## Some Examples of Rectification

## Control Points for UAF Campus Oblique Rectification Project










## Composite Map of Purdue University and Vicinity

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Description: The map displayed above is a representation of Purdue Univeristy and its immediate vicinity. It was created by overlaying a rectified color oblique image onto a larger monochrome reference image. The reference image used the Indiana State Plane coordinate system. The oblique image was scanned from a University postcard and then rectified to the North and East coordinates of the image in the Indiana State Plane system with the lower left of this image at 574200 North and 913450 East. A partial road network has been drawn in yellow.



## Raw HYDICE Imagery, Ft. Hood



## Orthorectified HYDICE Imagery



## Raw HYDICE Imagery, Wash. D.C.



## Orthorectified HYDICE Imagery



## Image Rectification and Orthorectification


(a) Tilted Perspective Image

(c) Differentially Rectified Image
(Orthophotograph)

## Panoramic Geometry - Manhattan \& New York City Area




Original panoramic image

Rectified image

Example of rectification where sampling rate is different in different parts of the image



## Mapping Polynomials or Rubber Sheeting



$$
\begin{aligned}
& r=a_{0}+a_{1} X+a_{2} Y+a_{3} X Y+a_{4} X^{2}+a_{5} Y^{2} \\
& c=b_{0}+b_{1} X+b_{2} Y+b_{3} X Y+b_{4} X^{2}+b_{5} Y^{2}
\end{aligned}
$$



For each point we create two equations. We need at least as many equations as unkowns. If more, then we use least squares. It is like a regression problem: linear, easy. But we are confounding the effects of sensor, platform motion, and terrain relief. What should be the order of the polynomial ?

## Graphical View of Rubber Sheet Transformation (2 ${ }^{\text {nd }}$ order, 12-parameter)

Reference grid


Transformed grid



## Physically Based Model



## Sensor parameters:

Focal length, principal point location, lens distortion, line rate, detector (pixel) size

Relate ground point and image point by equations with the above actual physical parameters, rather than the generic $a_{0}, a_{1}, a_{2}, \ldots$ parameters.

