

```
atmref3  
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alpha =  
    0.349065850398866  
alpha_r =  
    0.349063980913968  
displ_0 =  
    181985.117133101  
displ_atm_mod =  
    181984.058561991  
dalpha_r =  
    1.8694848983869e-006  
effect_m =  
    1.05857110992656  
term2 =  
    2.46734626918163e-032  
K =  
    4.67e-006  
dalpha_s =  
    1.69974099402316e-006  
effect_s_m =  
    0.962455927481642  
diary off
```

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atmref3
% atmref3.m 13-feb-11
% model atmospheric refraction with layered atmosphere
% and NASA Glenn equations that convert altitude to pressure
% then use simon newcomb's formula to convert pressure
% to refractive index n^2 = 1 + 2*C*rho
% rho = pressure kg/m^3
% C = 0.00022667, constant from schut, PERS v. 35, 1969, p. 81
% do again nadir aligned vertically per sketch
% this one hardwired for H=500 km and 20 degree off-nadir view

C=0.00022667;
degrad=180/pi;
alpha=20/degrad;
x=0;
y=6871;
R=y;
B=-pi/2 - alpha;
H=500;
for i=1:5000
    %i
    v=[cos(B);sin(B)];
    m=v(2)/v(1);
    b=y - m*x;
    % intersect next layer
    R=R-0.1;
    H=H-0.1;
    AA=1+m^2;
    BB=2*m*b;
    CC=b^2 - R^2;
    x=(-BB + sqrt(BB^2 - 4*AA*CC))/(2*AA);
    y=m*x + b;
    % unit normal vector (pointing down)
    n=[-x;-y];
    n=n/norm(n);
    costh1=dot(n,v);
    th1=acos(costh1);
    rho1=atmdens(H*1000 + 50);
    rho2=atmdens(H*1000 - 50);
    n1=sqrt(1+2*C*rho1);
    n2=sqrt(1+2*C*rho2);
    th2=asin((n1/n2)*sin(th1));
    Bnorm=atan2(n(2),n(1));
    Bnew=Bnorm - th2;
    B=Bnew;
end

alpha
alpha_r=atan(abs(x)/(6871-y))
% effect in meters on the ground
displ_0=500000*tan(alpha)
displ_atm_mod=500000*tan(alpha_r)

```

```
atmref3
dalpha_r=alpha - alpha_r
effect_m=displ_0 - displ_atm_mod

% compare with saastamoinen
K=saasta1(500,0)
dalpha_s=K*tan(alpha)
alpha_s=alpha-dalpha_s;
displ_sas=500000*tan(alpha_s);
effect_s_m=displ_0 - displ_sas
```

$$\left. \begin{array}{l} \alpha = 20^\circ \\ \alpha_r = 19.999899 \end{array} \right\} \quad \left. \begin{array}{l} da = \alpha - \alpha_r = 0.000107 \\ da = 0.000097 \end{array} \right\} \quad \begin{array}{l} \text{Saaatangonien:} \\ \text{differ by } \sim 10\% \end{array}$$

$$B = -110^\circ = -1.919862 \dots \text{ Rad}$$

$$\hat{v} = \begin{bmatrix} -1.34202 \\ -0.93969 \end{bmatrix}$$

$$m = \frac{v_y}{v_x} = 2.74747 \dots$$

$$b = 6871$$

$$y = mx + b$$

intersect with

$$x^2 + y^2 = (6870.9)^2$$

$$\underline{x^2 + m^2 x^2 + b^2 + 2mbx - 6870.9^2 = 0}$$

$$A = 1 + m^2$$

$$B = 2mb \quad \text{different } B \text{ than } \text{scarring!}$$

$$C = b^2 - 6870.9^2$$

$$x = \frac{-B + \sqrt{B^2 - 4AC}}{2A}$$

$$\left. \begin{array}{l} x = -0.036397 \dots \\ y = 6870.8999 \dots \end{array} \right\} \quad \begin{array}{l} \text{intersection with} \\ \text{circle} \end{array}$$

$$\hat{n} = [+0.036397, -6870.8999] / \text{length}$$

$$\hat{n} = \begin{bmatrix} 0.0000052 \dots \\ -0.9999999 \dots \end{bmatrix}$$

$$\cos \theta_1 = \hat{n} \cdot \vec{v}$$

$$\theta_1 = .34907 \dots \text{ Rad}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

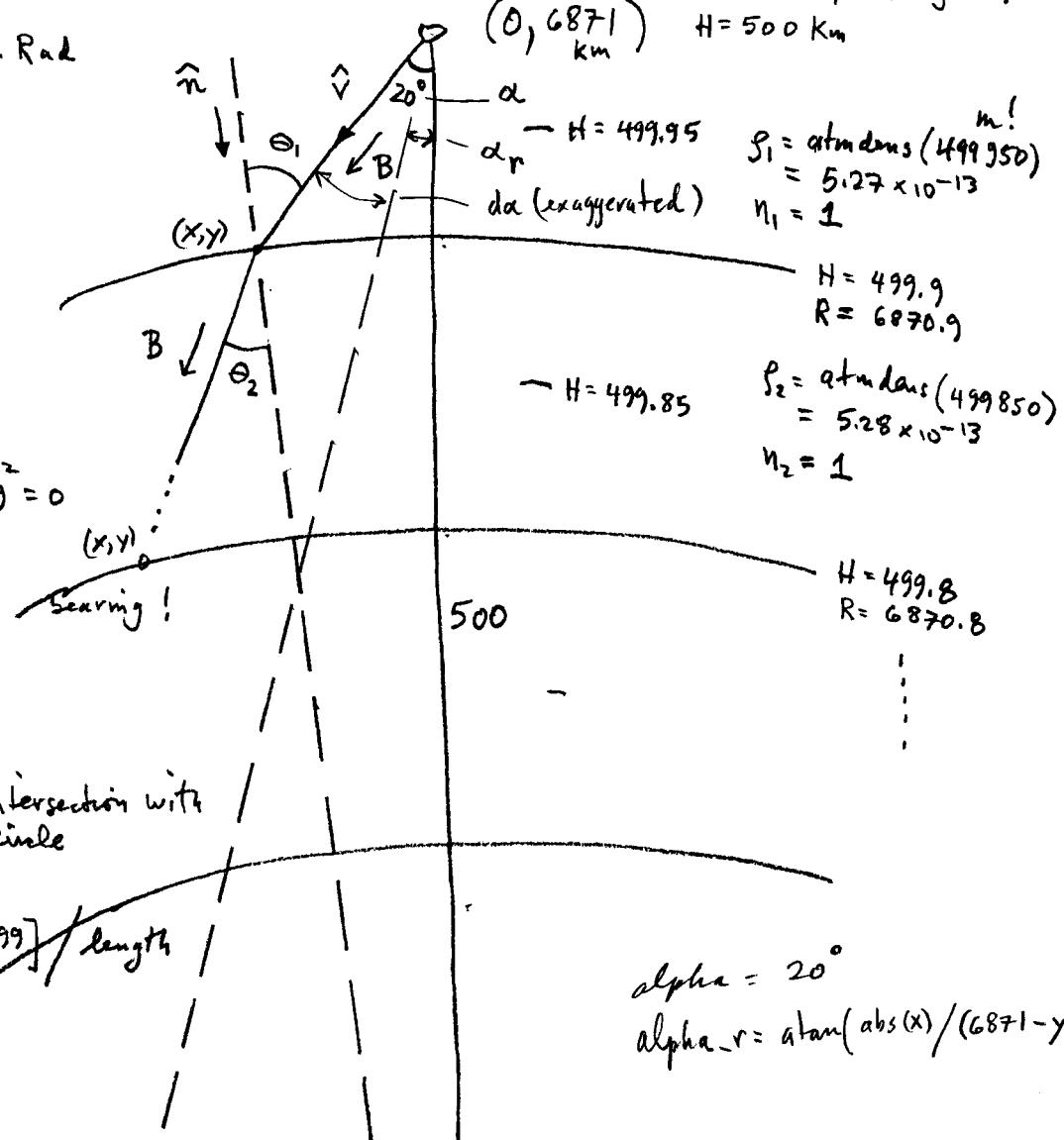
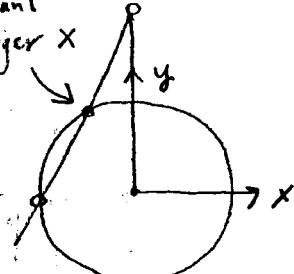
$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

$$\theta_2 = \theta_1 !$$

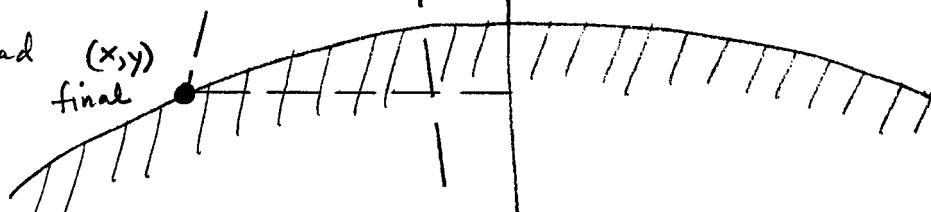
$$B_{\text{norm}} = \text{atan2}(n(2), n(0));$$

$$B_{\text{new}} = B_{\text{norm}} - \theta_2 \quad (\text{should be same as prior } B) \quad \text{want}$$

larger x



$$\begin{aligned} \alpha &= 20^\circ \\ \alpha_r &= \text{atan}(\text{abs}(x)/(6871 - y)) \end{aligned}$$



$$n^2 = 1 + 2c\rho$$

$$6371$$

$$\begin{bmatrix} 499.9 \\ 499.8 \\ \vdots \\ 0.1 \\ 0.0 \end{bmatrix}$$

$$\frac{499.9 - 0.0}{0.1} = 4999 \quad \begin{array}{l} \text{intervals} \\ \hline \end{array}$$

$4999 + 1$ positions
 \Rightarrow do loop 5000 times

