Figure 4 Measured (a) impedance bandwidth and (b) center operating frequency for the antenna shown in Figure 1 with $L = 65$ mm

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ground-plane length (about 45% of the free-space wavelength at 2050 MHz) for achieving maximum impedance bandwidth. On the other hand, there is a critical value for the ground-plane width (about 27% of the free-space wavelength at 2050 MHz); when the ground-plane width is less than the critical value, relatively very sharp variations in the impedance bandwidth have been seen.

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TIME-DOMAIN FINITE-ELEMENT SIMULATION OF CAVITY-BACKED MICROSTRIP PATCH ANTENNAS

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ABSTRACT: A time-domain finite-element method (TDFEM) is presented for simulating the radiation and scattering from cavity-backed microstrip patch antennas. The perfectly matched layer (PML) is utilized to efficiently truncate the TDFEM solution domain. The higher order vector basis functions are adopted to accurately represent unknown fields. Numerical examples are given to demonstrate its efficacy. © 2002 John Wiley & Sons, Inc. Microwave Opt Technol Lett 32: 251–254, 2002.

Key words: finite-element method; microstrip patch antennas; scattering time domain
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1. INTRODUCTION
Cavity-backed microstrip patch antennas are highly resonant structures. Their characteristics, such as the input impedance, vary drastically as a function of frequency. This increases the modeling difficulty when conventional frequency-domain-based methods are used for simulation since a set of algebraic equations must be solved repeatedly at many isolated frequency points. In this paper, a time-domain finite-element method (TDFEM) is presented to analyze the radiation and scattering from cavity-backed microstrip patch antennas. This method utilizes the perfectly matched layers (PMLs) to truncate the TDFEM solution domain, and the implementation is based on a recently developed algorithm in [1, 2]. The time-domain simulation captures the drastically varying frequency responses with one calculation. The finite-element analysis enhances the geometry-modeling capability. The adoption of higher order vector basis functions accurately describes the unknown fields. The utilization of PMLs permits the absorption of outgoing waves with any polarizations and at any frequencies and angles of incidence. Numerical results are compared with those obtained by measurements and the frequency-domain finite-element–boundary-integral (FDFE–BI) method.

2. FORMULATION
Consider a cavity-backed microstrip patch antenna recessed in a ground plane (Fig. 1). To formulate the TDFEM solution, we introduce a PML over the aperture $S_p$ to entirely enclose the computational domain $V_0$. Inside $V_0$, the electric
field satisfies the second-order vector wave equation
\[
\nabla \times \mu \nabla \times \mathbf{A}(r,t) + \nabla \times \mathbf{E}(r,t) + \sigma \partial_t \mathbf{E}(r,t) + \epsilon \nabla \times \mathbf{B}(r,t) = -\partial_t \mathbf{J}(r,t) - \mu \nabla \times \mathbf{M}(r,t)
\]

where \( \mathbf{J}(r,t) \) and \( \mathbf{M}(r,t) \) denote the electric and magnetic sources associated with the antenna feeds, \( \ast \) stands for temporal convolution, conductivity \( \sigma \) is introduced to characterize the loss of the substrate and the impedance load, \( \mathbf{E}(r,t) \) denotes the stretched electric field, and \( \mathbf{A}(r,t) \) is the time-domain counterpart of the diagonal tensor \([3]:\)
\[
\mathbf{A} = \bar{\epsilon} \left( \frac{S_x S_z}{S_x} \right) + \bar{\mu} \left( \frac{S_y S_z}{S_y} \right) + \bar{\mu} \left( \frac{S_y S_x}{S_y} \right) - \mu_0 \mathbf{1}
\]

where \( S_x(\xi = x, y, z) \) are the stretching variables given by
\[
S_x = 1 + \frac{\sigma\epsilon}{\omega\mu_0}, \quad \xi = x, y, z.
\]

Based on the algorithm developed in [2], the TDFEM solution of (1) results in an ordinary differential equation:
\[
\frac{d^2 \mathbf{u}}{dt^2} + (\mathbf{T}_p + \mathbf{R}) \frac{du}{dt} + \mathbf{Q} \frac{du}{dt} + \mathbf{T}_u u + \mathbf{S} u + \sum_{\xi=x, y, z} \mathbf{T}_\xi \psi_\xi = -f_{\text{int}}
\]

where \( \mathbf{T}, \mathbf{T}_p, \mathbf{R}, \mathbf{Q}, \mathbf{T}_u, \mathbf{S}, \mathbf{M}, \mathbf{T}_\xi, \) and \( \mathbf{T}_\psi(\xi = x, y, z) \) are square matrices, and \( f_{\text{int}} \) denotes the excitation vector
\[
f_{\text{int}} = \langle \mathbf{N}_i, \partial_t \mathbf{J}_{\text{int}} \rangle \psi_\xi + \langle \mu^{-1} \nabla \times \mathbf{N}_i, \mathbf{M}_{\text{int}} \rangle \psi_\xi
\]

where \( \mathbf{N}_i \) denotes the vector basis function.

For scattering analysis, the solution is formulated in terms of the scattered field, and for radiation analysis, it uses the total radiated field. For the spatial discretization, the unknown fields are expanded using higher order edge elements [4]. For the temporal discretization, the Newmark method is employed for time marching.

One of the important issues in the antenna simulation is the modeling of feeds and loads. The coaxial feed is commonly used as antenna excitation. For thin substrates, a coaxial feed can be replaced by a current filament \( I(t) \). The excitation vector in (5) becomes
\[
f_{\text{int}} = \partial_t I(t) \int \hat{\mathbf{J}} \cdot \mathbf{N}_i \delta(x-x_i) \delta(y-y_j) dx dy
\]

where \( I \) is the length of the current filament, and \( (x_i, y_j) \) denotes the position of the current source. Clearly, \( f_{\text{int}} \) is a vector whose elements are zero, except for the \( i \)th element, which is equal to \( \partial_t I(t) \) if the basis function \( \mathbf{N}_i \) is normalized. If higher order vector bases are used to expand the unknown fields, the current filament can be partitioned into several segments to consider its contribution since one edge is associated with more than one degree of freedom. For thicker substrates, a magnetic frill current \( \mathbf{M}_{\text{int}}(r,t) \) can be introduced over the aperture of the coaxial feed, while the inner conductor of the feed is modeled as a conducting post [5].

An impedance load of \( Z_\text{f} \) in \( \Omega \) can be modeled as a post of finite conductivity connecting the patch to the base of the cavity. Its contribution to matrix \( \mathbf{R} \) in (4) can be written as
\[
\mathbf{R}_{ij} = d^2 Z_\text{f}^{-1} \int \mathbf{N}_i \cdot \mathbf{N}_j \delta(x-x_L) \delta(y-y_L) dx dy
\]

where \( d \) is the length of the post, and \( (x_L, y_L) \) denotes the position of the impedance load. If the post coincides with the \( i \)th edge, it only contributes to the \( i \)th diagonal element of matrix \( \mathbf{R} \), which amounts to adding \( d^2 Z_\text{f}^{-1} \) to \( \mathbf{R}_{ii} \). If higher order basis functions are used, similar to the case of antenna feeds, the conducting post can be partitioned into several segments to consider its contribution. If the shorting pins are used, one can simply set the tangential electric field along the post to zero or specify a large conductivity for the conducting post.

The TDFEM scheme calculates near fields. The far-field signature, such as the radar cross section (RCS), can be computed as
\[
\text{RCS} = \lim_{r \to \infty} 4\pi r^2 \left| \frac{H_{\text{far}}(r,t)}{E_{\text{inc}}(r,t)} \right|^2
\]

where the far-zone scattered magnetic field \( H_{\text{far}} \) can be calculated from
\[
H_{\text{far}}(r = c^{-1} r) = (2 \pi \mu_0 c \eta_0)^{-1} \partial_t \left( \hat{\mathbf{\theta}} \partial_{\mathbf{\theta}} \phi + \hat{\mathbf{\phi}} \partial_{\mathbf{\phi}} \right) \mathbf{L}(r, t)
\]

in which \( \mathbf{L}(r, t) \) relates to the integration of the equivalent magnetic current \( \mathbf{K} \) over the aperture \( S_a \):
\[
\mathbf{L}(r, t) = \int_{S_a} \mathbf{K}(x', y', t + c^{-1} \hat{r} \cdot \mathbf{r}') dx' dy'.
\]

3. NUMERICAL EXAMPLES

The first example is scattering by an antenna consisting of a 3.66 cm x 2.60 cm rectangular conducting patch residing on a dielectric substrate having thickness \( t = 0.158 \) cm, relative permittivity \( \epsilon_r = 2.17 \), and conductivity \( \sigma = 0.604 \) ms/m. The substrate is housed in a 7.32 cm x 5.20 cm rectangular cavity recessed in a ground plane. The PML wraps the aperture,
and is 1 cm thick. The vertical distance from the PML to the aperture is 1 cm. The PML is formulated in a quadratic profile, and the maximum conductivity is chosen to be 0.9 s/\pi 114 m. The computational domain is discretized into 10,455 tetrahedra, yielding 66,338 unknowns with the use of the first-order vector basis functions. The incident pulse is specified as

\[ E^{inc}(r, t) = \hat{A} 2 [ t - t_0 - c^{-1} \hat{k} \cdot (r - r_0)] \]

\[ \times \exp \left\{ - [ t - t_0 - c^{-1} \hat{k} \cdot (r - r_0)]^2 / \tau^2 \right\} \]

in which \( t_0 = 0.49 \text{ ns}, \tau = 0.098 \text{ ns}, r_0 = \hat{z} 2 \text{ cm}, \) and \( \hat{k} = -\hat{x} \sin 60^\circ \cos 45^\circ - \hat{y} \sin 60^\circ \sin 45^\circ - \hat{z} \cos 60^\circ. \) Figure 2 shows the temporal backscattered far-field signatures. The monostatic RCS of the antenna is shown in Figure 3 as a function of frequency from 2 to 8 GHz. Clearly, the RCS is characterized by a series of peaks, each corresponding to a resonant mode of the patch. The result compares well with that generated by FDFE–BI, and the experimental data for the patch residing on an infinite substrate [6].

The second example is radiation by an antenna consisting of a 5.0 cm x 3.4 cm rectangular conducting patch residing
on a dielectric substrate having thickness $t = 0.08770$ cm, relative permittivity $\varepsilon_r = 2.17$, and conductivity $\sigma = 0.362$ ms/m. The substrate is housed in a $7.5 \text{ cm} \times 5.1 \text{ cm}$ rectangular cavity recessed in a ground plane. The PML has a thickness of 1 cm, and is placed in the same fashion as in the regular cavity recessed in a ground plane. The PML has a conductivity $\sigma = 0.16$ ns. A 50 $\Omega$ impedance load is placed at $x_y = -2.2 \text{ cm}$ and $y_z = -1.5 \text{ cm}$. Figure 4 shows the calculated voltage at the input port and the impedance load, respectively. Figure 5 shows the input impedance of the antenna as a function of frequency from 1 to 4 GHz. The calculated results compare well with that obtained by FDFE–BI, and the experimental data for the patch residing on an infinite substrate [6].

4. CONCLUSION
A TDFEM scheme is presented for the analysis of cavity-backed microstrip patch antennas. The method uses the PML for truncating the finite-element solution domain and the higher order vector basis functions for expanding the electric field. Numerical examples are given to demonstrate its validity.

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BROADBAND HYBRID MICROSTRIP COUPLERS—AMPLITUDE AND PHASE

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ABSTRACT: Several designs for a 180° hybrid coupler are discussed. Using the stepped-impedance method, the bandwidth of an 11 GHz hybrid coupler is increased to approximately 1.6 times the bandwidth of a conventional hybrid coupler. Comparisons are made between conventional and broadband hybrid couplers, as well as between circular and rectangular designs, and the phase behavior of each is compared for the first time. © 2002 John Wiley & Sons, Inc. Microwave Opt Technol Lett 32: 254–259, 2002.

Key words: hybrid coupler; broadband; microstrip; phase
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1. CONVENTIONAL 180° HYBRID COUPLER
180° hybrid couplers are commonly used in the design of microwave and millimeter-wave devices such as balanced mixers, modulators, frequency multipliers, and amplifiers. There is also an application in which a hybrid coupler can be integrated with a ferrite coupled-line (FCL) structure to produce a novel four-port FCL circulator. The performance of these circulators may be limited by the bandwidth of the

Figure 5 Input impedance versus frequency for a cavity-backed patch antenna with a probe feed at $x_f = 1.22$ cm and $y_f = 0.85$ cm, and a 50 $\Omega$ impedance load at $x_y = -2.2$ cm and $y_z = -1.5$ cm. (A = 7.5 cm, B = 5.1 cm, L = 5.0 cm, W = 3.4 cm, $d = 0.08779$ cm, $\varepsilon_r = 2.17$, tan $\delta = 0.0015$). (a) Resistance. (b) Reactance.