

## ④ Poisson

1063

1/31/2011

Ex: if  $\lambda = 0.5$

\* The sample space of a Poisson R.V  
is exactly the same as that of  
a geometric R.V.

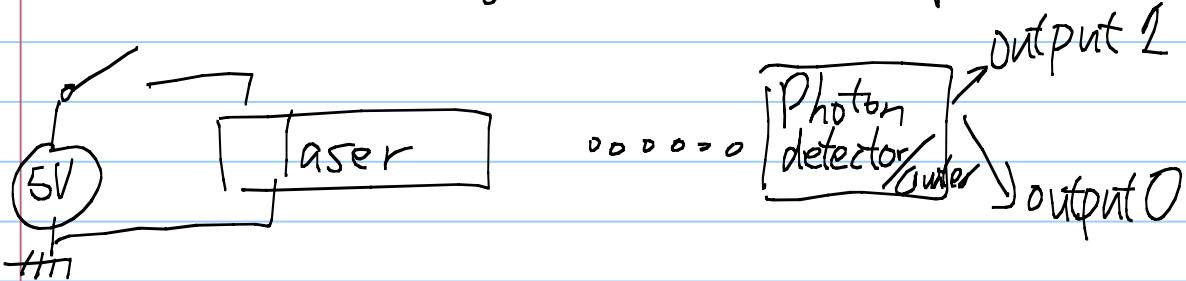
\* Poisson random variable is used to model  
the experiment that ①

②

③

④

\* Poisson is quite common, especially in physics.



A laser that can be turned on (5V)  
or off (0V)

Once it is on, in average  
1000 photons/msec.

A photon detector count the number  
of photons  $X$  in 0.1 msec. And output  
0 or 1 depending on  $X$ .

If there is no "ambient noise"

(but in reality, we choose  
instead).

What is the prob that the output

is 0 even if the laser is ON.

Ans:

Q: Suppose we reduce the interval to

0.01 msec

$\gamma$  is the # of photons in

0.01 msec.

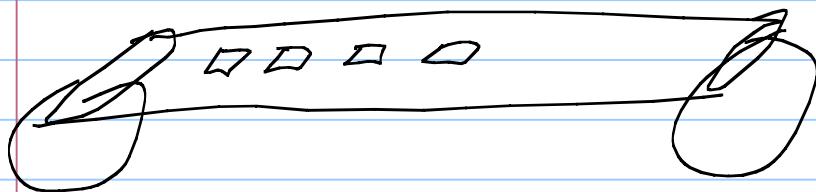
$P(\text{Output} = 0)$  | the laser is ON)  
=?

Ans:

Namely: sending at rate  $\frac{1}{0.01 \text{ msec}} = 10^4$  the error  
 $\text{prob} \geq 10^{-16}$  if we increase the rate to  $10^5$ .

the bit error rate increases to 1%.  
 a trade-off between communication speed  
 and the error rate.

Ex: A factory uses X-ray to test  
 the defective chips sequentially  
 [X-ray]



We know that in average we will find  
 3 defective chips every 20 minutes.

Let  $X$  be the number of defective  
 chips found from 1-2:30 pm

$$Q: P(X \leq 6) = ?$$

Ans:

Q:  $E(X) = ?$

Aus:

$$Q: E(X(X-1)) = ?$$

Ans:

$$Q: E(X^2) = ? \quad \text{Var}(X) = ?$$

Ans:  
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