00 [ECE-302 Lecture 01 are more inportant than textbooks. * Lectures * Ask questions — A small misunderstanding may affect your learning of the -entire semester. Outlines of this course: * What is "probability"? How to explain (model a real engineering problem by "probability" How to do simulation for ECE apps,? When simulations fail, how to analyze the problem by penal & paper. Example: The auto-filling function of Microsoft Word 3 How does Google search? 3 The opinion polls for a presidential election Auto-Trading algorithm in a Wall-Street not to bet. 5 Gambling, Poker, Lottery, To bet or

O Wireless/radar measurement is always Unreliable/random, how to trace a missile/vehicle accurately. O Wireless comm. is unreliable, how to design a cellular phone system that has the fewest dropped calls. O Real, large-scale system deployment is exprise how to build a good simulator that reflects the unpredictable practical world. 9 Clinical trials: Developing New drugs from a very small number of experiments In a nutshell, how to model "randomness" * Technical terms that you are going to learn, = random variables, random processes, independence correlations, Gaussian distributions, Law of Large Numbers, Central limit theorem You need to have an open mind for the new concept probability, which is different from what you have learned before! Prob = combination / permutation.

003 Q: What is "probability"? Historically, there was a debate between two types of "prob." Type 2 Frequencists view of prob: X Prob. is the long-term relative frequent Ex: Coin-flipping, Free-throw percentage hitting average The "frequency" can be obtained from historical data. Type 2. Bayesian Style Prob. (Thomas Bayes (702-1961 * Prob is how much you believe an event will happen Ex: Prob that I win a lottery tomorrow. Sprob that I will get an A in 3 A game of betting \$1 out the outcome of a particular die for the return of \$8 Q: Would you bet? A: Depends on how you believe the fairness of the dice " These exp. cannot be repeated. Thus no "fragung"

A unifying "prob theory" was not available until Kolmogorov in 1930's Probability is a surprisingly young branch of mathematics. || Calculus was developed in early 1700 * Kolmogorov noticed that the common ground of the above Two perspectives is "the additivity" of prob. Namely = F1 happens + F2 happens = F1 or 2 happens. For be freq or belief. * A unify New of prob, is thus Prob is the "weight assignment." (WA) The WA can be used to derive meaningful RhSWD15 to many practical questions. 3 different 3 different 3 possibilities 2 Weight 0,3 0,2 Weight assignment

605 Example: For a three-faced die, what is the prob of winning by betting. 2. Ars \$ 93 INF & US
What is the prob that I have more than > | apple today?
Ans: 0,3+0,2=0,5
What is the average # of fouch-downs for Pudue's next football game Ans: 0,5x/+ 0,3x2 + 0,2x3=1.7 (4) If Jimmy John's is running the following promotion. Let X be the number of touch downs of Purdue's next football game. Jimmy John's will give each customer X² number of free sandwich. (Interpretation: If 1 touch down, then each customer gets 1 sandwich. If 2 touch downs, then 4 sandwiches; If 3 touch downs, then 9 sandwiches Question: What is the average number of free sandwiches a customer can have? Ans: 0.5*1^2+0.3*2^2+0.2*3^2=3.5 (5) If X is the number of friends I talk to in the next hour. What is the average of X²? Ans: The same as the last question. (6) If my iphone runs ≤ 2 programs, then it can last a day. If it runs >=3 programs, then it can only last 0.5 day. What is the average hours that my iPhone can last? Ans: 0.5*24+0.3*24+0.2*12=21.6 hours

P005.2

* The prob methods aim at producing meaningful answers to the above question * Supplemented polt #1. * ONCE the weight assignment is made. [Prob Method] = Counting A Note that the prob methods do not question how the W.A is made. It is the user who has to determine whether the W.A is reasonable or not * The importance of the W.A Ex: Q1. What is the prob that the outcome of a die is 1? -> An invalid guestion Q2: What is the pub that the outcome of a fair die is 1?

006 The 2nd question specifies that the W.A must be f for ortcome each A2: -Q3: What is the pub that the outcome of a fair dice is a prime number? Ans: Prime # ; 2,3,5 => Prob = + + + + + = 3 - - ---> Inference / Decision Real world prob. methods. Prob. Weight Assignment A menningful decision vogures meaningful W.A + probabilistic/counting method Part of the reason of 2008's financial crisis was the incorrect assumption of the probabilistic models (using the wrong weight assignment). & We need a simple way to construct a W.A & a correct way to count the weights. Another example of the importance of the W.A. Ex: A coin-flip game as follows 1 The minimal bet is 1 M dollars 2 Flip a coin 1,000,000 times If the frez is between (0.499,0,50/) you win

\$ 2M Q should you bet or not? Ans: Before any meaningful answer, we need to decide the W.A we are going to 420 Ex: WA is "a fair coin" Prob = 1, 1, In this course, we will learn that the winning percentage 95,45% Tes, we should bet. Ex: WA is a slightly bent coin Prob = 0,49, 0,5No, we should not bet.

008 Q: Why we would need probability? (We already have calculus & differential equation.) Ans Many things are indeed random. Even for some events that are determistic, it is still important to use prob. Ex: A 2-player poker game (Texas Holdiem) - It actually has a deterministic outcome. . The end result is fixed once the deck is shuffled, even before dealing the card (pockets, flop, turn, river) - Nonotheless, there are too many unknowns in determining the deck. - Model the unknown/unidentified factors by randomness.

In summary: Prob interence is a way of counting based on a specific W.A. 509 The first step is always to design your W.A. Then we count. (Do not change your W.A during counting) Ex: Three doors, 1 prize Firstly, we place the prize randomly behind 1 of the doors. AFTER that, a stubborn player comes to she always chooses door #1. AFTER that, the host, knowing which door has the prize, apons a door from # 2 & # 3 that is without the prize. Q: Should the player switch or stay? Ans: Without knowing where the prize is, sometimes switching is better, sometimes staying is better. We need to quantify what is the probability that "switching is better", and what is the probability that "staying is better". Ans: The random part is "where is the prize & "which door the host will open. We use the following W.A. prize placement 13 3 possibilities

Åmong these 3 possibilities, when should we switch? 00 Prize is in #3 & Host opens # 2 or Pirize is in #2 & lotost opens #3 Prob $= \frac{1}{3} + \frac{1}{3} = \frac{2}{3}$ | Namely, f we always switch. $\frac{2}{3} + \frac{1}{3} = \frac{2}{3}$ | always switch. $\frac{2}{3} + \frac{1}{3} = \frac{2}{3}$ | $\frac{2}{3} + \frac{1}{3} + \frac{1}{$ what condition is staying good In Prive is in #1 better place. $P_{rob} = 1/3$ Ans: Switching is better. prize placement Atternative possibilities 2 0.25 0.50.25 Switch = + = It does not Stay 0.5 matter. Q: Is this a good W.A? O; Do you believe that the produces indeed put the prize behind a door before stort of the show? the

DL Steps of solving a prob problem Step 1: Construct the W.A Step 1.1: Identify all possible choices of the uncertain outcomes Step 1.2: Assign a reasonable weight for each outcome. Step 2: Counting Example: An urn contains 5 balls, 1,..., 5. Select two balls randomly with replacement Q1.1: How many distinct pairs? Q1.2: What's a reasonable W.A Q2: What is Prob (2 draws yield the same number)? Ans: 025 pairs (1,1)...(5,5)() Each pair has a weight 25 $\Im \frac{1}{25} \times 5 = \frac{1}{5} \left((1,1), (2,2), \cdots, (5,5) \right)$ Q: what is the prob that $(X_1^2 + X_2^2 \le 9)$ $An5^{=} \frac{1}{25} \times 4 \left(((.1) (1.2) (2.1), (2.2) \right)$

Step]: Constructing the W.A is not easy. Too many ways of constructing a W.A. (even for reasonable ones) DIt is cumbersome to describe the W.A & let other people know the W.A you are using We need a simple way(s) to describle & construct the W.A. And even to hep us We need mathematics. X We need new notation! (Use a 6-faced die for example) Set Global set. Element ?1, 2, 3,5} {'1,2,3,4,5,6} $1_{or} \rightarrow 2_{or} \rightarrow 3$ 4, 5, 6or [1,3] Somple space Outcome (Event) a group of All possible results. One possible result results Ex Die gives 1 Die being All possible a prime number prime die values/ (the outcome being prime) outcomes the outcome of the dice is 1,