

> diary filename  
⋮  
> diary off

} captures  
screen  
dialogue

R = [ 1 2 ; 3 4 ]

[ 1 2  
3 4 ]

v = [ 5 ; 6 ]

[ 5  
6 ]

{ More  
Matlab  
hints

$$P = R + V$$

$$\begin{bmatrix} 17 \\ 39 \end{bmatrix}$$

case sensitive

P, p are different variables

save

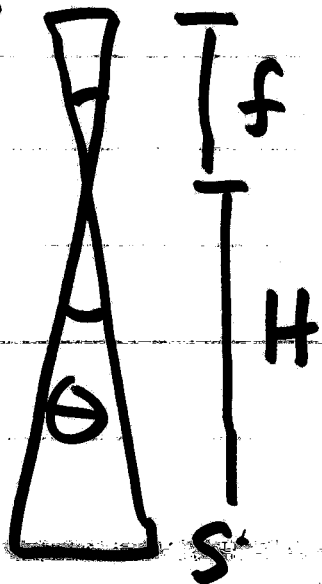
load

Resolving Power: If optics are diffraction limited, then

$$\text{Resolving power} = \beta_{\min} = \frac{1.22 \lambda}{D} = \frac{0.61 \lambda}{R_a}$$

$D$ : diameter of Aperture

$d$



Scale:

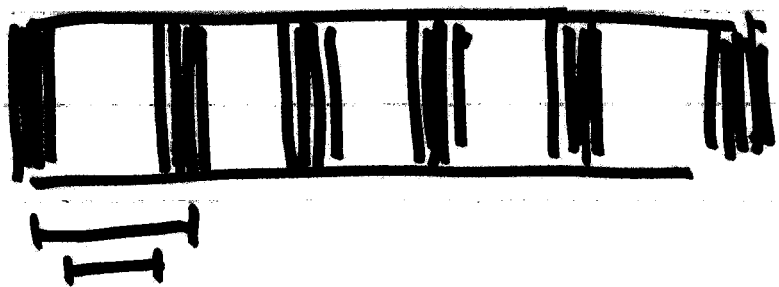
$$\frac{f}{H} = \frac{d}{s}$$

$$\theta \approx \frac{d}{f} = \frac{s}{H}$$

1. if actual angle

$\frac{d}{f} < \beta$ , then not resolving  
GSD

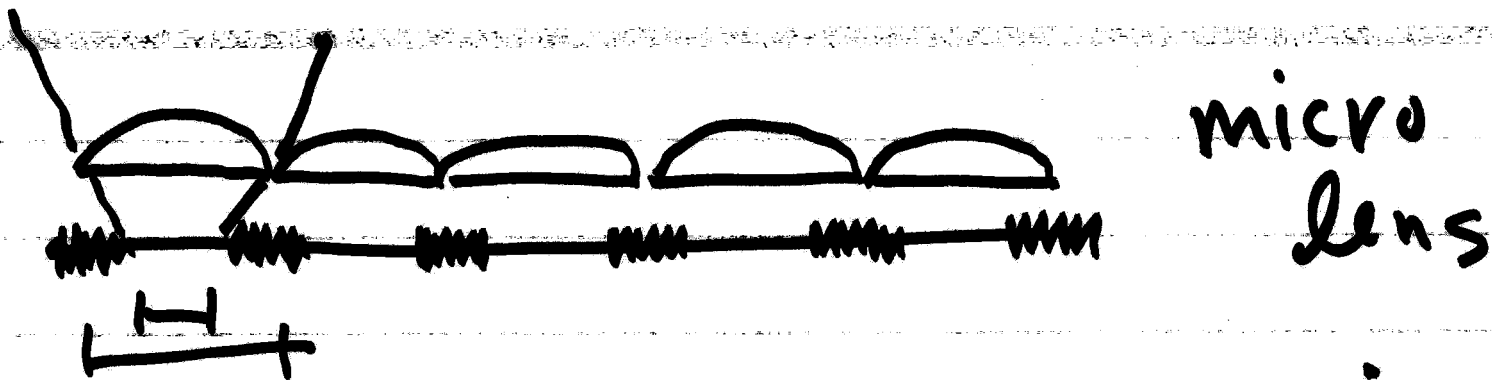
2. if  $\frac{d}{f} > \beta$ , then you may have  
to take corrective  
action



← fill factor < 100%

then you are undersampling  
the signal  $\Rightarrow$  aliasing

fix: defocus  
the optics



Dynamic Range :  $\frac{\text{full well capacity (e)}}{\text{noise (e)}}$

$$\frac{100,000}{31} = \underline{\underline{3225}}, \text{ this requires}$$

4096 levels

$$4096 = 2^{12}$$

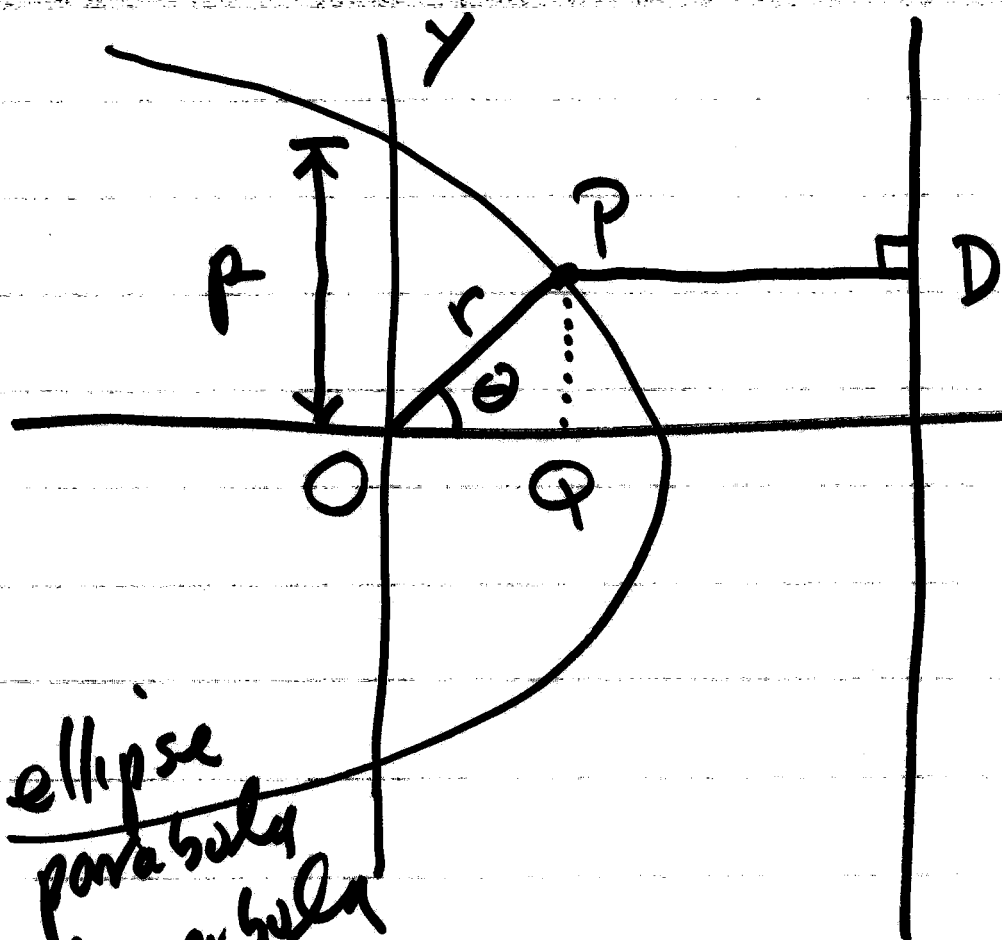
⇒ 12 bit quantization

A/D (in the analog to digital converter)

DR: in decibels dB

$$DR (dB) = 20 \cdot \log_{10} \left( \frac{100,000}{31} \right)$$

70



defn: conic

$$\overline{OP} = e \overline{PD}$$

$e = 1$  parabola

$e < 1$  ellipse

$e > 1$  hyperbola

ellipse  
parabola  
hyperbola

directrix

$$r = e (\overline{OD} - \overline{OQ})$$

$$r = e (\overline{OD} - r \cos \theta)$$

$$r = \underbrace{e \overline{OD}}_{\text{fixed constant } p} - er \cos \theta$$

$e$ : eccentricity

$p$ : semi-latus  
rectum

$$r = p - er \cos \theta$$

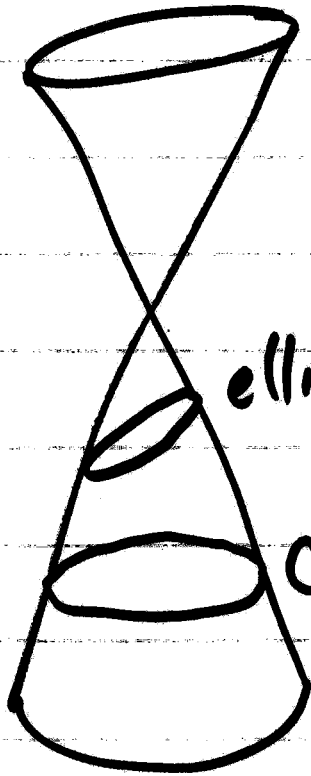
$$r + er \cos \theta = p$$

$$r(1 + e \cos \theta) = p$$

$$r = \frac{p}{1 + e \cos \theta}$$

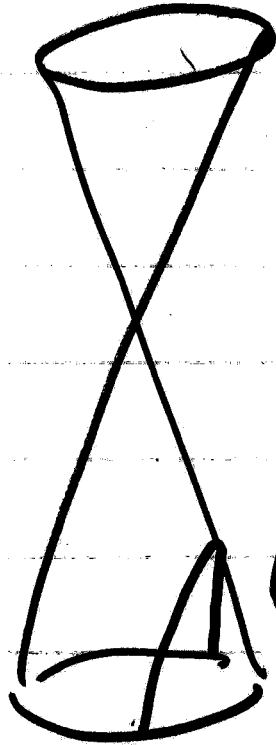
equation of conic in polar  
coordinates



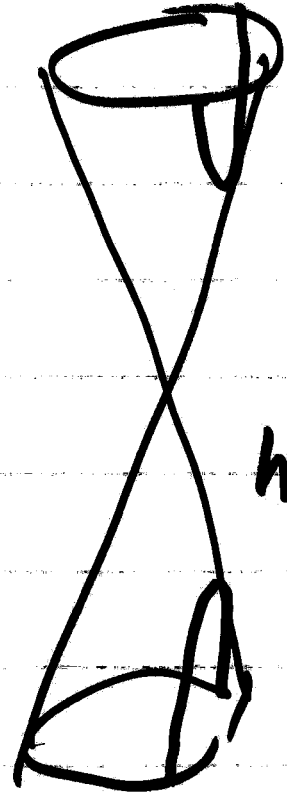


ellipse

Circle



parabola



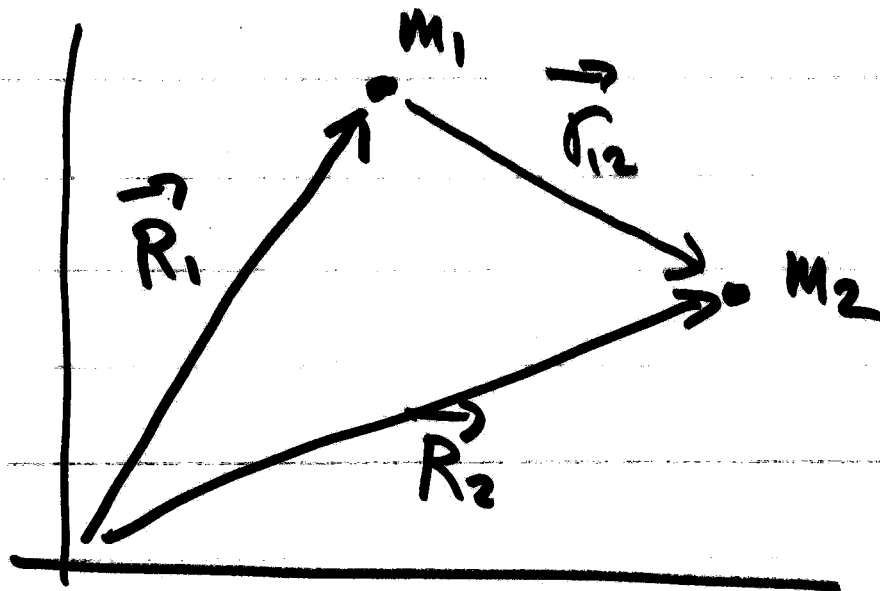
hyperbola

## obscure identities

$$\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{c})\vec{b} - (\vec{a} \cdot \vec{b})\vec{c} \quad (2)$$

$$(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = (\vec{a} \cdot \vec{c})(\vec{b} \cdot \vec{d}) - (\vec{a} \cdot \vec{d})(\vec{b} \cdot \vec{c}) \quad (3)$$

Newton's 2<sup>nd</sup> law  $\rightarrow$



inertial ref. frame

$$\vec{F} = m \vec{a} = \frac{d}{dt} (m \vec{v}) \quad \text{Newton}$$

Gravitation

$$\vec{F} = \frac{G m_1 m_2}{r^2} \left( \frac{\vec{r}}{r} \right)$$

$$\dot{\vec{q}} = \frac{d}{dt} \vec{q}$$

$$\ddot{\vec{q}} = \frac{d^2}{dt^2} \vec{q}$$

for 2-body problem

$$\vec{F}_1 = \frac{G m_1 m_2}{r_{12}^3} \vec{r}_{12} = m_1 \left( \frac{G m_2}{r_{12}^3} \vec{r}_{12} \right) = m_1 \ddot{\vec{R}}_1$$

$$\vec{F}_2 = \frac{G m_1 m_2}{r_{12}^3} \vec{r}_{21} = m_2 \left( \frac{G m_1}{r_{12}^3} \vec{r}_{21} \right) = m_2 \ddot{\vec{R}}_2$$

$$\ddot{\vec{R}}_2 - \ddot{\vec{R}}_1 = \underbrace{\frac{GM_1}{r_{12}^3} \vec{r}_{21}} - \frac{GM_2}{r_{12}^3} \vec{r}_{12}$$

$$\ddot{\vec{r}}_{12} = - \frac{GM_1}{r_{12}^3} \vec{r}_{12} - \frac{GM_2}{r_{12}^3} \vec{r}_{12}$$

$$\ddot{\vec{r}}_{12} = - \frac{G(M_1 + m_2)}{r_{12}^3} \vec{r}_{12}$$

$M_1 \gg m_2$  for earth satellite

$$G(M_1 + m_2) \approx GM_1 = \mu$$

$$\boxed{\ddot{\vec{r}} = - \frac{\mu}{r^3} \vec{r}} \quad \text{2 body equation of relative motion (12)}$$

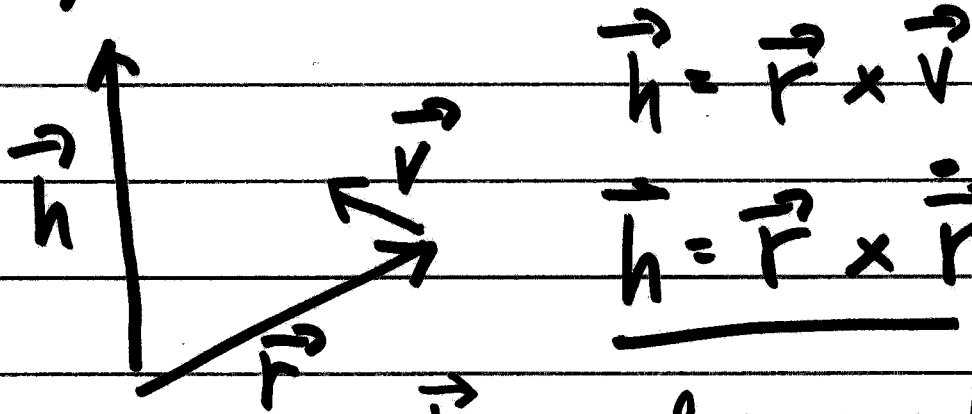
$$M_{\text{earth}} = 5.974 \times 10^{24} \text{ kg}$$

$$G = 6.67259 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$$

product  $\underline{GM} = \mu$

$$\mu = 398600.4405 \text{ km}^3 \text{ s}^{-2}$$

$$\mu = 3.986004405 \times 10^{14} \text{ m}^3 \text{ s}^{-2}$$



$\vec{h}$ : angular momentum vector

$$\frac{d}{dt} \vec{h} = \underbrace{\dot{\vec{r}} \times \dot{\vec{r}}}_{\phi} + \vec{r} \times \underbrace{\ddot{\vec{r}}}_{\wedge}$$

$$\dot{\vec{h}} = 0 - \frac{\mu}{r^3} \underbrace{\vec{r} \times \vec{r}}_{\phi}$$

$$\dot{\vec{h}} = 0, \text{ since time derivative } 0$$

$\vec{h}$  is constant

relative motion occurs in  
a plane w/  $\vec{h}$  normal

$$\frac{d}{dt} \left( \frac{\vec{r}}{r} \right) = \frac{r \dot{\vec{r}} - r \dot{r} \vec{r}}{r^2}$$

---


$$\frac{d}{dt} (\vec{r} \cdot \vec{r}) = \frac{d}{dt} (r^2)$$

$$2 \dot{\vec{r}} \cdot \vec{r} = 2 r \dot{r}$$

$$\dot{\vec{r}} \cdot \vec{r} = r \dot{r}$$

$$\dot{r} = \frac{\dot{\vec{r}} \cdot \vec{r}}{r}$$

$$\frac{d}{dt} \left( \frac{\vec{r}}{r} \right) = \frac{1}{r^3} (r^2 \dot{\vec{r}} - (\dot{\vec{r}} \cdot \vec{r}) \vec{r})$$

$$\frac{d}{dt} (\dot{\vec{r}} \times \vec{h})$$

↓

next show that this expression will be almost equal to the one at the left — only scale factor difference

$$\begin{aligned}\frac{d}{dt}(\dot{\vec{r}} \times \vec{h}) &= \ddot{\vec{r}} \times \vec{h} + \dot{\vec{r}} \times \dot{\vec{h}} \\ &= \ddot{\vec{r}} \times \vec{h} \\ &= \ddot{\vec{r}} \times (\vec{r} \times \dot{\vec{r}})\end{aligned}$$

$$= -\frac{\mu}{r^3} \vec{r} \times (\vec{r} \times \dot{\vec{r}})$$

vector identity #2

$$= -\frac{\mu}{r^3} ((\vec{r} \cdot \dot{\vec{r}})\vec{r} - r^2 \dot{\vec{r}})$$