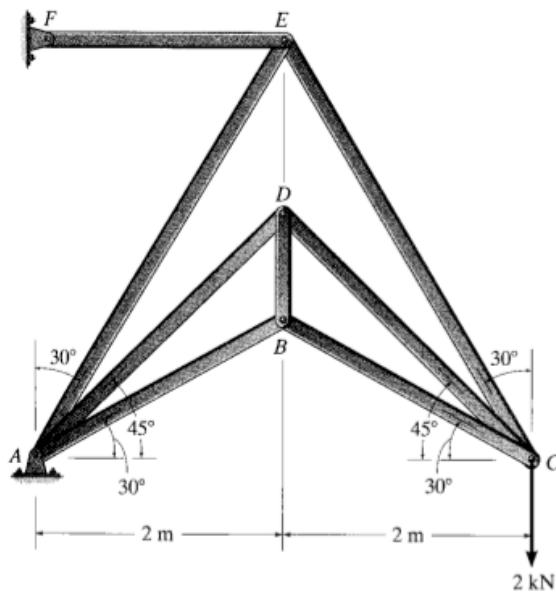


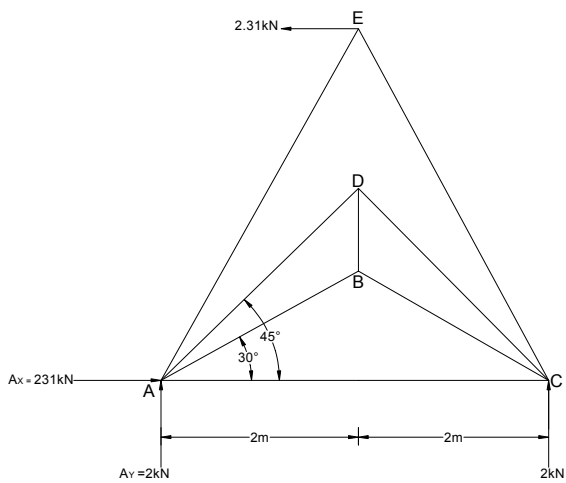
CE 371.02 – Structural Analysis I
Homework #4 Solutions

3-14. Determine the force in each member of the truss. State if the members are in tension or compression.

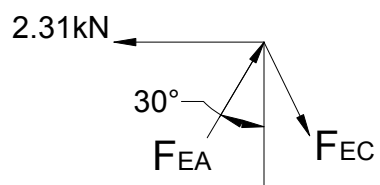


Prob. 3-14

Sol:



Joint E:

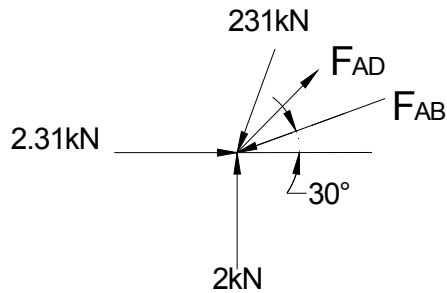


$$\begin{aligned}
 +\uparrow \Sigma F_Y = 0; & & F_{EA} &= F_{EC} \\
 +\rightarrow \Sigma F_X = 0; & & 2.31 - 2F_{EA} \sin 30^\circ &= 0 \\
 & & F_{EA} &= 2.31 \text{ kN (C)} \\
 & & F_{EC} &= 2.31 \text{ kN (T)}
 \end{aligned}$$

Ans (2 Points)

Ans (1 Point)

Joint A:

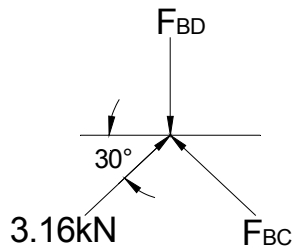


$$\begin{aligned}
 +\rightarrow \Sigma F_X = 0; & & 2.31 - 2.31 \sin 30^\circ - F_{AB} \cos 30^\circ + F_{AD} \cos 45^\circ &= 0 \\
 +\uparrow \Sigma F_Y = 0; & & 2 - 2.31 \sin 30^\circ + F_{AD} \sin 45^\circ - F_{AB} \sin 30^\circ &= 0 \\
 & & F_{AD} &= 2.24 \text{ kN (T)} \\
 & & F_{AB} &= 3.16 \text{ kN (C)}
 \end{aligned}$$

Ans (2 Points)

Ans (1 Point)

Joint B:

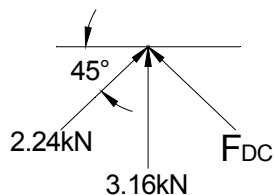


$$\begin{aligned}
 +\rightarrow \Sigma F_X = 0; & & F_{BC} &= 3.16 \text{ kN (C)} \\
 +\uparrow \Sigma F_Y = 0; & & 2(3.16) \sin 30^\circ - F_{BD} &= 0 \\
 & & F_{BD} &= 3.16 \text{ kN (C)}
 \end{aligned}$$

Ans (Point 1)

Ans (2 Points)

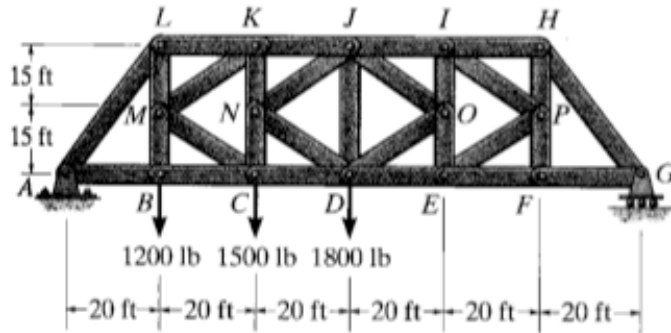
Joint D:



$$F_{DC} = 2.24 \text{ (T)}$$

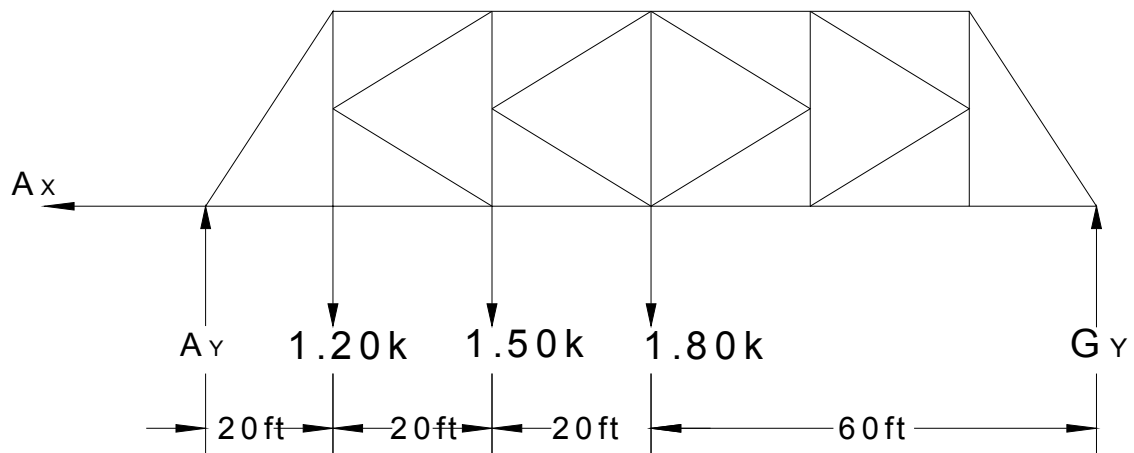
Ans (Point 1)

***3-44.** Determine the force in members KJ , NJ , ND , and CD of the K truss. Indicate if the members are in tension or compression.



Prob. 3-44

Sol:



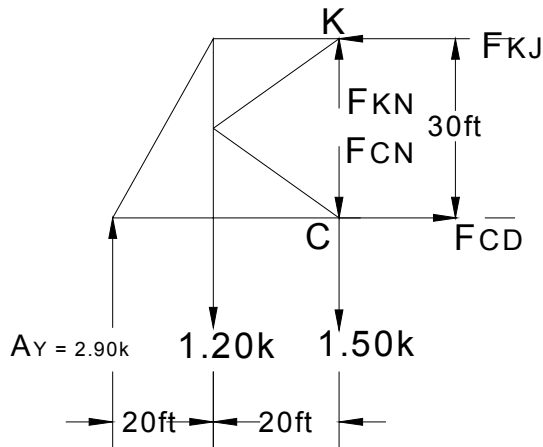
Support Reactions:

$$\curvearrowright \Sigma M_G = 0; \quad 1.20(100) + 1.50(80) + 1.80(60) - A_Y(120) = 0$$

$$A_Y = 2.90\text{k}$$

$$\rightarrow \Sigma F_X = 0; \quad A_X = 0$$

Method of Section: From section a-a₁, FKJ and FCD can be obtained directly by summing moment about points C and K respectively.



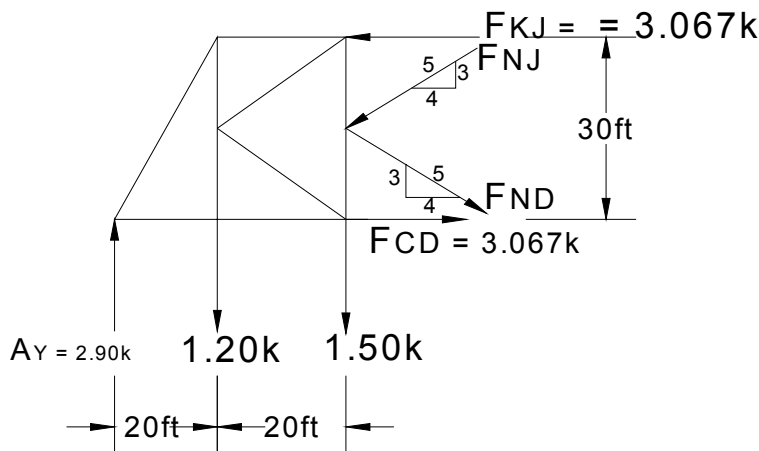
$$\begin{aligned} \curvearrowright + \Sigma M_C = 0; & \quad F_{KJ}(30) + 1.20(20) - 2.90(40) = 0 \\ & \quad F_{KJ} = 3.067k \text{ (C)} \end{aligned}$$

Ans (3 Points)

$$\begin{aligned} \curvearrowright + \Sigma M_K = 0; & \quad F_{CD}(30) + 1.20(20) - 2.90(40) = 0 \\ & \quad F_{CD} = 3.067k \text{ (T)} \end{aligned}$$

Ans (3 Points)

From sec b-b, summing forces along x and y axes yields



$$\begin{aligned} + \Sigma F_x = 0; & \quad F_{ND}(4/5) - F_{NJ}(4/5) + 3.067 - 3.067 = 0 \\ & \quad F_{ND} = F_{NJ} \end{aligned} \tag{1}$$

$$\begin{aligned} + \uparrow \Sigma F_y = 0; & \quad 2.90 - 1.20 - 1.50 - F_{ND}(3/5) - F_{NJ}(3/5) = 0 \\ & \quad F_{ND} + F_{NJ} = 0.3333 \end{aligned} \tag{2}$$

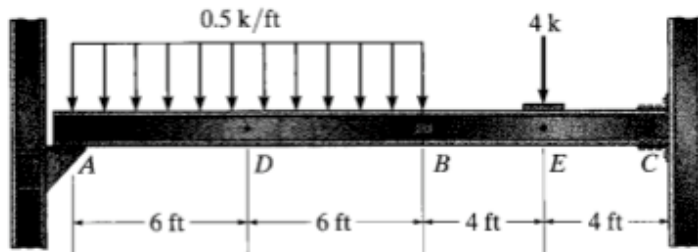
Solving (1) and (2) yields

$$F_{ND} = 0.167k \text{ (T)} \quad F_{NJ} = 0.167k \text{ (C)}$$

Ans (4 Points)

4-10. Determine the internal shear, axial load, and bending moment in the beam at points *D* and *E*. Point *E* is just to the right of the 4-k load. Assume *A* is a roller support, the splice at *B* is a pin, and *C* is a fixed support.

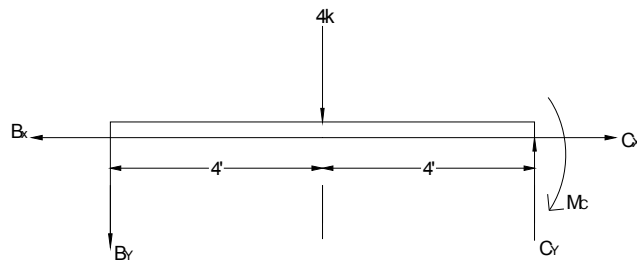
4-11. Draw the shear and moment diagrams for the beam in Prob. 4-10.



Probs. 4-10/4-11

Sol:

Reactions:



$$\rightarrow + \Sigma F_x = 0;$$

$$B_x = C_x = 0$$

$$\curvearrowright + \Sigma M_B = 0;$$

$$12A_y - 6(6) = 0; A_y = 3k$$

$$+ \uparrow \Sigma F_y = 0;$$

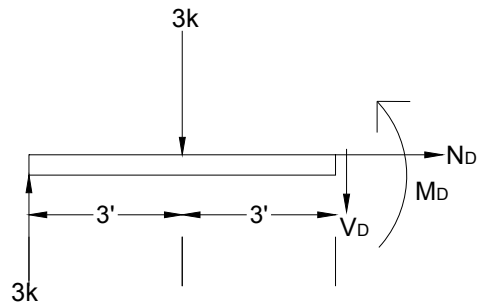
$$3 - 6 + B_y = 0; B_y = 3k$$

$$-3 - 4 + C_y = 0; C_y = 7k$$

$$\curvearrowright + \Sigma M_C = 0;$$

$$-3(8) - 4(4) + M_C = 0; M_C = 40k.ft$$

For D:



$$+\Sigma F_X = 0;$$

$$N_D = 0$$

Ans (Point 1)



$$+\uparrow \Sigma F_Y = 0;$$

$$3 - 3 - V_D = 0;$$

$$V_D = 0$$

Ans (2 Points)

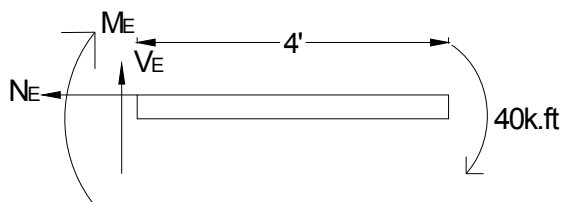
$$\curvearrowright + \Sigma M_D = 0;$$

$$3(6) - 3(3) - M_D = 0$$

$$M_D = 9\text{k.ft}$$

Ans (2 Points)

For E:



$$\rightarrow +\Sigma F_X = 0;$$

$$N_E = 0$$

Ans (Point 1)

$$+\uparrow \Sigma F_Y = 0;$$

$$V_E + 7 = 0;$$

$$V_E = -7\text{k}$$

Ans (2 Points)

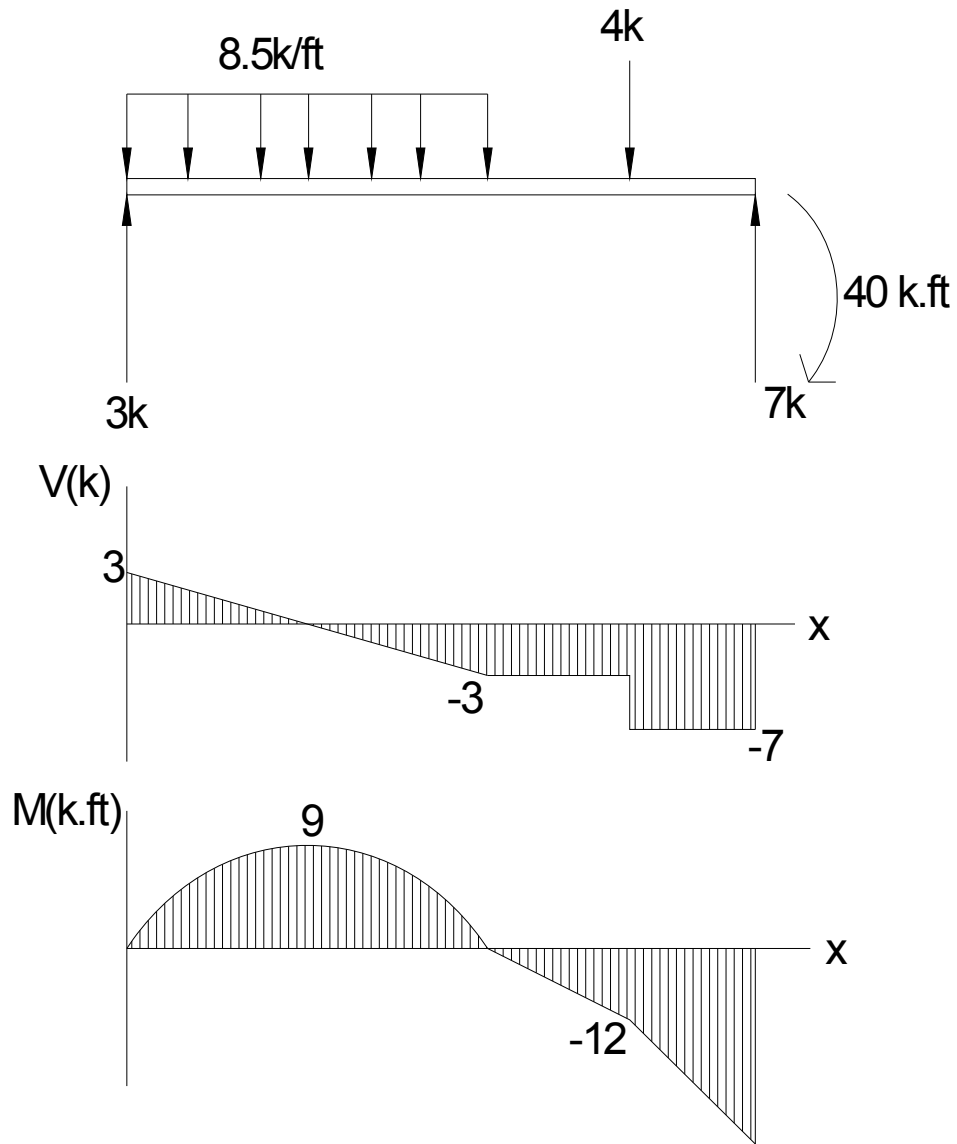
$$\curvearrowright + \Sigma M_E = 0;$$

$$M_E - 7(4) + 40 = 0; M_E = -12\text{k.ft}$$

Ans (2 Points)

4 - 11:

Sol:
Shear Force and Bending Moment Diagram:



(Shear Force Diagram - 5 Points)
(B.M. Diagram - 5 Points)