

Design and optimization of donor-based spin qubits in silicon

Yu Wang

Network for Computational Nanotechnology

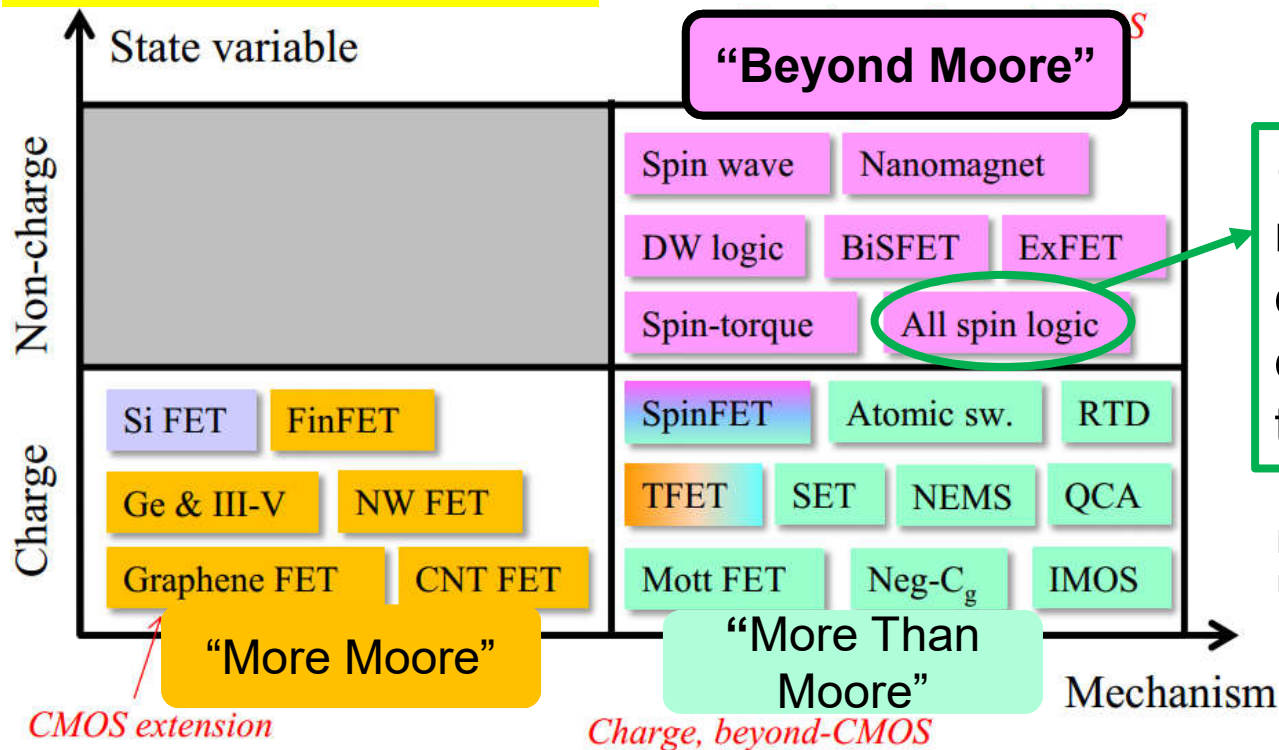
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PURDUE
UNIVERSITY

Emerging logic devices



Quantum spin logic -- massive parallelism in quantum mechanics: 30 qubits more powerful than a supercomputer!

<http://computer.howstuffworks.com/quantum-computer1.htm>

A. Chen, IEEE International Conference on IC Design & Technology, Pg. 1-4 (2014).

<http://docplayer.net/120178-On-the-convergences-between-more-moore-more-than-moore-and-beyond-cmos.html>

Research area: quantum spin logic devices

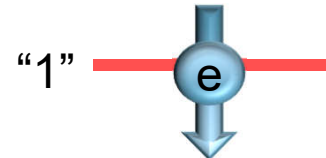
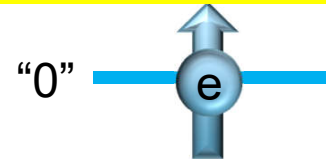
Basic unit: quantum bit (qubit)

"0" 

"1" 

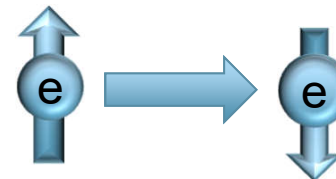
$$|Q\rangle = \alpha|0\rangle + \beta|1\rangle$$

Implementation



$$\alpha|\uparrow\rangle + \beta|\downarrow\rangle$$

Computing with quantum logic:



Number of qubits  allowed functionalities 

- 4 qubits to factorize 143 (N. Xu et al., PRL 108, 130501 (2012))
- 30 qubits can outperform a classical computer (~3 billion transistors). <http://computer.howstuffworks.com/quantum-computer1.htm>

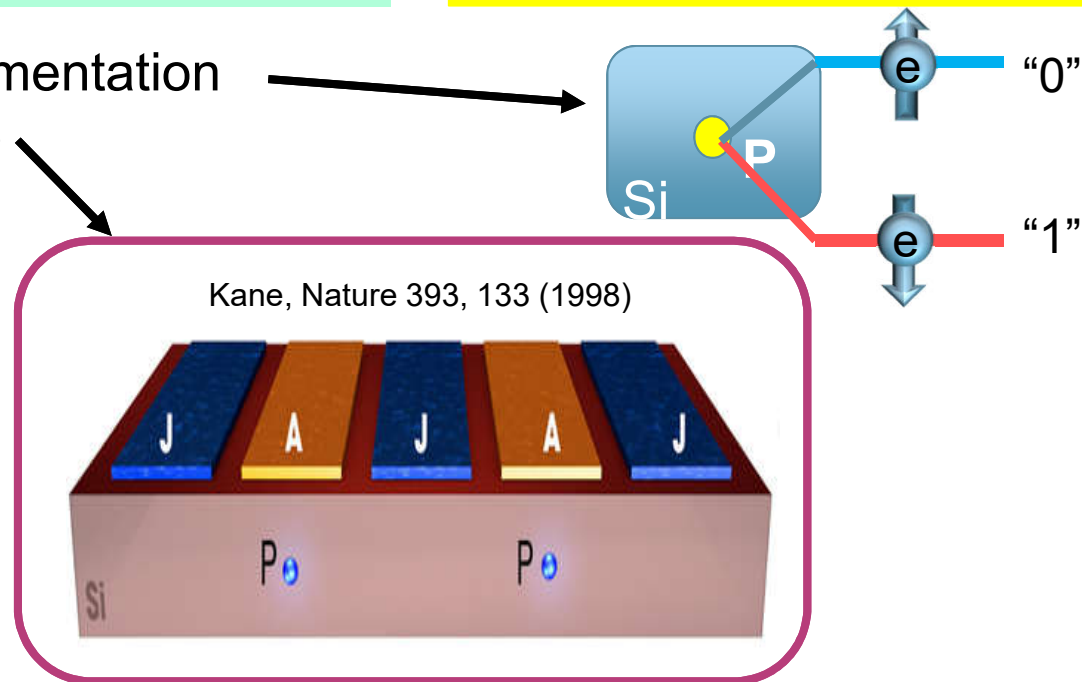
Allowed functionalities/Performance $\propto 2^N$

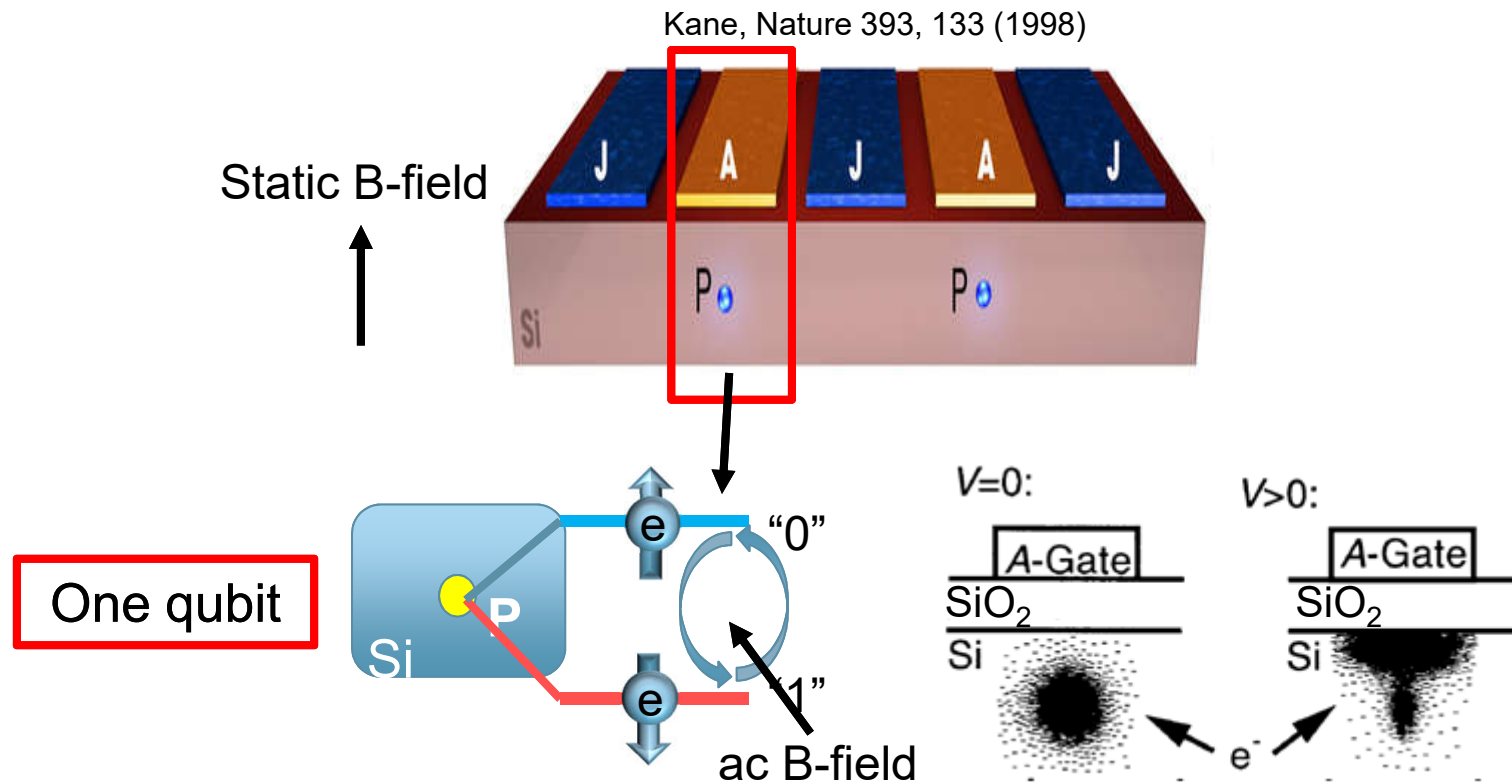
Realizing multi-qubit operations is the key

Hardware: scalability is the key

Focus: donor electron spin qubit

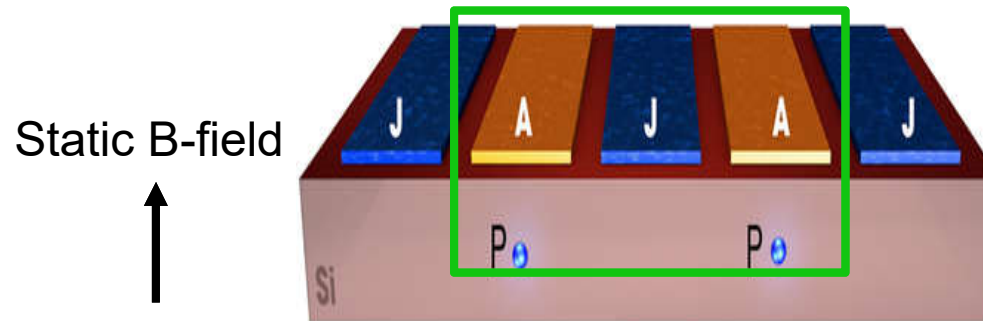
- Qubit implementation
- Architecture



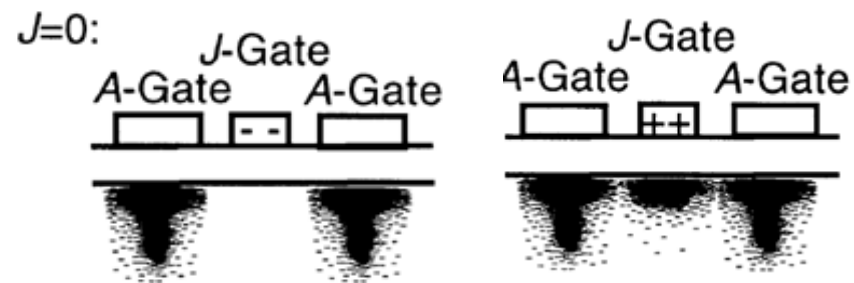


1-qubit control:
Gate controlled resonance frequency

Kane, Nature 393, 133 (1998)



Two qubits



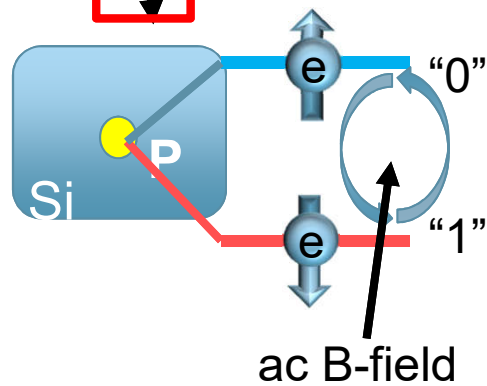
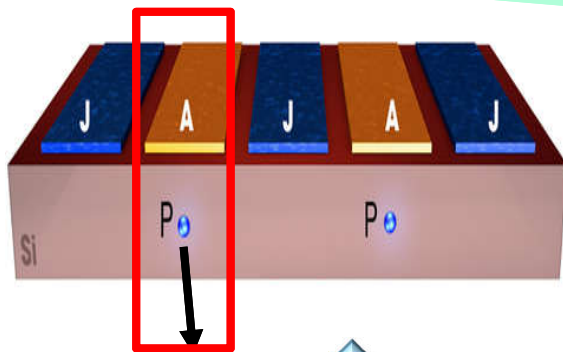
2-qubit control:
Exchange (J) \propto wavefunction overlap

Efforts in experiment on Kane architecture?

1998

2012

2015

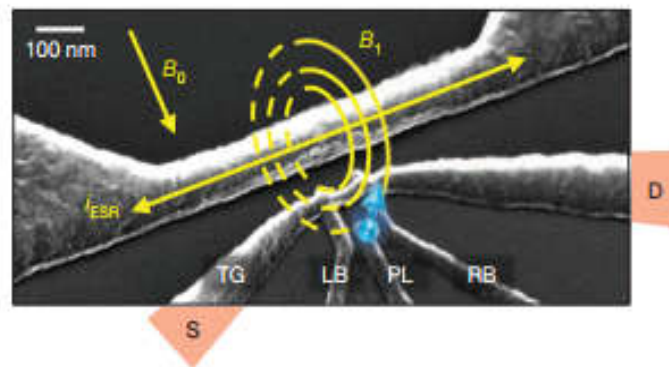


Kane, Nature 393, 133 (1998)

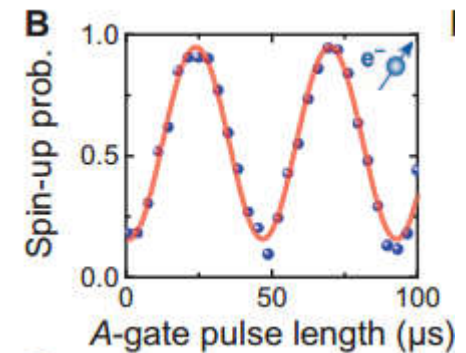
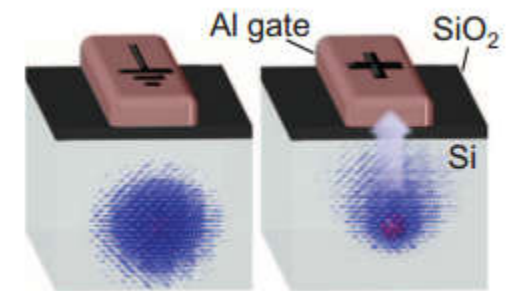
LETTER

A single-atom electron spin qubit in silicon

Jarryd J. Pla¹, Kuan Y. Tan^{1†}, Juan P. Dehollain¹, Wee H. Lim¹, John J. L. Morton^{2†}, David N. Jamieson³, Andrew S. Dzurk & Andrea Morello¹



Pla et al., Nature 489, 541 (2012)



Laucht et al., Sci. Adv. 10 (2015)

✓ Single qubit

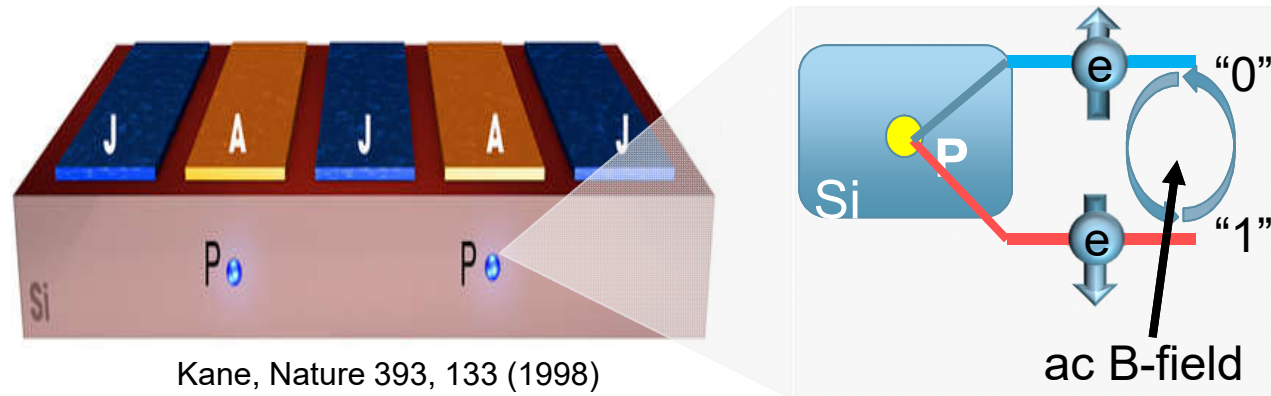
However, multiple-qubit operations haven't been realized. What is preventing us?

Challenges to realize multiple-qubit operations using Kane architecture

Fabrication

Magnetic control
(single qubit)

Exchange control
(2 qubits)



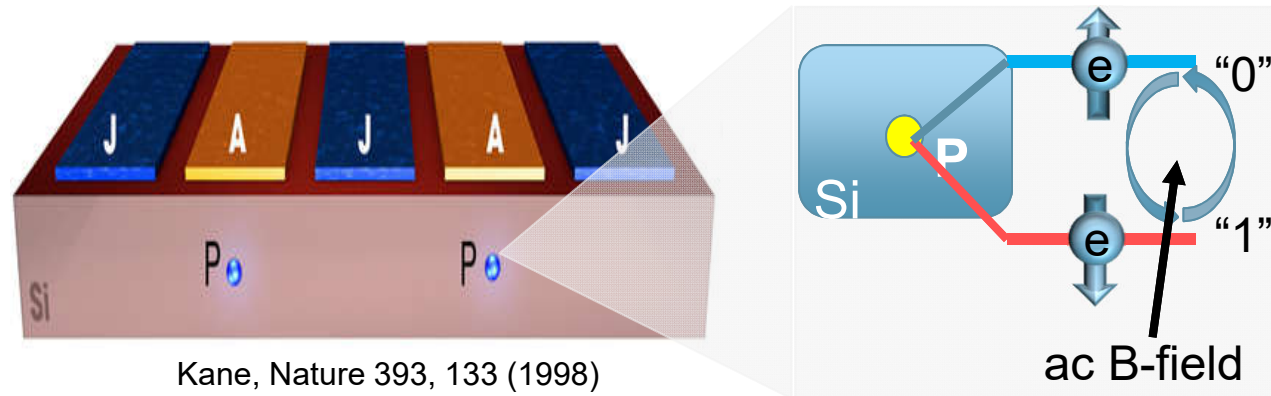
Kane, Nature 393, 133 (1998)

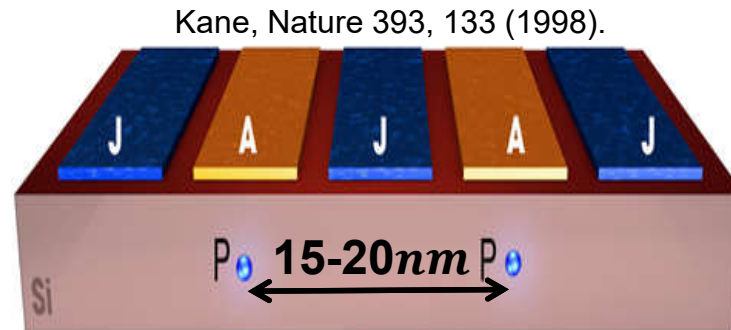
Challenges of realizing multiple-qubit operations using Kane architecture

Fabrication

Magnetic
control
(single qubit)

Exchange
control
(2 qubits)





Fabrication challenge

pack 3 gates in an ultra small length scale

→ gate short and crosstalk

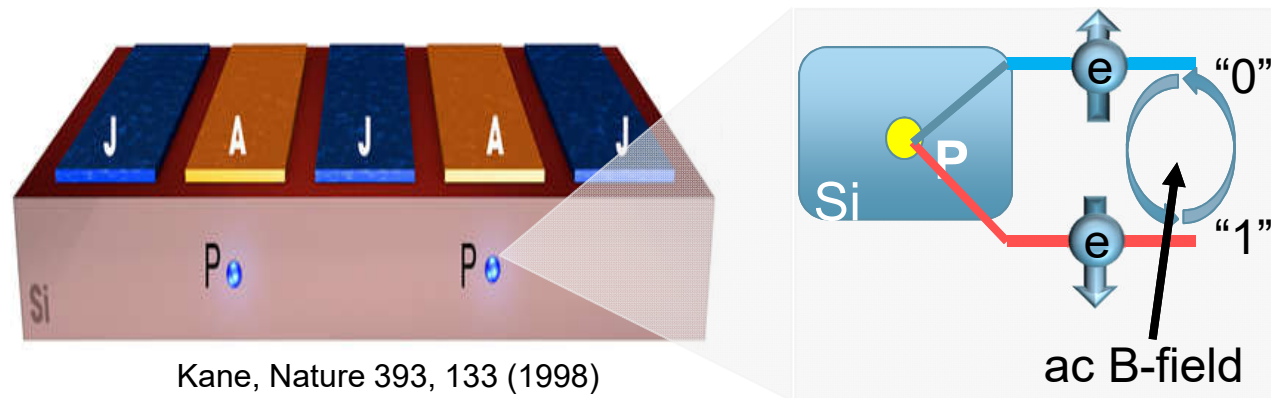
An alternative design with lower gate density is needed.

Challenges of realizing multiple-qubit operations using Kane architecture

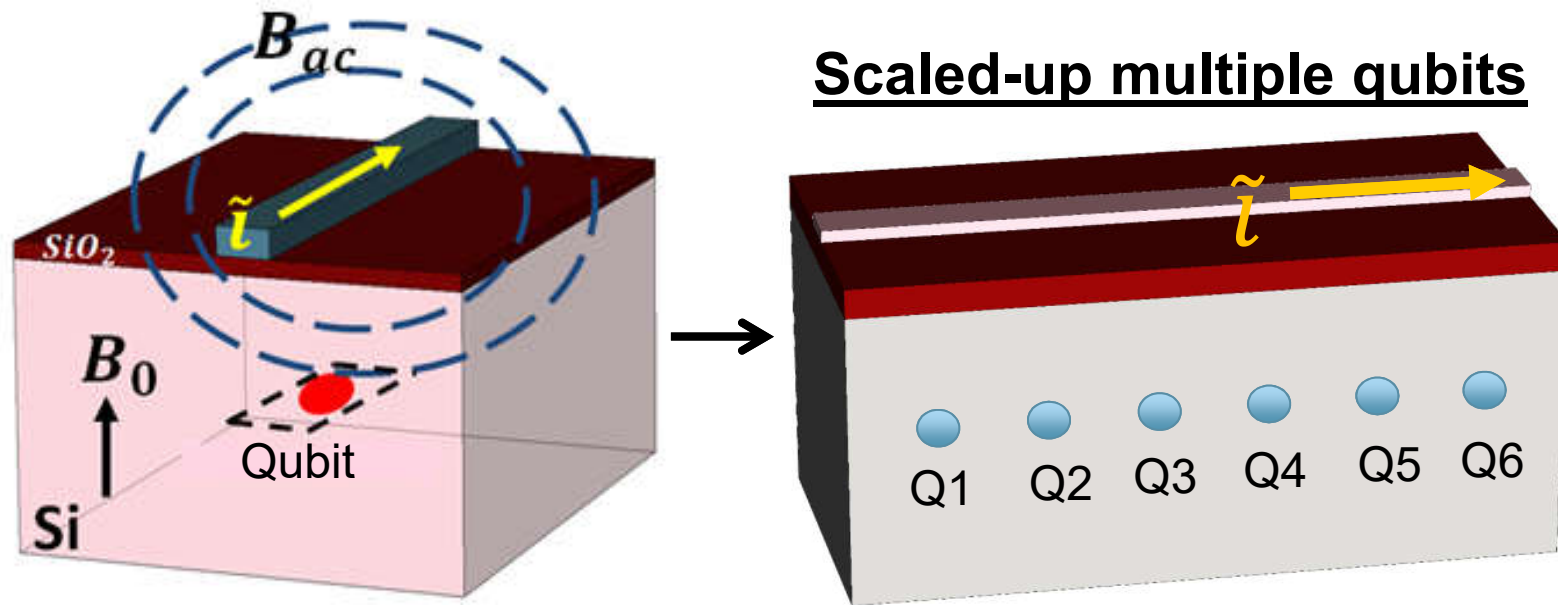
Fabrication

**Magnetic
control
(single qubit)**

Exchange
control
(2 qubits)



Kane, Nature 393, 133 (1998)



Issues of magnetic control

- Difficult to apply local ac B-fields
- The metal wire introduces deleterious noise

J. Muhonen et al., Nature Nanotechnology 9, 986 (2014)

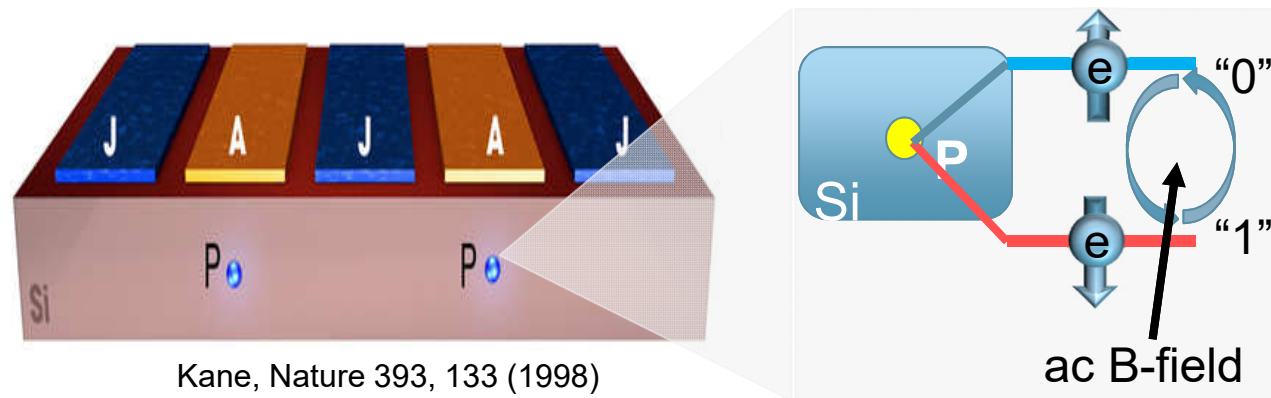
An alternative way to control spins locally is needed.

Challenges of realizing **multiple-qubit** operations using Kane architecture

Fabrication

Magnetic control
(single qubit)

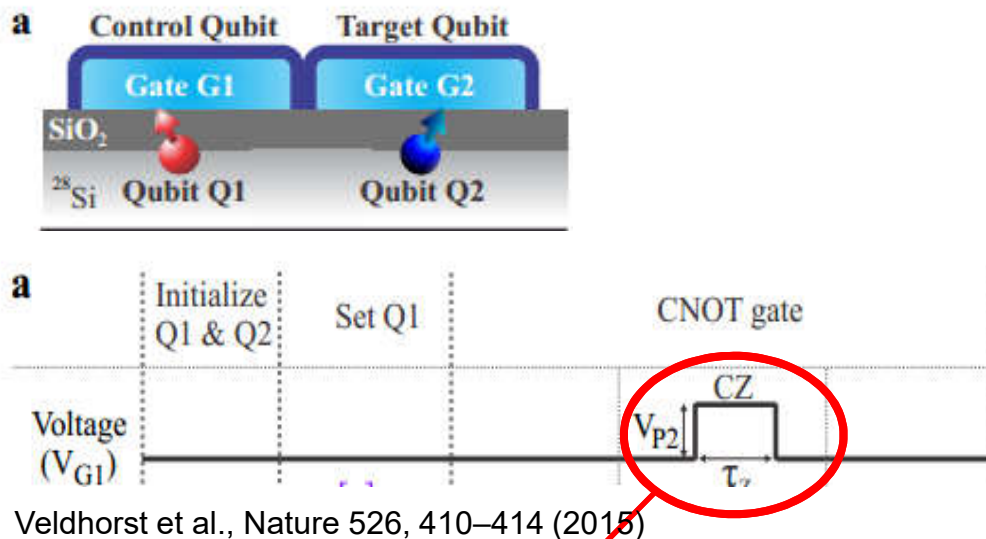
**Exchange control
(2 qubits)**



Kane, Nature 393, 133 (1998)

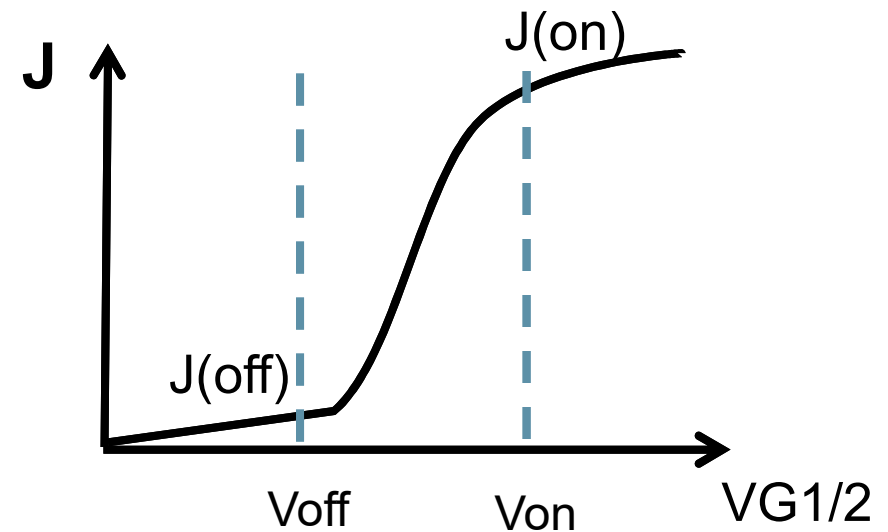
Key step in two-qubit operations: turn exchange on and off

A two-qubit gate in double quantum dots



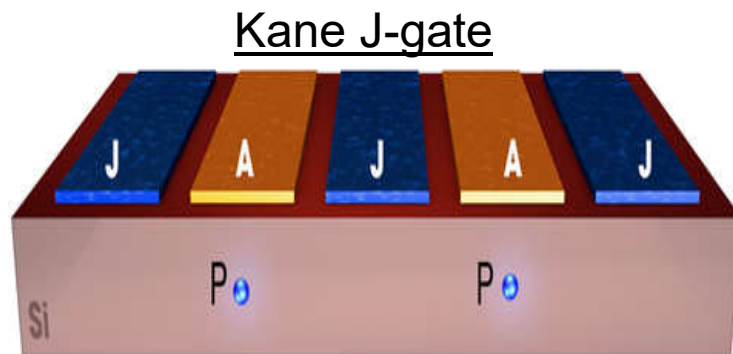
One of the key factors to success:
turn J on and off

Ideal tunability of J



We need J(on) orders of magnitude larger than J(off).

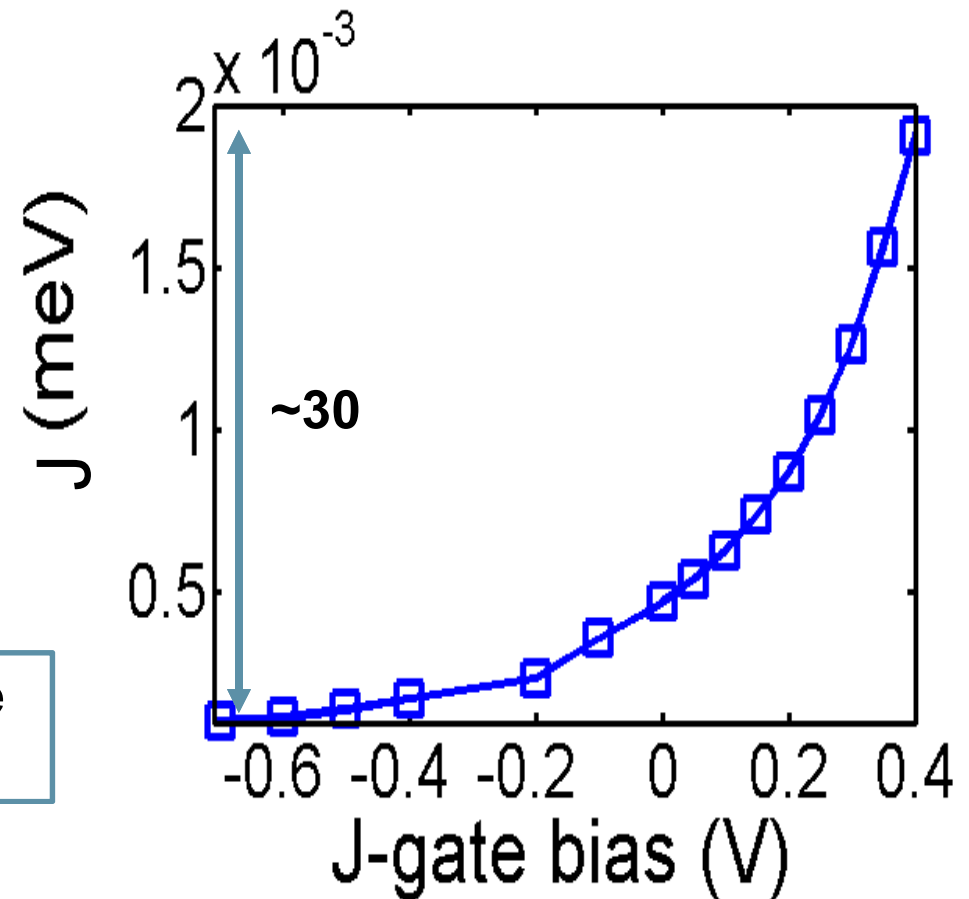
Can this be achieved with Kane architecture?



Kane, Nature 393, 133 (1998).

Limited J tunability:
 $J(\text{on})/J(\text{off}) = \sim 30$

Not enough to effectively turn the two-qubit operation on and off.



An alternative design that can provide enough J-tunability is needed.

Challenges of realizing multiple-qubit operations using Kane architecture

Gate density

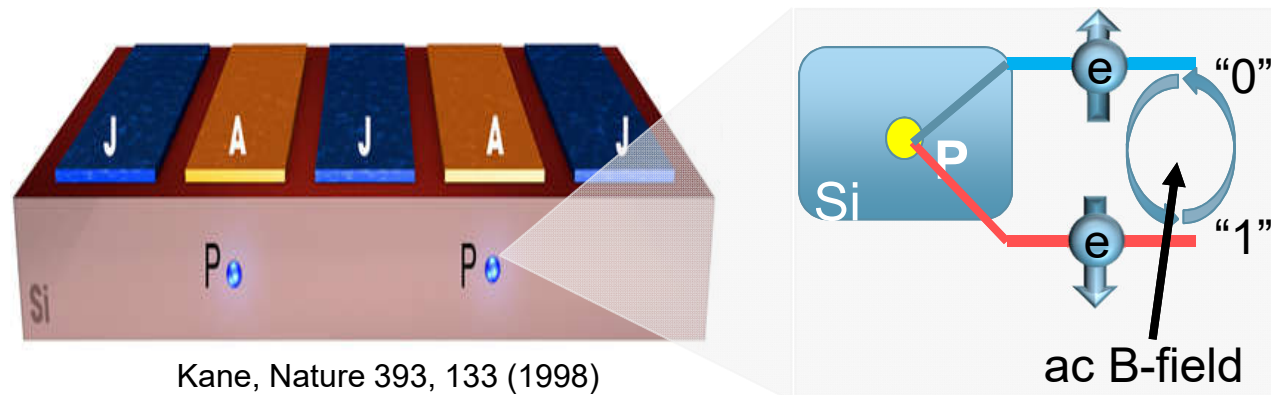
Fabrication

Local control

**Magnetic
control
(single qubit)**

J tunability

**Exchange
control
(2 qubits)**

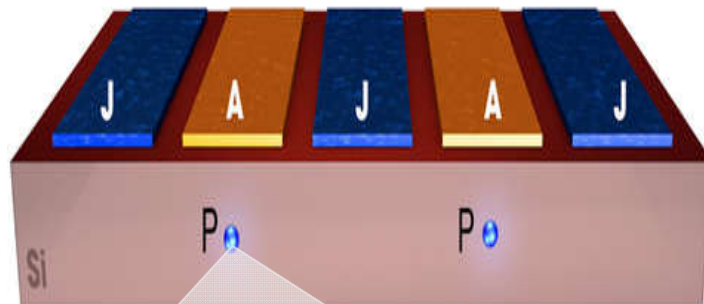


Kane, Nature 393, 133 (1998)

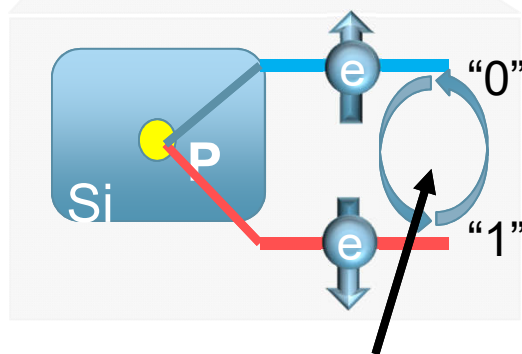
We need a design that could overcome all these challenges.

Challenges to overcome

- ☐ High gate density
- ☐ Exchange tunability
- ☐ Magnetic control



Kane, Nature 393, 133 (1998)



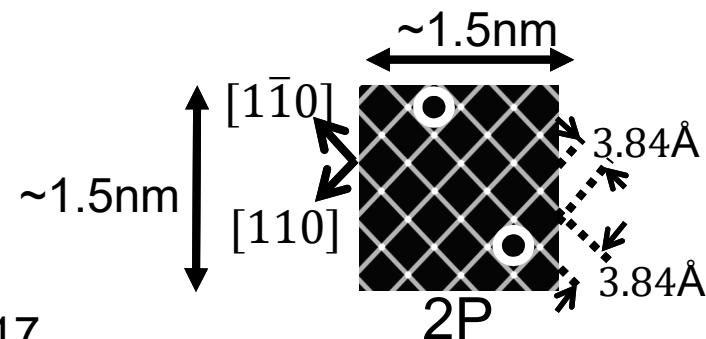
ac B-field

Proposed design

Wang et al., Nature Quantum Info. 2, 16008 (2016)

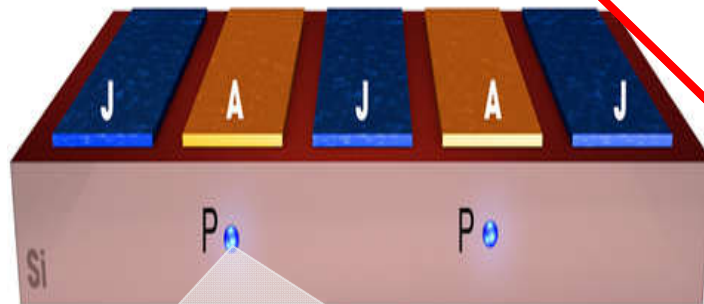


- Gate density is reduced by ~2.
- Exchange can still be tuned even without a J-gate.

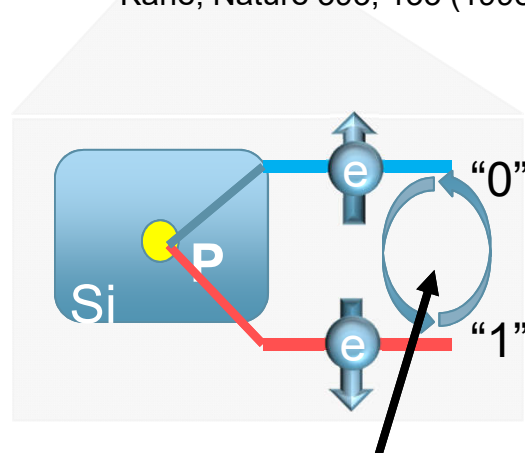


Challenges to overcome

- ☐ High gate density
- ☐ Exchange tunability
- ☒ Magnetic control



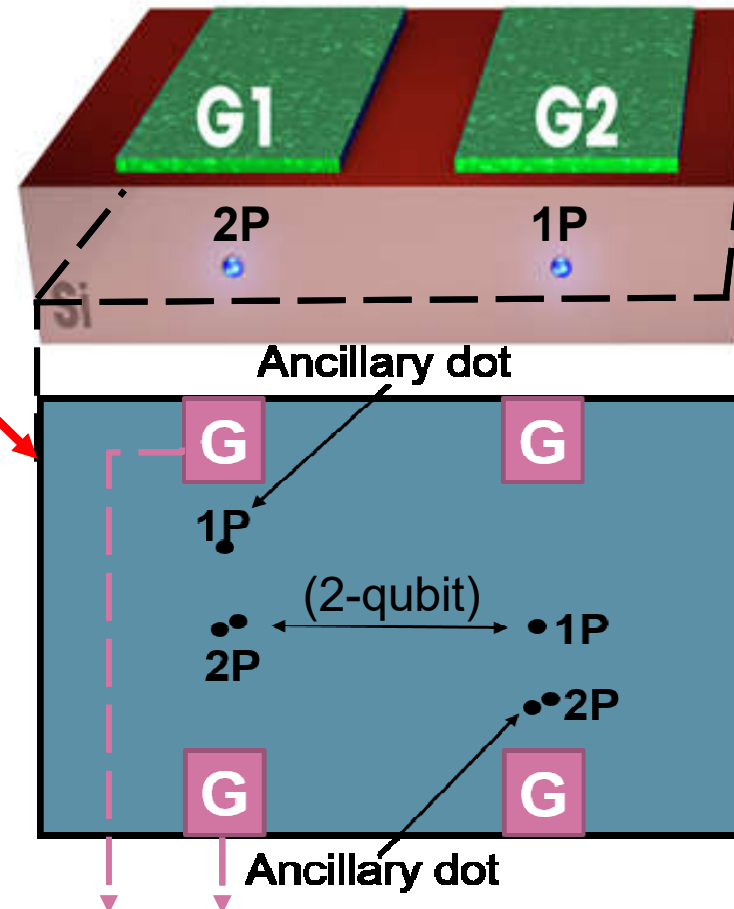
Kane, Nature 393, 133 (1998)



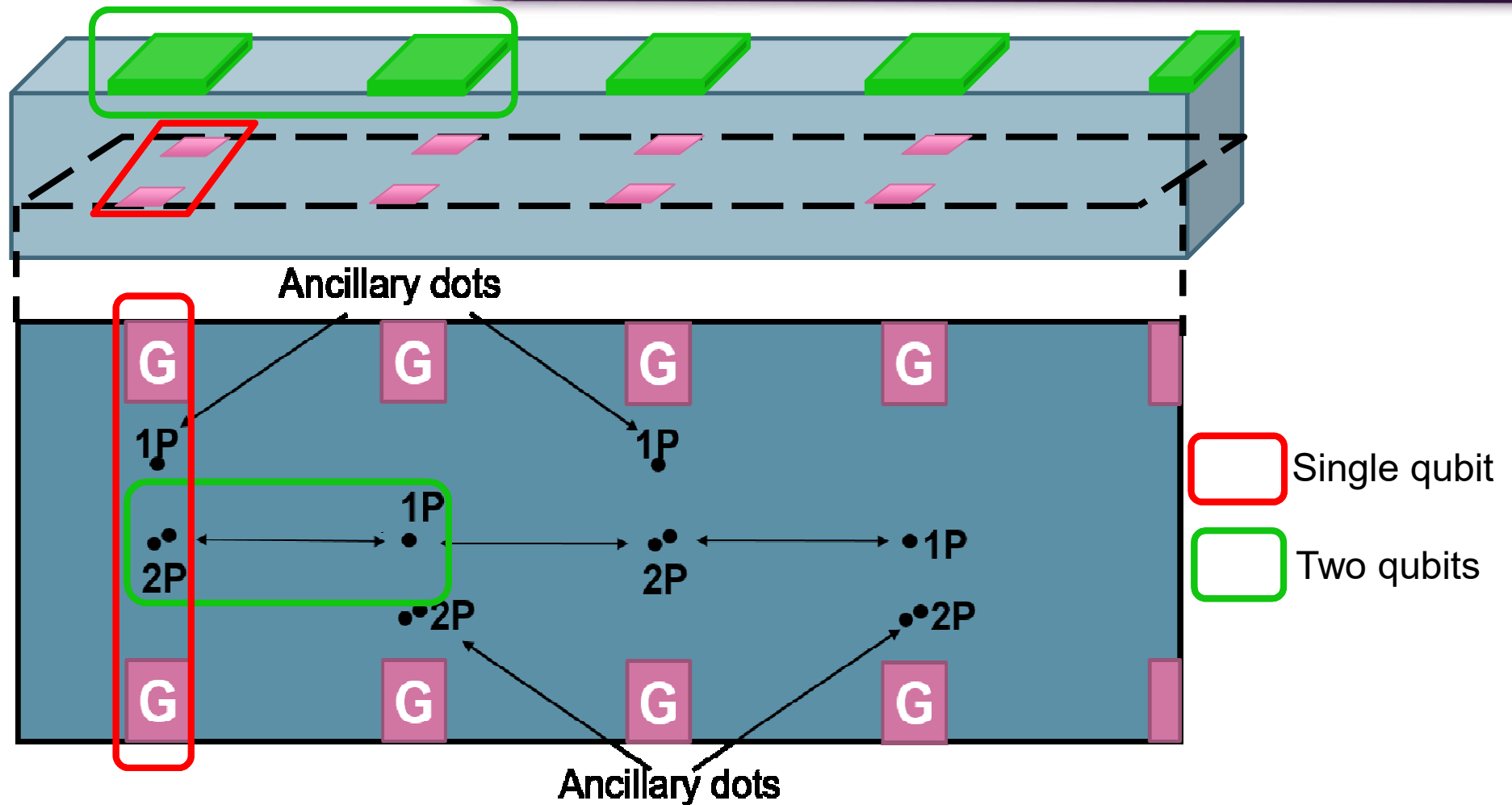
ac B-field

Proposed design

Wang et al., arXiv:1703.05370 (2017).

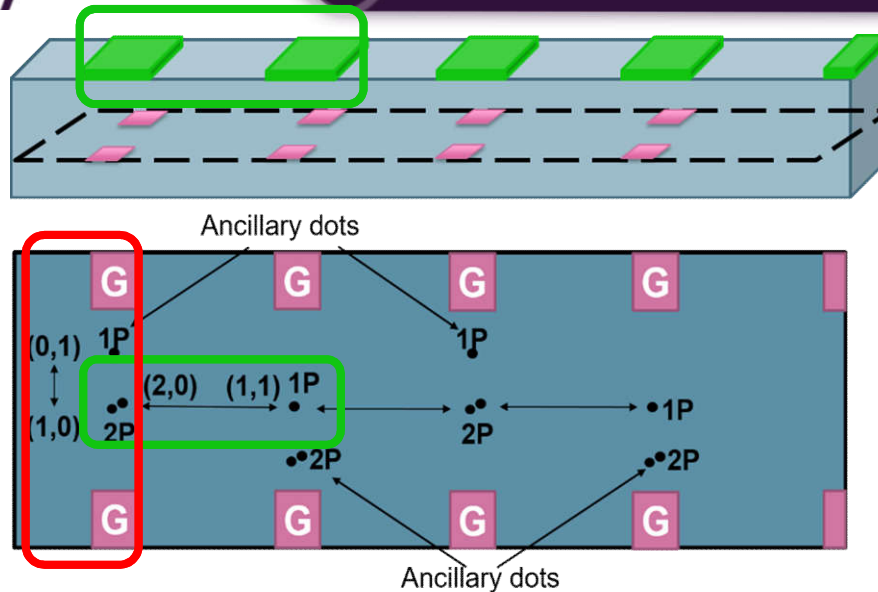


To achieve electrical
control of spin qubits



Linear 1NN quantum computing: A. Fowler et al.,
Quant. Info. Comput. 4, 237-251 (2004)

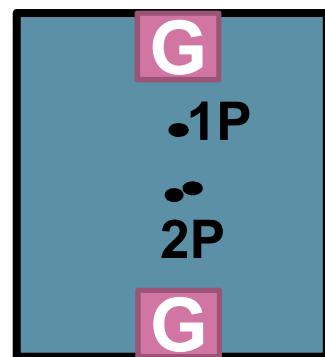
This device structure realizes all-electrical-control of spin and is potentially scalable.



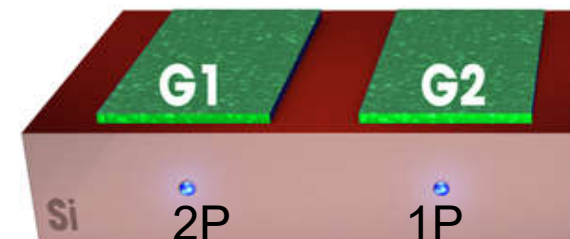
Overcome challenges in Kane's architecture

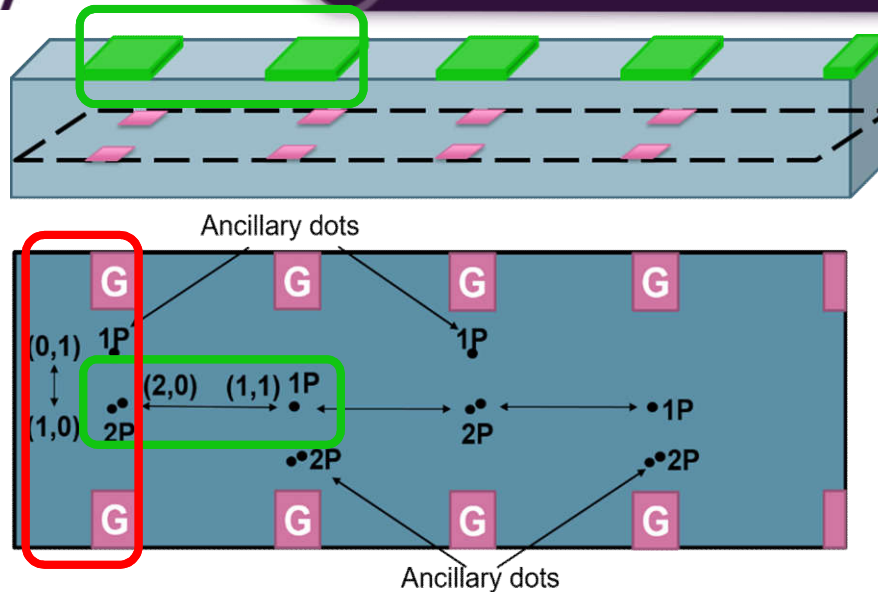
- ✓ Fabrication:
 - ✓ Gate separation
- ✓ All-electrical control
- ✓ Exchange tunability

All-electrical control of donor-based spin qubits



Engineering exchange coupling of two donor qubits

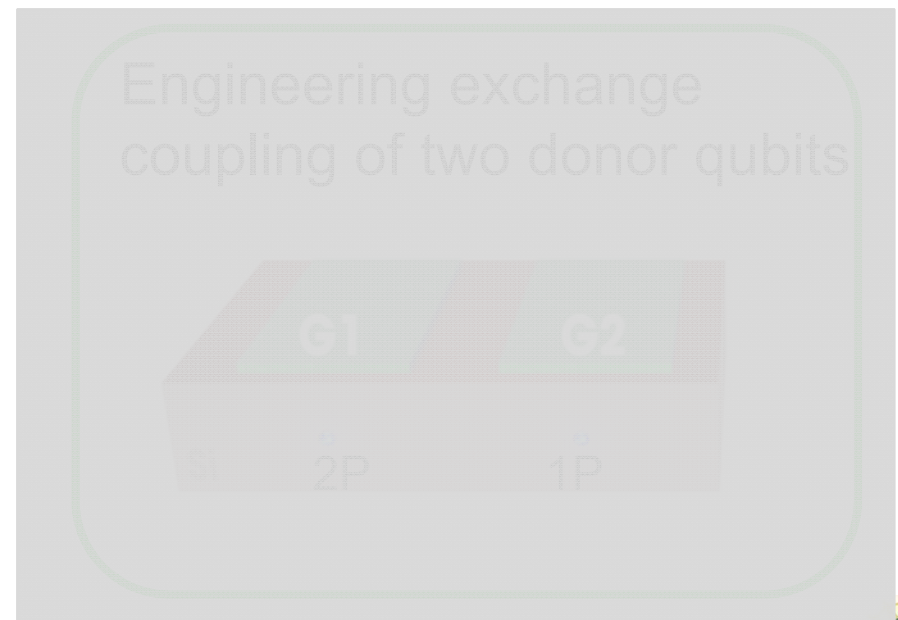
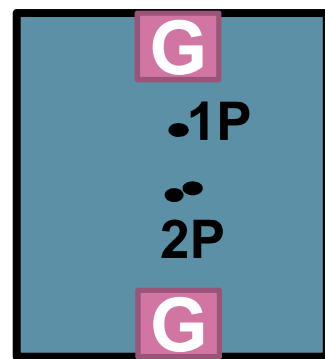




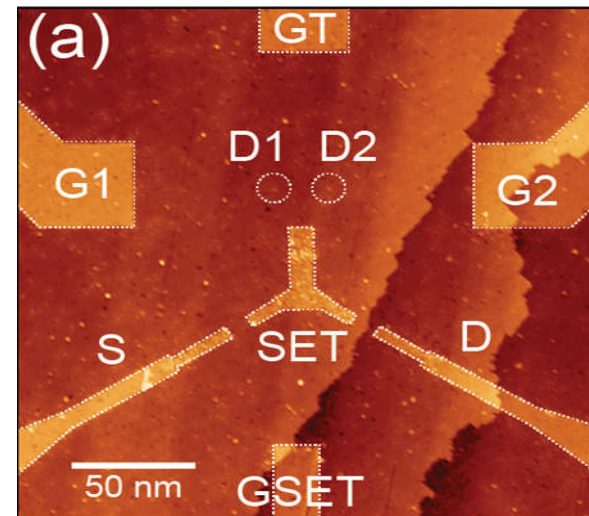
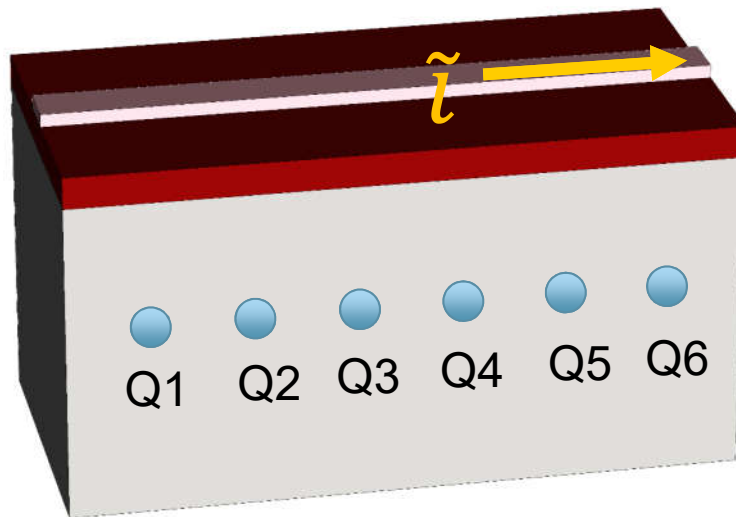
Overcome challenges in Kane's architecture

- ✓ Fabrication:
 - ✓ Gate separation
- ✓ All-electrical control
- ✓ Exchange tunability

All-electrical control of donor-based spin qubits



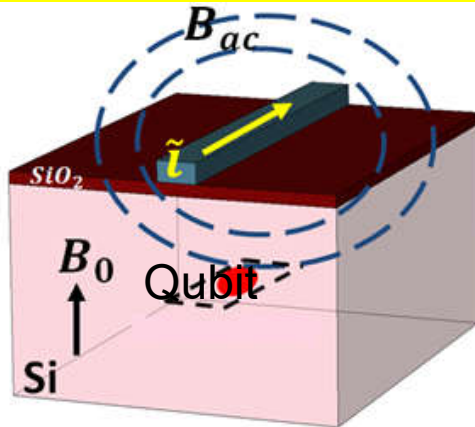
- Difficult to apply local ac magnetic fields.



Watson et al., PRL 115, 166806 (2015).

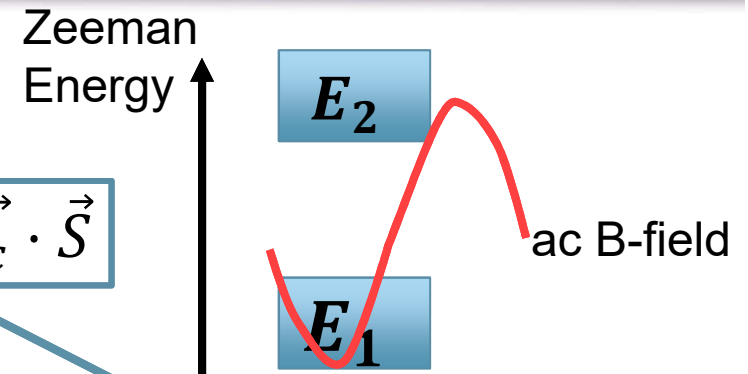
- Applying localized, high-frequency electric fields is easier, and handy with existing circuitry.
- **Electrical control of spin qubits is more favorable.**
 - **How to realize it?**

Spin control with time-varying B-field



$$H = g\mu_B \vec{B}_0 \cdot \vec{S} + g\mu_B \vec{B}_{ac} \cdot \vec{S}$$

$$\vec{B}_{ac} = b_0 \sin(\omega t)$$



Spin control with spatially different B-field + ac E-field

LETTERS

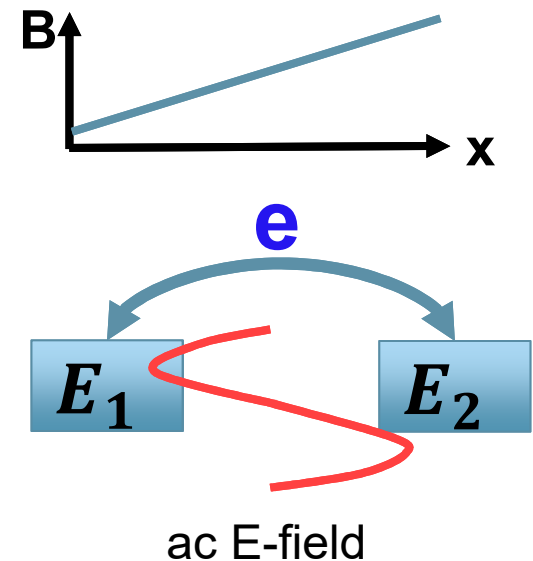
PUBLISHED ONLINE: 10 AUGUST 2014 | DOI: 10.1038/NNANO.2014.153

nature
nanotechnology

Electrical control of a long-lived spin qubit in a Si/SiGe quantum dot

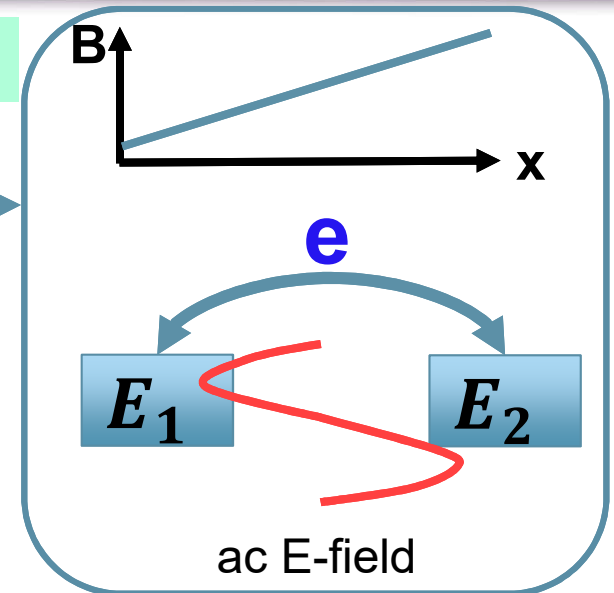
E. Kawakami^{1‡}, P. Scarlino^{1‡}, D. R. Ward², F. R. Braakman^{1†}, D. E. Savage², M. G. Lagally²,
Mark Friesen², S. N. Coppersmith², M. A. Eriksson² and L. M. K. Vandersypen^{1*}

**Spin rotation can be driven by ac E-field
with local Zeeman energy difference.**



Spin control with spatially different B-field + ac E-field

$$H = g\mu_B \vec{B}_0 \cdot \vec{S} + g\mu_B \vec{B}_{ac} \cdot \vec{S}$$

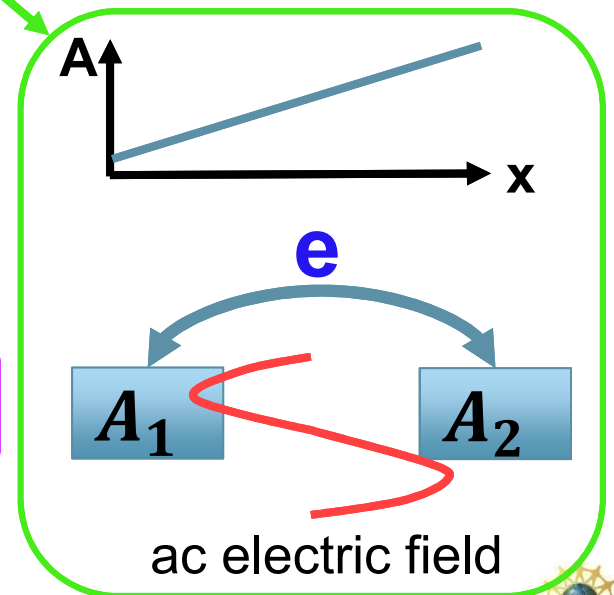


Spin control with spatially different hyperfine couplings + ac E-field

$$H = g\mu_B \vec{B}_0 \cdot \vec{S} + A\vec{I} \cdot \vec{S}$$

Introduces an effective B-field

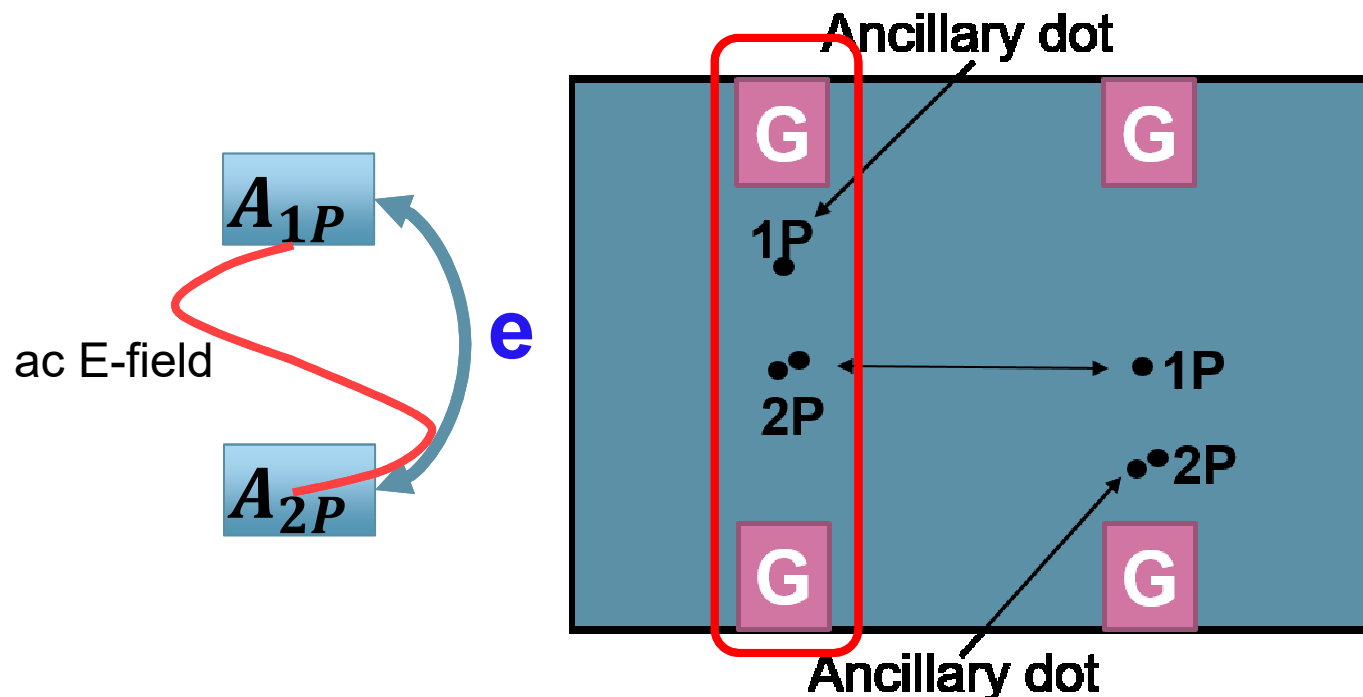
Effective ΔE_{Zeeman} can be created by ΔA



Electron spin rotation can be driven electrically using spatially different hyperfine couplings.

In a QD system: Laird et al. PRL 99, 246001 (2007)

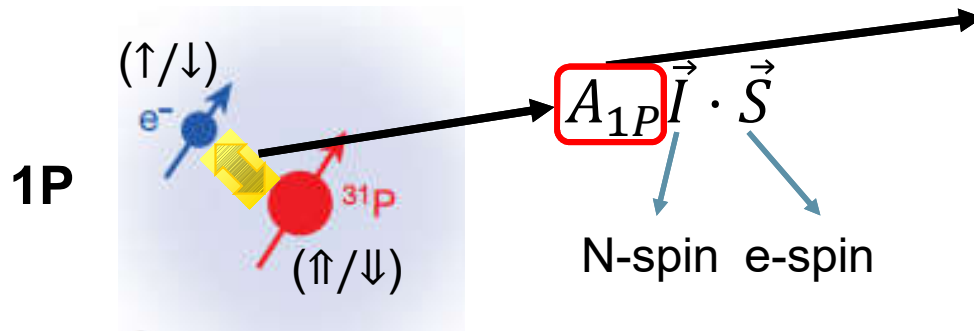
Introduce local hyperfine coupling difference with donors



Modulation can be realized with the in-plane gates.

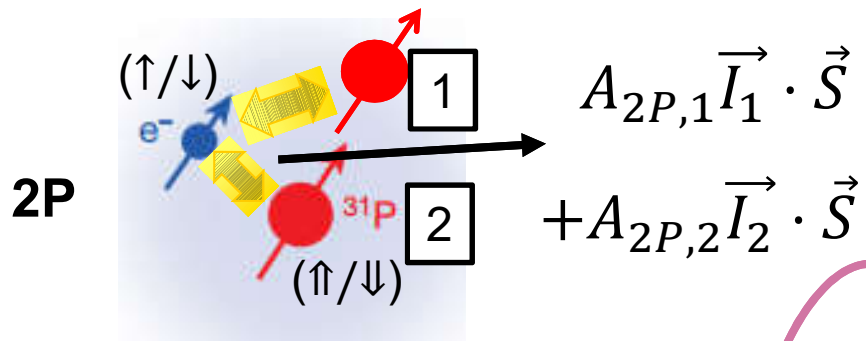
In principle, electrical control of electron spin can be realized in the proposed design.

J. J. Pla et al., Nature 489, 541-545 (2013)



➤ A describes the strength of hyperfine interaction

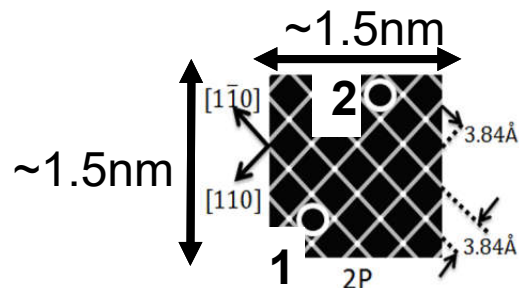
➤ $A \propto |\Psi(\text{at donor site})|^2$



A_{1P} and A_{2P} are different due to different quantum confinement

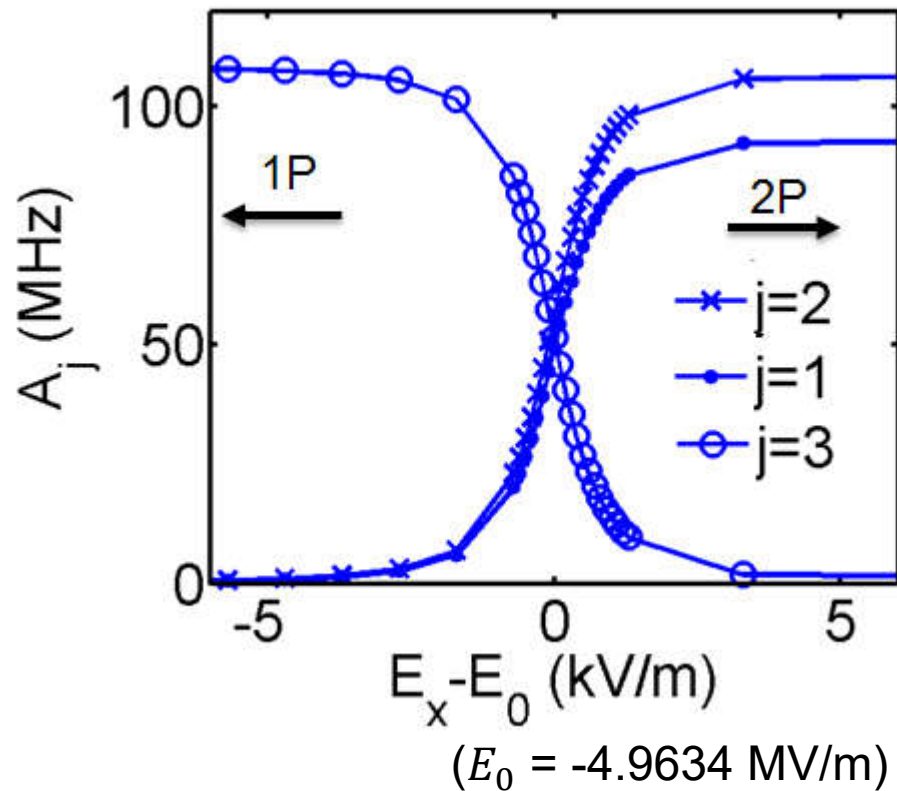
➤ $|\Psi(\text{at donor site})|^2$ depends on E-field $\rightarrow A(\text{E-field})$

1. Rahman et al., PRL 99, 036403 (2007)

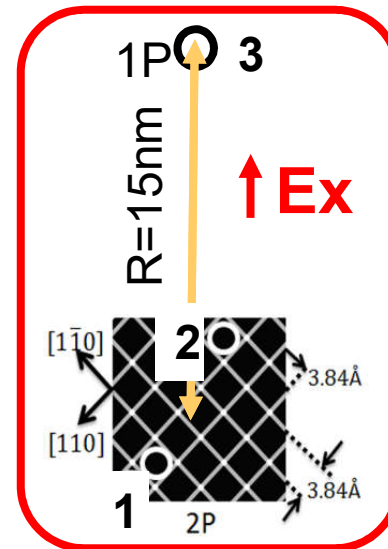
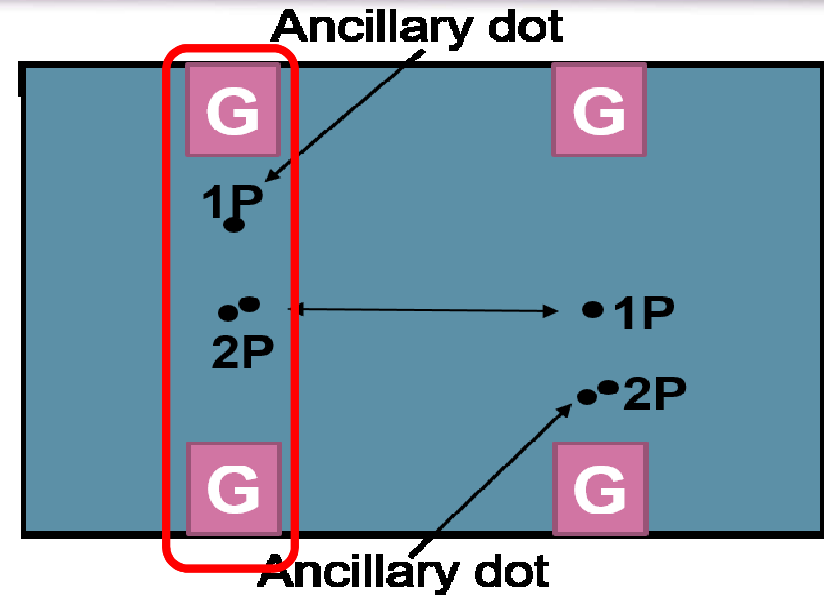


Utilize these for electrical control of spin.

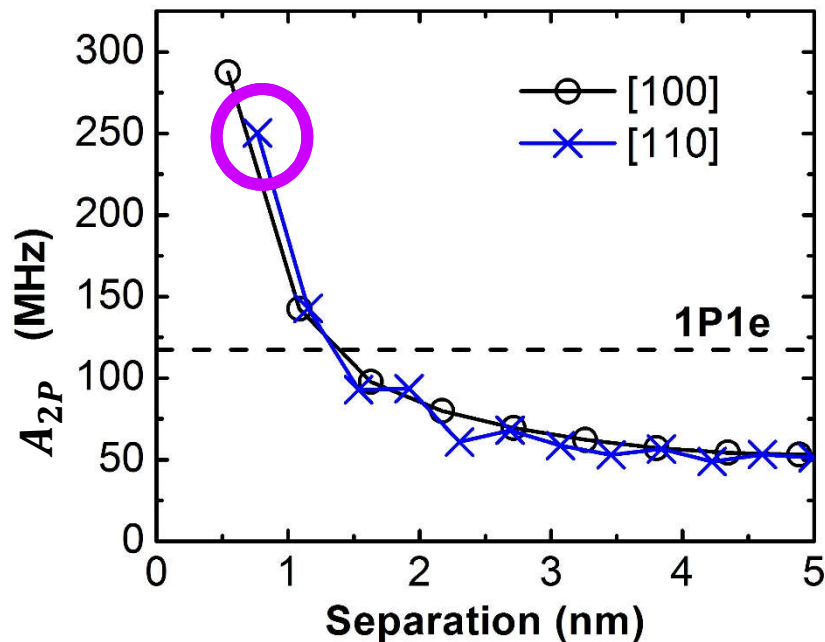
Hyperfine modulation in 2P-1P



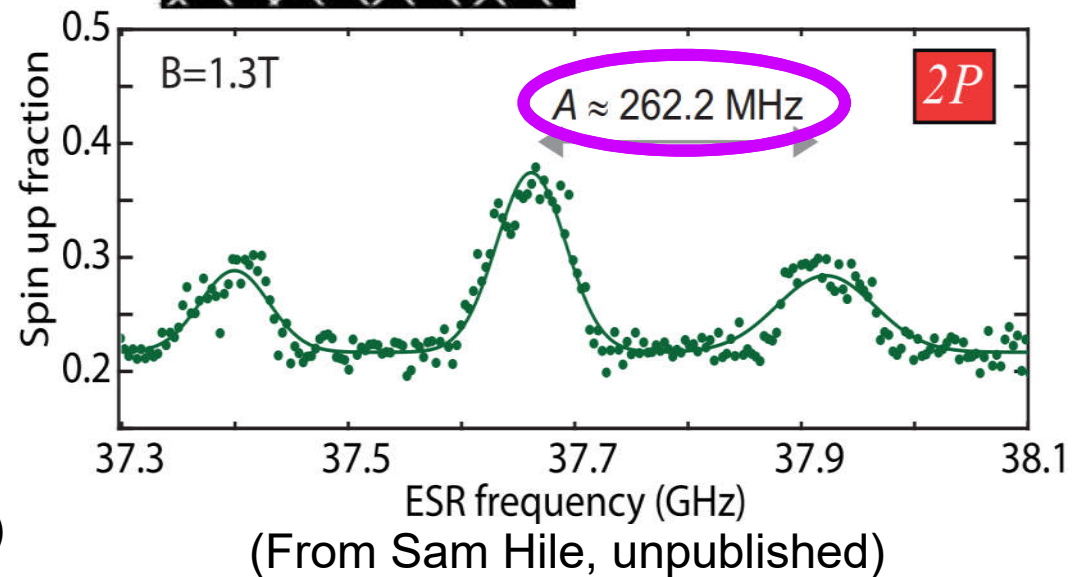
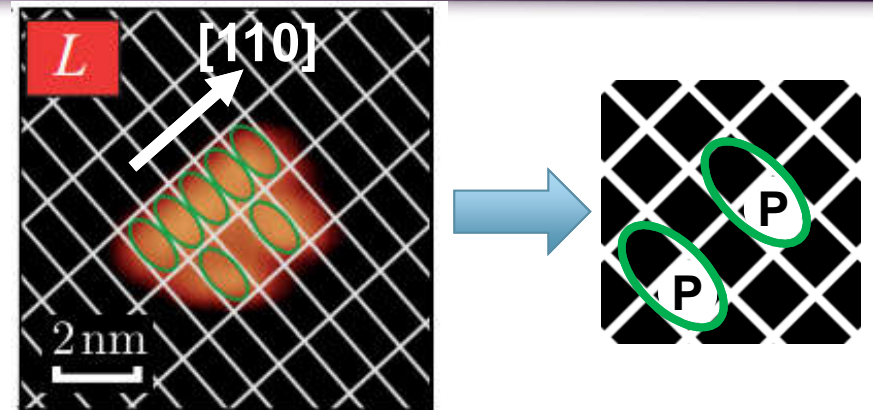
The hyperfine couplings can be modulated with electric fields.



Metrology: mapping out 2P donor locations using hyperfine couplings.



Wang et al., Sci. Rep. 6, 31830 (2016)



(From Sam Hile, unpublished)

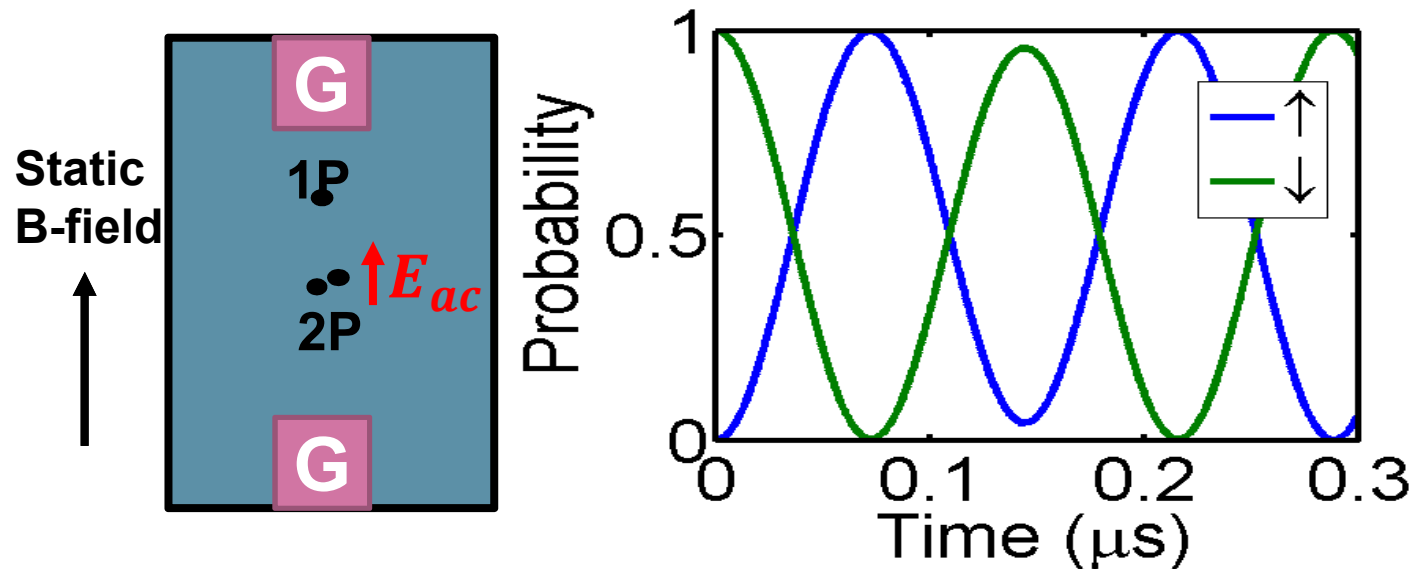
The hyperfine couplings in 2P agree with measurement.

Effective Hamiltonian describing the spin evolution

$$H = H_{Zeeman} + H_{hyperfine} + H_{tc} + H_{E_{ac}}$$

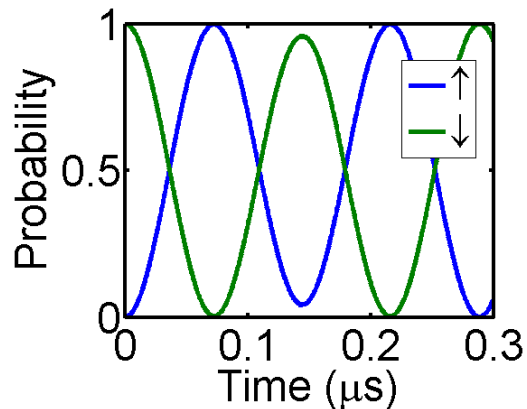
Allows charge transfer between 2P and 1P

To drive the spin rotation

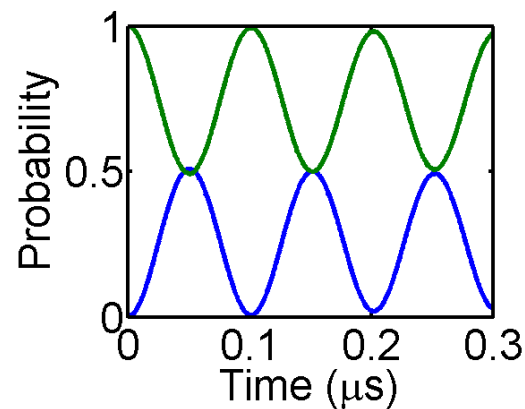


Electrical control of spin qubit can be realized with the proposed design.

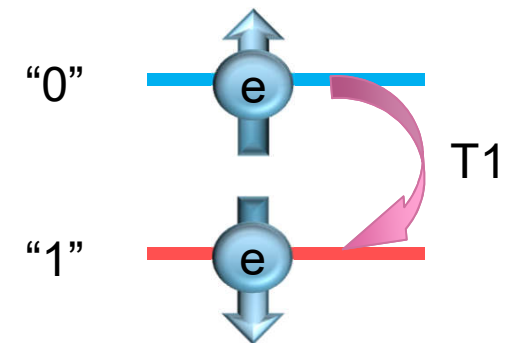
1. High control fidelity



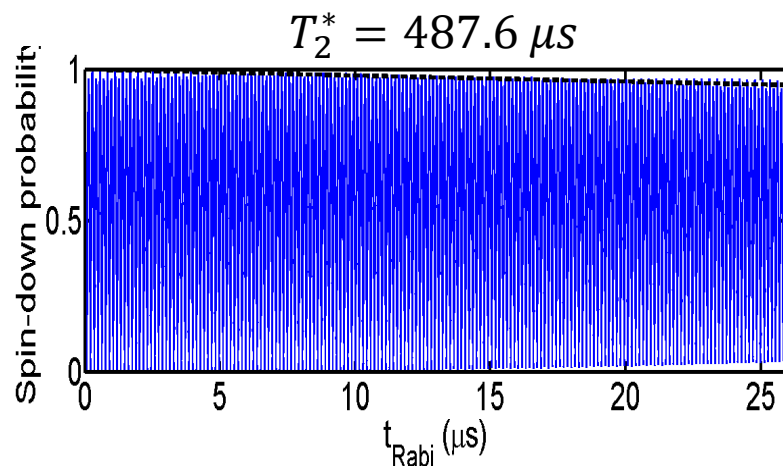
vs



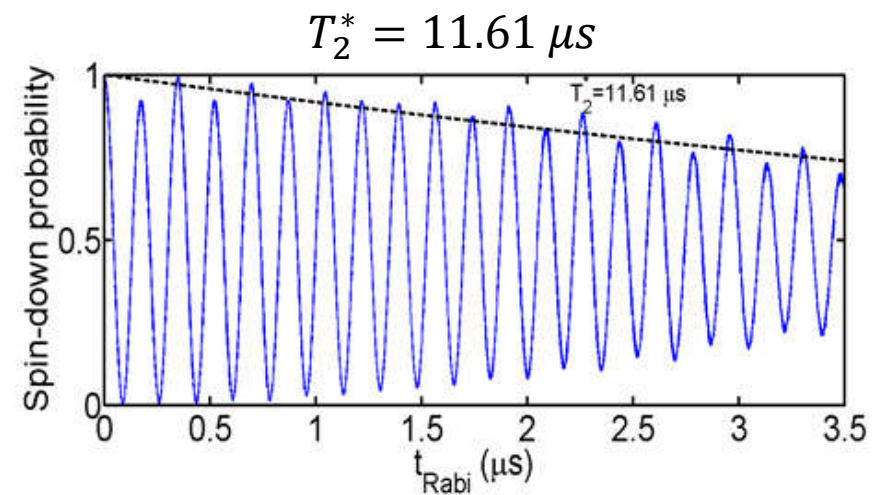
3. Long spin storage time (no operation)



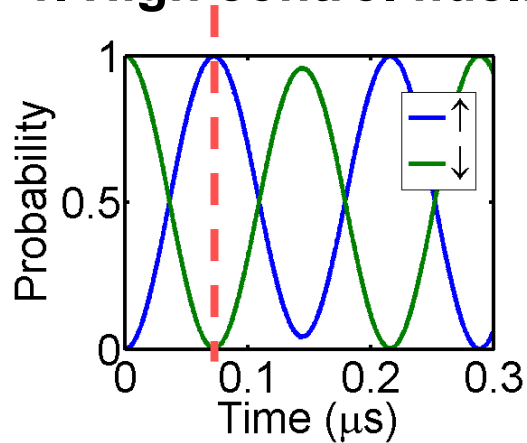
2. Long coherence time



vs

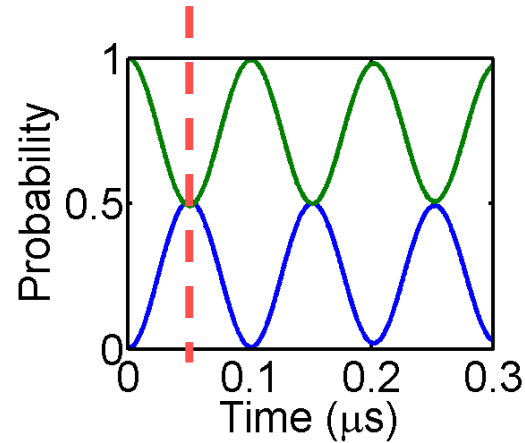


1. High control fidelity



~100%

vs

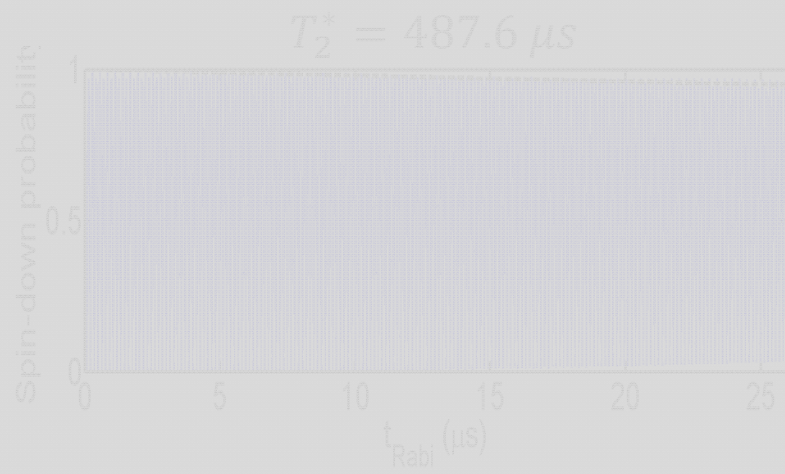


~50%

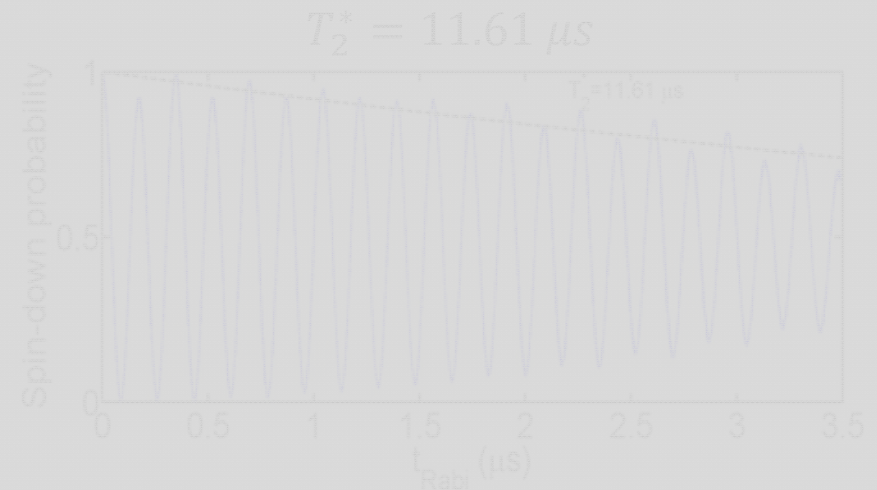
3. Long spin storage time (no operation)



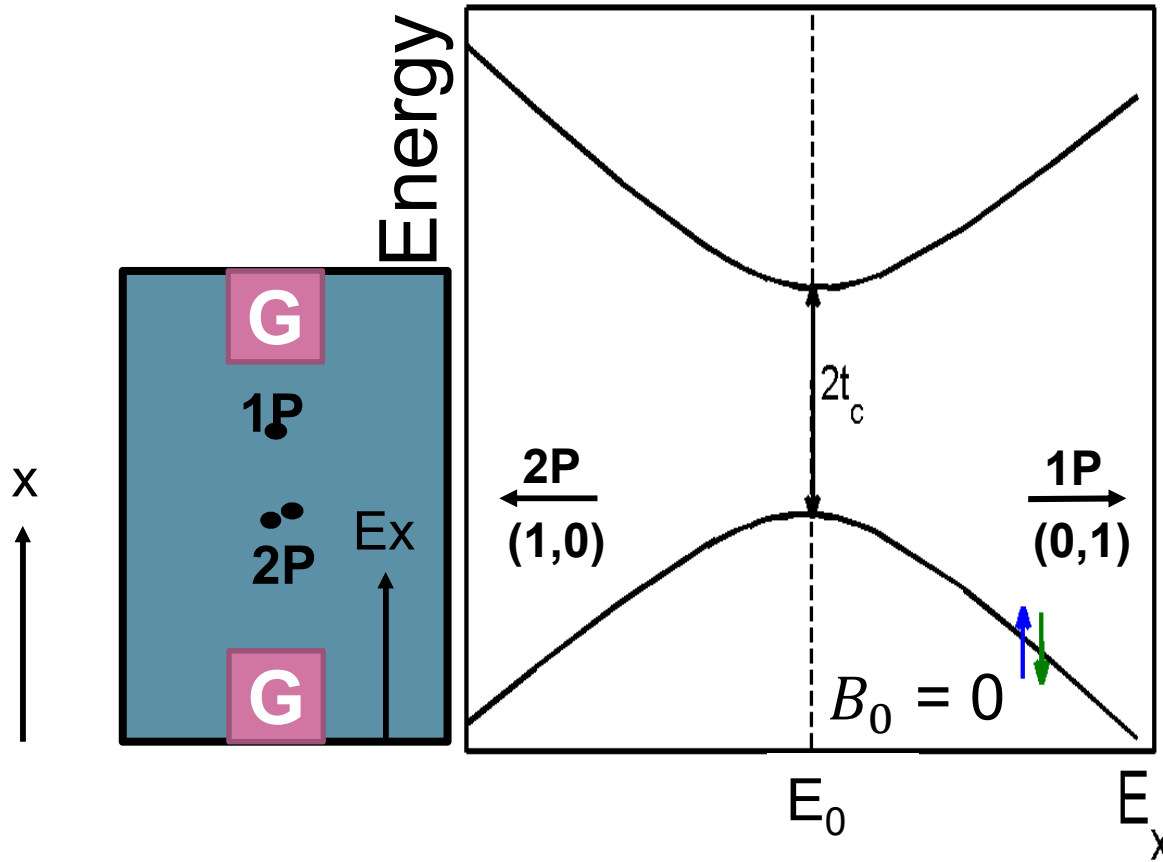
2. Long coherence time



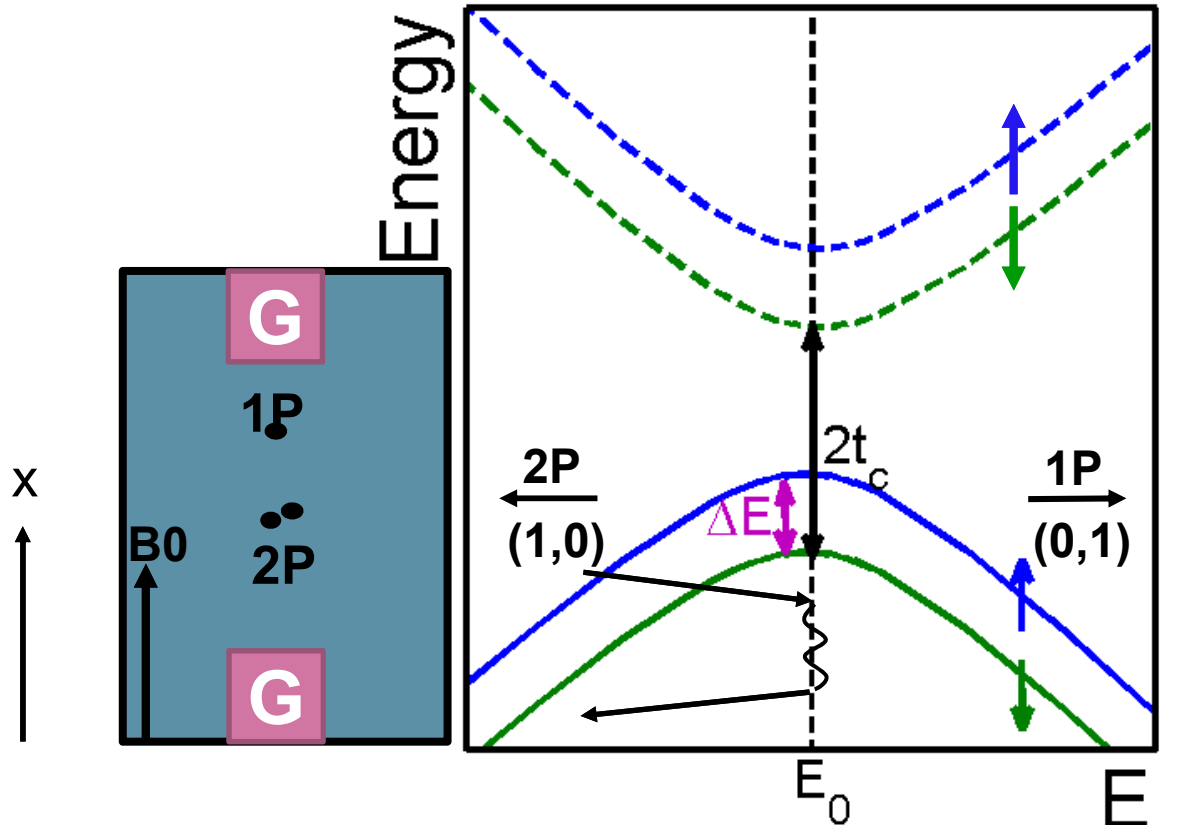
vs



Energy



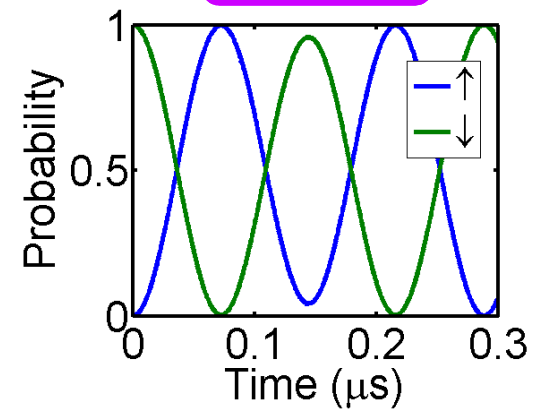
Charge + spin energy diagram



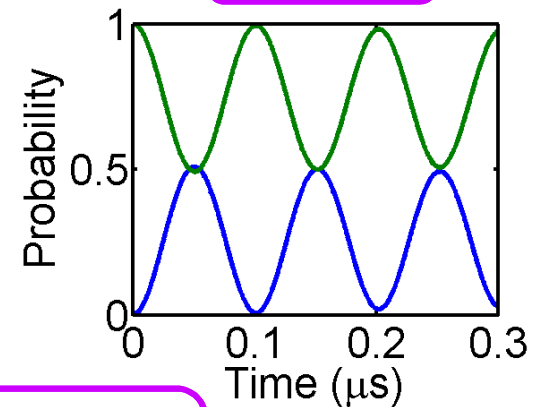
$\Delta E \propto B_0, B_0$: typically 0.1 – 2 T

**To achieve high control fidelity, $2t_c > \Delta E$ is needed.
How to engineer t_c ?**

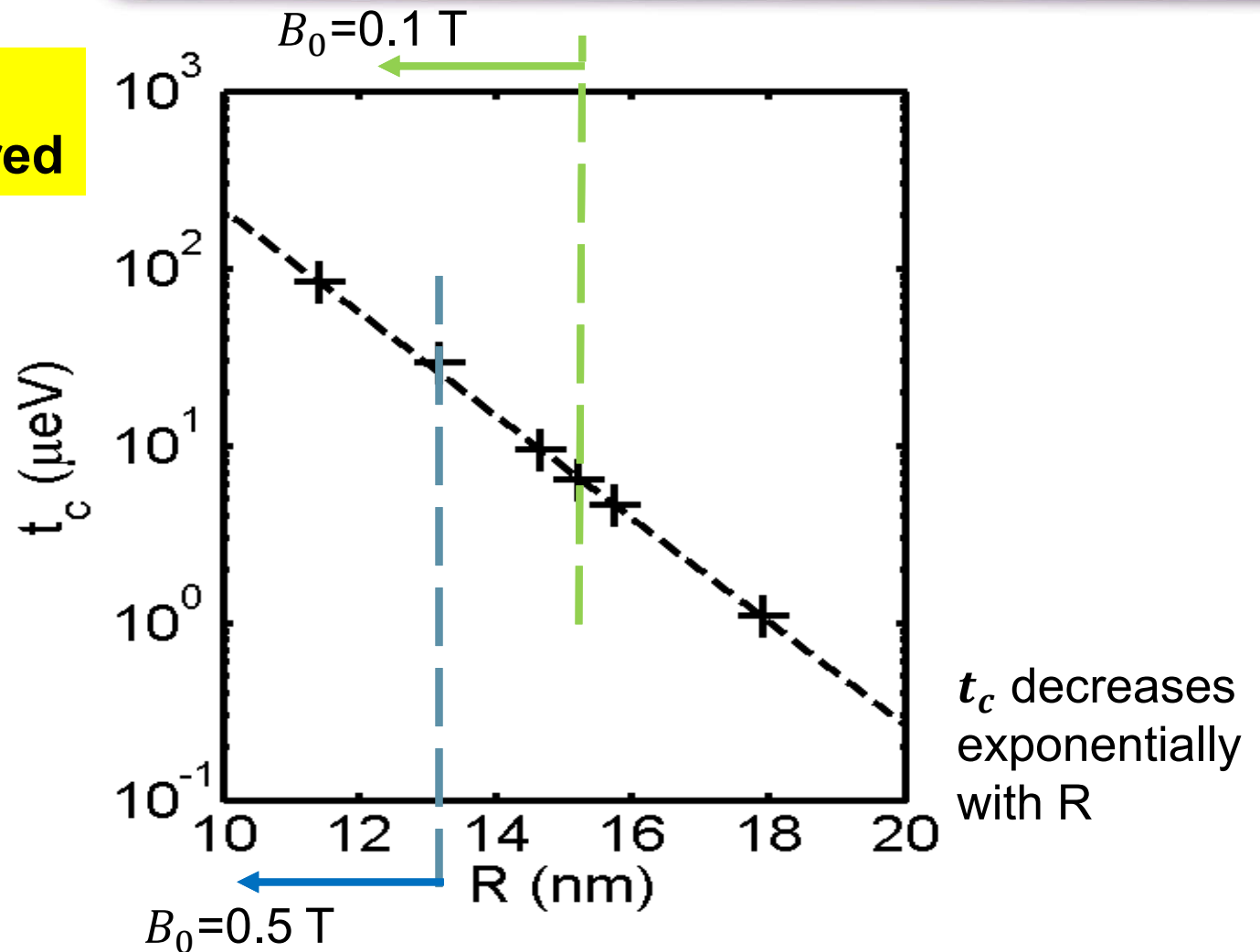
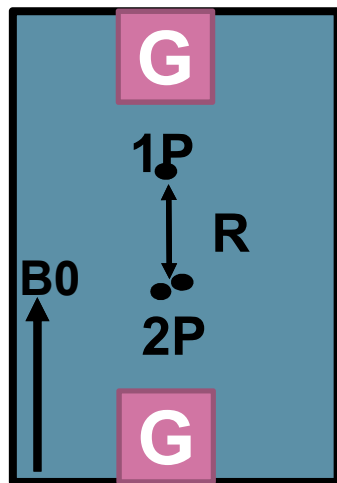
$$\Delta E < 2t_c$$



$$\Delta E \approx 2t_c$$

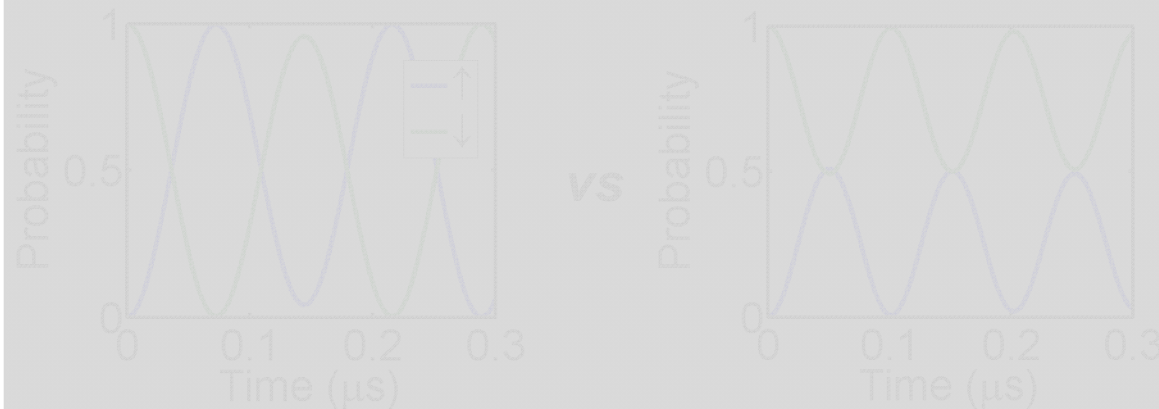


$\Delta E \propto B_0$,
 $\Delta E < 2t_c$ is required



To achieve high control fidelity, $R < 15\text{nm}$ is preferred.

1. High control fidelity

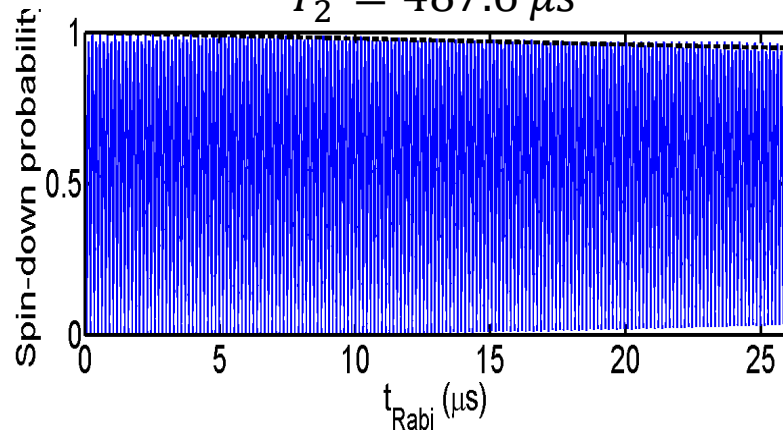


3. Long spin storage time (no operation)



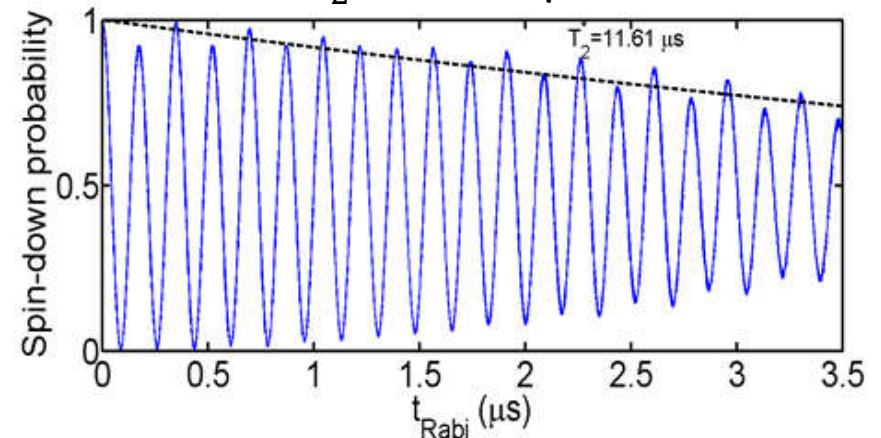
2. Long coherence time

$$T_2^* = 487.6 \mu\text{s}$$



vs

$$T_2^* = 11.61 \mu\text{s}$$

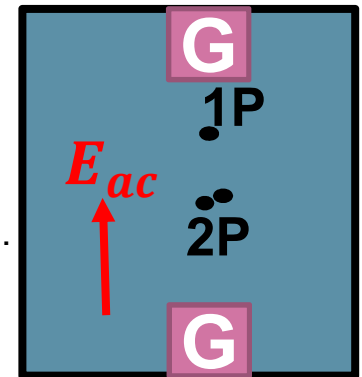


T_2^* : oscillation magnitude decays by e^{-1}

Proposed method to calculate coherence time under charge noise

$$\frac{1}{T_2^*} = \frac{q^2}{\hbar^2} |\langle \Psi_{\uparrow} | r | \Psi_{\uparrow} \rangle - \langle \Psi_{\downarrow} | r | \Psi_{\downarrow} \rangle|^2 \frac{S_E(\omega)}{\omega} \bigg|_{\omega \rightarrow 0} \frac{2k_B T}{\hbar}$$

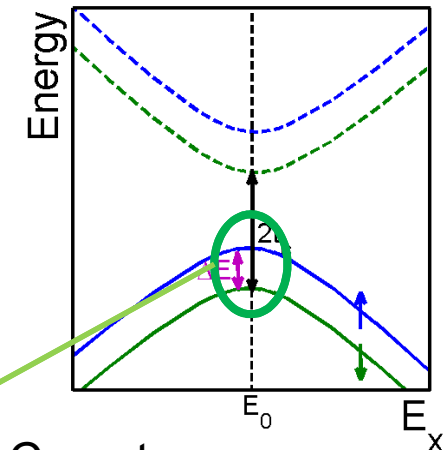
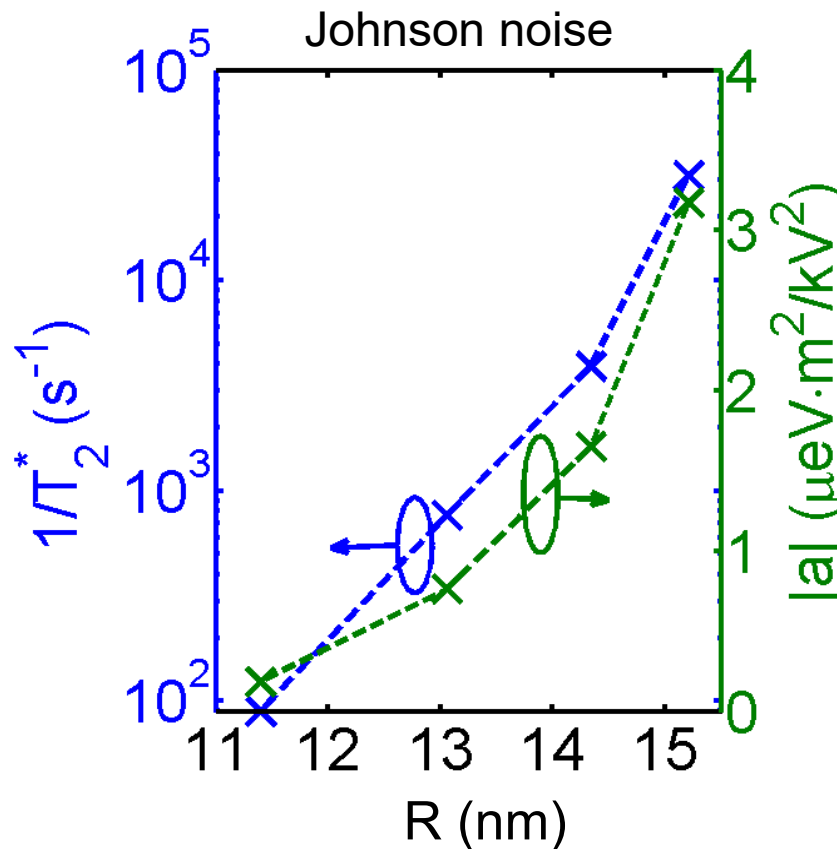
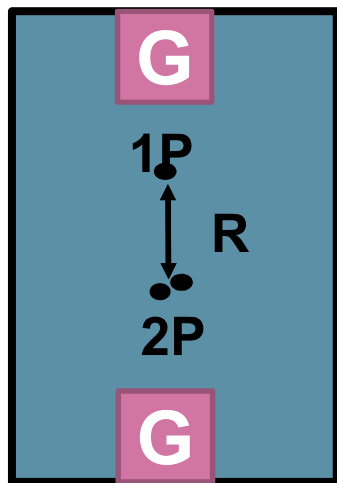
Chirolli & Burkard, Adv. in Phys., 57:3, 225-285 (2008).



- ❑ Atomistic molecular wavefunction with electric-field, magnetic field and spin-orbit interactions.
- ❑ $S_E(\omega)$: Charge noise power spectrum
1/f noise, Johnson noise, Evanescent wave Johnson noise

Noise spectrum Ref: P. Huang & X. Hu, PRB **89**, 195302 (2014)

Enabled decoherence calculation due to charge noise with an atomistic approach.

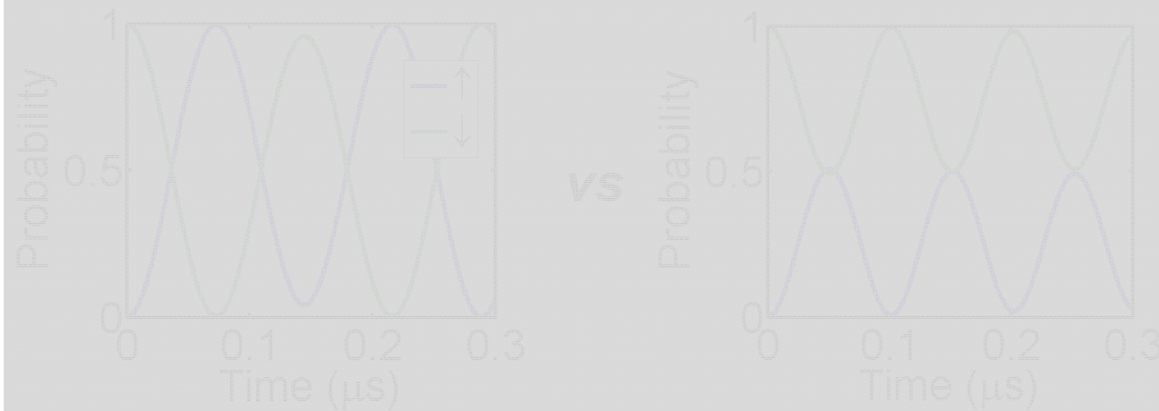


Curvature

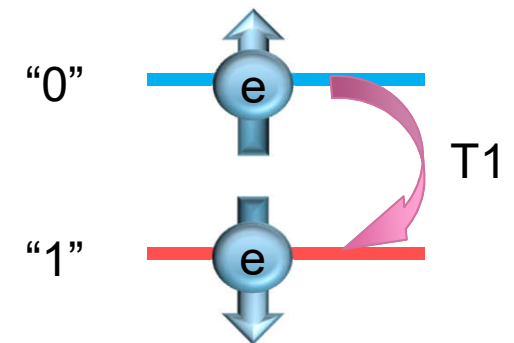
Larger curvature →
sharper charge
transition →
more prone to noise

Smaller R is more favorable to suppress qubit decoherence due to charge noise.

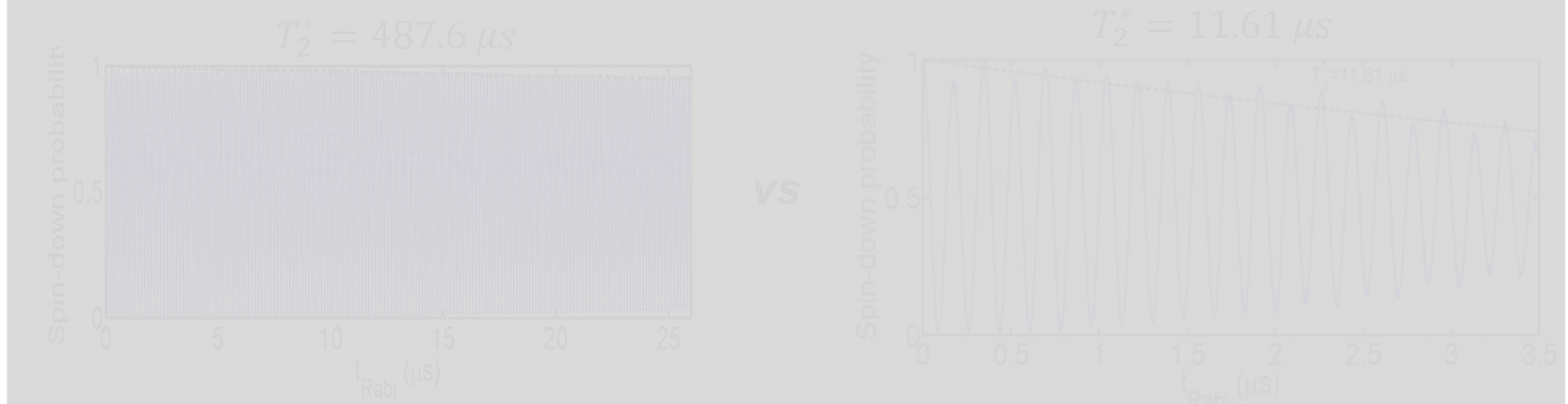
1. High control fidelity



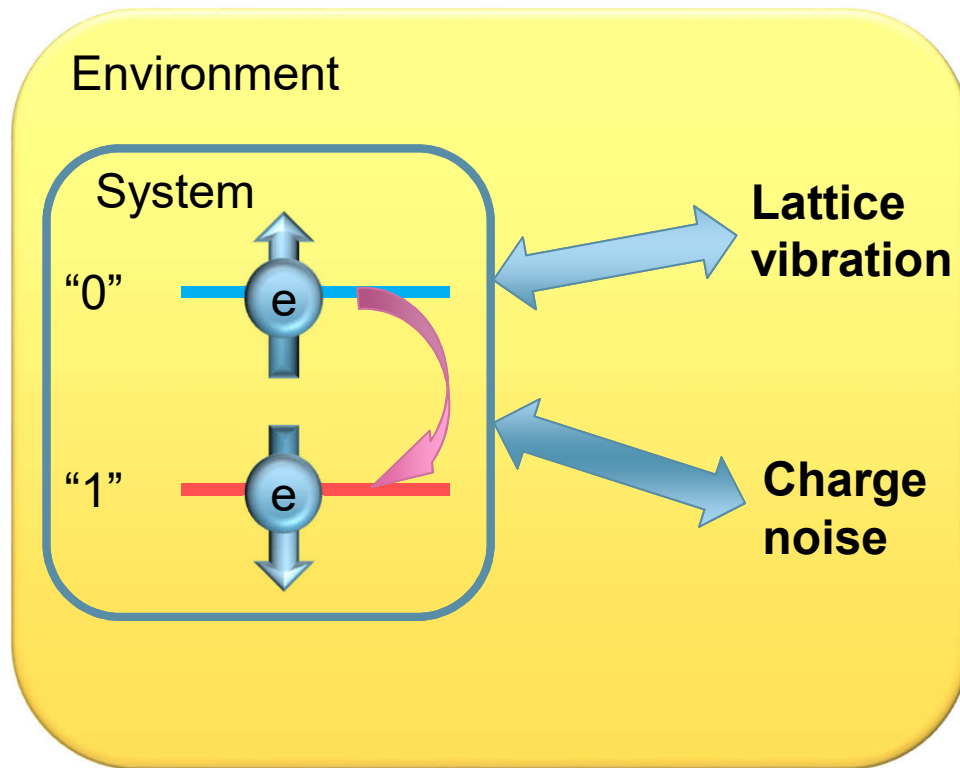
3. Long spin storage time (no operation)



2. Long coherence time

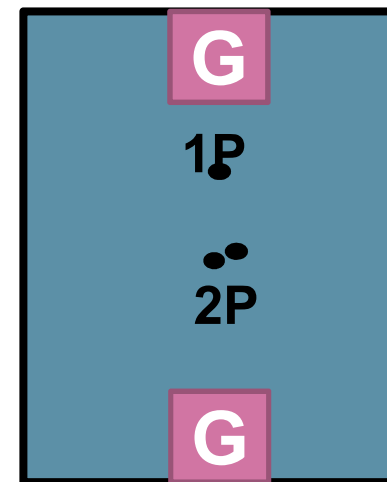


Spin relaxation

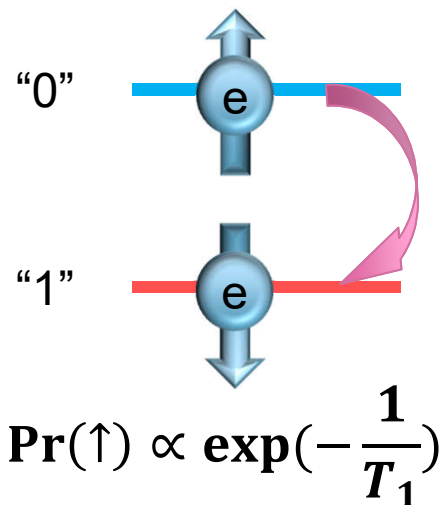


$$\text{Pr}(\uparrow) \propto \exp\left(-\frac{1}{T_1}\right)$$

- Spin relaxation is critical for information storage (T_1 as long as possible)

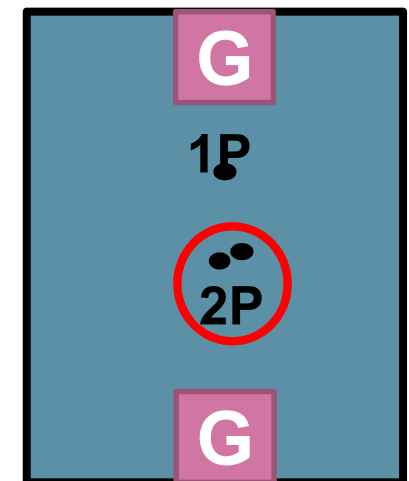


How to optimize T_1 for information storage?



□ Information storage: spin lifetime (T_1)

- $T_1(2P) \approx 30\text{s}$, $T_1(1P) \approx 4\text{s}$.
(Experiment: Watson et al., unpublished)

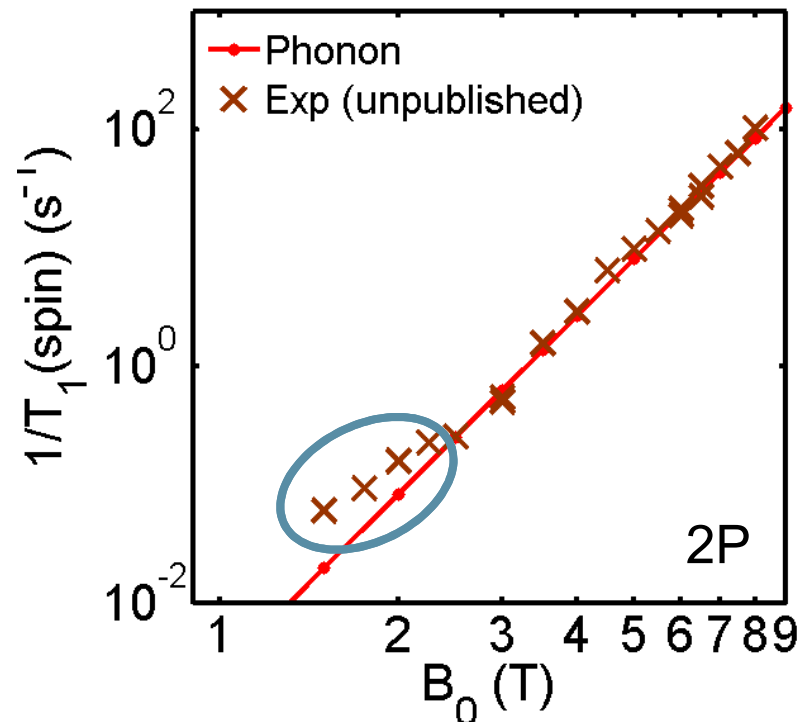


Qubit information is preferred to be stored in 2P.

What makes the spin relax?

- Mechanisms of spin relaxation:
 - Relaxation due to phonon

Hsueh et al., Phys. Rev. Lett. 113, 246406 (2014)



Exp. Data from T. Watson, unpublished.

Deviation at low B-field regime (<2.5T). Other mechanisms?

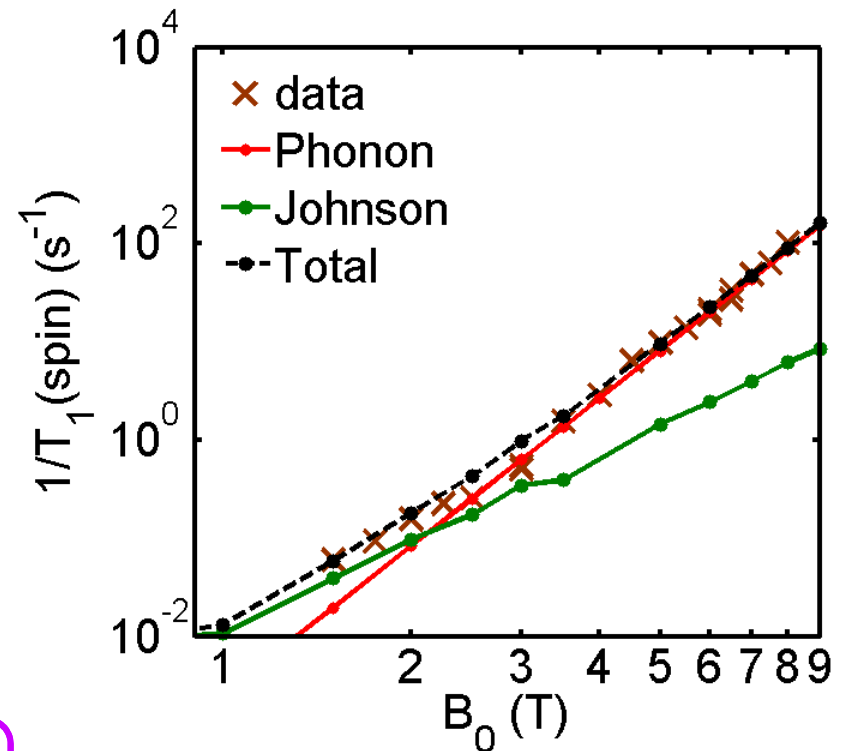
- Mechanisms of spin relaxation:
 - Relaxation due to phonon
 - Relaxation due to charge noise

- Developed formalism:

$$\frac{1}{T_1} = \frac{q^2 D D^*}{\hbar^2} S_E(\omega),$$

$$D = \sum_{o=x,y,z} \langle \Psi_{\downarrow} | o | \Psi_{\uparrow} \rangle$$

Deviation at low B-field regime is possibly due to charge noise.



Exp. Data from T. Watson, unpublished.

To optimize electrical control of 2P-1P based spin qubit

1. High control fidelity

-- optimization through R or t_c ($R < 15\text{nm}$)

2. Long coherence time

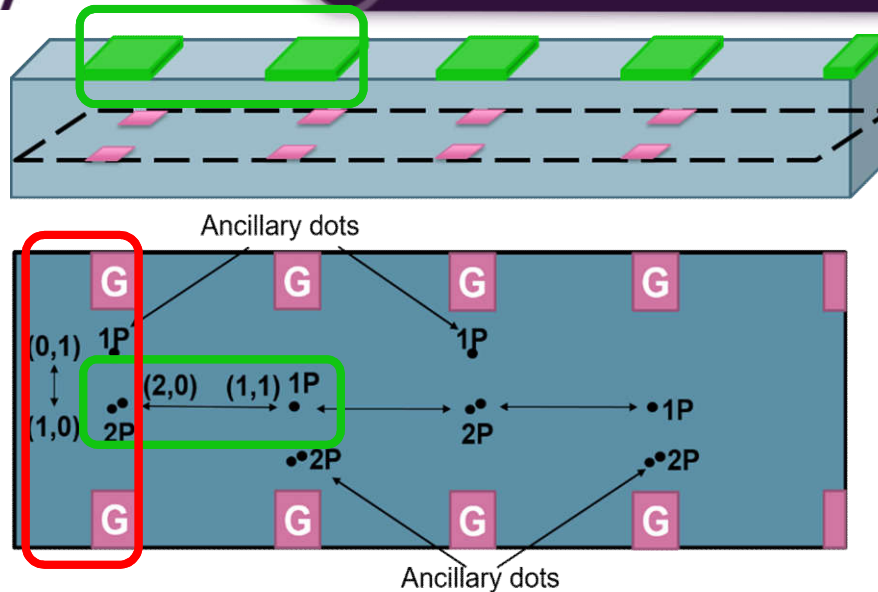
-- Johnson noise is the major influential factor

-- optimization through R or t_c (small R preferred)

3. Long spin storage time (no operation)

-- 2P is preferred

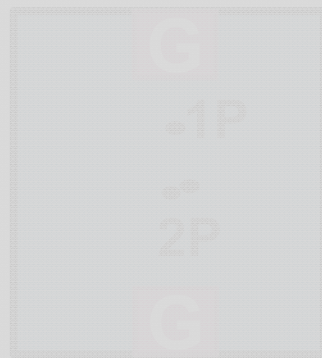
-- Johnson noise could be dominating over phonon in the low B-field regime



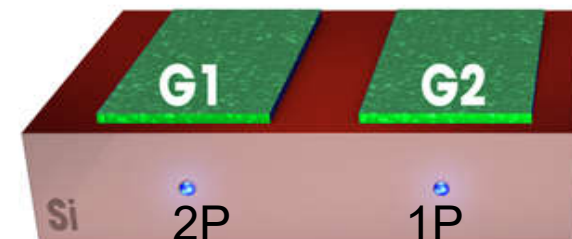
Overcome challenges in Kane's architecture

- ✓ Fabrication:
 - ✓ Gate separation
- ✓ All-electrical control
- ✓ Exchange tunability

All-electrical control of donor-based spin qubits



Engineering exchange coupling of two donor qubits

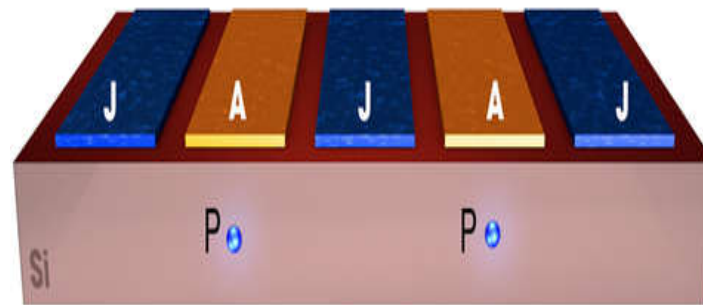


Challenges of realizing multiple-qubit operations using Kane architecture

Fabrication

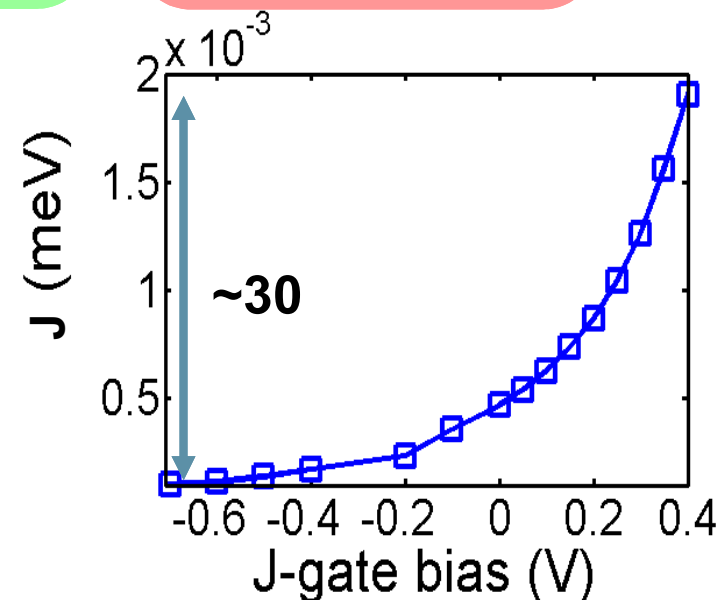
**Magnetic control
(single qubit)**

**Exchange control
(2 qubits)**

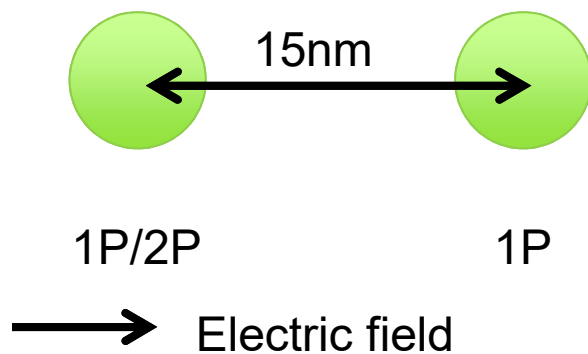


Kane, Nature 393, 133 (1998)

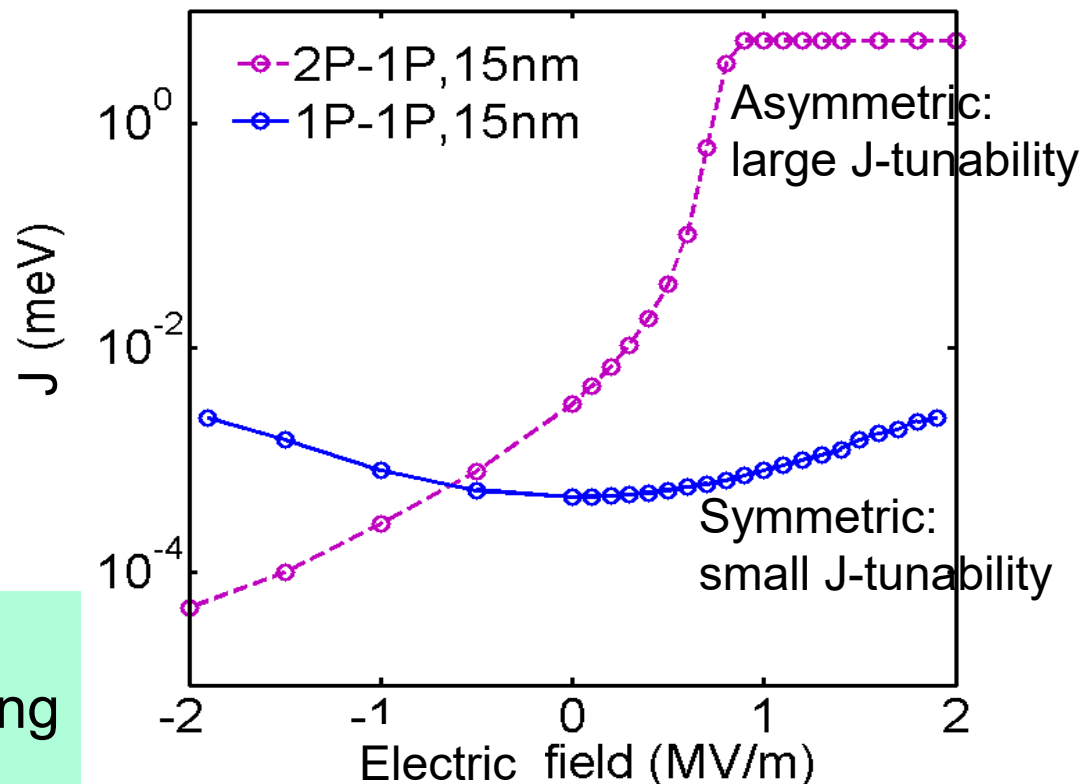
Does the 2P-1P system provide highly tunable exchange?



J tunability with E-field



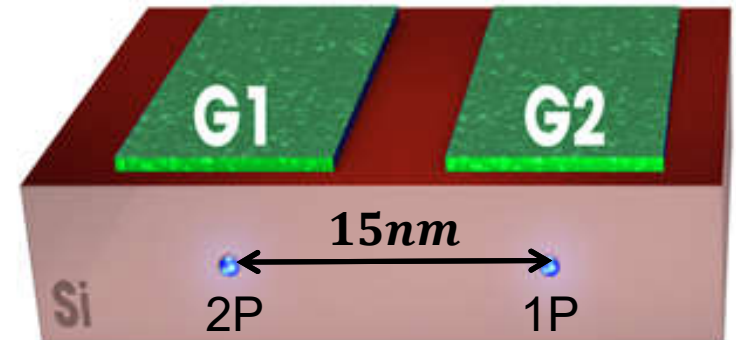
2P: the extra positive charge helps in attracting the 1P electron



Over **5** orders of magnitude J tunability can be achieved within **3MV/m** detuning field (**48 neV** to **5.5 meV**).

Asymmetric 2P-1P systems are promising to realize two-qubit gates.

- Using detuning gates is less challenging in fabrication.
- Exchange coupling can be tuned by over 5 orders of magnitude.



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ARTICLE OPEN

Highly tunable exchange in donor qubits in silicon

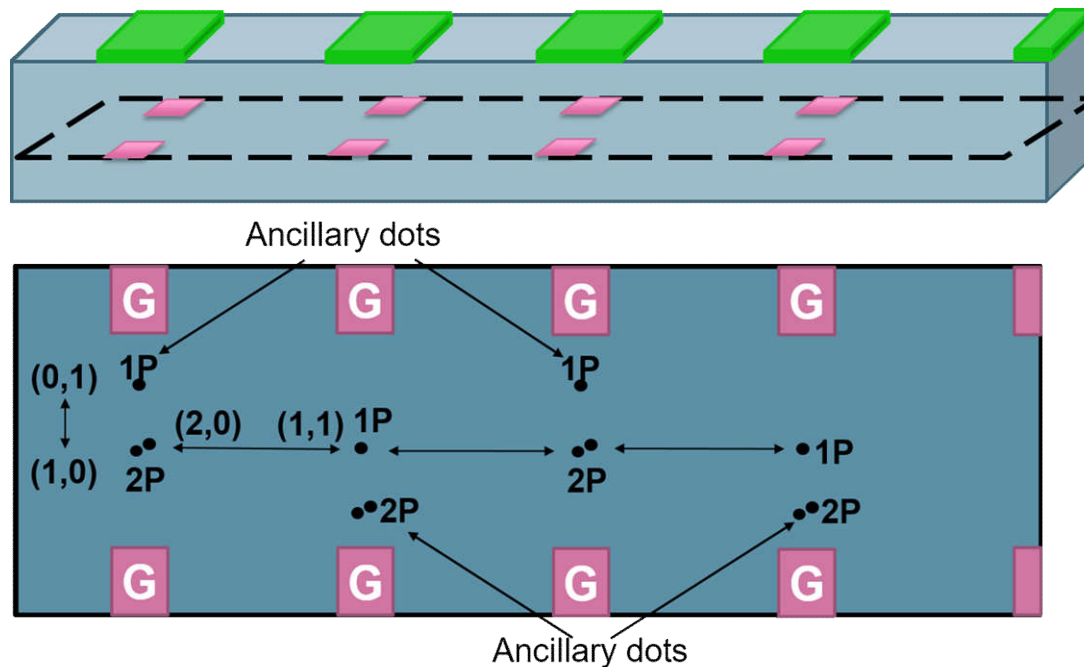
Yu Wang¹, Archana Tankasala¹, Lloyd CL Hollenberg², Gerhard Klimeck¹, Michelle Y Simmons³ and Rajib Rahman¹

npj Quantum Information (2016) 2, 16008; doi:10.1038/npjqi.2016.8; published online 12 April 2016

Lower Gate density

All-electrical control of spin qubits

High exchange tunability



A potentially scalable structure for donor-based spin qubits in silicon.

- Committee members:

Professor Gerhard Klimeck, Dr. Rajib Rahman, Professor Supriyo Datta, Professor Zhihong Chen, Professor Michelle Simmons

- Archana Tankasala, Pengyu Long, Yuling Hsueh, Harshad Sahasrabudhe, Rifat Ferdous, Chin-Yi Chen, Yaohua Tan, Kai Miao, Hesameddin Ilatikhameneh, Fan Chen, Tarek Ameen, Yu He, Junzhe Geng, Prasad Sarangapani, Yuanchen Chu, Zhengping Jiang, Jun Huang, Xufeng Wang, Kuang-chong Wang and all my colleagues
- Professor Lloyd Hollenberg, Professor Andrew Dzurak, Holger Buch, Bent Weber, Thomas Watson, Matthew House, Sam Hile, Matthew Broome, Charles D. Hill, Menno Velderhost, Kok Wai Chan, Henry Yang, Wister Huang, Jianjun Zhang, Chunming Yin
- Ms. Vicki Johnson, Ms. Leslie Schumacher, Ms. Ashley Byrne

Thank you!

Backup

- ❑ Characterizing Si:P quantum dot qubits with spin resonance techniques
-- Wang et al., Sci. Rep. 6, 31830 (2016)
- ❑ Exchange engineering in MOS triple quantum dots
- ❑ Optimizing tunnel time for high-fidelity spin readout
- ❑ Electronic structure of donor bound exciton in silicon

Problem:

- There exists uncertainty in the configuration of a donor-cluster
- ESR of donor-cluster qubits hasn't been demonstrated experimentally

Objective:

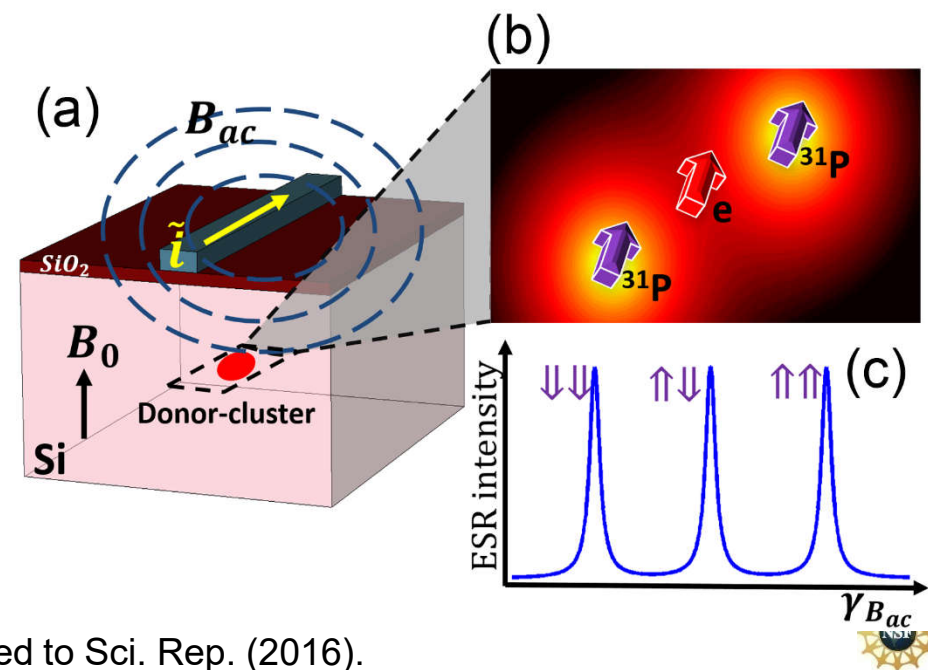
- To characterize and manipulate donor-cluster spin qubits

Results / Impact:

- A non-invasive characterization technique
- More reliable and robust compared to the existing method based on measuring charging energies

Approach:

- Using electron spin resonance (ESR) techniques to measure ESR frequencies
- Map out the configuration of a donor-cluster by experiment-theory comparison



Objective:

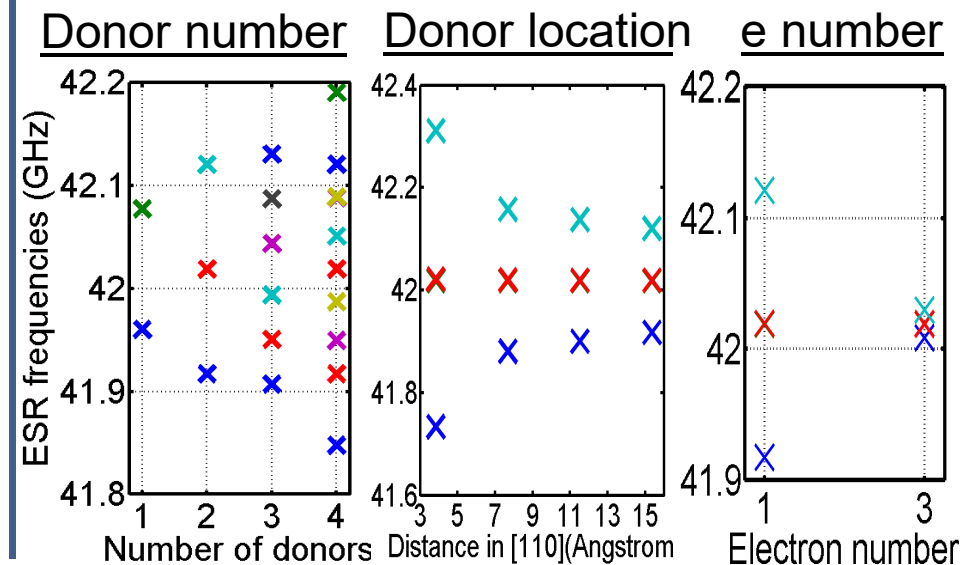
- To calculate the ESR spectra of donor-clusters with different donor numbers, locations and bound electron numbers

Results / Impact:

- Number of ESR frequencies goes up with number of donors.
- The separation of ESR frequencies decrease two-donor distance.
- The separations of ESR frequencies decrease with the bound electron number.

Approach:

- Obtain Fermi-contact hyperfine and dipolar interactions from atomistic tight-binding approach
- Obtain ESR spectra by solving effective spin Hamiltonian including Zeeman and hyperfine effects



Problem:

- To model a experimental device that has large active domain and multi-physics

Objective:

- To perform realistic simulations of electrostatics and electron wavefunction

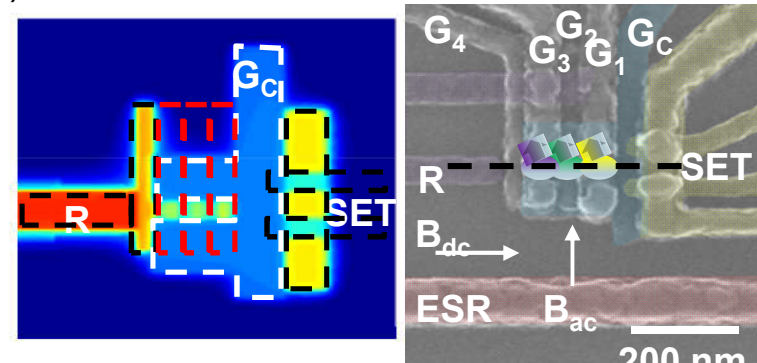
Results / Impact:

- The multi-scale modeling scheme can handle simulations in the scale of μm
- Device physics like interface trap, work function difference, bandgap narrowing, incomplete ionization can be captured

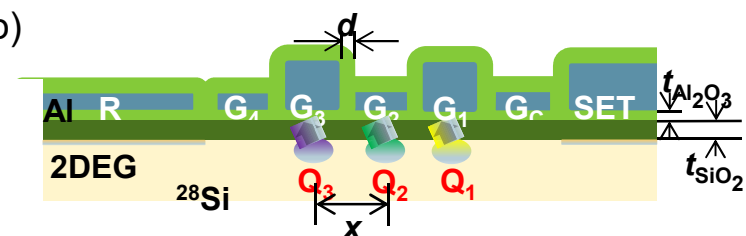
Approach:

- Multi-scale modeling:
 - Semi-classical self-consistent charge/potential solution in the framework of TCAD
 - Quantum wavefunction solution with atomistic tight-binding approach

(a)



(b)



Problem:

- To study the impact of device geometry on exchange energy

Objective:

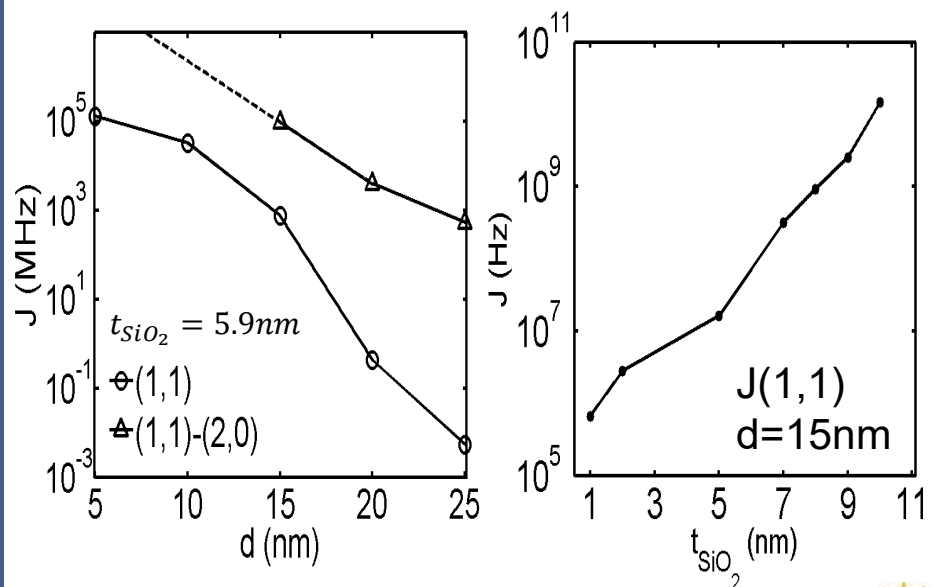
- To engineer and optimize exchange coupling in MOS quantum dot multi-qubit devices

Approach:

- A full configuration interaction (FCI) method for electron-electron exchange calculation, which accurately captures exchange and correlations, with the atomistic tight-binding basis.

Results / Impact:

- The residue $J((1,1))$ varies by ~ 7 orders of magnitude with $d = 5-25\text{nm}$; the active $J((1,1)-(2,0))$ is varied by ~ 2 orders of magnitude with $d = 15-25\text{nm}$; best match with experiment at $d = 23-24\text{nm}$
- $J((1,1))$ varies by ~ 4 orders of magnitude with t_{SiO_2}



Problem:

- Optical readout haven't been utilized in single donor spin qubits.

Objective:

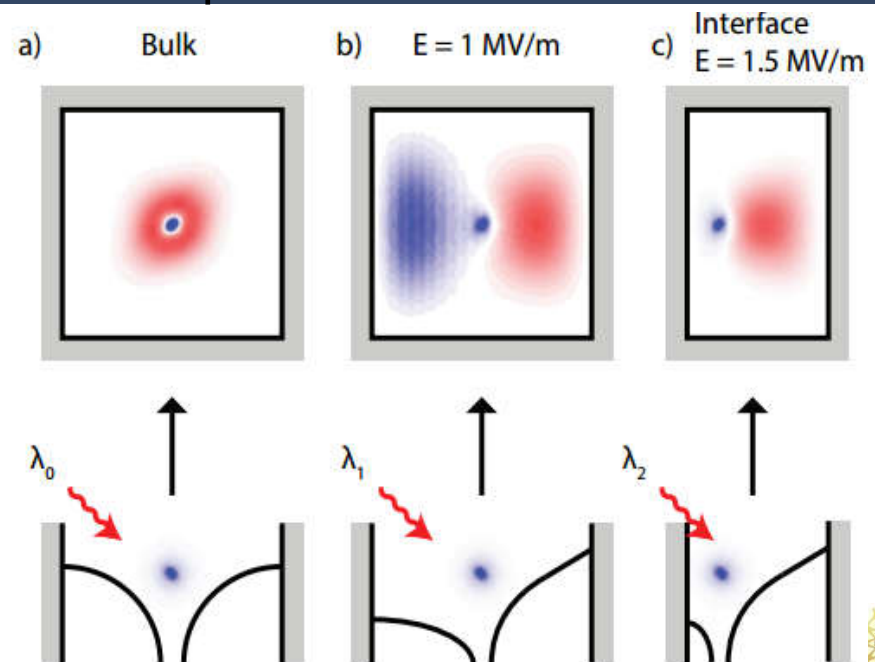
- To investigate the electronic structure of D^0X in silicon under the influence of electric fields and interfaces.

Approach:

- Atomistic tight-binding approach for electron and hole wavefunctions
- Developed Hartree self-consistent field method for three-particle ($2e+1h$) quantum solutions

Results / Impact:

- The calculated bulk transition energy (1145meV) is close to the reported experimental measurements (~1150meV)
- Provide quantitative guidance to experiments aiming to realize hybrid opto-electric techniques for addressing donor qubits



Problem:

- A comprehensive quantitative theory that can provide design guidance for spin readout devices using a quantum mechanical description is lacking.

Objective:

- To interpret the tunnel time of experiment qubit devices.

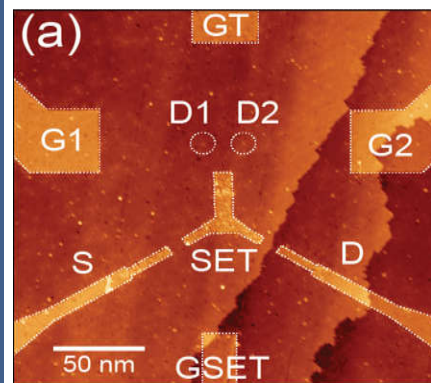
Results / Impact:

- Proposed a comprehensive theory based on atomistic modeling for tunneling time calculation in spin readout devices.
- Bandgap narrowing effect can be captured

Approach:

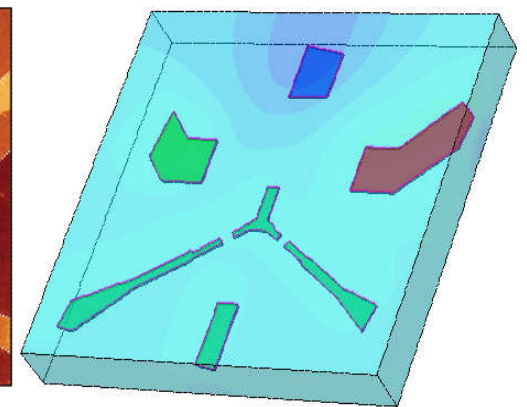
- Multi-scale modeling:
 - Semi-classical approach for the electrostatic solution of the SET island in the framework of Sentaurus TCAD tool.
 - Atomistic tight-binding for donor and SET wavefunction

Experiment



T. Watson et al., Phys. Rev. Lett. 115, 166806 (2015)

TCAD modeling



Problem:

- To optimize the tunnel time for single-shot readout to achieve high-fidelity

Objective:

- Provide guidelines for SET-donor separation to achieve high-fidelity spin readout

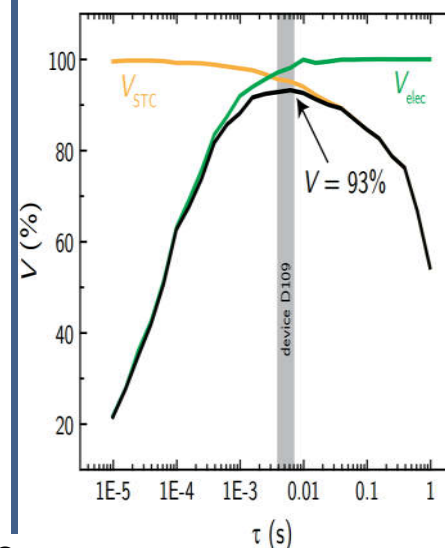
Results / Impact:

- Proposed a comprehensive theory based on atomistic modeling for tunnel time calculations
- The tunneling time between the qubit and the SET island can vary by ~ 5 orders of magnitude with their separation changing by ~ 10 nm, and is sensitive to the qubit net charge

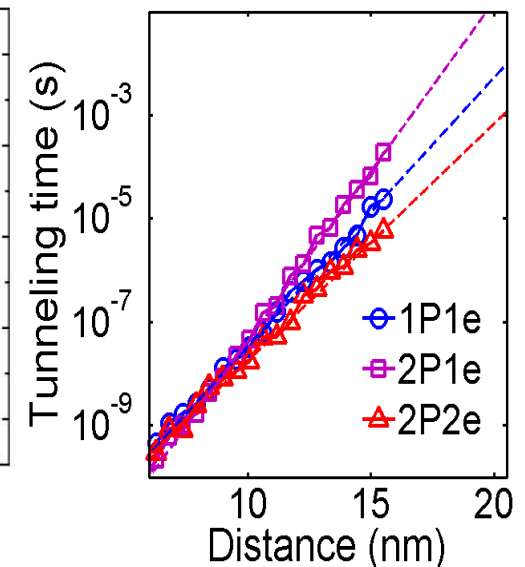
Approach:

- Utilize the impurity model in the frame work of atomistic tight-binding approach
- Hartree self-consistent field approach to capture multi-electron occupation
- Use Bardeen's tunneling theory to calculate tunnel time

Fidelity vs tunnel time



Calculation



Problem:

- Two-qubit logic haven't been demonstrated with donor-based spin qubits

Objective:

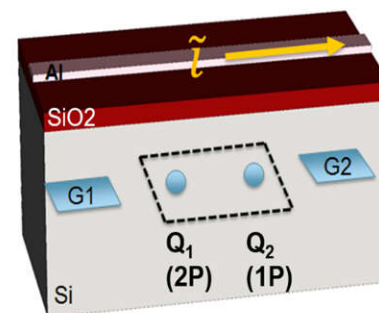
- To provide guideline for realizing a CNOT gate with donor-based qubits experimentally

Results / Impact:

- Theoretical evidence that a CNOT gate is feasible with donor-based qubits
- Provide guidelines to optimization for experiments.

Approach:

- Use ESR to address individual spin qubits.
- Use detuning bias to control the exchange coupling between the two qubits
- Modeling: atomistic tight-binding + configuration interaction + effective spin Hamiltonian



- CNOT is realized with $J \sim 26 \text{ GHz}$ and $\tau_Z \sim 294.77 \text{ ns}$

