

# ECE 255, MOSFET Amplifiers

26 October 2017

In this lecture, the basic configurations of MOSFET amplifiers will be studied similar to that of BJT. Previously, it has been shown that with the transistor DC biased at the appropriate point (Q point or operating point), linear relations can be derived between the small voltage signal and current signal. We will continue this analysis with MOSFETs, starting with the common-source amplifier.

## 1 Common-Source (CS) Amplifier

The common-source (CS) amplifier for MOSFET is the analogue of the common-emitter amplifier for BJT. Its popularity arises from its high gain, and that by cascading a number of them, larger amplification of the signal can be achieved.

### 1.1 Characteristic Parameters of the CS Amplifier

Figure 1(a) shows the small-signal model for the common-source amplifier. Here,  $R_D$  is considered part of the amplifier and is the resistance that one measures between the drain and the ground. The small-signal model can be replaced by its hybrid- $\pi$  model as shown in Figure 1(b). Then the current induced in the output port is  $i = -g_m v_{gs}$  as indicated by the current source. Thus

$$v_o = -g_m v_{gs} R_D \quad (1.1)$$

By inspection, one sees that

$$R_{in} = \infty, \quad v_i = v_{sig}, \quad v_{gs} = v_i \quad (1.2)$$

Thus the open-circuit voltage gain is

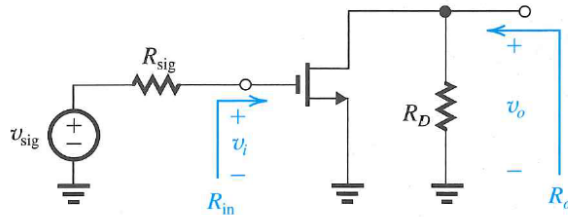
$$A_{vo} = \frac{v_o}{v_i} = -g_m R_D \quad (1.3)$$

One can replace a linear circuit driven by a source by its Thévenin equivalence. Then from the equivalent-circuit model in Figure 1(b) and the test-current method by setting  $v_i = 0$ , the output resistance, which is the Thévenin resistor is

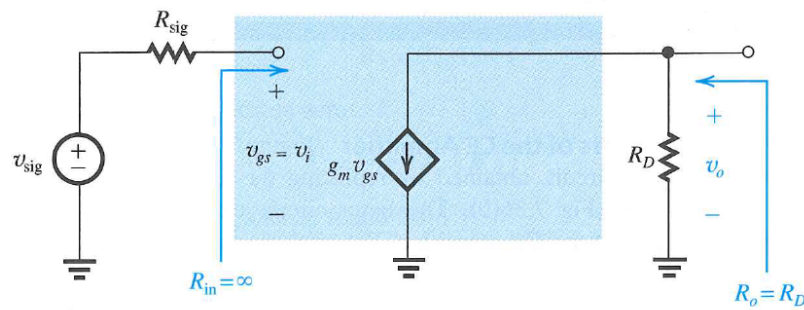
$$R_o = R_D \quad (1.4)$$

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(a)



(b)

Figure 1: (a) Small-signal model for a common-source amplifier. (b) The hybrid- $\pi$  model for the common-source amplifier (Courtesy of Sedra and Smith).

If now, a load resistor,  $R_L$  is connected to the output across  $R_D$ , then the voltage gain proper (also called terminal voltage gain), by the voltage divider formula, is

$$A_v = A_{vo} \frac{R_L}{R_L + R_o} = -g_m \frac{R_D R_L}{R_L + R_D} = -g_m (R_D \parallel R_L) \quad (1.5)$$

From the fact that  $R_{in} = \infty$ , then  $v_i = v_{sig}$ . The overall voltage gain,  $G_v$ , is the same as the voltage gain proper,  $A_v$ , namely

$$G_v = \frac{v_o}{v_{sig}} = -g_m (R_D \parallel R_L) \quad (1.6)$$

## 1.2 Final Remarks on CS Amplifier

1. The CS amplifiers has infinite input impedance (draws no current at DC), and a moderately high output resistance (easier to match), and a high voltage gain (a desirable feature of an amplifier).

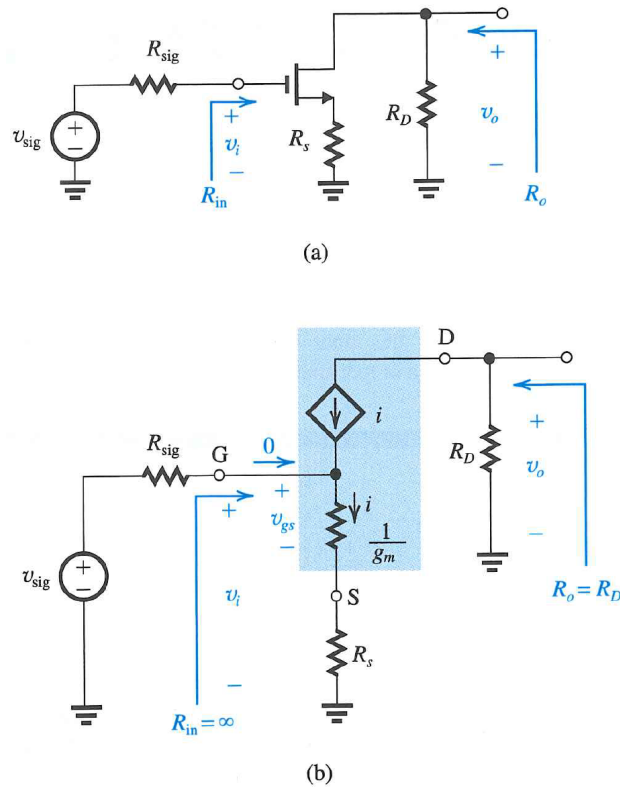


Figure 2: A CS amplifier with a source resistance: (top) detail circuit, (bottom) equivalent circuit T model (Courtesy of Sedra and Smith).

2. Reducing  $R_D$  reduces the output resistance of a CS amplifier, but unfortunately, the voltage gain is also reduced. Alternate design can be employed to reduce the output resistance (to be discussed later).
3. A CS amplifier suffers from poor high frequency performance, as most transistor amplifiers do.

## 2 Common-Source Amplifier with a Source Resistance

As shown in Figure 2, a T model is used for the equivalent circuit for simplicity. It is seen that the input resistance of the circuit is infinite because no gate current flows. As a consequence,  $v_i = v_{sig}$ . However, because of the existence of the source resistance, less of the input voltage is divided to  $v_{gs}$ , by the voltage-

divider formula. Thus

$$v_{gs} = v_i \frac{1/g_m}{1/g_m + R_s} = \frac{v_i}{1 + g_m R_s} \quad (2.1)$$

It is seen that  $R_s$  can be used to make  $v_{gs}$  small so that there is less nonlinear distortion as the small-signal approximations will become better. The output voltage is generated by the controlled current source yielding

$$v_o = -iR_D \quad (2.2)$$

The current  $i$  can be found by

$$i = \frac{v_i}{1/g_m + R_s} = \frac{g_m}{1 + g_m R_s} v_i \quad (2.3)$$

Thus the open-circuit voltage gain (assume that  $R_D$  is part of the amplifier) is

$$A_{vo} = \frac{v_o}{v_i} = -\frac{g_m R_D}{1 + g_m R_s} = -\frac{R_D}{1/g_m + R_s} \quad (2.4)$$

The above shows that including the source resistance reduces the amplifier gain by a factor of  $1 + g_m R_s$ , but linearity and bandwidth performance (to be shown later) will improve. This is called negative feedback because when the input voltage  $v_i$  or  $v_{gs}$  attempts to increase, the voltage drop across  $R_s$  increases reducing  $v_{gs}$ . The source resistance is also called **source-degeneration resistance**.

Since this is a linear circuit, the Thévenin equivalence of the amplifier looking in from the right can be easily found. The open-circuit voltage allows us to easily find the equivalent Thévenin voltage source. The equivalent Thévenin resistor is  $R_o$  which is just  $R_D$  in this case.

When a load resistor  $R_L$  is added, then the voltage gain proper (also called terminal voltage gain)

$$A_v = -\frac{g_m(R_D \parallel R_L)}{1 + g_m R_s} = -\frac{R_D \parallel R_L}{1/g_m + R_s} \quad (2.5)$$

Because the input resistance is infinite, hence  $v_i = v_{\text{sig}}$  and the overall voltage gain  $G_v = A_v$ .

## 2.1 Summary of the CS Amplifier with Source Resistance

1. The input resistance  $R_{\text{in}}$  is infinite.
2. The open-circuit voltage gain,  $A_{vo}$ , is reduced by a factor of  $1 + g_m R_s$  as seen in (2.4).
3. For the same nonlinear distortion, the input signal can be increased by a factor of  $1 + g_m R_s$  compared to without  $R_s$ .
4. As shall be shown later, the high-frequency response of this design is improved.

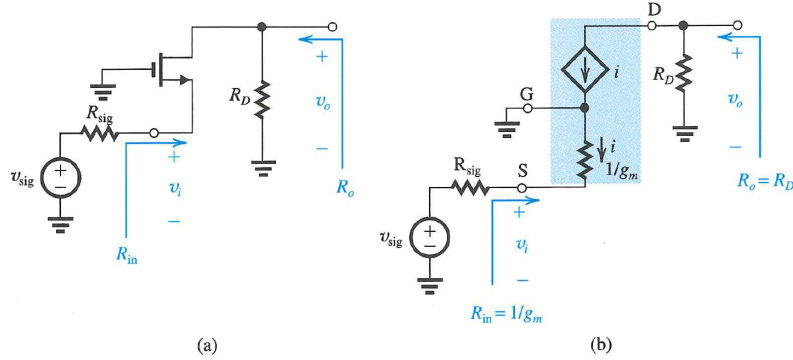


Figure 3: (a) Small-signal model for a common-gate amplifier. (b) The T model equivalent circuit for the common-gate amplifier. Note that the gate current is always zero in the T model (Courtesy of Sedra and Smith).

In general, the addition of the source resistance  $R_s$  gives rise to a “negative” feedback factor  $1 + g_m R_s$  that reduces voltage gain, but improves linearity, and high-frequency response. Because of the negative-feedback action of  $R_s$ , it is also called the **source-degenerate resistance**.

### 3 Common-Gate (CG) Amplifier

The small-signal and a T-model equivalent-circuit common-gate (CG) amplifier is shown in Figure 3. By inspection, the input resistance  $R_{in}$  is given by

$$R_{in} = \frac{1}{g_m} \quad (3.1)$$

which is typically a few hundred ohms, a low input impedance. The output voltage is

$$v_o = -iR_D, \text{ where } i = -\frac{v_i}{1/g_m} = -g_m v_i \quad (3.2)$$

Hence the open-circuit voltage gain is

$$A_{vo} = \frac{v_o}{v_i} = g_m R_D \quad (3.3)$$

which is similar to that of the CS amplifier save for a sign change. The output resistance (or the Thévenin equivalent resistor) of the circuit is

$$R_o = R_D \quad (3.4)$$

The smaller input impedance is deleterious to the amplifier gain, as by the voltage divider formula, one gets

$$\frac{v_i}{v_{sig}} = \frac{R_{in}}{R_{in} + R_{sig}} = \frac{1/g_m}{1/g_m + R_{sig}} \quad (3.5)$$

meaning that the  $v_i$  is attenuated compared to  $v_{\text{sig}}$ , since  $R_{\text{sig}}$  is typically larger than  $1/g_m$ .

When a load resistor  $R_L$  is connected to the output, the voltage gain proper (terminal voltage gain) is then

$$A_v = g_m R_D \parallel R_L \quad (3.6)$$

Thus the overall voltage gain is

$$G_v = \frac{1/g_m}{R_{\text{sig}} + 1/g_m} g_m (R_D \parallel R_L) = \frac{R_D \parallel R_L}{R_{\text{sig}} + 1/g_m} \quad (3.7)$$

As the input impedance is low, it is good for matching sources with a low input impedance due to the maximum power theorem, but it draws more current, implying high power consumption from the signal source.

## 4 The Source Follower

This is similar to the emitter follower for the BJT, which is used as a voltage buffer. It is a unit-gain amplifier with a very large input impedance but a smaller output impedance. Therefore it is good for matching a high-impedance circuit to a low-impedance circuit.

### 4.1 Characteristics of a Source Follower

Figure 4 shows the small-signal circuit and a T-model equivalent circuit diagram for a source follower. The input source is represented by a Thévenin equivalent voltage  $v_{\text{sig}}$  and resistor  $R_{\text{sig}}$ . A load resistor is connected to the output between the source and ground.

Since the gate current is zero for this circuit,

$$R_{\text{in}} = \infty \quad (4.1)$$

Using the voltage divider formula, it is seen that voltage gain proper or terminal voltage gain is

$$A_v = \frac{v_o}{v_i} = \frac{R_L}{R_L + 1/g_m} \quad (4.2)$$

For the open-circuit voltage gain,  $R_L = \infty$  and

$$A_{v_o} = 1 \quad (4.3)$$

The output resistance is obtained by replacing the proper part of the amplifier with a Thévenin equivalence. To this end, with the use of the test-current method, the value of  $v_i = 0$ , and thus

$$R_o = 1/g_m \quad (4.4)$$

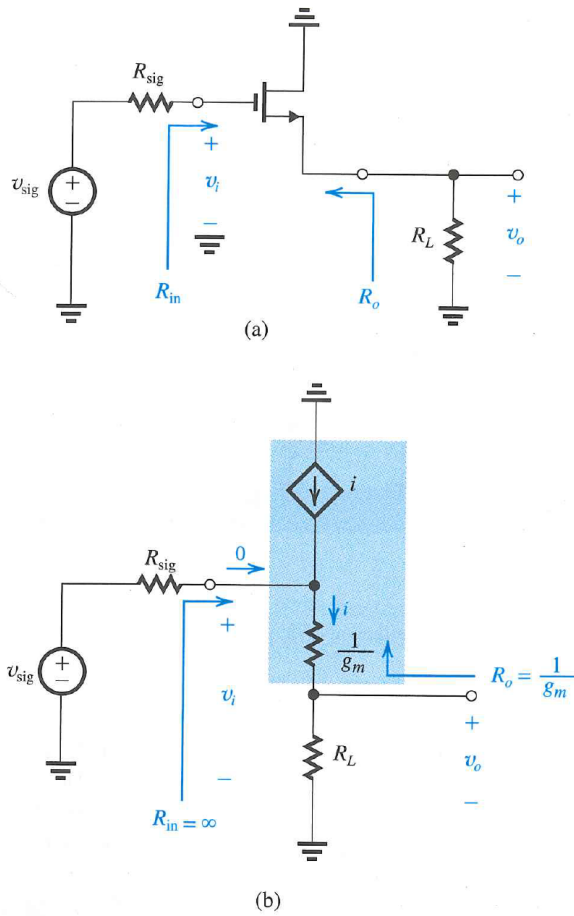


Figure 4: (a) Common-drain MOSFET amplifier or source follower for small signals. (b) The T model equivalent circuit for the common-drain or source follower amplifier. Note that the gate current is always zero in this model (Courtesy of Sedra and Smith).

Because of the infinite input impedance  $R_{in}$ , then  $v_i = v_{sig}$ , and the overall voltage gain  $G_v$  (also called the total voltage gain) is the same as the voltage gain proper  $A_v$  (also called terminal voltage gain)

$$G_v = A_v = \frac{R_L}{R_L + 1/g_m} \quad (4.5)$$

Since  $1/g_m$  is typically small, with large  $R_L$ , the gain is less than unity, but is close to unity. Hence, this is a *source follower*.

## 5 Summary Table and Comparisons

The following concluding points are in order for the MOSFET and BJT amplifiers.

1. MOS amplifiers have high input impedance (except for CG amplifiers). This is an advantage over BJT amplifiers.
2. BJT's have higher transconductance  $g_m$  than MOSFET's giving BJT amplifiers higher gains.
3. Discrete-circuit amplifiers, e.g., circuits assembled on printed-circuit board (PCB), BJT's are prevalent because of their longer history and wider commercial availability.
4. Because of easier fabrication, integrated circuit (IC) amplifiers are dominated by MOSFET's.
5. The CS and CE configurations are best suited for gain amplifiers because of their larger than unity gain. A cascade of them can be used to increase the gain.
6. The addition of  $R_s$  in a CS amplifier improves the linearity of the circuit and better high frequency performance.

Table 7.4 from Sedra and Smith summarizes the characteristics of the MOSFET amplifiers.

## 6 Discrete-Circuit Amplifiers

Due to history and tradition, most discrete-circuit amplifiers are BJT's. Also, capacitive coupling is often used in discrete amplifier design. They make the design simpler as capacitors are DC blockers, and can be approximated as a short circuit for AC signals.



**Table 7.4** Characteristics of MOSFET Amplifiers

Amplifier type	Characteristics <sup>a</sup>				
	$R_{in}$	$A_{vo}$	$R_o$	$A_v$	$G_v$
Common source (Fig. 7.35)	$\infty$	$-g_m R_D$	$R_D$	$-g_m(R_D \parallel R_L)$	$-g_m(R_D \parallel R_L)$
Common source with $R_s$ (Fig. 7.37)	$\infty$	$-\frac{g_m R_D}{1 + g_m R_s}$	$R_D$	$-\frac{g_m(R_D \parallel R_L)}{1 + g_m R_s}$ $-\frac{R_D \parallel R_L}{1/g_m + R_s}$	$-\frac{g_m(R_D \parallel R_L)}{1 + g_m R_s}$ $-\frac{R_D \parallel R_L}{1/g_m + R_s}$
Common gate (Fig. 7.39)	$\frac{1}{g_m}$	$g_m R_D$	$R_D$	$g_m(R_D \parallel R_L)$	$\frac{R_D \parallel R_L}{R_{sig} + 1/g_m}$
Source follower (Fig. 7.42)	$\infty$	1	$\frac{1}{g_m}$	$\frac{R_L}{R_L + 1/g_m}$	$\frac{R_L}{R_L + 1/g_m}$

<sup>a</sup> For the interpretation of  $R_{in}$ ,  $A_{vo}$ , and  $R_o$ , refer to Fig. 7.34(b).

## 6.1 A Common-Source (CS) Amplifier

The circuit to be analyzed here is shown in Figure 5(a). The bias point which is a DC operating point, is determined by Figure 5(b) where all capacitors are open circuited. The small signal model, which is for AC signal, is shown in Figure 5(c) where all capacitors are short circuited.

It is noted that the MOSFET source (S) terminal is grounded for the AC signal because of the large coupling capacitor  $C_S$ , and hence, it is also called the **signal ground** or **AC ground**. Hence,  $C_S$  is also called the **bypass capacitor** as its impedance is much smaller than that of  $R_S$ . The presence of  $R_S$  is to stabilize the biasing point. Looking at Figure 5(b), if  $R_S$  is not there, since  $V_{GS}$  is small, and hence,  $V_G$  has to be small. Thus, all of the fluctuation of  $V_G$  will appear across  $V_{GS}$ . However, with  $R_S$  present, any fluctuation in  $V_G$  will be shared by  $V_{GS}$  and the voltage drop across  $R_S$ .

Then  $C_{C1}$  is another **coupling capacitor**, which will be acting approximately like a short circuit to AC signals, but is a DC blocker. The second coupling capacitor  $C_{C2}$  is also acting like a short circuit to the AC signal, or the small signal. These give the rationale for the small signal model in Figure 5(c).

Using the small signal model for AC signals, and the hybrid- $\pi$  model for MOSFET as shown in Figure 5(c), it is seen that

$$R_{in} = R_{G1} \parallel R_{G2} \quad (6.1)$$

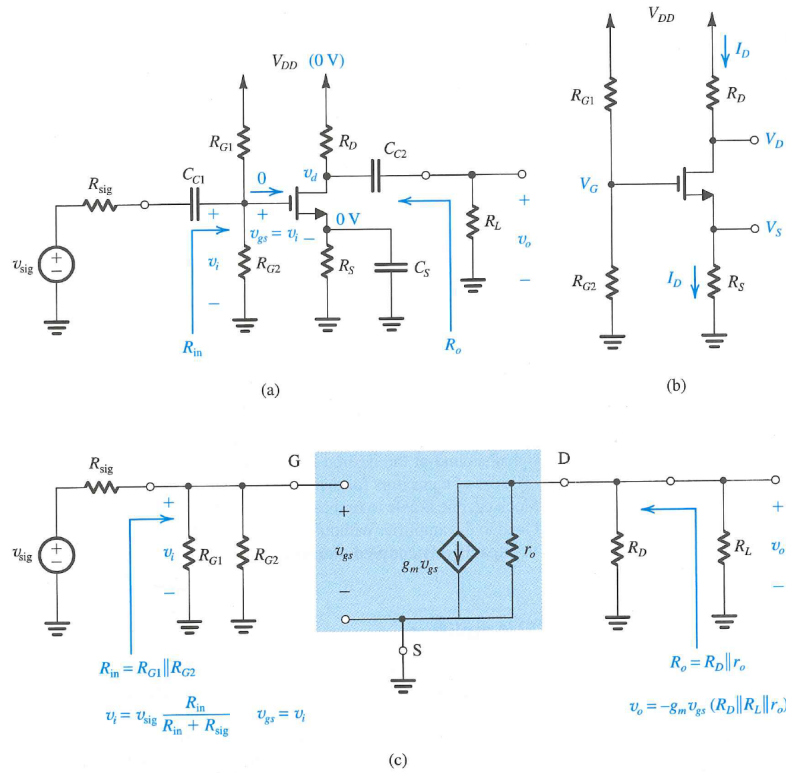


Figure 5: (a) Common-source MOSFET amplifier with the biasing circuit in place. (b) The biasing circuit at DC, where the capacitors are open circuited. (c) Small signal equivalent circuit model for AC signals where the capacitors are assumed to be short circuited (Courtesy of Sedra and Smith).

Here,  $R_{in}$  can be kept high by making  $R_{G1}$  and  $R_{G2}$  high, usually in the megaohm range. It is seen that the voltage gain proper (terminal voltage gain) is

$$A_v = -g_m(R_D \parallel R_L \parallel r_o) \quad (6.2)$$

and the overall voltage gain

$$G_v = -\frac{R_{in}}{R_{in} + R_{sig}} g_m(R_D \parallel R_L \parallel r_o) \quad (6.3)$$

## 6.2 A Common-Emitter Amplifier

This is the most commonly used configuration of the BJT amplifiers, as shown in Figure 6(a) with the coupling capacitors  $C_{C1}$  and  $C_{C2}$ , and the bypass capacitor

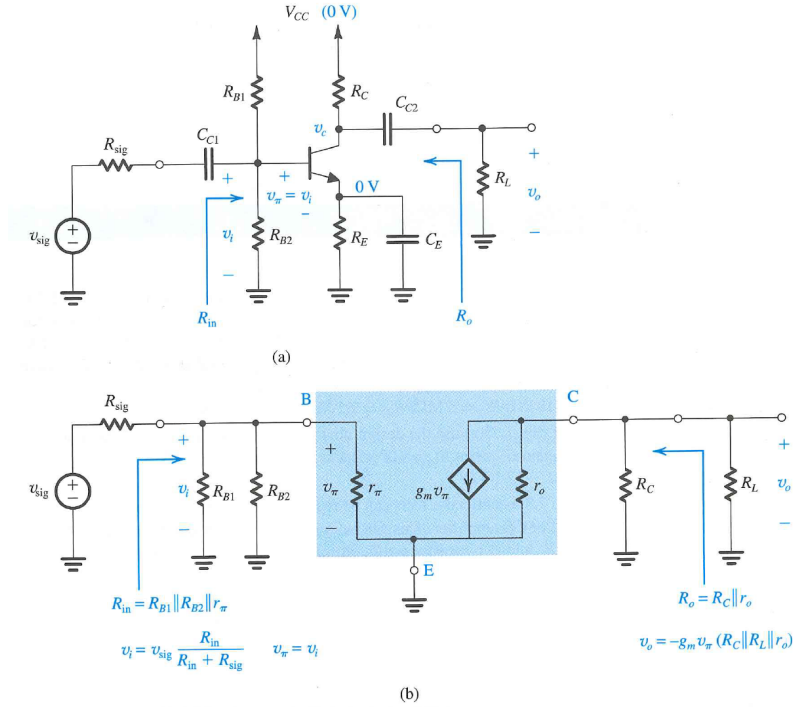


Figure 6: (a) Common-emitter BJT amplifier with the biasing circuit in place. (b) The biasing circuit at DC, where the capacitors are open circuited. (c) Small signal equivalent circuit model for AC signals where the capacitors are assumed to be short circuited (Courtesy of Sedra and Smith).

$C_E$  in place. These capacitors, to simplify the analysis, are assumed to be open circuited for DC or the bias-point analysis, but are short circuited for the AC small signal analysis. Again, as in the MOSFET case,  $R_E$  is there to stabilize the bias point of the base voltage.

The equivalent small signal model is shown in Figure 6(b). From it, it is seen that

$$R_{in} = R_{B1} \parallel R_{B2} \parallel r_\pi \quad (6.4)$$

In the above  $R_{B1}$  and  $R_{B2}$  should be kept large, around tens to hundreds of kilo-ohms, to maintain high input impedance.

The overall voltage gain  $G_v$  is then given by

$$G_v = -\frac{R_{in}}{R_{in} + R_{sig}} g_m (R_C \parallel R_L \parallel r_o) \quad (6.5)$$