

⑤ Differentiation

$$x(t) \longleftrightarrow a_k, \omega_0$$

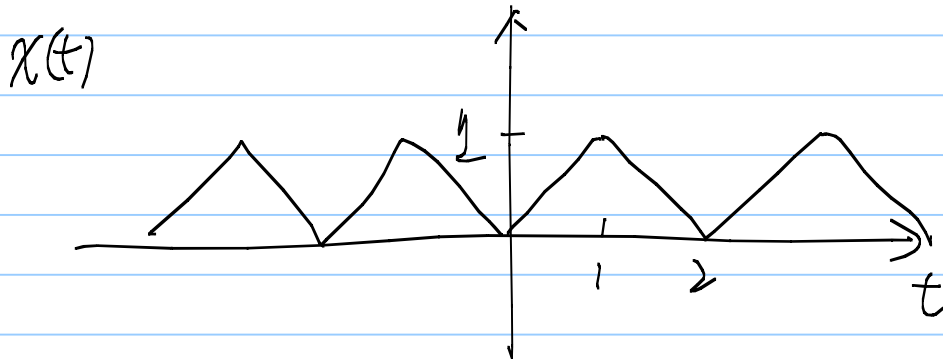
$$y(t) = \frac{d}{dt} x(t)$$

$$y(f) \longleftrightarrow b_k, \square$$

Find the F.S of  $y(t)$

Ans=

by inspection



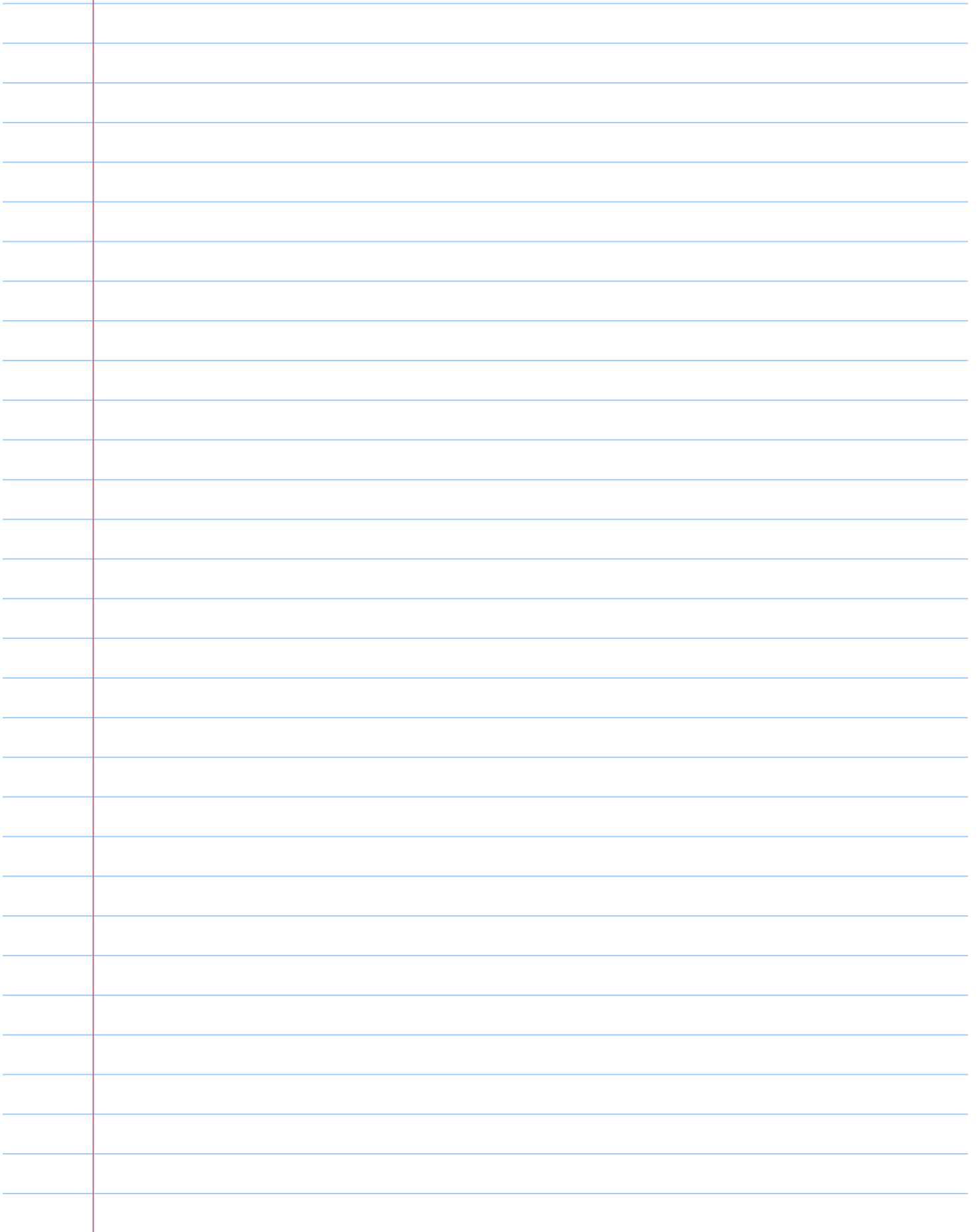
Q: F.S.

Ans:

Sub-Q:  $y(t) = \frac{d}{dt} x(t)$ , plot  $y(t)$

Q: F.S of  $y(t)$

Ans:



## § ⑥ Multiplication

Suppose

$$\begin{array}{l} x(t) \xleftrightarrow{\text{F.S.}} a_k, \omega_0 \\ y(t) \xleftrightarrow{\text{F.S.}} b_k, \omega_0 \end{array} \left. \vphantom{\begin{array}{l} x(t) \\ y(t) \end{array}} \right\} \begin{array}{l} \text{the same} \\ \text{freq } \omega_0 \end{array}$$

$$z(t) = x(t) \cdot y(t) \xleftrightarrow{\text{F.S.}} c_k, \boxed{\phantom{0}}$$

Find the FS. representation of  $z(t)$ .

Ans.

## ① Parseval's Relationship

~~It~~

$$X(t) \longleftrightarrow a_k, \omega_0$$

then

Intuition, we first note that

Since  $X(t) = \sum_{k=-\infty}^{\infty} a_k e^{j k \omega_0 t}$  contains many HRCEs, the avg power of  $X(t)$  should be the sum of the avg powers of each HRCE.

\* The Parseval's relationship is sometimes referred as the "power conservation law."