

Solutions to Homework 3

Solution Hwk # 3 - Prob. # 1 (Text 3.2-2)

Structural Steel: C8 x 11.5

$$A_g := 3.37 \text{ in}^2 \quad d := 8 \text{ in} \quad t_w := 0.220 \text{ in} \quad b_f := 2.26 \text{ in} \quad t_f := 0.390 \text{ in}$$

$$w := 11.5 \frac{\text{lb}}{\text{ft}} \quad I_{xx} := 32.5 \text{ in}^4 \quad I_{yy} := 1.31 \text{ in}^4 \quad \text{Table 1-5, pg. 1-30}$$

Material A572 Grade 50 Yield Strength $\Rightarrow F_y := 50 \text{ Ksi}$ Ultimate Strength $\Rightarrow F_u := 65 \text{ Ksi}$

$$\text{Net Bolt dimension} \quad d_h := \left(\frac{7}{8} + \frac{1}{16} + \frac{1}{16} \right) \quad d_h = 1 \text{ in}$$

$$\text{Net Section Area} \quad A_n := A_g - 2 \cdot d_h \cdot t_w \quad A_n = 2.93 \text{ in}^2$$

$$\text{Assumed that} \quad A_e := 0.85 A_n \quad A_e = 2.49 \text{ in}^2$$

$$\text{Gross Yielding design strength} \quad F_{yd} := 0.9 F_y \cdot A_g \quad F_{yd} = 151.65 \text{ Kips}$$

$$\text{Fracture design strength} \quad F_{ud} := 0.75 F_u \cdot A_e \quad F_{ud} = 121.412 \text{ Kips}$$

$$\text{Design Strength} \quad F_d := \text{if}(F_{yd} > F_{ud}, F_{ud}, F_{yd}) \quad F_d = 121.412 \text{ Kips}$$

We know factored load combinations is greater of 1.4 DL or 1.2 DL + 1.6 LL

Given that the ratio of live load to dead load is 3, therefore, LL = 3 DL, Substituting in

$$1.2 \text{ DL} + 1.6 \text{ LL} = 6 \text{ DL}$$

$$\text{Hence,} \quad \text{DL} := \frac{F_d}{6} \quad \text{DL} = 20.235 \text{ Kips}$$

$$\text{LL} := 3 \cdot \text{DL} \quad \text{LL} = 60.706 \text{ Kips}$$

$$\text{Total Service load resisted} \quad \text{SL} := \text{DL} + \text{LL} \quad \text{SL} = 80.941 \text{ Kips}$$

Solution Hwk # 3, Prob # 2, Text Prob # 3.3-6

W 16 x 45 Grade A 992 steel (Table 3-1, pg. 3-18)

$$A_g := 13.3 \text{ in}^2 \quad A_e := 9.98 \text{ in}^2 \quad F_y := 50 \text{ Ksi} \quad F_u := 65 \text{ Ksi}$$

$$d := 16.1 \text{ in} \quad t_f := 0.565 \text{ in} \quad b_f := 7.04 \text{ in}$$

$$\text{Diameter of the bolts used} \quad d_b := \frac{7}{8} \text{ in}$$

$$\text{Nominal Yield Strength, } \phi_t P_{ny} = \quad F_{ny} := 599 \text{ Kip}$$

$$\text{Fracture Strength, } \phi_t P_{nu} = \quad F_{nu} := 487 \text{ Kip}$$

$$\text{Net Area} = \quad A_n := A_g - 4 \left(d_b + \frac{1}{8} \right) \cdot t_f \quad A_n = 11.04 \text{ in}^2$$

$$\text{From Comm. 3 of AISC codes} \quad \frac{b_f}{d} = 0.437 < 2/3 \quad \text{Therefore,} \quad U := 0.85$$

$$\text{From Table 1-8, pg. 1-46 \& 1-47,} \quad x := 1.86 \text{ in}$$

$$\text{From Figure,} \quad l := 3(3) \quad l = 9 \text{ in}$$

$$U := 1 - \frac{x}{l} \quad U = 0.793$$

$$\text{Effective Area} = \quad A_e := U \cdot A_n \quad A_e = 8.758 \text{ in}^2$$

$$\text{Fracture Strength :} \quad F_{nu} := 0.75 A_e \cdot F_u \quad F_{nu} = 426.972 \text{ Kip}$$

$$\text{Yield Strength :} \quad F_{ny} := 0.9 A_g \cdot F_y \quad F_{ny} = 598.5 \text{ Kip}$$

Therefore, design strength = 427 kips

Solution Hwk # 3, Prob. # 3 (Text - 3.3-1)

Part (a): Two Bolts on L 4 x 3 x 1/4

(1) AISC Specification

$$A_g := 1.69 \text{ in}^2 \quad A_n := A_g - \left(\frac{3}{4} + \frac{1}{8} \right) \cdot \frac{1}{4} \quad A_n = 1.471 \text{ in}^2$$

$$x := 0.725 \text{ in} \quad l := 3 \text{ in} \quad U := 1 - \frac{x}{l} \quad U = 0.758 < 0.9$$

$$A_e := U \cdot A_n \quad A_e = 1.116 \text{ in}^2$$

(2) Average value of U

$$U := 0.75 \quad A_e := A_n \cdot U \quad A_e = 1.103 \text{ in}^2$$

Part (b): Welded Connection of L 5 x 5 x 3/8 - not a special case

(1) AISC Specification

$$A_g := 5.9 \text{ in}^2 \quad A_n := A_g \quad A_n = 5.9 \text{ in}^2$$

$$x := 1.47 \text{ in} \quad l := 5 \text{ in} \quad U := 1 - \frac{x}{l} \quad U = 0.706 < 0.9$$

$$A_e := U \cdot A_n \quad A_e = 4.165 \text{ in}^2$$

(2) Average value of U

$$U := 0.75 \quad \text{0.85 is also accepted due to confusion in the AISC code. However 0.75 was clear from Lecture notes}$$

$$A_e := A_n \cdot U \quad A_e = 4.425 \text{ in}^2$$

Part (c): Flange Bolted Connection W 8 x 24

(1) AISC Specification

$$A_g := 7.08 \text{ in}^2 \quad A_n := A_g - 4 \left(\frac{7}{8} + \frac{1}{8} \right) \cdot 0.4 \quad A_n = 5.48 \text{ in}^2$$

$$\text{W8 x 24} \quad x := 0.695 \text{ in} \quad l := 9 \text{ in} \quad U := 1 - \frac{x}{l} \quad U = 0.923 > 0.9$$

$$\text{Using, } U := 0.9 \quad A_e := U \cdot A_n \quad A_e = 4.932 \text{ in}^2$$