00 [ECE-302 Lecture 01 are more important than textbooks. * Lectures * Ask questions — A small misunderstanding may affect your learning of the -entire semester. Outlines of this course: * What is "probability"? How to explain (model a real engineering problem by "probability" How to do simulation for ECE apps.? When simulations fail, how to analyze the problem by penal & paper. Example: The auto-filling function of Microsoft Word 3 How does Google search? The opinion polls for a presidential lexit election
Auto-Trading algorithm in a Wall-Street firm not to bet. 5 Gambling, Poker, Lottery, To bet or

O Wireless/radar measurement is always Unreliable/random, how to trace a missile/vehicle accurately. O Wireless comm. is unreliable, how to design a cellular phone system that has the fewest dropped calls. O Real, large-scale system deployment is exprise how to build a good simulator that reflects the unpredictable practical world. 9 Clinical trials: Developing New drugs from a very small number of experiments In a nutshell, how to * Technical terms that you are going to learn, = random variables, random processes, independence correlations, Gaussian distributions, Law of Large Numbers, Central limit theorem You need to have an open mind for the new concept probability, which is different from what you have learned before! In particular

003 Q: What Is "probability"? Historically, there was a debate between two types of "prob." lype 1: EX: Coin-flipping, Free-throw percentage Bhitting average The "frequence" can be obtained from lype 2° Ex: Prob that I win a lottery tomorrow. @ Prob that I will get an A in ECE 302 3 A game of betting \$1 on the outame of a particular die for the return of \$8 Q: Would you bet?

004 A unifying "prob theory" was not available until Kolmogorov in 1930's. Probability is a surprisingly young branch of mathematics. || Calculus was developed in early 1700 Kolmogorov noticed that the common ground of the above Two perspectives is X A unity new of prob, is thus Prob is the The derive meaningui be used to Can RhSW015 to many practical questions. 3 different possibilities

605 Example: For a three-faced die, what is the prob of winning by betting. 2. Ans & What is the prob that I have more than > | apple today? Ans: What is the average # of fouch-downs for Produe's next football game Ans: (4) If Jimmy John's is running the following promotion. Let X be the number of touch downs of Purdue's next football game. Jimmy John's will give each customer X² number of free sandwich. (Interpretation: If 1 touch down, then each customer gets 1 sandwich. If 2 touch downs, then 4 sandwiches; If 3 touch downs, then 9 sandwiches.) Question: What is the average number of free sandwiches a customer can have? (5) If X is the number of friends I talk to in the next hour. What is the average of X²? (6) If my iphone runs ≤ 2 programs, then it can last a day. If it runs >=3 programs, then it can only last 0.5 day. What is the average hours that my iPhone can last?

P005.2

* The prob methods aim at producing meaningful answers to the above question * Supplemented polt #1. * ONCE the weight assignment is made. [Prob Method] = [Counting] A Note that the prob methods do not question how the W.A is made. It is the user who has to determine whether the W.A is reasonable or not * The importance of the W.A Ex: Q1. What is the prob that the outcome of a die is 1? Q2: What is the pub that the outcome of a fair die is 1?

The 2nd question specifies that the 1006 W.A must be 6 for each outcome. A2: Q3: What is the pub that the outcome of a <u>fair</u> dice is a prime number? Áns; - ---> Inference / Decision Real world prob. methods. Prob. Weight Assignment A menningful decision voquires meaningful W.A + probabilistic/counting method Part of the reason of 2008's financial crisis was the incorrect assumption of the probabilistic models (using the wrong weight assignment). I We need a simple way to construct a W.A Su a correct way to count the weights. Another example of the importance of the W.A. Ex: A coin-flip game as follows 1. The minimal bet is 1 M dollars 2 Flip a coin 1,000,000 times. If the frag is between (0.499,0,50/) you win

DC \$ 2M Q: should you bet or not? Ans: Before any meaningful answer, we need to decide the W.A we are going to use

008 Q: Why we would need probability? (We already have calculus & differential equation.) Ans Many things are indeed random. Even for some events that are determistic, it is still important to use prob. Ex: A 2-player poker game (Texas Holdiem) - It actually has a deterministic outcome. . The end result is fixed once the deck is shuffled, even before dealing the card (pockets, flop, turn, river) - Nonotheless, there are too many unknowns in determining the deck. - Model the unknown/unidentified factors by randomness.

In summary: Prob inference is a way of counting based on a specific W.A. 009 The first step is always to design your W.A. Then we count. (Do not change your W.A during counting) Ex: Three doors, 1 prize Firstly, we place the prize randomly behind 1 of the doors. AFTER that, a stubborn player comes le she always chooses door #1. AFTER that, the host, knowing which door has the prize, up 5 a door from # 2 & # 3 that is without the prize. Q: Should the player switch or stay?

Among these 3 possibilities, when should we switch? 00 ternative solution this a good W.A? $\mathbb{Q}^{\circ}_{\circ}$ Do you believe that the produces indeed put the prize behind a door be P 9 \bigcirc before the show? a stort the

DL Stops of solving a prob problem Example: An urn contains 5 balls, 1,...,5. Select two balls randomly with replacemen Q1.1: How many distinct pairs? Q1.2: What's a reasonable W.A Q2: What is Prob (2 draws yield the same number)? is the prob that $(X_1^2 + X_2^2 \le 9)$ D: What n5-

Step 1: Constructing the W.A B. not easy. Too many ways of constructing a W.A. (even for reasonable ones) is cumbersome BH the In let other W.A people HOW W.A you are using We need a simple ways to describle & construct the W.A. And even to hep us &r We need mathematics. new notation! We need (Use a 6-faced die for example)

013 The B the for all the outcomes in the event Ex: the prob of "X being a prime number event Set/Event operations \mathcal{O} Q: What is the prob of a null event? Ans: (\mathbf{E}) Q: What is the prob of a global -event Ars : : A tool to help us visualize the set operations.

014	(3)
	(4)
	(3)
	Why are we interested in the set operation?
	Ans: We are more intersted in the
	Weights assigned to each set. Nonether,
	thowing how to an
	outrome is essential before we can
	properly count the total weight assigned
	tor an event.

(015 Ex: A= [all multiples of 4.7. 4,8,12. B: { all multiples of 2.7. 2,4,6,8,... 6 (1) 8

1016 Once we know how to include/exclude events/sets, we need to assign weights A valid W.A satisfies the following 3 axions Axiom 1: Axiom 2: Axioms: AxIDA 3,13