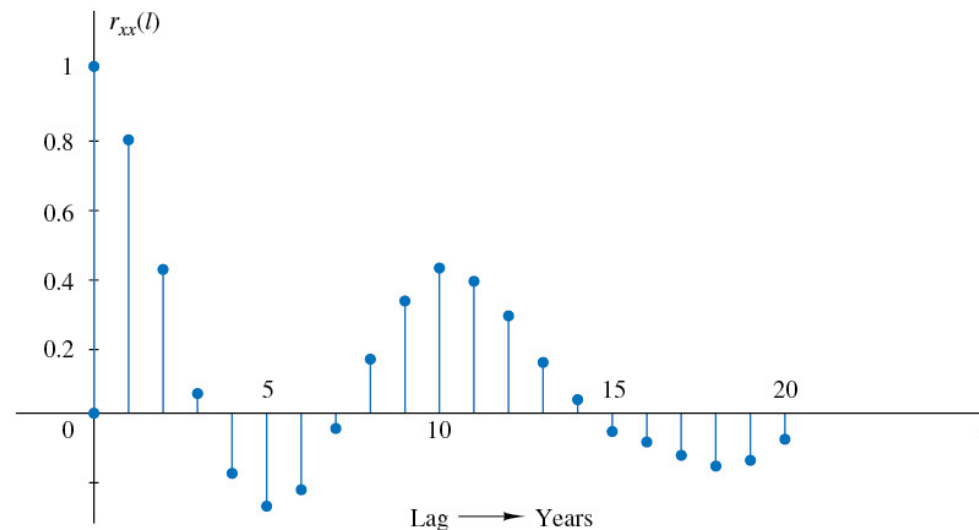
**Figure 2.6.2** Computation of the autocorrelation of the signal  $x(n) = a^n$ ,  $0 < a < 1$ .



**Figure 2.6.3** Identification of periodicity in the Wölfer sunspot numbers: (a) annual Wölfer sunspot numbers; (b) normalized autocorrelation sequence.

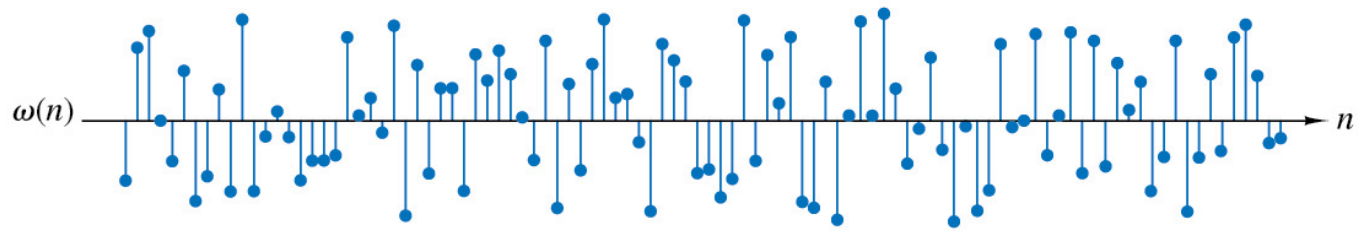


(a)

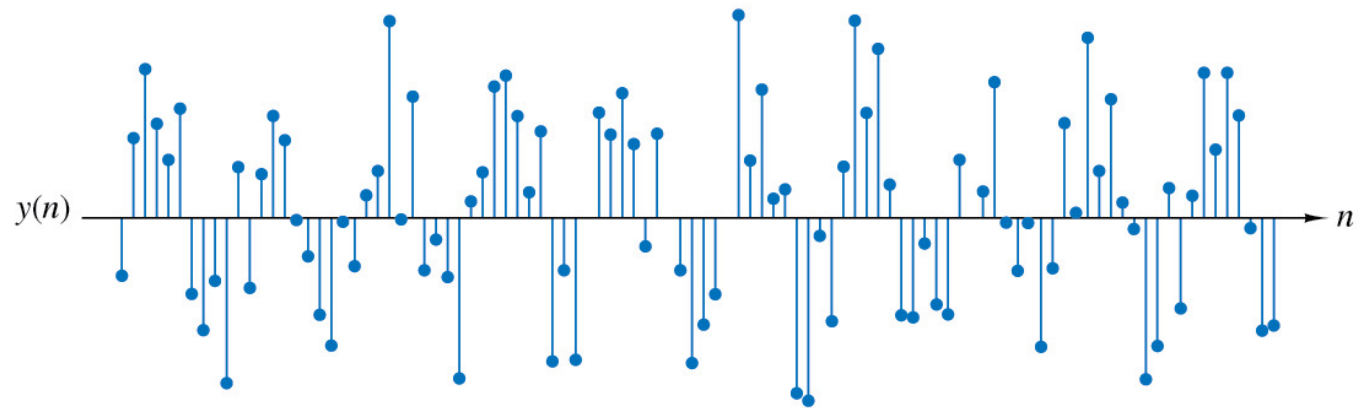


(b)

**Figure 2.6.4** Use of autocorrelation to detect the presence of a periodic signal corrupted by noise.

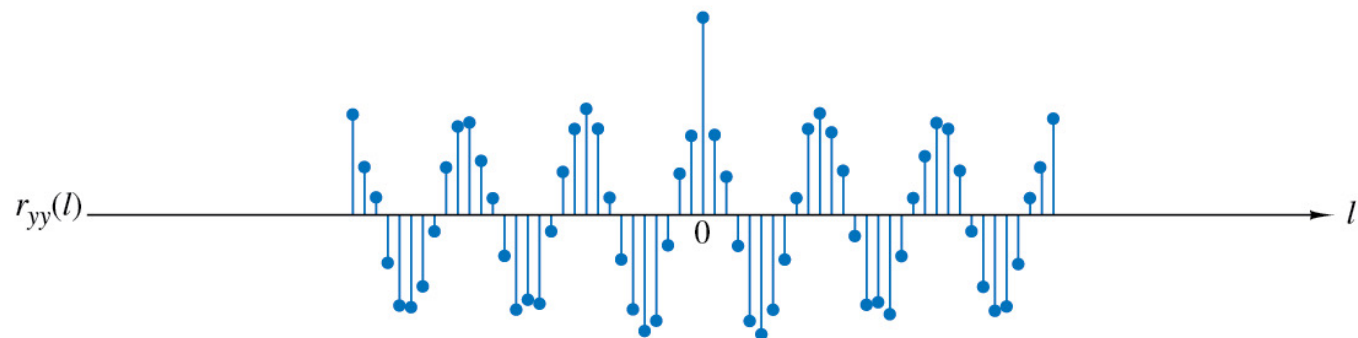


(a)



(b)

$SNR = 1 \text{ dB}$



(c)

Figure P2.2

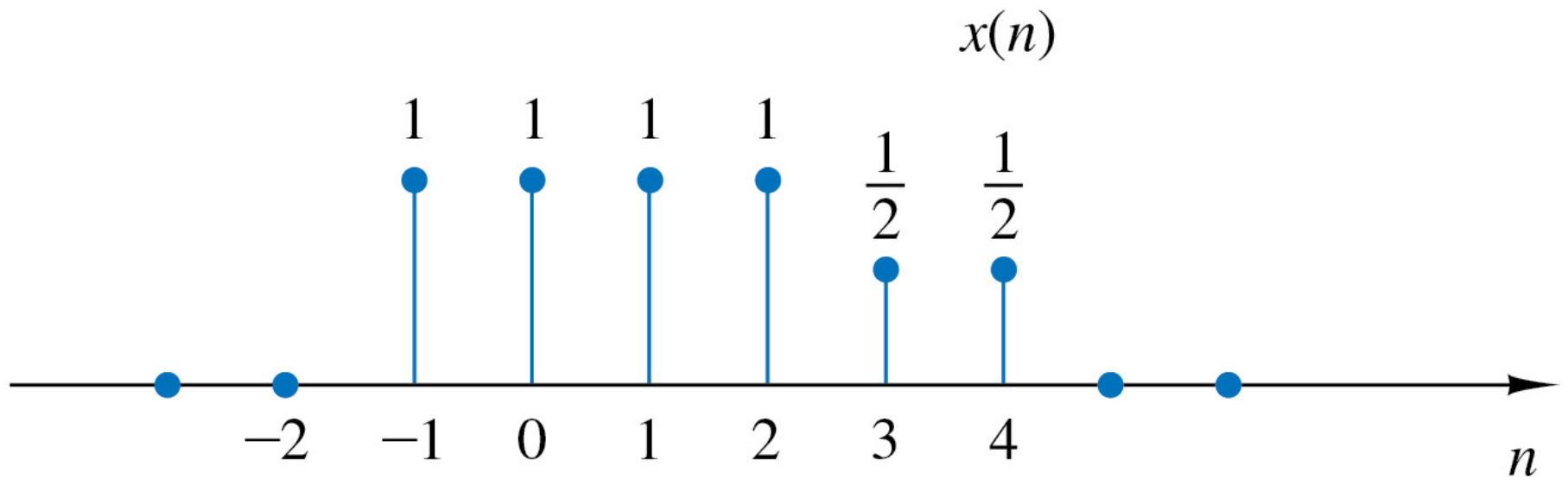
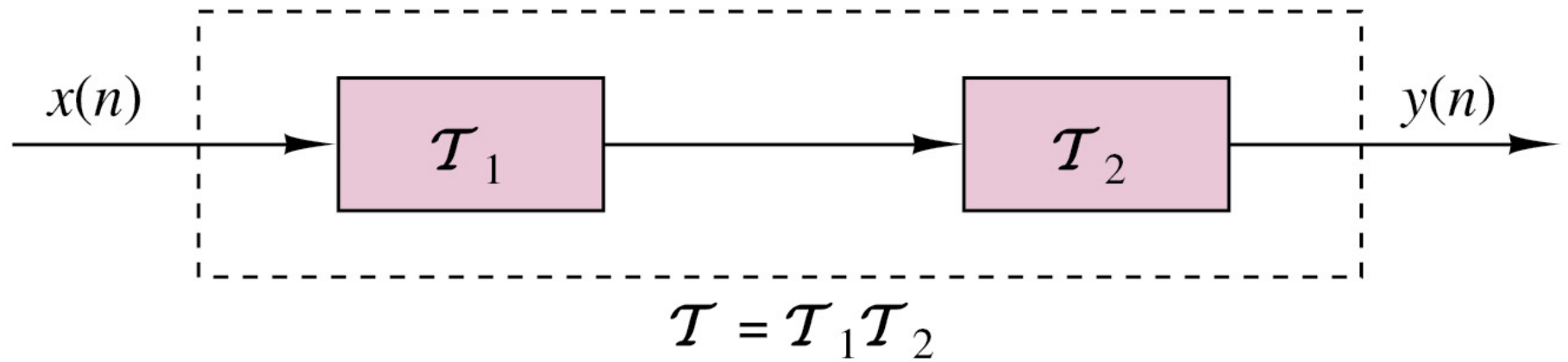
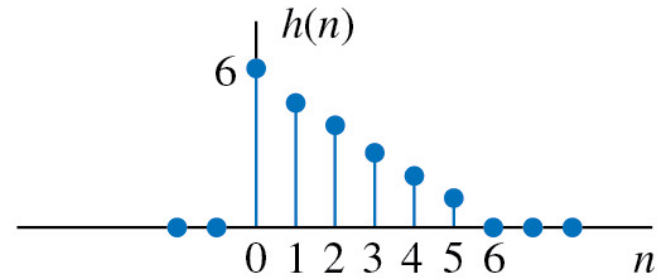
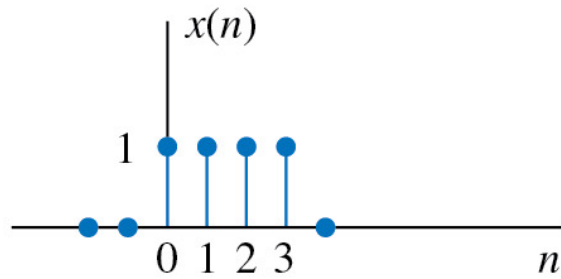


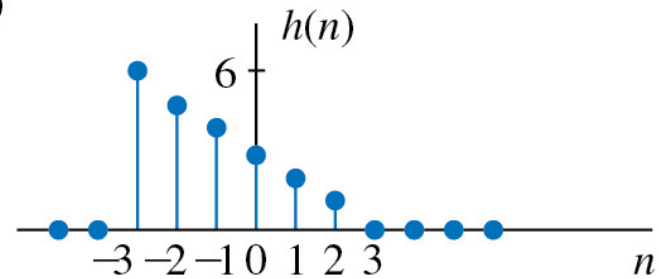
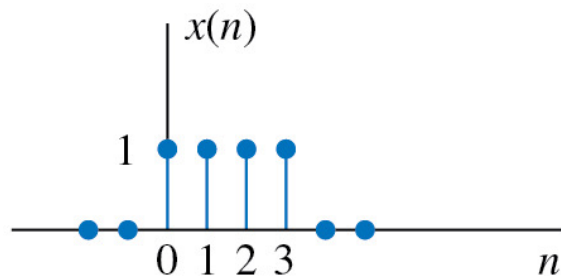
Figure P2.8



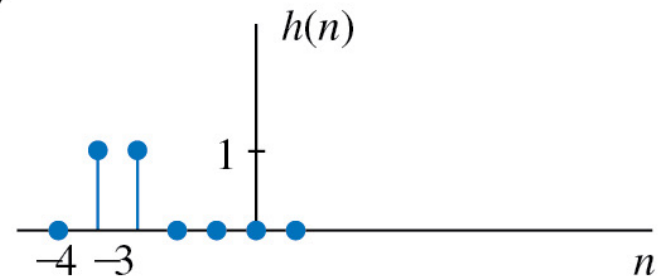
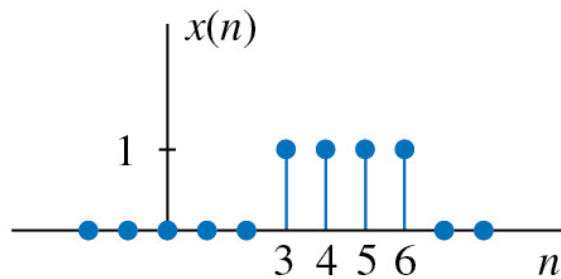
**Figure P2.17**



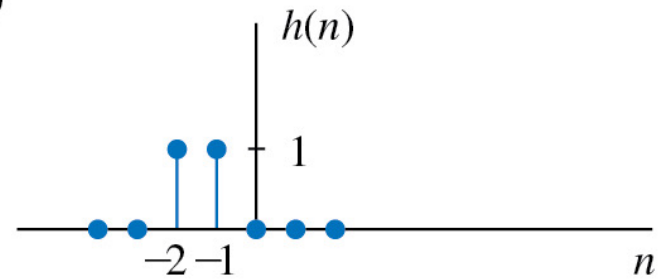
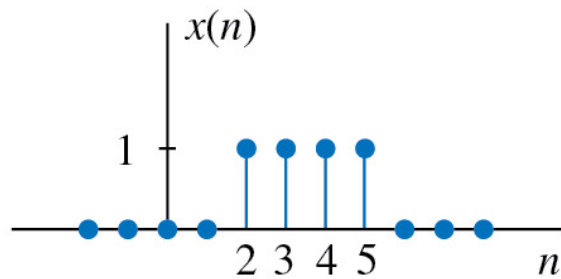
(a)



(b)



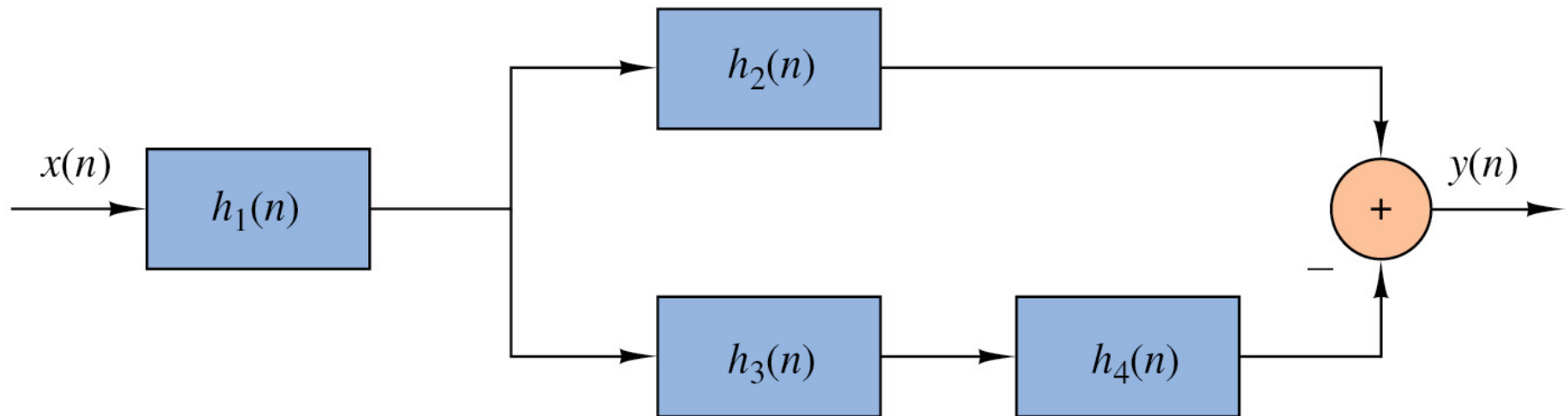
(c)



(d)



Figure P2.31



**Figure P2.32**

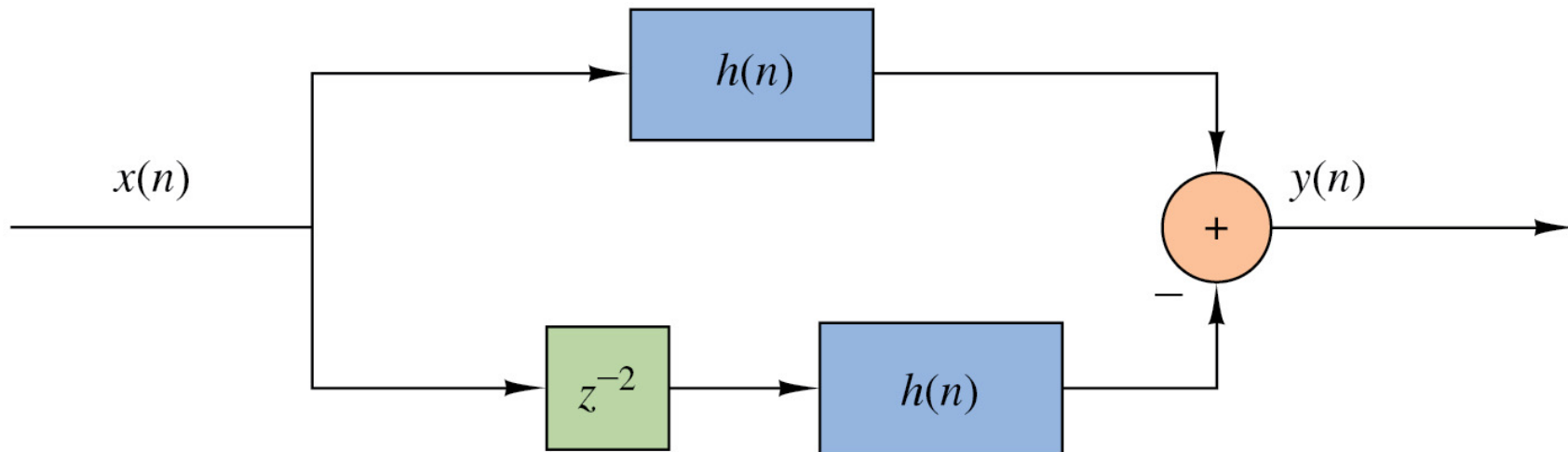


Figure P2.43

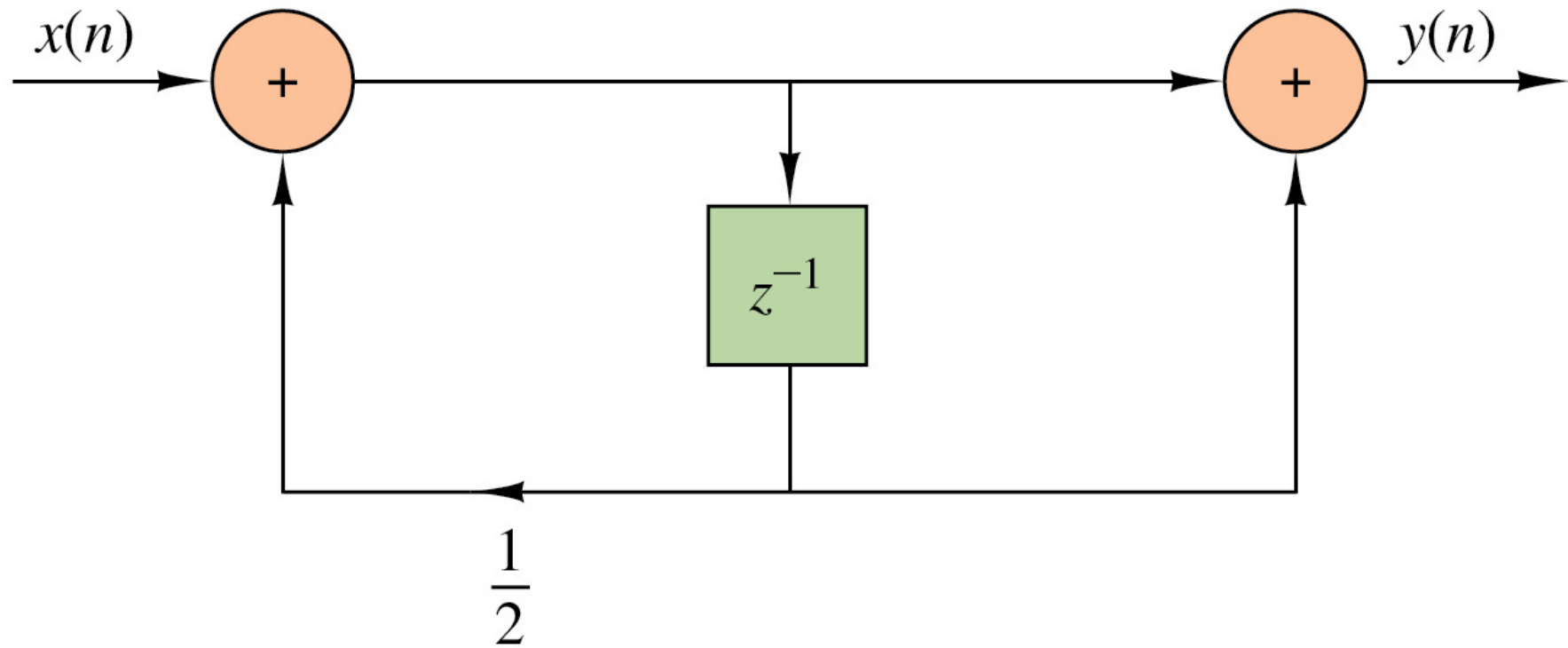


Figure P2.45

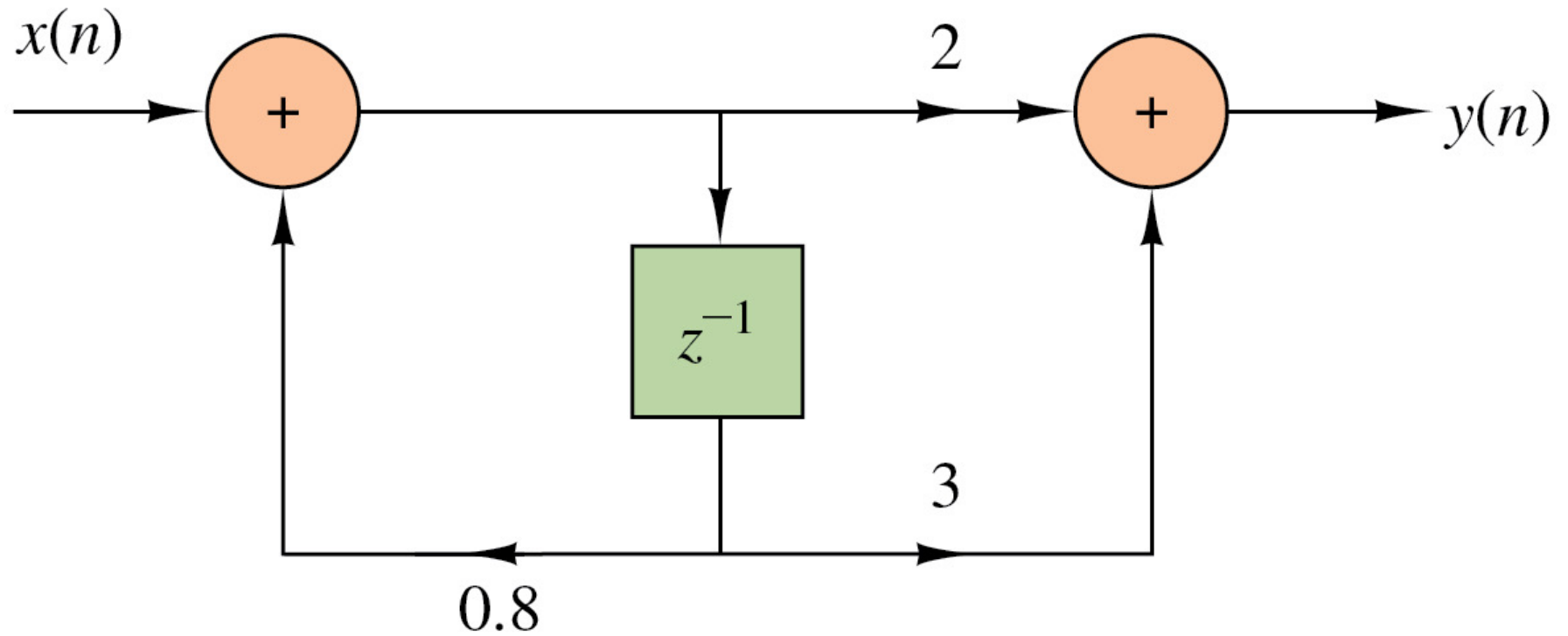
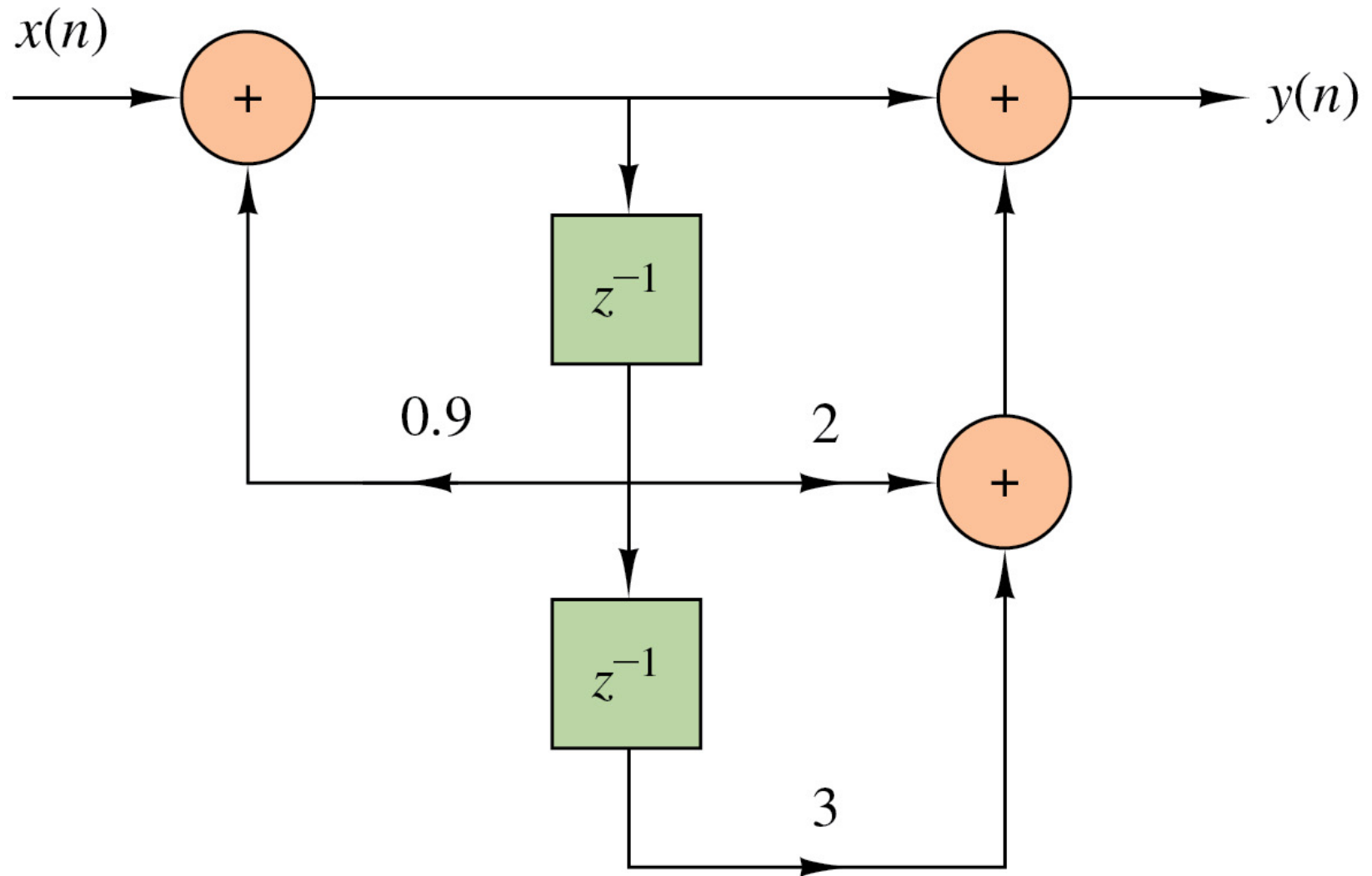
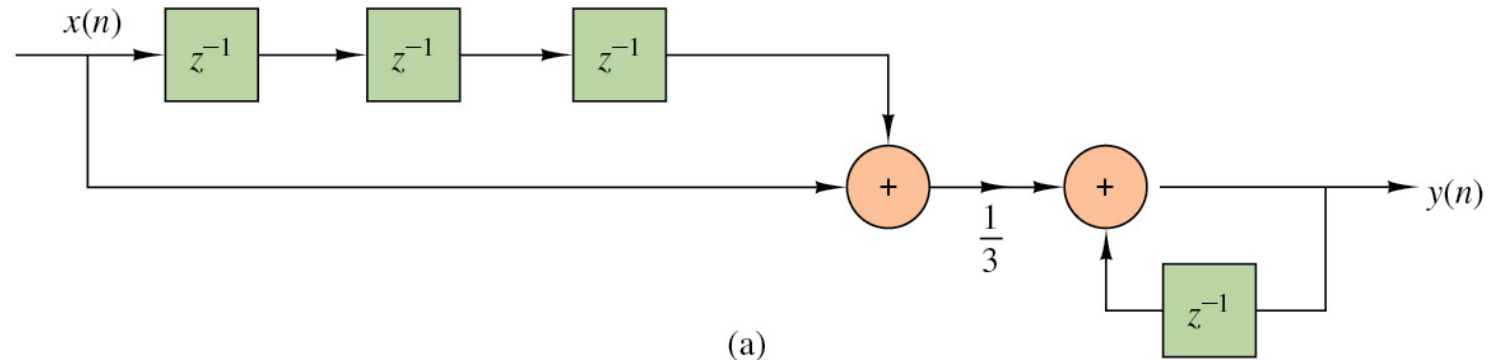


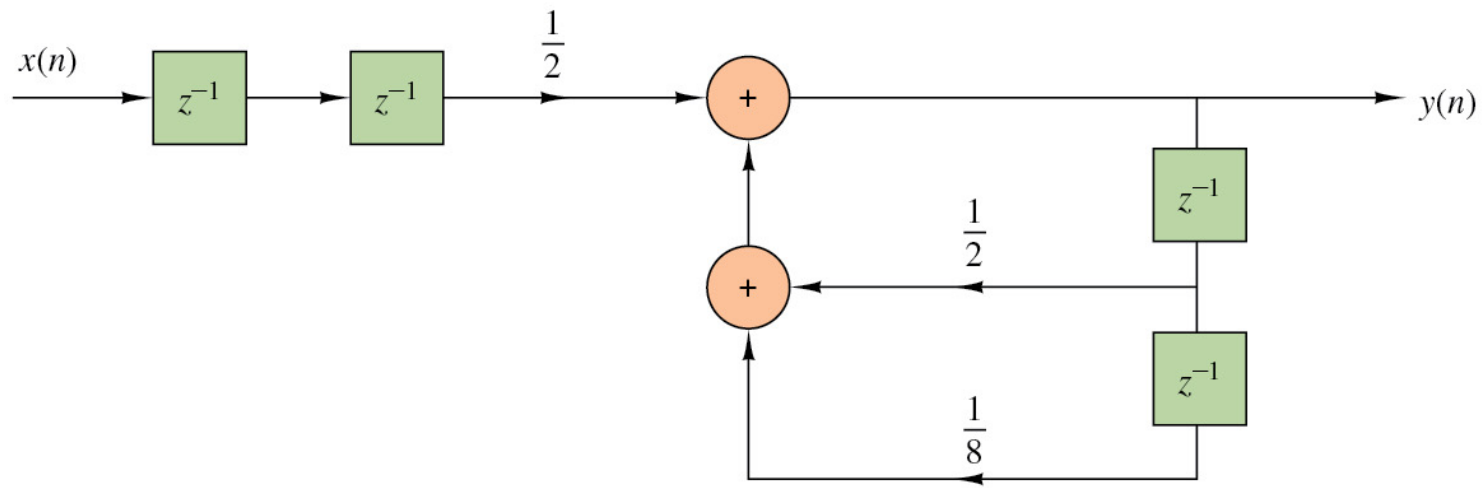
Figure P2.46



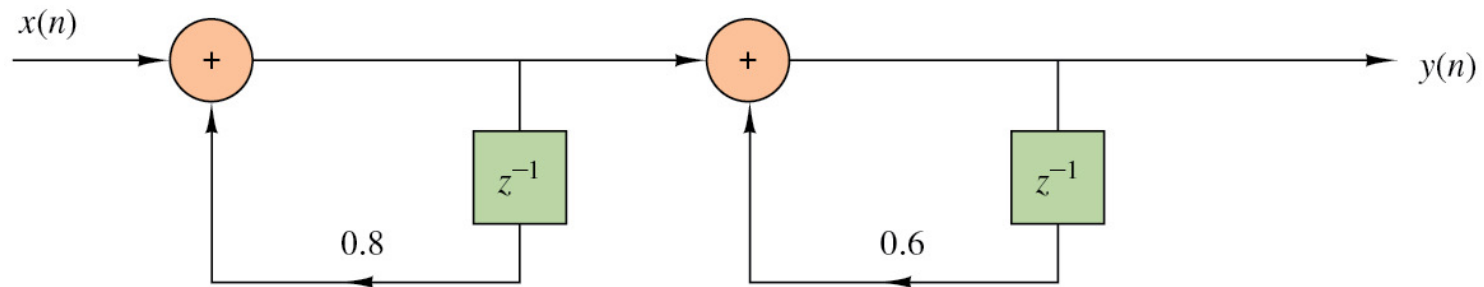
**Figure P2.47**



(a)



(b)



(c)

Figure P2.48

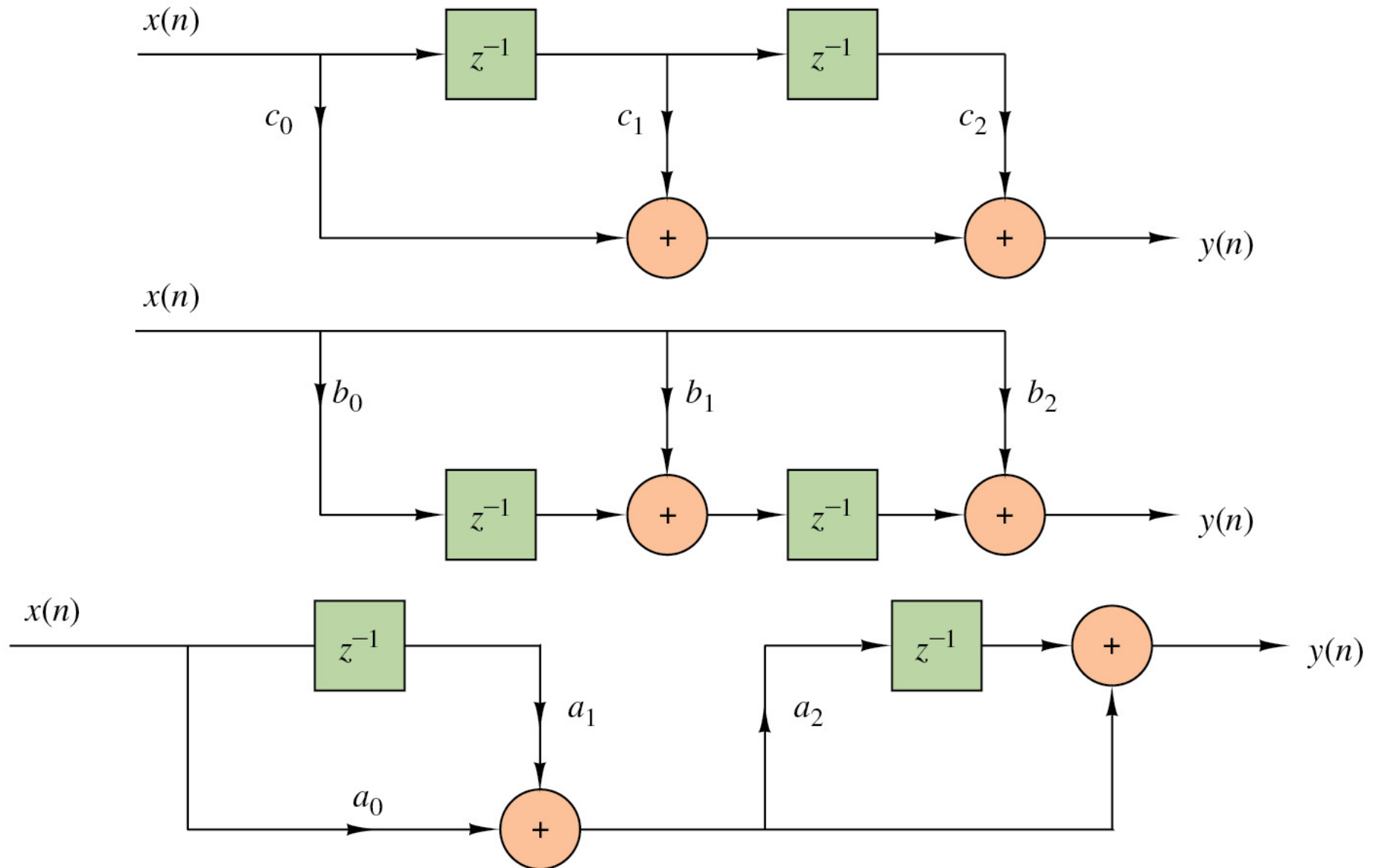
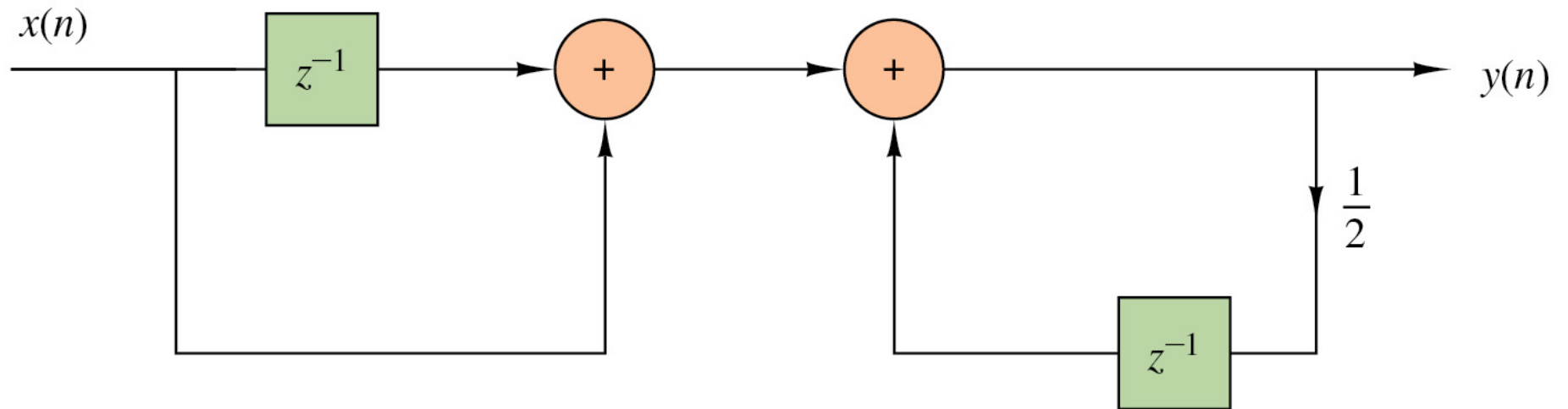
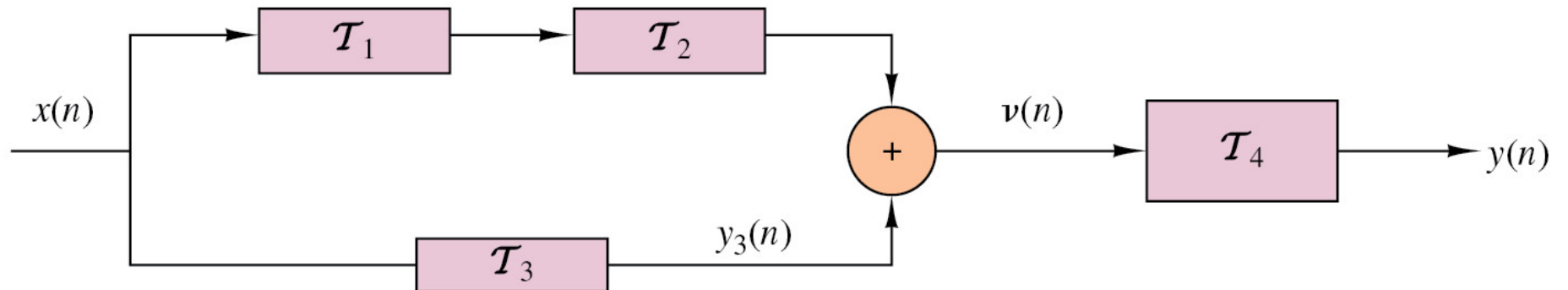


Figure P2.49





**Figure CP2.15**



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