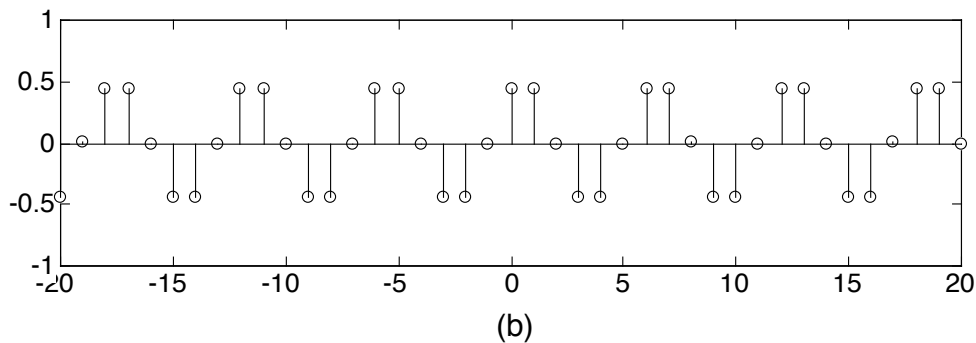
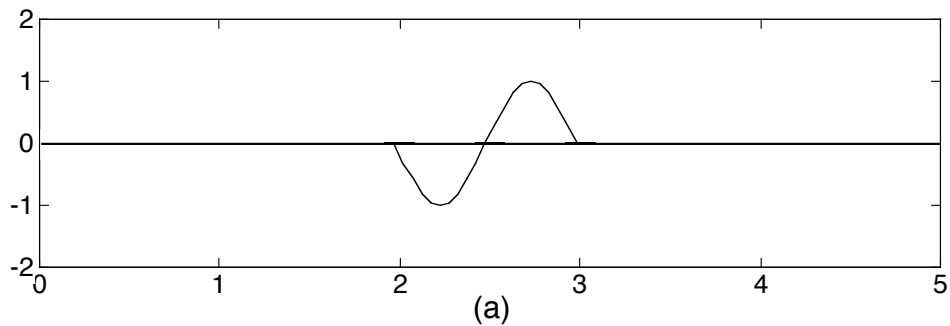


EE 438 Digital Signal Processing with Applications
Homework #1 due 8/31/2007

1. For each signal below, do the following:
 - i. Sketch $x(t)$
 - ii. State whether it is right-sided, left-sided, or two-sided.
 - iii. State whether it is causal, anti-causal, or neither.
 - iv. Calculate the metrics E_x , P_x , x_{rms} , M_x , A_x , and x_{avg} .
 - a. $x(t) = te^{-t/2}u(t)$
 - b. $x(t) = \sum_k (-1)^k \text{rect}(t / 2 - 2k)$
 - c. $x[n] = e^{(j-1)\pi n/2}$

2. Express each signal shown below in terms of standard functions. Note that the signal for part (b) is a sinusoid, and should be expressed as such.



3. For each system below, determine whether or not it is:
 - i. linear,
 - ii. time-invariant,
 - iii. causal,

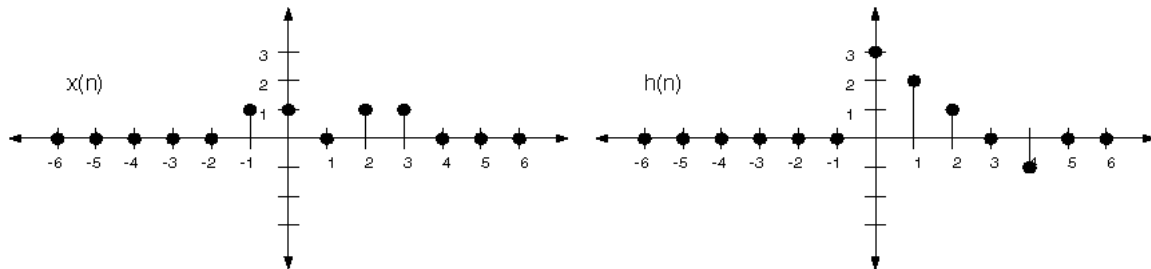
- iv. stable,
v. memoryless

For each of the above properties, if you think it holds, prove it. Otherwise, find a counter-example. In addition, find the response to an impulse.

- a) $y(t) = \int_{t-1}^t x(\tau) d\tau$
 b) $y(t) = \text{rect}(x(t))$
 c) $y[n] = x[n] + (1/2)y[n-1]$
 d) $y[n] = \begin{cases} x[n], & x[n] < |n| \\ |n|, & \text{else} \end{cases}$

4. A LTI system has input $x(n)$ and impulse response $h(n)$. Compute the output $y(n)$ for each of the following cases ($a, b < 1$).

- a) $x(n) = u(n) - u(n-4)$; $h(n) = a^n u(n)$
 b) $x(n) = a^n u(n)$; $h(n) = b^n u(n)$ ($a \neq b$)
 c) $x(n) = a^n u(n)$; $h(n) = a^n u(n)$
 d)



5. Find a general expression for the N roots $z_i, i = 0, 1, \dots, N-1$ of the following polynomial, where z and w are complex-valued: $z^N - w = 0$. *Hint:* Express both z and w in polar coordinates, and note that angles need only match within a multiple of 2π radians. Sketch the roots in the complex plane for the following values of N and w :
- a. $N = 8, w = 1$,
 b. $N = 4, w = 2$,
 c. $N = 5, w = j$,