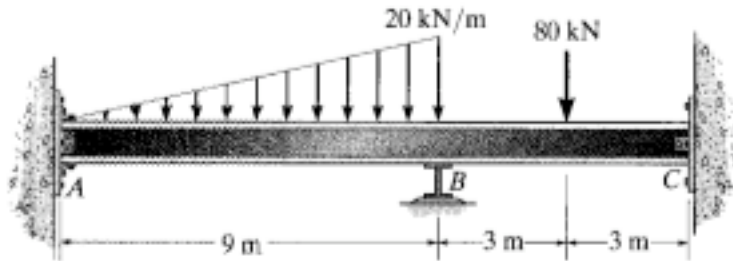


CE 371 - HOMEWORK NO. 9

Instructor: Varma, Section 1.

11-7. Determine the moments acting at *A* and *B*. Assume *A* is fixed supported, *B* is a roller, and *C* is a pin. *EI* is constant.



Prob. 11-7

Sol:

$$FEM_{AB} = wL^2/30 = -54, \quad FEM_{BC} = 3PL/16 = -90$$

$$FEM_{BA} = wL^2/20 = 81$$

(Points 2)

$$M_{AB} = 2EI(\theta_B)/9 - 54$$

$$M_{BA} = 2EI(2\theta_B)/9 + 81$$

$$M_{BC} = 3EI(\theta_B)/6 - 90$$

(Points 3)

Moment equilibrium at B

$$M_{BA} + M_{BC} = 0$$

$$4EI(\theta_B)/9 + 81 + EI(\theta_B)/2 - 90 = 0$$

$$\theta_B = 9.529/EI$$

(Points 2)

Thus,

$$M_{AB} = -51.9 \text{ kN.m}$$

Ans

(Point 1)

$$M_{BA} = 85.2 \text{ kN.m}$$

Ans

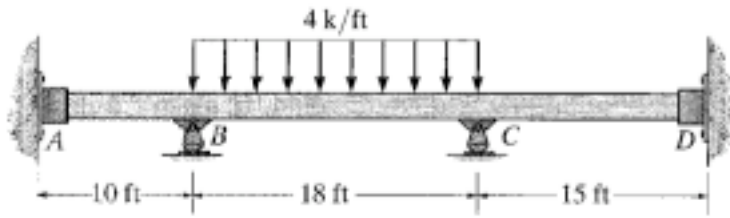
(Point 1)

$$M_{BC} = -85.2 \text{ kN.m}$$

Ans

(Point 1)

*11-8. Determine the moments at the supports, then draw the moment diagram. Assume A and D are fixed. EI is constant.



Prob. 11-8

Sol:

$$FEM_{BC} = -wL^2/12 = -108$$

$$FEM_{CB} = wL^2/12 = 108$$

$$\theta_A = \theta_C = \psi_{AB} = \psi_{BC} = \psi_{CD} = 0$$

$$M_N = 2EI(2\theta_N + \theta_F - 3\psi)/L + FEM_N$$

$$M_{AB} = 2EI(\theta_B)/10$$

$$M_{BA} = 2EI(2\theta_B)/10$$

$$M_{BC} = 2EI(2\theta_B + \theta_C)/18 - 108$$

$$M_{CB} = 2EI(2\theta_C + \theta_B)/18 + 108$$

$$M_{CD} = 2EI(2\theta_C)/15$$

$$M_{DC} = 2EI(\theta_C)/15$$

$$M_{BA} + M_{BC} = 0$$

$$M_{CB} + M_{CD} = 0$$

$$2EI(2\theta_B)/10 + 2EI(2\theta_B + \theta_C)/18 - 108 = 0$$

$$28EI\theta_B + 5EI\theta_C = 4860$$

$$2EI(2\theta_C + \theta_B)/18 + 108 + 2EI(2\theta_C)/15 = 0$$

$$22\theta_C + 5\theta_B = -4860$$

$$\theta_C = -271.37/EI$$

$$\theta_B = 222.03/EI$$

Thus,

$$M_{AB} = 44.4 \text{ k.ft} \quad \text{Ans} \quad (\text{Point 1})$$

$$M_{BA} = 88.8 \text{ k.ft} \quad \text{Ans} \quad (\text{Point 1})$$

$$M_{BC} = -88.81 \text{ k.ft} \quad \text{Ans} \quad (\text{Point 1})$$

$$M_{CB} = 72.37 \text{ k.ft} \quad \text{Ans} \quad (\text{Point 1})$$

$$M_{CD} = -72.4\text{k.ft}$$

Ans

(Point 1)

$$M_{DC} = -36.2\text{k.ft}$$

Ans

(Point 1)

Segment AB

$$\curvearrowright + \Sigma M_A = 0;$$

$$44.4 + 88.8 - V_{BL}(10) = 0$$

$$V_{BL} = 13.32\text{k}$$

$$\uparrow + F_Y = 0$$

$$A_Y = 13.322\text{k}$$

Segment BC:

$$\curvearrowright + \Sigma M_B = 0;$$

$$72.37 - V_{CL}(18) + 72(9) - 88.8 = 0$$

$$V_{CL} = 35.619\text{k}$$

$$\uparrow + \Sigma F_Y = 0$$

$$V_{BR} = 36.381\text{k}$$

Segment CD:

$$\curvearrowright + \Sigma M_C = 0$$

$$D_Y(15) - 36.18 - 72.37 = 0$$

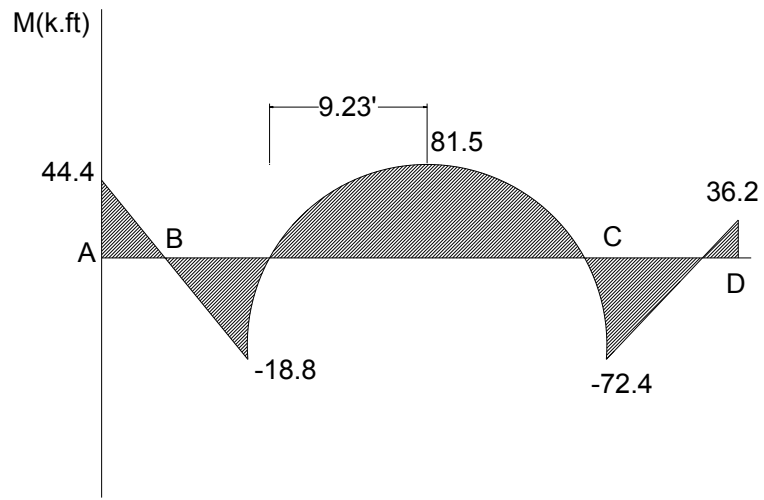
$$D_Y = 7.237\text{k}$$

$$\uparrow + \Sigma F_Y = 0; \quad V_{CR} = 7.237\text{k}$$

At B and C:

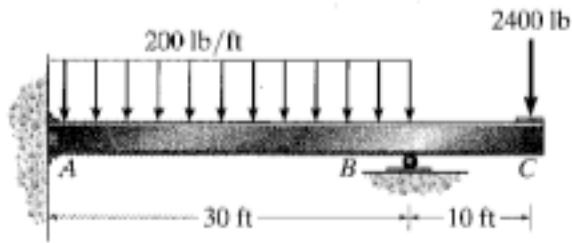
$$B_Y = 36.381 + 13.32 = 49.603\text{k}$$

$$C_Y = 35.619 + 7.237 = 42.846\text{k}$$



(Points 4)

11-10. Determine the moments at *A* and *B*, then draw the moment diagram for the beam. *EI* is constant.



Prob. 11-10

Sol:

$$FEM_{AB} = -wL^2/12 = -200(30^2)/12 = -15\text{kft}$$

$$M_{AB} = 2EI(0 + \theta_B - 0)/30 - 15$$

$$M_{BA} = 2EI(2\theta_B + 0 - 0)/30 + 15$$

$$\Sigma M_B = 0; \quad M_{BA} = 2.4(10)$$

Solving

$$\theta_B = 67.5/EI$$

$$M_{AB} = -10.5\text{k.ft}$$

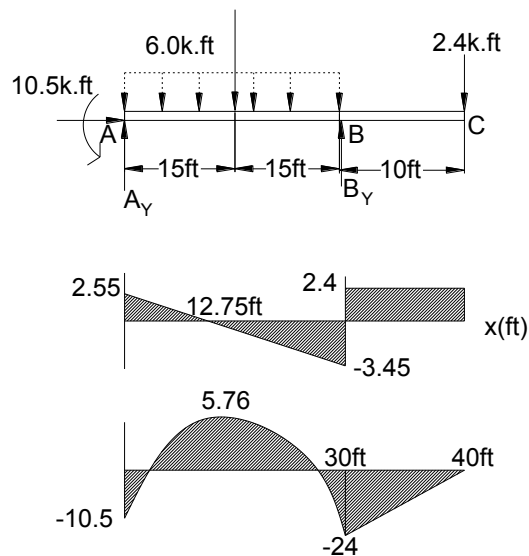
$$M_{BA} = 24\text{k.ft}$$

Ans

(Points 3)

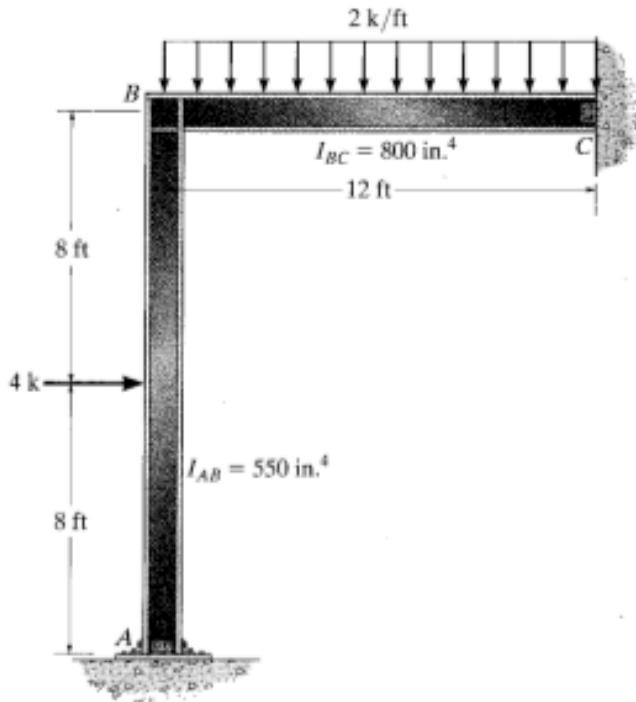
Ans

(Points 3)



(Points 4)

11-13. Determine the moments at the ends of each member of the frame. Take $E = 29(10^3)$ ksi. The moment of inertia of each member is listed in the figure. Assume the joint at B is fixed, C is pinned, and A is fixed.



Prob. 11-13

Sol:

$$FEM_{BC} = -wL^2/8 = -36$$

$$FEM_{AB} = -PL/8 = -8,$$

$$FEM_{BA} = PL/8 = 8$$

(Points 2)

$$\theta_A = \psi_{AB} = \psi_{BC} = 0$$

$$M_N = 2EI(2\theta_N + \theta_F - 3\psi)/L + FEM_N$$

$$M_{AB} = 2E(550)(2(0) + \theta_B - 3(0))/12^2(16) - 8$$

$$M_{BA} = 2E(550)(2\theta_B)/12^2(16) + 8$$

$$M_{BC} = 3E(800)(\theta_B)/12^2(12) - 36$$

Moment equilibrium at B:

$$M_{BA} + M_{BC} = 0$$

$$\theta_B = 11.9467/E$$

(Points 2)

Thus,

$$M_{AB} = -2.30\text{k.ft}$$

Ans

(Points 2)

$$M_{BA} = 19.4\text{k.ft}$$

Ans

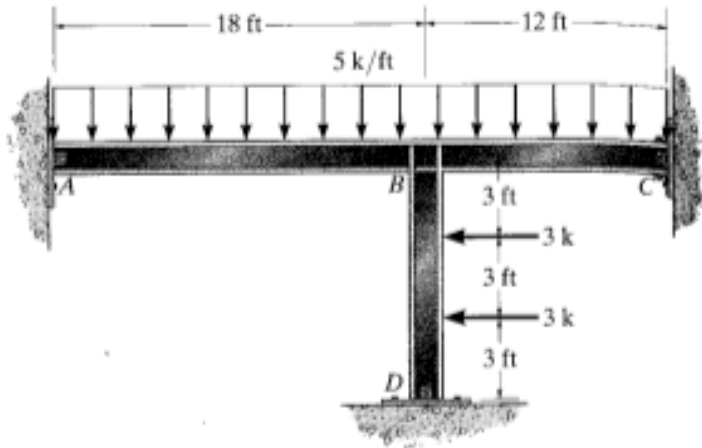
(Points 2)

$$M_{BC} = -19.4\text{k.ft}$$

Ans

(Points 2)

***11-16.** Determine the moments acting at the ends of each member. Take $E = 29(10^3)$ ksi, $I_{ABC} = 700 \text{ in}^4$, and $I_{BD} = 1100 \text{ in}^4$. Assume A and D are pin supported and C is fixed.



Prob. 11-16

Sol:

$$FEM_{BA} = wL^2/8 = 202.5$$

$$FEM_{BC} = -wL^2/12 = -60$$

$$FEM_{CB} = wL^2/12 = 60$$

$$FEM_{BD} = -PL/3 = -9$$

(Points 3)

$$\theta_C = \psi_{AB} = \psi_{BD} = \psi_{BC} = 0$$

$$M_{BA} = 3E(700)(\theta_B)/18 + 202.5$$

$$M_{BC} = 2E(700)(2\theta_B)/12 - 60$$

$$M_{CB} = 2E(700)(\theta_B)/12 + 60$$

$$M_{BD} = 3E(1100)(\theta_B)/9 - 9$$

Moment equilibrium at B:

$$M_{BA} + M_{BC} + M_{BD} = 0$$

$$\theta_B = -0.18628/E$$

(Points 3)

Thus,

$$M_{BA} = 181 \text{ k.ft}$$

Ans

(Point 1)

$$M_{BC} = -103 \text{ k.ft}$$

Ans

(Point 1)

$$M_{CB} = 38.3 \text{ k.ft}$$

Ans

(Point 1)

$$M_{BD} = -77.3 \text{ k.ft}$$

Ans

(Point 1)