

## Homework 7 Adj. Geodetic Obs.

assigned 19 Nov. 2018, due \_\_\_\_\_

Data is given for 20 points in 2 3D coordinate systems, related by a 3D rotation and 3 shifts (no scale parameter)

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}_{\text{(obs.)}} = M \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{\text{(const.)}} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix} \quad \sigma x, y, z = 0.1$$

1. First, verify that your 6-parameter model is working by replicating results for the "test" data set. Use conventional rotations  $M = M_k M_\phi M_w$ . use approximations  $w = 18^\circ$ ,  $\phi = 6^\circ$ ,  $k = 54^\circ$ ,  $t_x = 9$ ,  $t_y = 3$ ,  $t_z = 3$
2. Try this verified code on the "real" data set (it will fail). Use approximations  $w = 18^\circ$ ,  $\phi = 88^\circ$ ,  $k = 54^\circ$ ,  $t_x = 9$ ,  $t_y = 3$ ,  $t_z = 3$   
What do you notice about the parameter corrections ?
3. Try the LS estimation with the rotation generated from unit quaternions, with appropriate constraint equations (It should succeed). Use approximations  $q_i = -0.42$ ,  $q_j = -0.57$ ,  $q_k = -0.43$ ,  $q_s = +0.56$ .
4. For extra credit go back to the euler angle code, but change the order of the rotations from  $w-\phi-k$  to  $\phi-w-k$ . This is another "work around"
5. For more extra credit implement the quaternion approach but handle the constraint by elimination and independent parameters, rather than by dependent parameters with constraint.