
 Fig. 8. Decoding module (level  $p$ ).

With the feedback decoder, the LLR  $\Lambda_1(d_k)$  generated by decoder  $\text{DEC}_1$  is now equal to

$$\Lambda_1(d_k) = \frac{2}{\sigma_z^2} x_k + \frac{2}{\sigma_z^2} z_k + W_{1k} \quad (44)$$

where  $W_{1k}$  depends on sequence  $\{z_n\}_{n \neq k}$ . As indicated above, information  $z_k$  has been built by decoder  $\text{DEC}_2$ . Therefore  $z_k$  must not be used as input information for decoder  $\text{DEC}_2$ . Thus decoder  $\text{DEC}_2$  input sequences will be sequences  $\{\tilde{\Lambda}_1(d_n)\}$  and  $\{y_{2k}\}$  with

$$\tilde{\Lambda}_1(d_n) = \Lambda_1(d_n)_{z_n=0}. \quad (45)$$

Finally, from (40), decoder  $\text{DEC}_2$  extrinsic information  $z_k = W_{2k}$  after deinterleaving can be written as

$$z_k = W_{2k} = \Lambda_2(d_k) |_{\tilde{\Lambda}_1(d_k)=0} \quad (46)$$

and the decision at the decoder  $\text{DEC}$  output is

$$\hat{d}_k = \text{sign}[\Lambda_2(d_k)]. \quad (47)$$

The decoding delays introduced by the component decoders, the interleaver and the deinterleaver imply that the feedback piece of information  $z_k$  must be used through an iterative process.

The global decoder circuit is made up of  $P$  pipelined identical elementary decoders. The  $p$ th decoder  $\text{DEC}$  (Fig. 8) input, is made up of demodulator output sequences  $(x)_p$  and  $(y)_p$  through a delay line and of extrinsic information  $(z)_p$  generated by the  $(p-1)$ th decoder  $\text{DEC}$ . Note that the variance  $\sigma_z^2$  of  $(z)_p$  and the variance of  $\tilde{\Lambda}_1(d_k)$  must be estimated at each decoding step  $p$ .

For example, the variance  $\sigma_z^2$  is estimated for each  $M^2$  interleaving matrix by the following:

$$\sigma_z^2 = \frac{1}{M^2} \sum_{k=1}^{M^2} (|z_k| - m_z)^2 \quad (48a)$$

where  $m_z$  is equal to

$$m_z = \frac{1}{M^2} \sum_{k=1}^{M^2} |z_k|. \quad (48b)$$

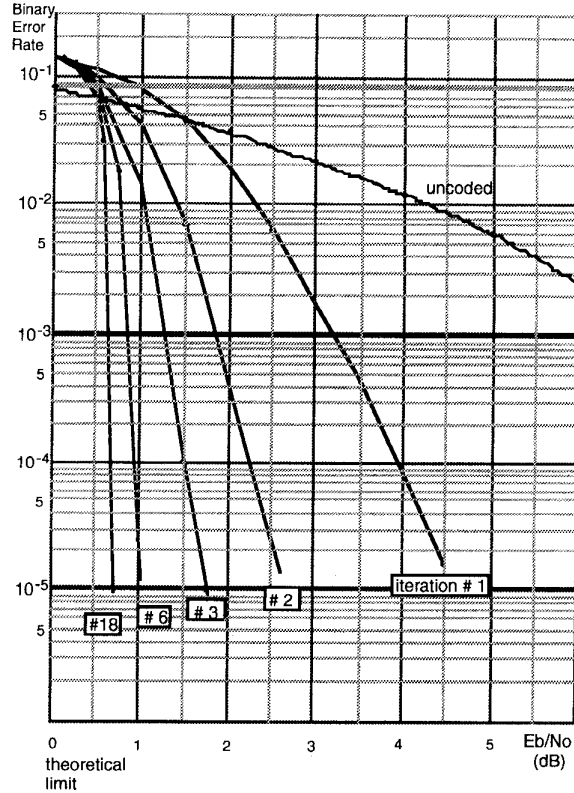


Fig. 9. BER given by iterative decoding ( $p = 1, \dots, 18$ ) of a rate  $R = 1/2$  encoder, memory  $\nu = 4$ , generators  $G_1 = 37, G_2 = 21$ , with interleaving  $256 \times 256$ .

### B. Interleaving

The interleaver is made up of an  $M \cdot M$  matrix and bits  $\{d_k\}$  are written row by row and read following the nonuniform rule given in Section III-B2. This nonuniform reading procedure is able to spread the residual error blocks of rectangular form, that may set up in the interleaver located behind the first decoder  $\text{DEC}_1$ , and to give a large free distance to the concatenated (parallel) code.

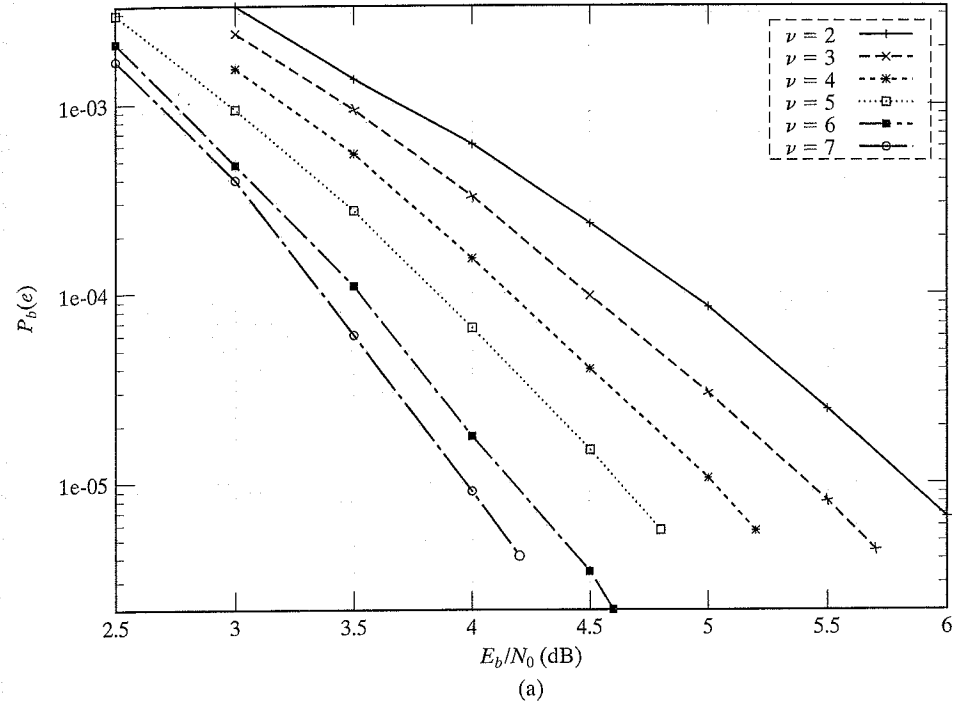
For the simulations, a  $256.256$  matrix has been used and from (19), the addresses of line  $i_r$  and column  $j_r$  for reading are the following:

$$i_r = 129(i + j) \quad \text{mod} \cdot 256$$

f the decoding trellis. Thus, tial dependence of decoding application of the Viterbi since the branch complexity ce more time to decode. This eliminated using a technique

erbi algorithm by employing it must be performed at each used to do the operations in  $2^v$  operations serially. Thus, s a factor of  $2^v$  advantage in  $2^v$  times as much hardware. about 1/3 for a large subclass compare-select-add (CSA) ls of this *differential Viterbi*

sults illustrating the perfor- Figure 12.17. The bit-error rates with constraint lengths as a function of the bit SNR channel in Figure 12.17(a), d-quantized ( $Q = 2$ ) channel memory was  $\tau = 32$ . Note that of soft decisions (unquantized 2). This improvement is illus- e of the optimum constraint  $\infty$  (unquantized outputs) and .2.17(c) is the uncoded curve es shows real coding gains of 1B in the quantized ( $Q = 8$ )  $= \infty$ ) soft-decision case at a . only about 0.2-dB difference and the unquantized ( $Q = \infty$ ) h to gain by using more than (d), the performance of this and  $\infty$  (no truncation) for a tput. Note that in both cases ance by about 1.25 dB, that at  $\tau = 32 = 8v$  performs the 1/2 codes.) The performance engths  $v = 3, 5,$  and  $7$  listed a continuous-output AWGN than the corresponding rate a 0.25 dB and 0.5 dB. This is 1  $d_{free}$  in decibels, is larger at



(b)

FIGURE 12.17: Simulation results for the Viterbi algorithm.