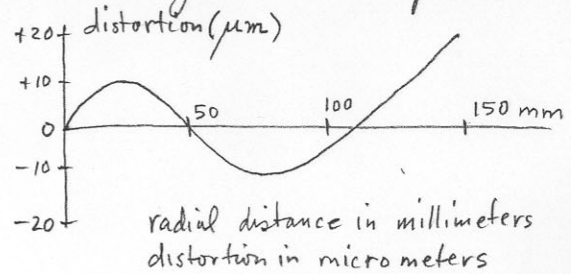
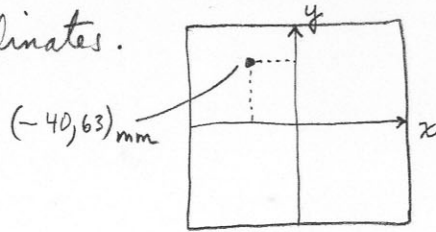


1 page of Notes allowed

1. A photograph measurement is made with  $(x, y) = (-40, 63)$  mm as shown. The lens distortion curve is also given. Compute the refined coordinates.

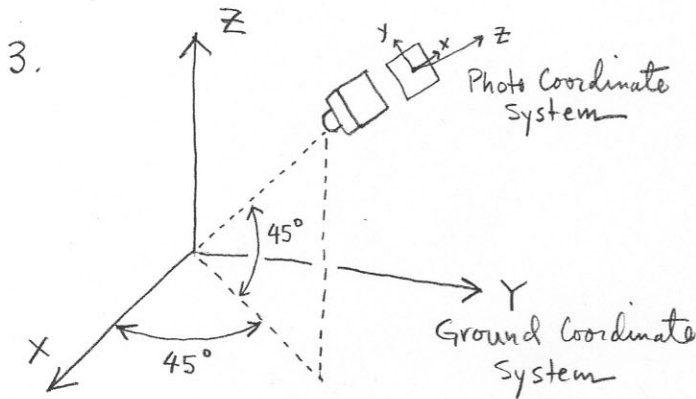


2. For the given rotation matrix, what are  $\omega, \phi, \kappa$  ?

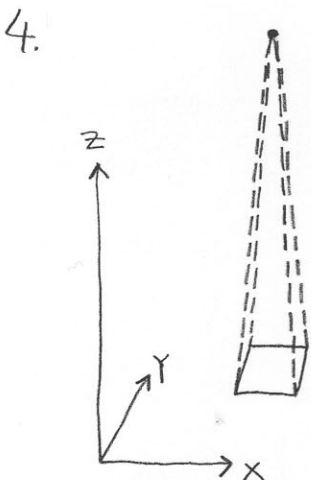
$$\begin{bmatrix} .9513 & .2432 & .1897 \\ -.2549 & .9662 & .0394 \\ -.1736 & -.0858 & .9811 \end{bmatrix}$$

$$M = \begin{bmatrix} \cos \phi \cos \kappa & \cos \phi \sin \kappa & \sin \phi \\ -\cos \phi \sin \kappa & \cos \phi \cos \kappa & \sin \phi \\ \sin \phi & \sin \phi & \cos \phi \end{bmatrix}$$

$$\begin{bmatrix} \cos \omega \sin \kappa + \sin \omega \sin \phi \cos \kappa & \sin \omega \sin \kappa - \cos \omega \sin \phi \cos \kappa \\ \cos \omega \cos \kappa - \sin \omega \sin \phi \sin \kappa & \sin \omega \cos \kappa + \cos \omega \sin \phi \sin \kappa \\ -\sin \omega \cos \phi & \cos \omega \cos \phi \end{bmatrix}$$



Give a set of sequential rotations to generate the rotation matrix for the camera in the sketch.

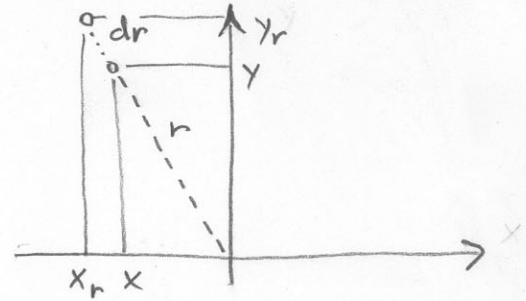


A downward looking camera has a narrow field of view as shown in the sketch. List 2 pairs of the resection parameters  $(X_L, Y_L, Z_L, \omega, \phi, \kappa)$  which are strongly coupled or correlated (that is, a small change in one looks like a small change in the other one).

1.  $(x, y) = (-40, 63) \text{ mm}$ ,  $r = 74.6 \text{ mm}$ , interpolate visually  $d = \begin{cases} -10 \mu\text{m} \\ -0.010 \text{ mm} \end{cases}$

$$\left. \begin{aligned} dx &= \frac{-40}{74.6} (-.010) = .005 \\ dy &= \frac{63}{74.6} (-.010) = -.008 \end{aligned} \right\} \text{distortion components}$$

( $1 \mu\text{m} = .001 \text{ mm}$ )



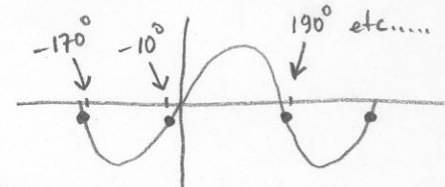
we want to make correction so we subtract

$$x_{\text{refined}} = -40 - .005 = \boxed{-40.005}$$

$$y_{\text{refined}} = 63 - (-.008) = \boxed{63.008}$$

2.  $M = \begin{bmatrix} .9513 & .2432 & .1897 \\ -.2549 & .9662 & .0394 \\ -.1736 & -.0858 & .9811 \end{bmatrix}$

$\sin \phi = m_{31} = -.1736$   
 $\Rightarrow \phi = -10^\circ, \text{ or } -170^\circ$



assume  $\phi = \boxed{-10^\circ}$

assume  $\phi = \boxed{-170^\circ}$

$$\tan k = \frac{-m_{21} / \cos \phi}{m_{11} / \cos \phi} = \frac{.258832}{.965975}$$

$$\tan k = \frac{-.258832}{-.965975}$$

$k = \boxed{15^\circ}$  +, + quadrant

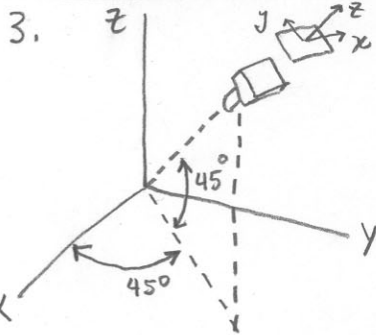
$k = \boxed{-165^\circ}$  -, - quadrant

$$\tan w = \frac{-m_{32} / \cos \phi}{m_{33} / \cos \phi} = \frac{.087123}{.996235}$$

$$\tan w = \frac{-.087123}{-.996235}$$

$w = \boxed{5^\circ}$  +, + quadrant

$w = \boxed{-175^\circ}$  -, - quadrant



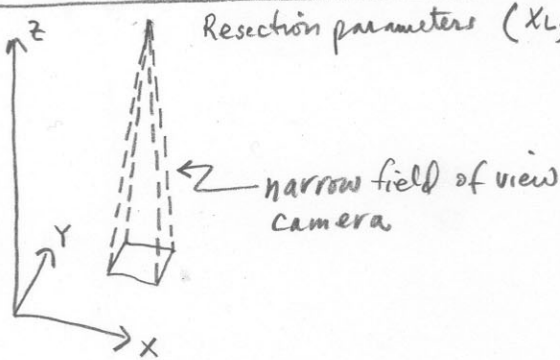
rotate ground  $\rightarrow$  image with sequential rotations

- $M_z (45^\circ + 90^\circ) = M_z (135^\circ)$
- $M_x (45^\circ)$

$$M = \begin{bmatrix} .707 & .707 & 0 \\ -.5 & -.5 & .707 \\ .5 & .5 & .707 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & .707 & .707 \\ 0 & -.707 & .707 \end{bmatrix} \begin{bmatrix} -.707 & .707 & 0 \\ -.707 & -.707 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

you could also write  $R = R_x(45^\circ) \cdot R_z(135^\circ)$

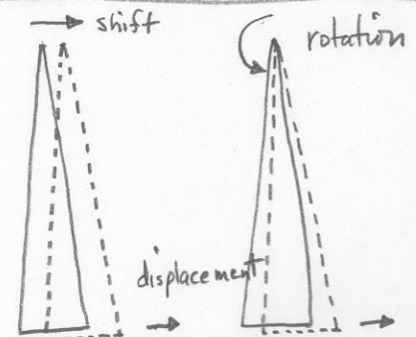
4.



Resection parameters  $(X_L, Y_L, Z_L, w, \phi, k)$

correlated pairs:

- $(X_L, \phi)$
- $(Y_L, w)$



The same displacement can be produced by either shift or rotation. Given only the image, we don't know what caused the displacement