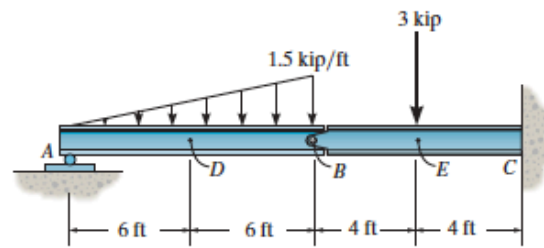


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•1–5. Determine the resultant internal loadings in the beam at cross sections through points *D* and *E*. Point *E* is just to the right of the 3-kip load.



Support Reactions: For member *AB*

$$\zeta + \Sigma M_B = 0; \quad 9.00(4) - A_y(12) = 0 \quad A_y = 3.00 \text{ kip}$$

$$\rightarrow \Sigma F_x = 0; \quad B_x = 0$$

$$+\uparrow \Sigma F_y = 0; \quad B_y + 3.00 - 9.00 = 0 \quad B_y = 6.00 \text{ kip}$$

Equations of Equilibrium: For point *D*

$$\rightarrow \Sigma F_x = 0; \quad N_D = 0 \quad \text{Ans.}$$

$$+\uparrow \Sigma F_y = 0; \quad 3.00 - 2.25 - V_D = 0$$

$$V_D = 0.750 \text{ kip} \quad \text{Ans.}$$

$$\zeta + \Sigma M_D = 0; \quad M_D + 2.25(2) - 3.00(6) = 0$$

$$M_D = 13.5 \text{ kip} \cdot \text{ft} \quad \text{Ans.}$$

Equations of Equilibrium: For point *E*

$$\rightarrow \Sigma F_x = 0; \quad N_E = 0 \quad \text{Ans.}$$

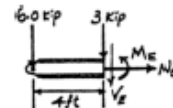
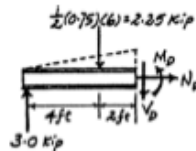
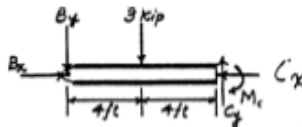
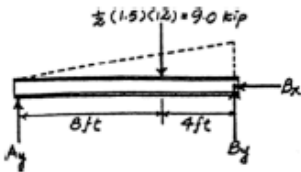
$$+\uparrow \Sigma F_y = 0; \quad -6.00 - 3 - V_E = 0$$

$$V_E = -9.00 \text{ kip} \quad \text{Ans.}$$

$$\zeta + \Sigma M_E = 0; \quad M_E + 6.00(4) = 0$$

$$M_E = -24.0 \text{ kip} \cdot \text{ft} \quad \text{Ans.}$$

Negative signs indicate that M_E and V_E act in the opposite direction to that shown on FBD.



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1-7. The cable will fail when subjected to a tension of 2 kN. Determine the largest vertical load P the frame will support and calculate the internal normal force, shear force, and moment at the cross section through point C for this loading.

Support Reactions:

$$\zeta + \sum M_A = 0; \quad P(2.25) - 2(0.6) = 0$$

$$P = 0.5333 \text{ kN} = 0.533 \text{ kN}$$

$$\rightarrow \sum F_x = 0; \quad 2 - A_x = 0 \quad A_x = 2.00 \text{ kN}$$

$$+\uparrow \sum F_y = 0; \quad A_y - 0.5333 = 0 \quad A_y = 0.5333 \text{ kN}$$

Equations of Equilibrium: For point C

$$\rightarrow \sum F_x = 0; \quad -N_C - 2.00 = 0$$

$$N_C = -2.00 \text{ kN}$$

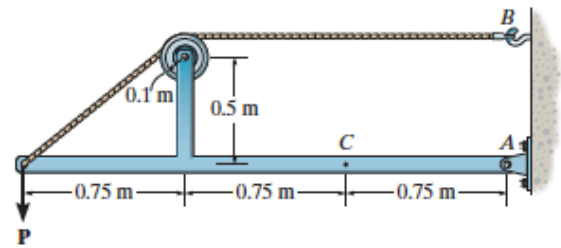
$$+\uparrow \sum F_y = 0; \quad V_C + 0.5333 = 0$$

$$V_C = -0.533 \text{ kN}$$

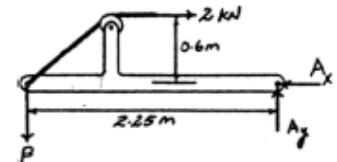
$$\zeta + \sum M_C = 0; \quad 0.5333(0.75) - M_C = 0$$

$$M_C = 0.400 \text{ kN} \cdot \text{m}$$

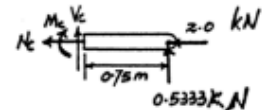
Negative signs indicate that N_C and V_C act in the opposite direction to that shown on FBD.



Ans.



Ans.



Ans.

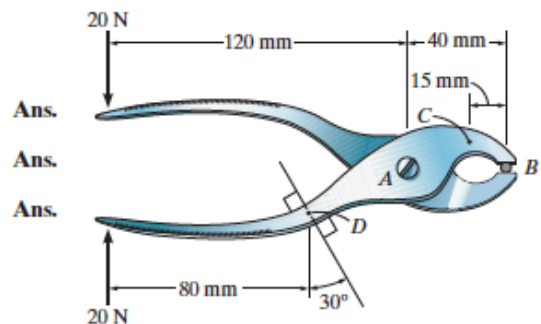
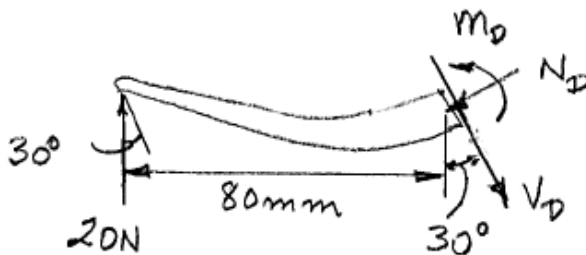
Ans.

*1-16. Determine the resultant internal loading on the cross section through point D of the pliers.

$$+\uparrow \sum F_y = 0; \quad V_D - 20 \cos 30^\circ = 0; \quad V_D = 17.3 \text{ N}$$

$$+\leftarrow \sum F_x = 0; \quad N_D - 20 \sin 30^\circ = 0; \quad N_D = 10 \text{ N}$$

$$+\curvearrowright \sum M_D = 0; \quad M_D - 20(0.08) = 0; \quad M_D = 1.60 \text{ N} \cdot \text{m}$$



Ans.

Ans.

Ans.

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•1-17. Determine resultant internal loadings acting on section $a-a$ and section $b-b$. Each section passes through the centerline at point C .

Referring to the FBD of the entire beam, Fig. a ,

$$\zeta + \Sigma M_A = 0; \quad N_B \sin 45^\circ (6) - 5(4.5) = 0 \quad N_B = 5.303 \text{ kN}$$

Referring to the FBD of this segment (section $a-a$), Fig. b ,

$$+\swarrow \Sigma F_x = 0; \quad N_{a-a} + 5.303 \cos 45^\circ = 0 \quad N_{a-a} = -3.75 \text{ kN}$$

Ans.

$$+\nearrow \Sigma F_y = 0; \quad V_{a-a} + 5.303 \sin 45^\circ - 5 = 0 \quad V_{a-a} = 1.25 \text{ kN}$$

Ans.

$$\zeta + \Sigma M_C = 0; \quad 5.303 \sin 45^\circ (3) - 5(1.5) - M_{a-a} = 0 \quad M_{a-a} = 3.75 \text{ kN} \cdot \text{m}$$

Ans.

Referring to the FBD (section $b-b$) in Fig. c ,

$$\leftarrow \Sigma F_x = 0; \quad N_{b-b} - 5 \cos 45^\circ + 5.303 = 0 \quad N_{b-b} = -1.768 \text{ kN}$$

$$= -1.77 \text{ kN}$$

Ans.

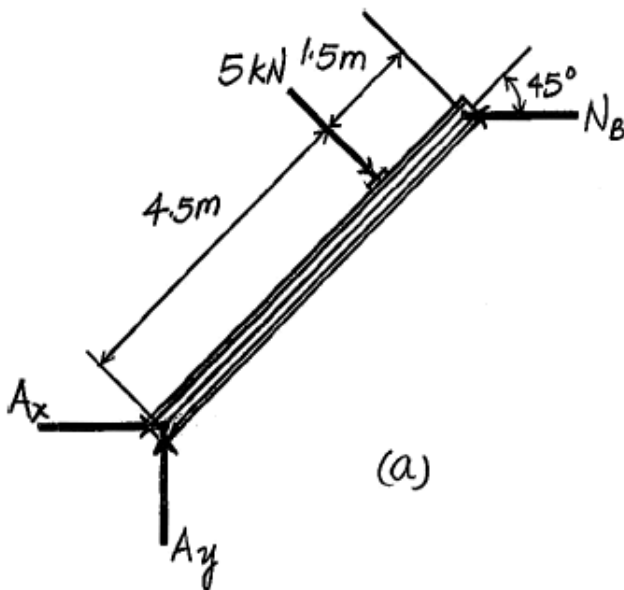
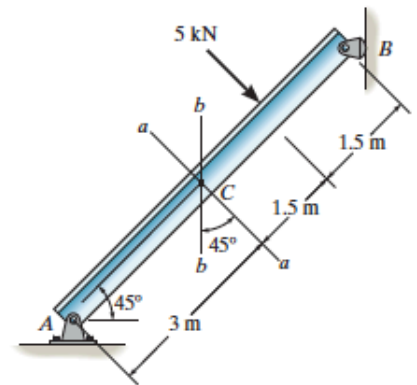
$$+\uparrow \Sigma F_y = 0; \quad V_{b-b} - 5 \sin 45^\circ = 0 \quad V_{b-b} = 3.536 \text{ kN} = 3.54 \text{ kN}$$

Ans.

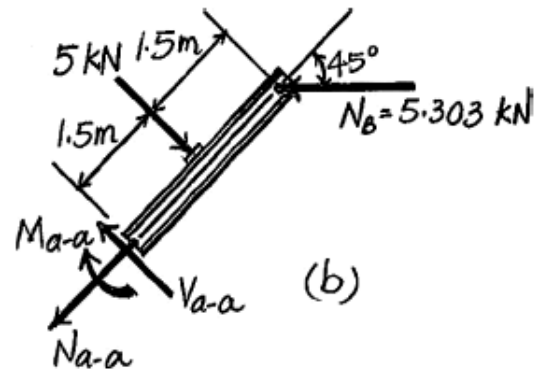
$$\zeta + \Sigma M_C = 0; \quad 5.303 \sin 45^\circ (3) - 5(1.5) - M_{b-b} = 0$$

$$M_{b-b} = 3.75 \text{ kN} \cdot \text{m}$$

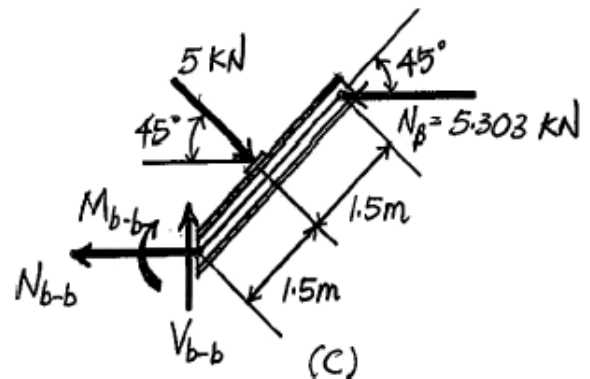
Ans.



(a)



(b)



(c)

(For fundamental problem solutions please see the back of your course textbook)