## 4.6 TABLES OF FOURIER PROPERTIES AND OF BASIC FOURIER TRANSFORM PAIRS

In the preceding sections and in the problems at the end of the chapter, we have considered some of the important properties of the Fourier transform. These are summarized in Table 4.1, in which we have also indicated the section of this chapter in which each property has been discussed.

In Table 4.2, we have assembled a list of many of the basic and important Fourier transform pairs. We will encounter many of these repeatedly as we apply the tools of

Section	Property	Aperiodic signa	d 	Fourier transform
Section	х	c(t)		ζ(jω) <sub>ζ</sub> (jω)
4.3.1 4.3.2 4.3.6 4.3.3 4.3.5 4.3.5 4.4 4.5	Time Shifting Frequency Shifting Conjugation Time Reversal	$ax(t) + by(t)$ $x(t - t_0)$ $e^{j\omega_0 t} x(t)$ $x^*(t)$ $x(-t)$ $x(at)$ $x(t) * y(t)$ $x(t)y(t)$ $\frac{d}{dt} x(t)$		$AX(j\omega) + bY(j\omega)$ $e^{-j\omega t_0}X(j\omega)$ $X(j(\omega - \omega_0))$ $X^*(-j\omega)$ $X(-j\omega)$ $\frac{1}{ a }X\left(\frac{j\omega}{a}\right)$ $X(j\omega)Y(j\omega)$ $\frac{1}{2\pi}\int_{-\infty}^{+\infty}X(j\theta)Y(j(\omega - \theta))d\theta$ $j\omega X(j\omega)$
4.3.4	Integration  Differentiation in	$\int_{-\infty}^{t} x(t)dt$ $tx(t)$		$\frac{1}{j\omega}X(j\omega) + \pi X(0)\delta(\omega)$ $j\frac{d}{d\omega}X(j\omega)$
4.3.6	Frequency  Conjugate Symmetry  for Real Signals	x(t) real $x(t)$ real and even		$\begin{cases} X(j\omega) = X^*(-j\omega) \\ \Re e\{X(j\omega)\} = \Re e\{X(-j\omega)\} \\ \Im m\{X(j\omega)\} = -\Im m\{X(-j\omega)\} \\  X(j\omega)  =  X(-j\omega)  \\ \not\sim X(j\omega) = -\not\sim X(-j\omega) \\ X(j\omega) \text{ real and even} \end{cases}$
4.3.3	Symmetry for Real and Even Signals Symmetry for Real and	x(t) real and odd		$X(j\omega)$ purely imaginary and $^{ m od}$
4.3.3	Odd Signals	$x_e(t) = \mathcal{E}\nu\{x(t)\}$	[x(t)  real]	Re{X(jω)} jIm{X(jω)}
4.3.3	Even-Odd Decomposition for Real Sig- nals	$x_o(t) = \mathfrak{O}d\{x(t)\}$	[x(t)  real]	Jam(v(Im))

4.3.7 Parseval's Relation for Aperiodic Signals 
$$\int_{-\infty}^{+\infty} |x(t)|^2 dt = \frac{1}{2\pi} \int_{-\infty}^{+\infty} |X(j\omega)|^2 d\omega$$