

Plot  $y(t) = \frac{1}{3} x(4 - 0.5t)$ .

Ans:

Prof. Balakrishnan's handout.

\* Classification #3: By the period.

\* We say  $x(t)$  is a periodic signal with period  $T$  if we let  $y(t) = x(t-T)$  be the shifted version of  $x(t)$ , then the new signal "looks" exactly like the old signal: sometimes we just write

For DT:

Ex:  $x(t) = \sin(2t)$  Plot  $x(t)$  vs.  $t$ .

$$\text{Ex: } x[n] = (-1)^n$$

Q: Is  $x[n]$  periodic?

A:

\* If  $x(t)$  is periodic with period  $T$   
 then it is periodic with period  $mT$   
 for any  $m \geq 1$  integers

Ex:  $\pi, 2\pi, 3\pi, \dots$  are all periods

for  $x(t) = \sin(2t)$

\* Def: The fundamental period is the smallest period of a periodic signal  $x(t)$  or  $x[n]$ .

\* If  $x(t) = X_{Re}(t) + jX_{Im}(t)$  is a periodic complex signal, then both  $X_{Re}(t)$  &  $X_{Im}(t)$  are periodic real signals.

Proof :

Question If both  $x_1(t)$  and  $x_2(t)$  are periodic, must  $x_1(t) + x_2(t)$  periodic?

How to decide the period of a signal?

Ans :