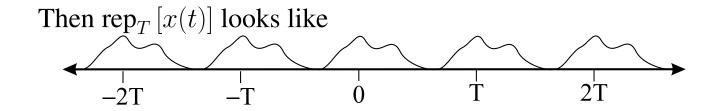
## 1-D Rep Operation

The rep operator periodically replicates a function with some specified period T.

$$\operatorname{rep}_{T}[x(t)] = \sum_{k=-\infty}^{\infty} x(t - kT)$$

If x(t) looks like





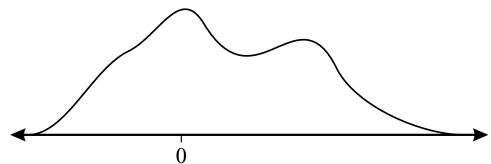
The resulting function is periodic with period T.

### 1-D Comb Operation

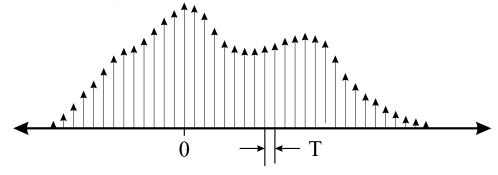
The *comb* operator multiplies a function by a periodic train of impulses.

$$comb_{T}[x(t)] = \sum_{k=-\infty}^{\infty} \delta(t - kT)x(t)$$
$$= x(t) \sum_{k=-\infty}^{\infty} \delta(t - kT)$$





Then  $comb_T [x(t)]$  looks like



The spacing between impulses is T.

# 1-D Rep and Comb Transform Properties

Assume that:

$$x(t) \stackrel{CTFT}{\Leftrightarrow} X(f)$$

Then the transform relationship is:

$$\operatorname{comb}_{T}\left[x(t)\right] \quad \overset{CTFT}{\Leftrightarrow} \quad \frac{1}{T}\operatorname{rep}_{\frac{1}{T}}\left[X(f)\right]$$

$$\operatorname{rep}_{T}\left[x(t)\right] \ \stackrel{CTFT}{\Leftrightarrow} \ \frac{1}{T} \operatorname{comb}_{\frac{1}{T}}\left[X(f)\right]$$

## 2-D Rep and Comb Operators

## 2-D Rep function:

$$\operatorname{rep}_{X,Y}\left[f(x,y)\right]$$

$$= \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} f(x - mX, y - nY)$$

#### 2-D Comb function:

$$comb_{X,Y} [f(x,y)]$$

$$= f(x,y) \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} \delta(x - mX, y - nY)$$

## 2-D Rep and Comb Transform Properties

Assume that:

$$f(x,y) \stackrel{CSFT}{\Leftrightarrow} F(u,v)$$

Then the transform relationship is:

$$\begin{split} & \operatorname{comb}_{X,Y}\left[f(x,y)\right] \quad \overset{CSFT}{\Longleftrightarrow} \quad \frac{1}{XY} \mathrm{rep}_{\frac{1}{X},\frac{1}{Y}}\left[F(u,v)\right] \\ & \operatorname{rep}_{X,Y}\left[f(x,y)\right] \quad \overset{CSFT}{\Longleftrightarrow} \quad \frac{1}{XY} \mathrm{comb}_{\frac{1}{X},\frac{1}{Y}}\left[F(u,v)\right] \end{split}$$