

Tight binding parameterization from *ab-initio* calculations and its application

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Motivation for Empirical Tight Binding (ETB)

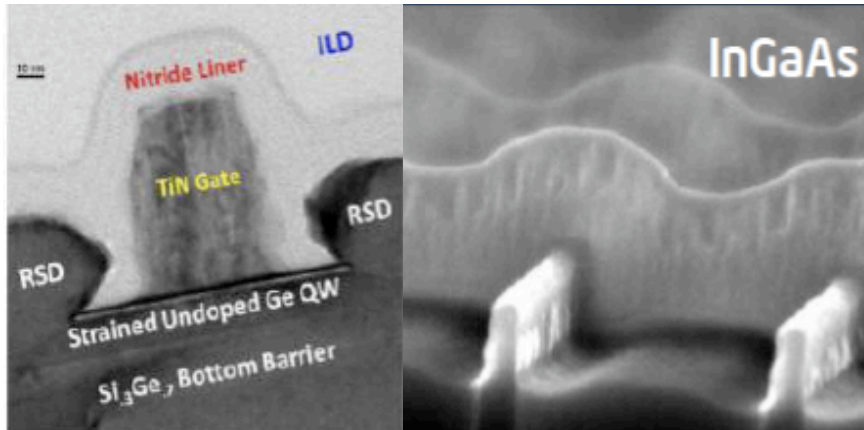
Shortcomings of ETB

Solutions for ETB's shortcomings

Summary & Outlook

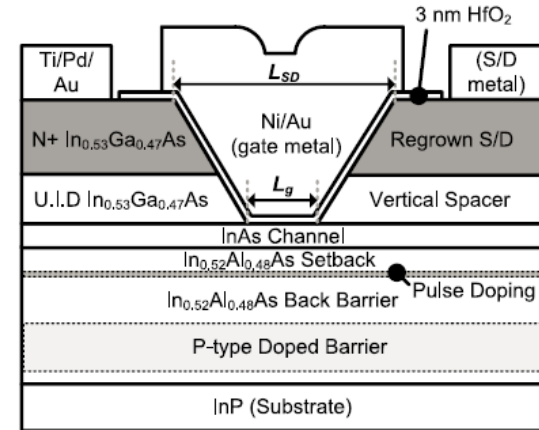
Motivation for Empirical Tight Binding (ETB)

Device fabrication



<http://nextbigfuture.com/2011/06/intel-roadmap-from-june-2011-with-7nm.html>

Device design

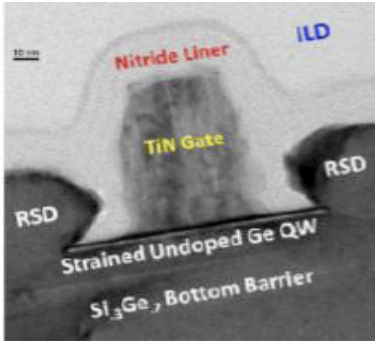


S. Lee, et al. IEEE. Trans. Elect. Dev. Lett, Vol 35, p 621 (2014)

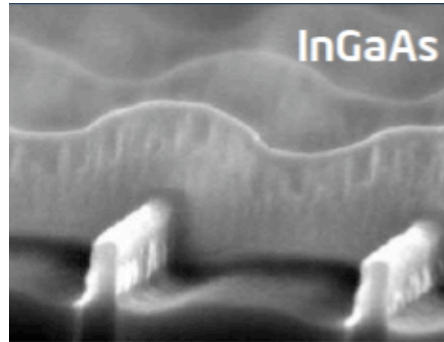
How to understand device performance?

How to predict device performance?

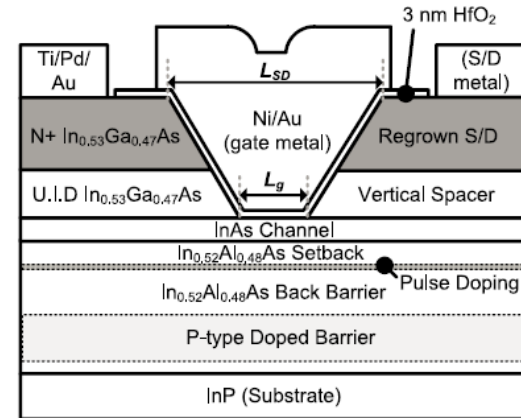
Device level simulations are needed to understand and predict nanoscale device performance.



Strained materials



Low dimensional structures



interfaces

Complicated systems

- Complicated geometries
- Multiple materials
- Strain, Interfaces, disorders

Transferable model

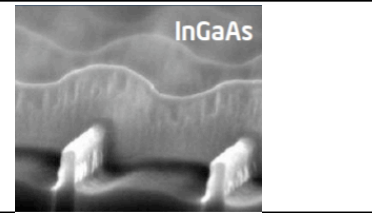
Challenging simulation domain

- 10000 ~ 10 million atoms (active domain)

Computationally efficient model

What model can we use for device level simulations?

To simulate a real device



Ab-initio methods

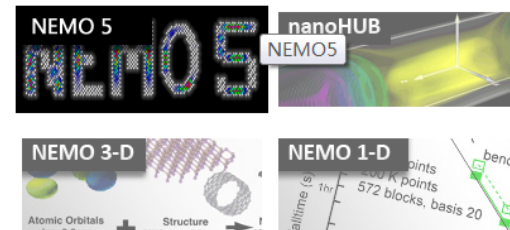
- First principle
- Use fundamental material information
- A few parameters
- Provide physical insights (Ek, wave functions)

Empirical methods, e.g. empirical tight binding (ETB)

- Requires fitting parameters,
- Have been applied to device level simulations

accuracy and computational capability are being improved

Software

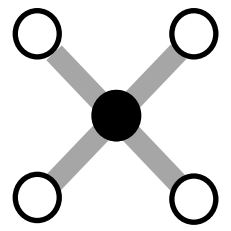
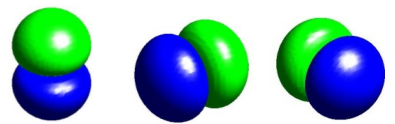


Why are ETB models so efficient?

s orbital



p orbitals



$$H_{s,s} = V_{ss\sigma}$$

$$H_{x,y} = lm(V_{pp\sigma} - V_{pp\pi})$$

A few Localized basis functions per atom

- $Y_{lm}(\theta, \varphi)R_{n,l}(r)$
- 10~20 per atom
- No explicitly $R_{n,l}(r)$

Short range Interactions

- Nearest neighbors interactions

Empirical method

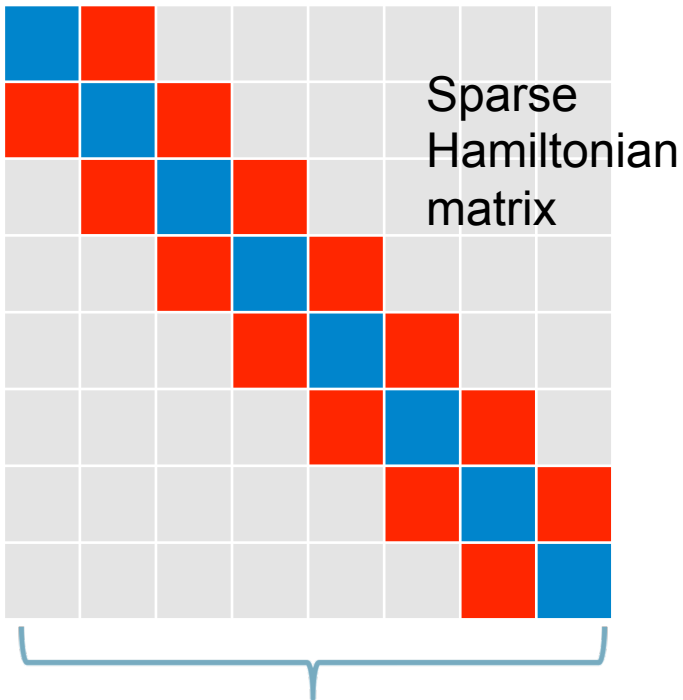
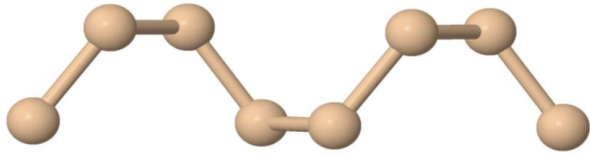
- Slater Koster type formula with **fitting parameters**

Hamiltonian Matrix size:
 $N_{\text{atom}} N_{\text{orbitals}}$

Sparse Hamiltonian matrix

Fast Hamiltonian construction

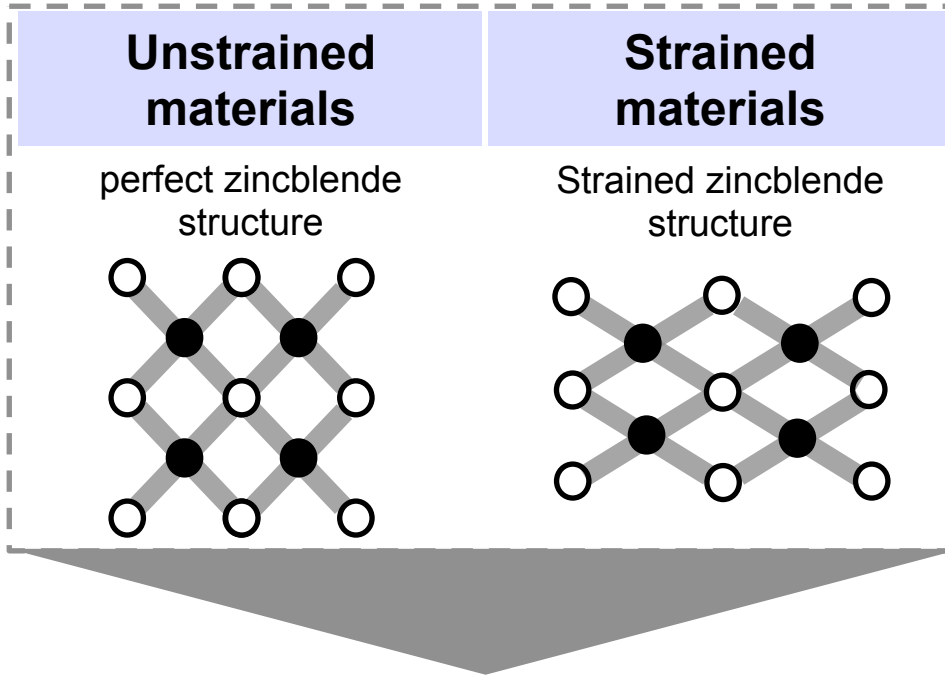
How does ETB Hamiltonian look like?



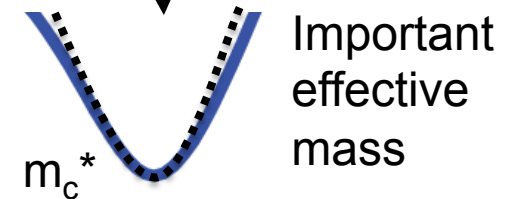
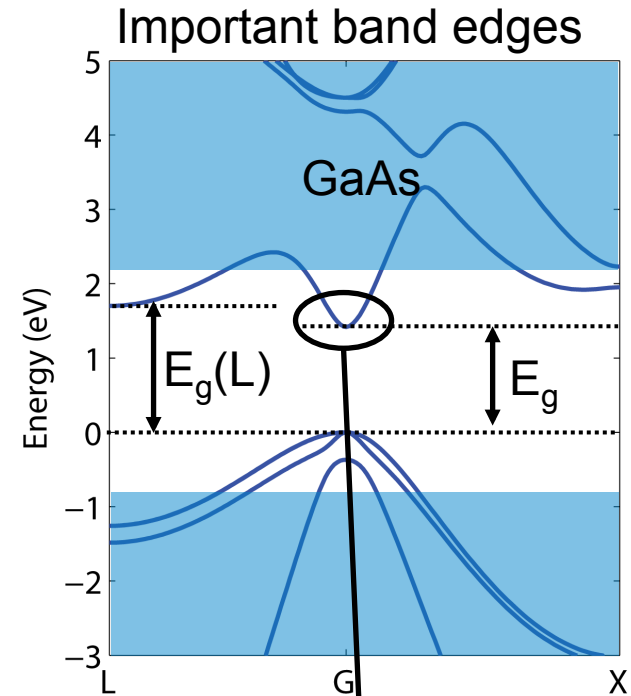
$N_{\text{atom}} N_{\text{orbitals}}$

- **Materials** → parameters
 - **Atoms** → onsite blocks ■
 - **Bonds** → interatomic interactions ■

How do we get the parameters for the ETB model?



ETB parameters:
Fit to theoretical or experimental
band structures



ETB models parameterized by traditional fitting have problems!

Shortcomings of ETB

ETB shortcomings

1 Unphysical results in confined structures

2 Ambiguity for heterostructures

Ideal/Simple systems

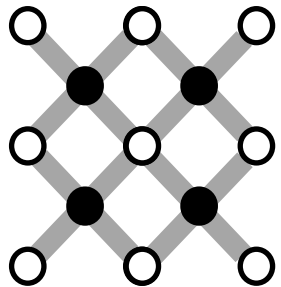
Realistic/Complicated systems

Unstrained materials

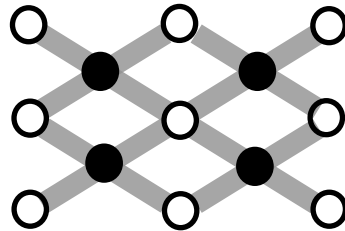
Strained materials

Strained nano structures, heterojunctions ...

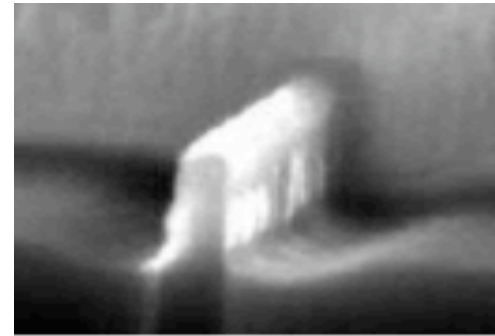
perfect zincblende structure



Strained zincblende structure



nanostructures



ETB parameters:
Fit to theoretical and experimental
band structures

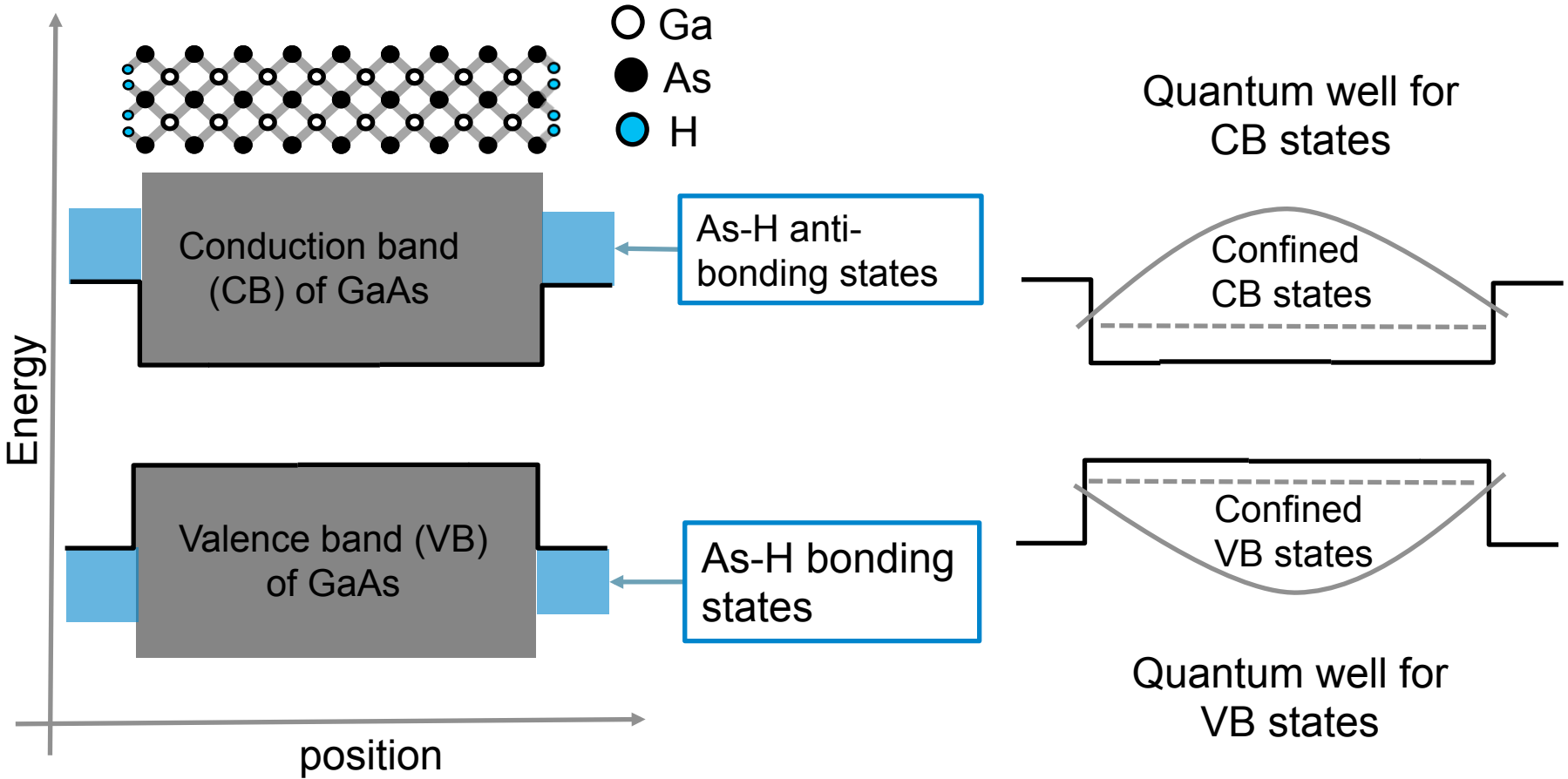
Are ETB models good enough for nanostructures?

- **Confined structures (Problem 1)**
- **Hetero structures (Problem 2)**

ETB shortcomings

1 Unphysical results in confined structures

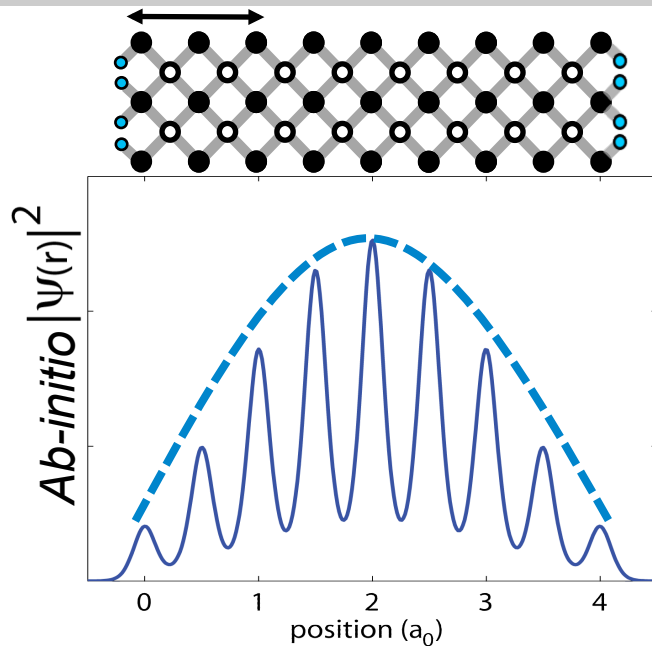
2 Ambiguity for heterostructures



Confined CB and VB states are expected in H-passivated UTBs

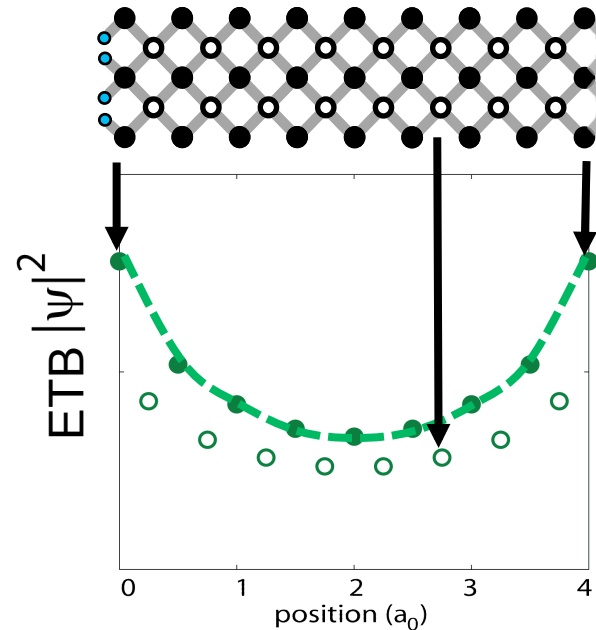
Top VB states in a As terminated GaAs UTB

Ab-initio wave function



- **Confined states**
- Explicit passivation

ETB wave function (existing model/parameters)



ETB ref : T. Boykin et al. PRB 66, 125207 (2002).

- **Un-confined states**
- Implicit passivation

Existing ETB model/parameters
 → unphysical states in some nanostructures

ETB shortcomings

1 Unphysical results in confined structures

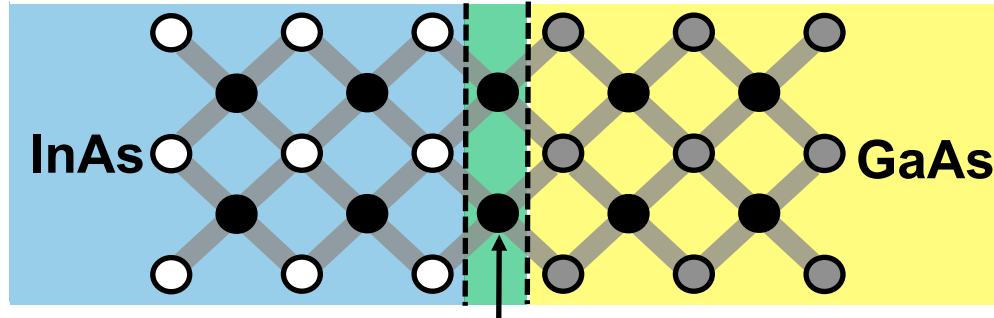
2 Ambiguity for heterostructures

ETB shortcomings

1 Unphysical results in confined structures

2 Ambiguity for heterostructures

Assumption 3



Interface As atoms \rightarrow average of GaAs and InAs

$$E_{As}(\text{interface}) = (E_{As}(\text{GaAs}) + E_{As}(\text{InAs}))/2$$

based on
assumption
without
validation

$$E_{As}(\text{GaAs}) \neq E_{As}(\text{InAs})$$

$$E_{As}(\text{interface}) =$$

$$E_{As}(\text{GaAs})$$

$$E_{As}(\text{InAs})$$

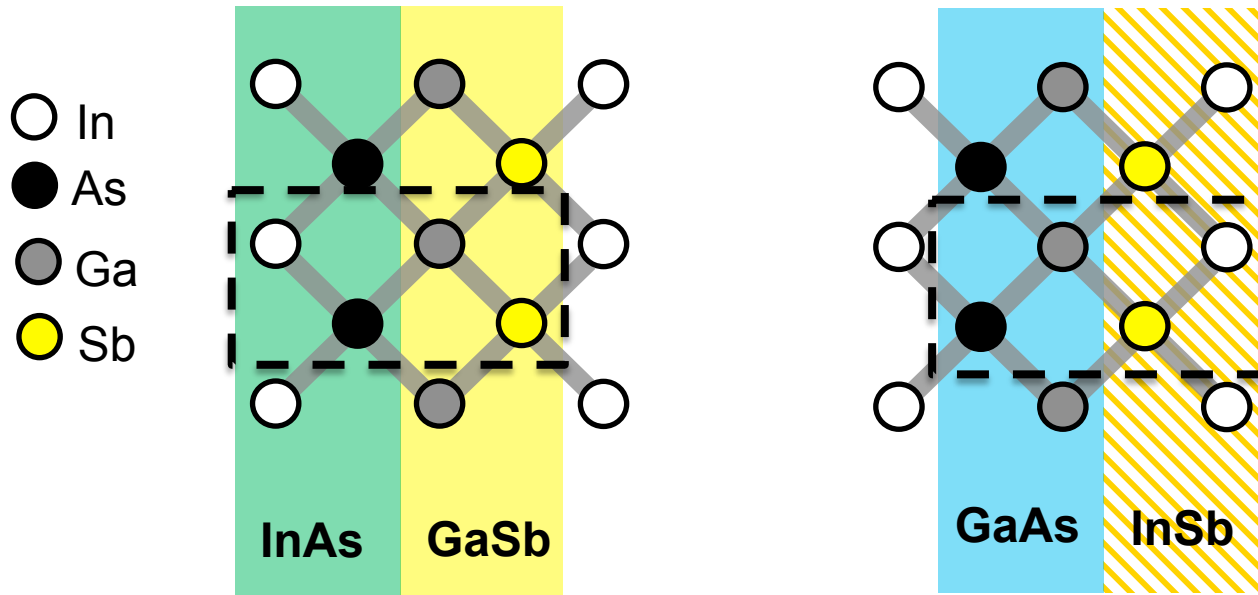
$$(E_{As}(\text{GaAs}) + E_{As}(\text{InAs}))/2$$

?

Traditional ETB parameters at interface are not clearly defined \rightarrow ambiguous results.

Ultra small InAs/GaSb superlattice

- Four different atoms, no common cation/anions
- Or GaAs/InSb superlattice
- Where are interfaces? (Everywhere)



Traditional ETB parameters at interface are not clearly defined → ambiguous results.

Solutions for ETB's shortcomings

Problems of traditional ETB

1. Unphysical wave functions in UTBs

2. Ambiguities at material interfaces

Can we solve these problems without losing efficiency?

- Keep number of basis functions
- Keep interaction range (1st nearest neighbors)

Solutions and applications

- Parameterization algorithm from *ab-initio* calculations
- Application to unstrained bulk
- Application to ultra thin bodies (UTBs)

- Environment dependent strain model
- Transferability to interface

ETB model : $sp^3d^5s^*$ +SO with 1st nearest neighbor interactions

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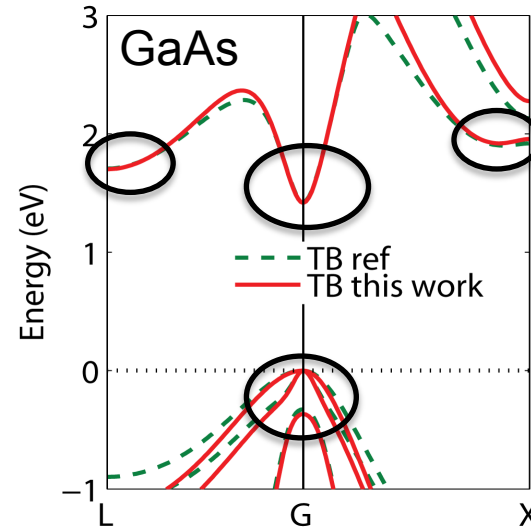
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5 Transferability to interface

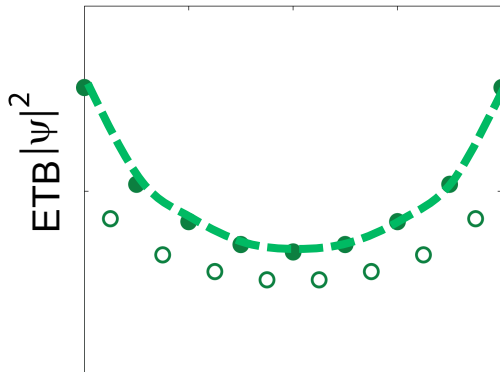
Ambiguous ETB parameters from traditional parameterization

- Different parameter sets exist
- Fitted to the same targets (band structures)
- Almost identical band structure ~ Very different parameters

- Degree of freedom exist in pure band structure fitting.
- More fitting targets can be included



TB ref : T. Boykin et al.
PRB 66, 125207 (2002).



Problematic ETB wave functions



Include wave functions into fitting

Traditional way

Fitting to experimental band structures.

Problems:

- Ambiguous parameter sets
- Unphysical results in some applications

Not enough physical insights are considered in fitting

This work

Ab-initio calculations
+ TB parameters construction

Advantages:

- Physical insights from *ab-initio* wave functions
- ETB wave functions match *ab-initio* ones

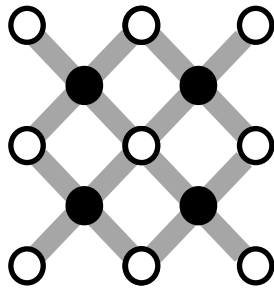
Less empirical parameters

- Efficiency of the ETB model maintained.

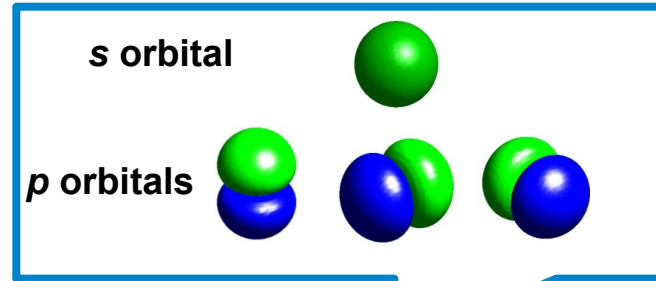
How to relate ETB wave functions to *ab-initio* ones?

- ETB basis functions

Unstrained materials



ETB parameters:
Fit to theoretical or experimental
band structures



Basis function: $Y_{lm}(\theta, \varphi)R_{n,l}(r)$


Can not get $R_{n,l}(r)$:

- No fitting parameters for $R_{n,l}(r)$
- No targets requires basis functions

**Radial parts of the basis functions
in traditional ETB are missing**

1. *ab-initio* calculations $\rightarrow E(k), \varphi(r), H_{ab-initio}$
2. initial TB basis functions \square \rightarrow radial part $R(r)$ only
initial TB Hamiltonian H
3. Represent *ab-initio* wave functions on ETB basis functions
4. Solve TB band structures and wave functions
5. Compare the TB band structures and wave functions to *ab-initio* targets;
6. Reconstruct exact TB basis functions.

Iteratively optimize the TB basis functions and Hamiltonian



Inputs: *ab-initio* band structures and wave functions

Outputs: TB parameters, TB basis functions

In the fitting process,

- match TB band structure and **wave functions** with *ab-initio* results.

Solutions and applications

1 Parameterization algorithm from *ab-initio* calculations

2 Application to unstrained bulk

3 Application to ultra thin bodies (UTBs)

4 Environment dependent strain model

5 Transferability to interface

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2 **Application to unstrained bulk**

3 Application to ultra thin bodies (UTBs)

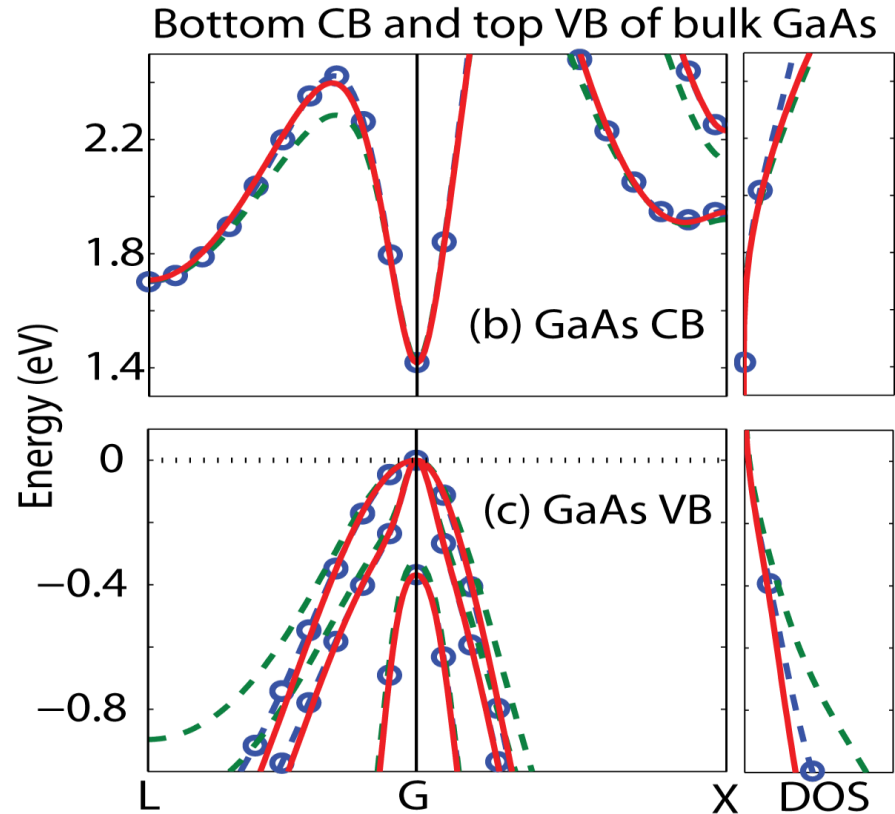
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Bulk GaAs

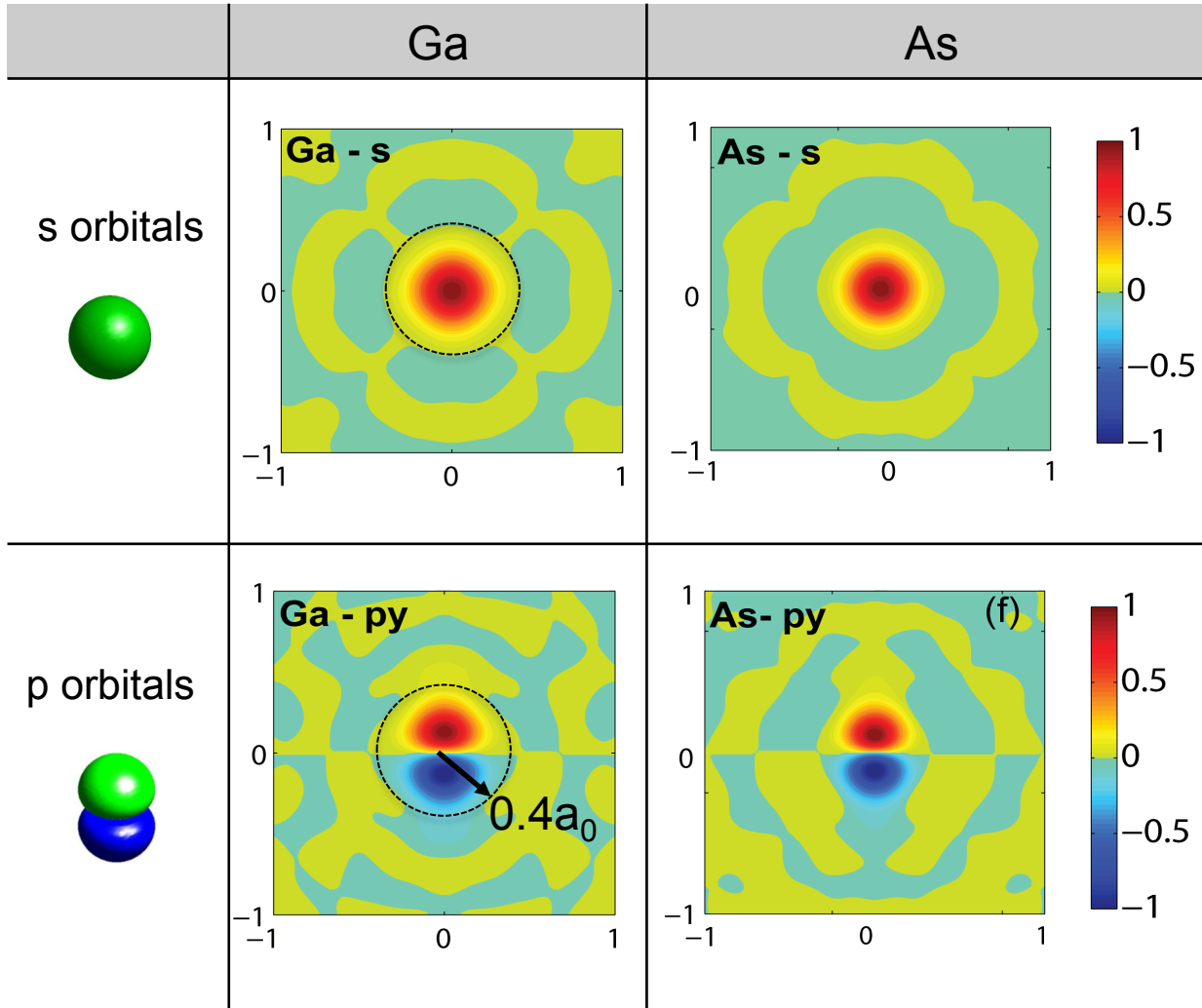
sp3d5s* ETB model + nearest neighbor interactions.

ETB ref : T. Boykin et al. PRB 66, 125207 (2002).



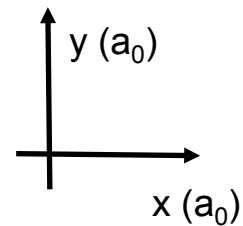
ETB band agree with HSE06 calculations in bulk case

HSE06 is a kind of hybrid functional used in *ab-initio* calculations.



ETB basis functions:

- Have the feature of sp(d) orbitals
- Highly localized (within $0.4a_0$)



Highly localized ETB basis functions are obtained

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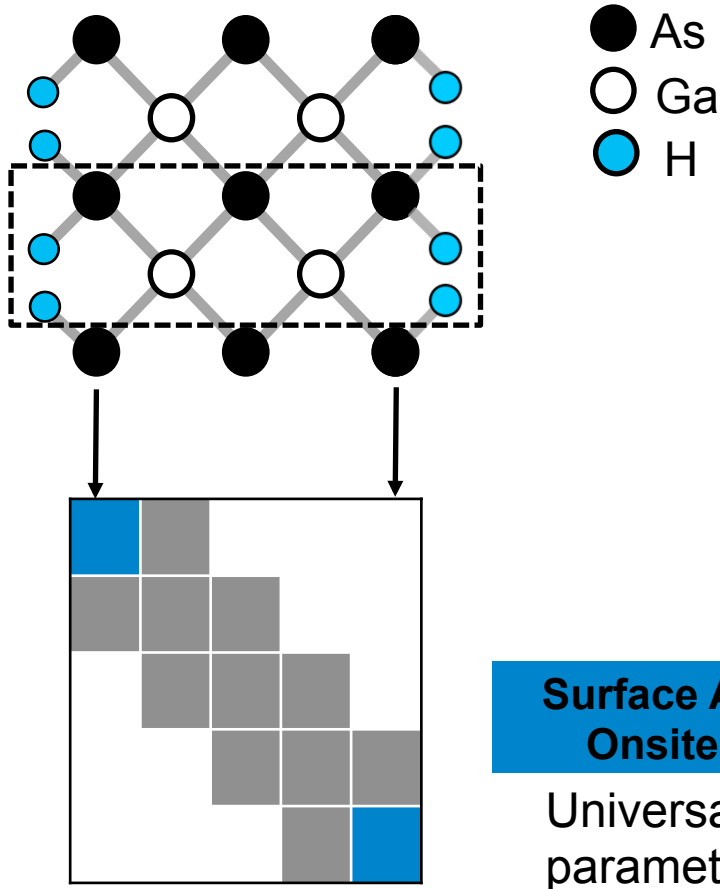
2 Application to unstrained bulk

3 **Application to ultra thin bodies (UTBs)**

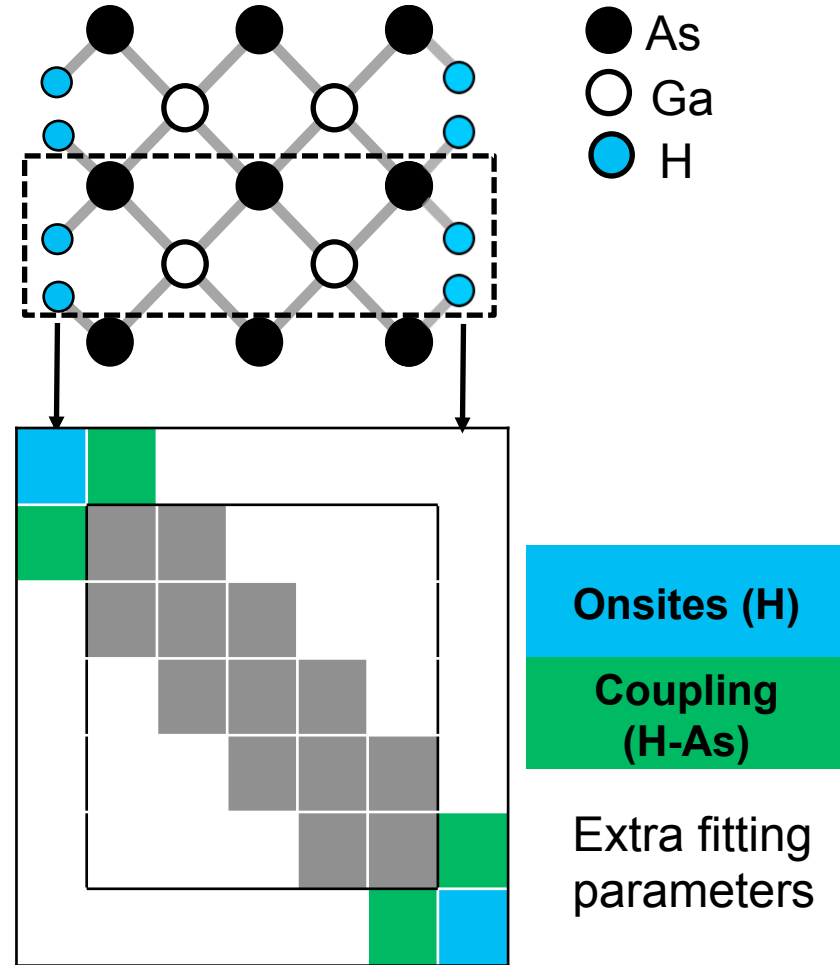
4 Environment dependent strain model

5 Transferability to interface

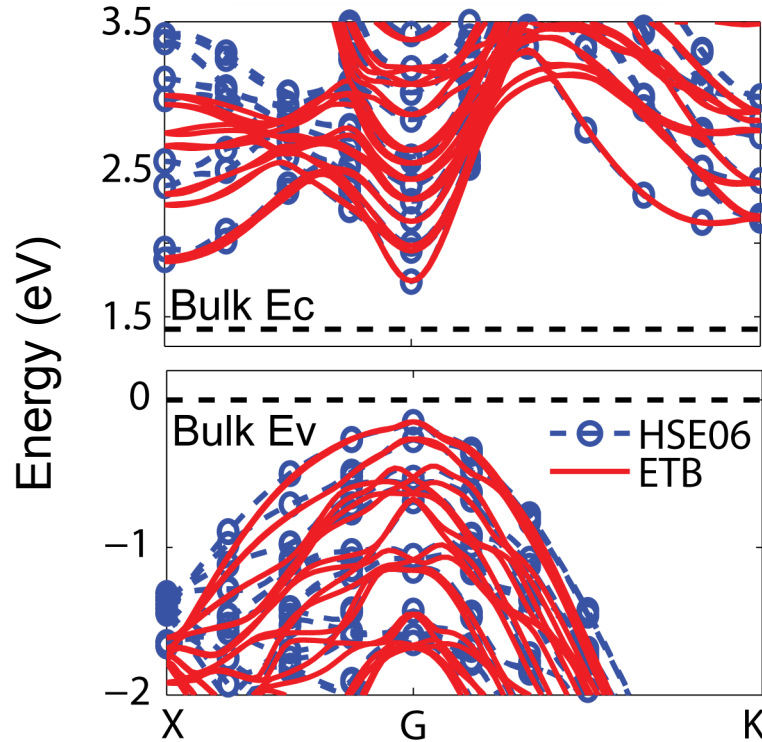
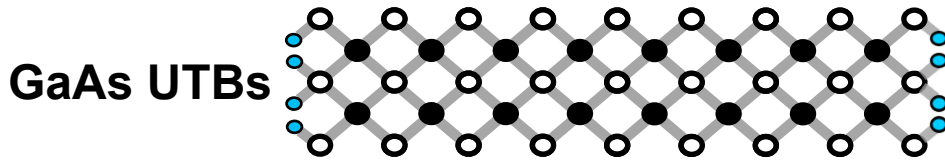
Implicit passivation model



Explicit passivation model

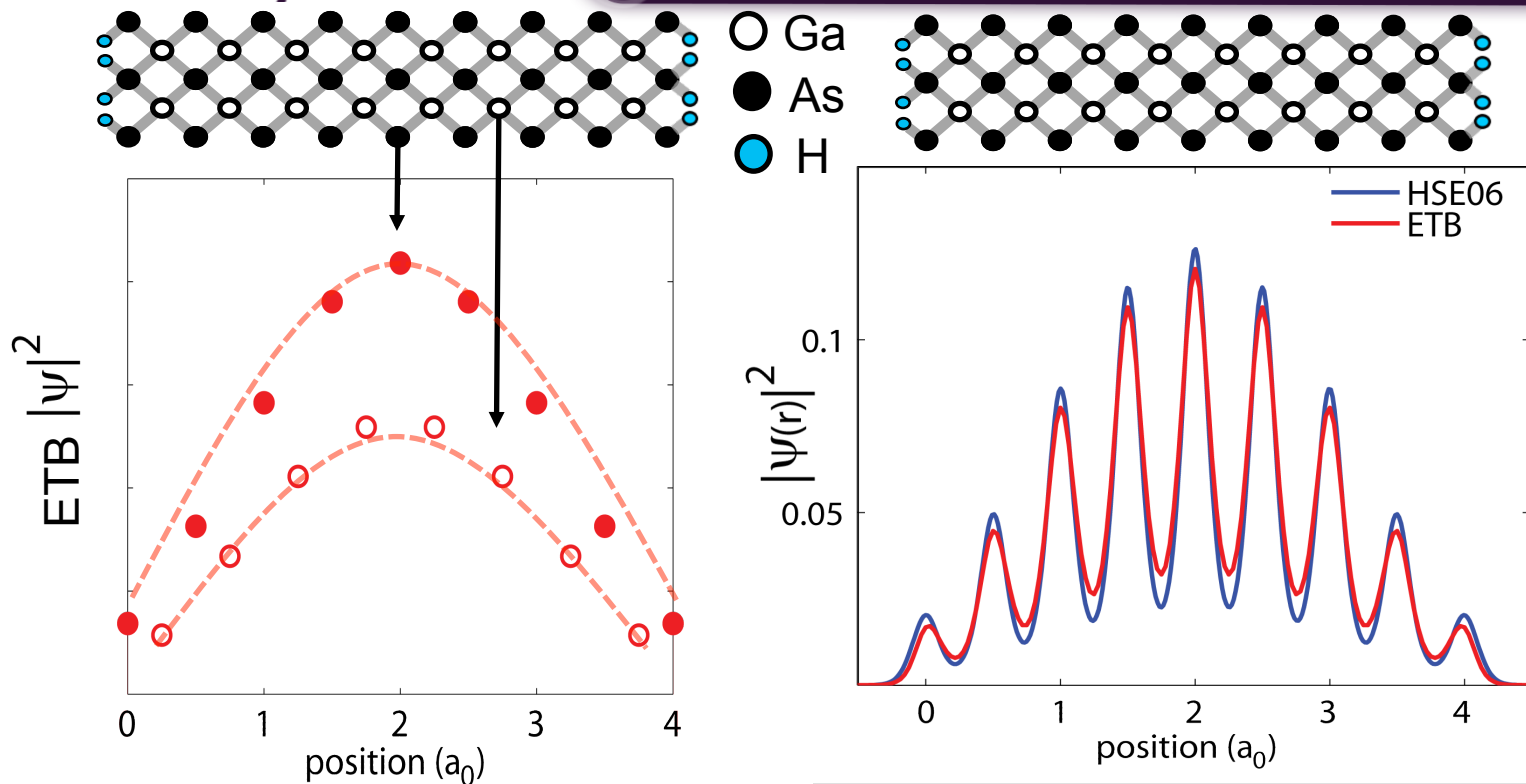


Previous work: implicit passivation model
 This work: explicit passivation model



- $sp^3d^5s^*$ ETB model + nearest neighbor interactions.
- Bulk GaAs parameters presented are used
- Use explicit passivation model

ETB band agree with HSE06 calculations in UTB case.



Without basis functions:

- Discrete
- Cations and anions form different envelope

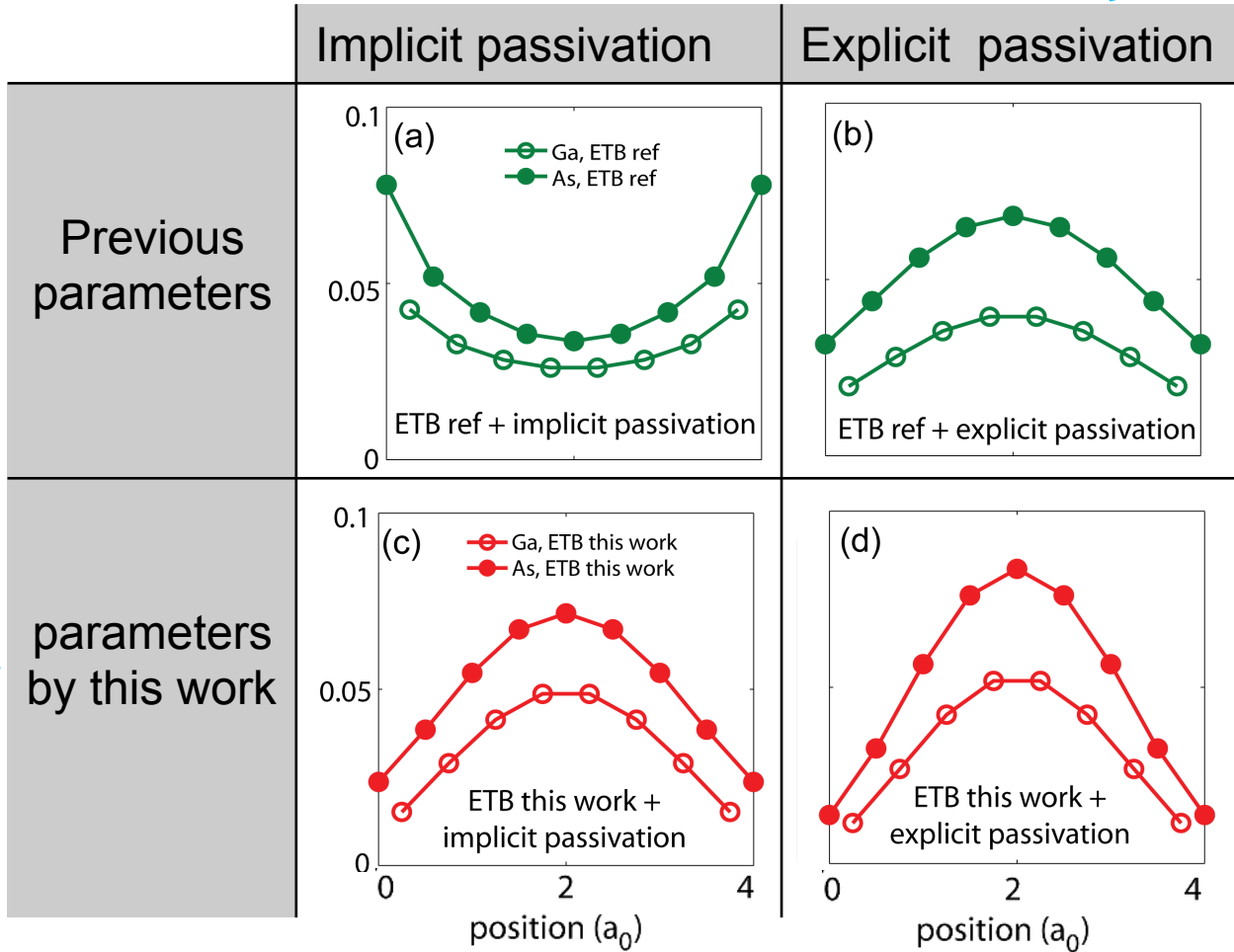
With basis functions:

- Continuous
- Subatomic resolution can be achieved

Realspace ETB wave function match HSE06 wave functions well.

More confined states

More confined states



ETB ref : T. Boykin et al. PRB 66, 125207 (2002).

What property does the new parameters improve?

Explicit passivation model and better ETB parameters → more physical VB states

	UTB wave functions	Bulk wave functions
Previous parameters		
Parameters In this work		

d-orbital contribute too much.

Fitting of ETB wave functions constraint the d contribution

New parameters have better quality
 → Wave function is properly controlled

- Tight binding parameter obtained from *ab-initio* calculations has better transferability;
- TB model with nearest neighbor interactions can work for unstrained bulk and UTBs.
- Unphysical TB states in GaAs UTBs are eliminated.

Solutions and applications

1 Parameterization algorithm from *ab-initio* calculations

2 Application to unstrained bulk

3 **Application to ultra thin bodies (UTBs)**

4 Environment dependent strain model

5 Transferability to interface

Solutions and applications

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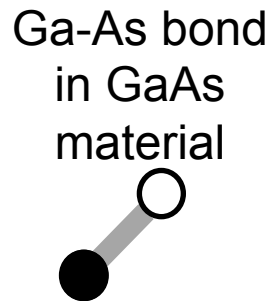
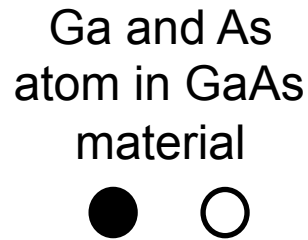
2 Application to unstrained bulk

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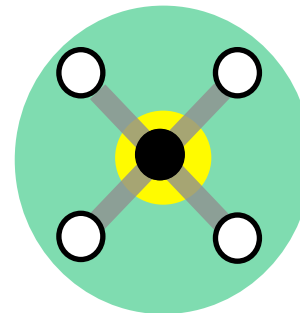
4 **Environment dependent strain model**

5 Transferability to interface

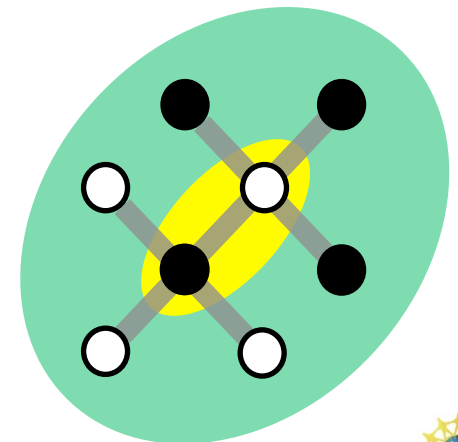
	Traditional ETB model	Environment dependent ETB model (this work)
Onsite blocks	Atom + material	Atom + environment
Interatomic interaction blocks	Bond + material	Bond + environment



Ga atom and its environment

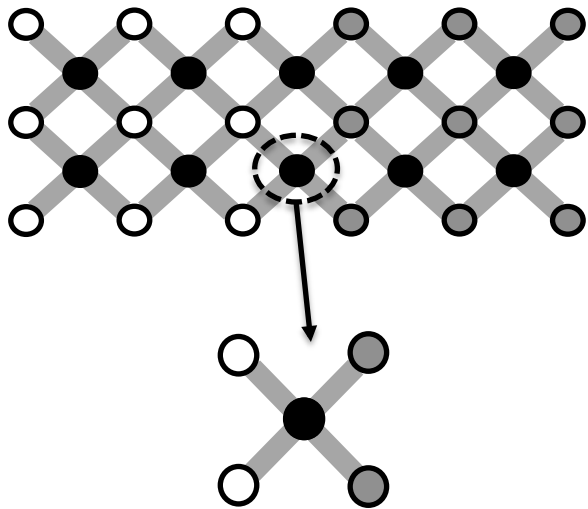


Ga-As bond and its environment

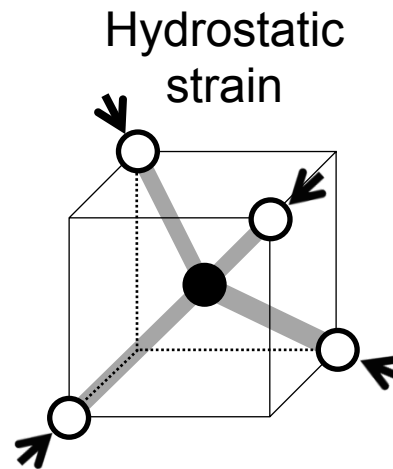


Environments: (the status of neighbors)

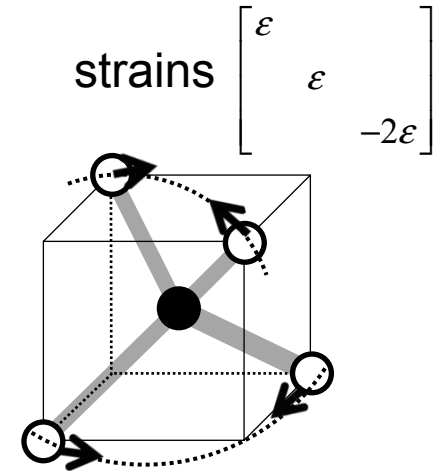
Atom types of neighbors



Bond lengths



Bond angles

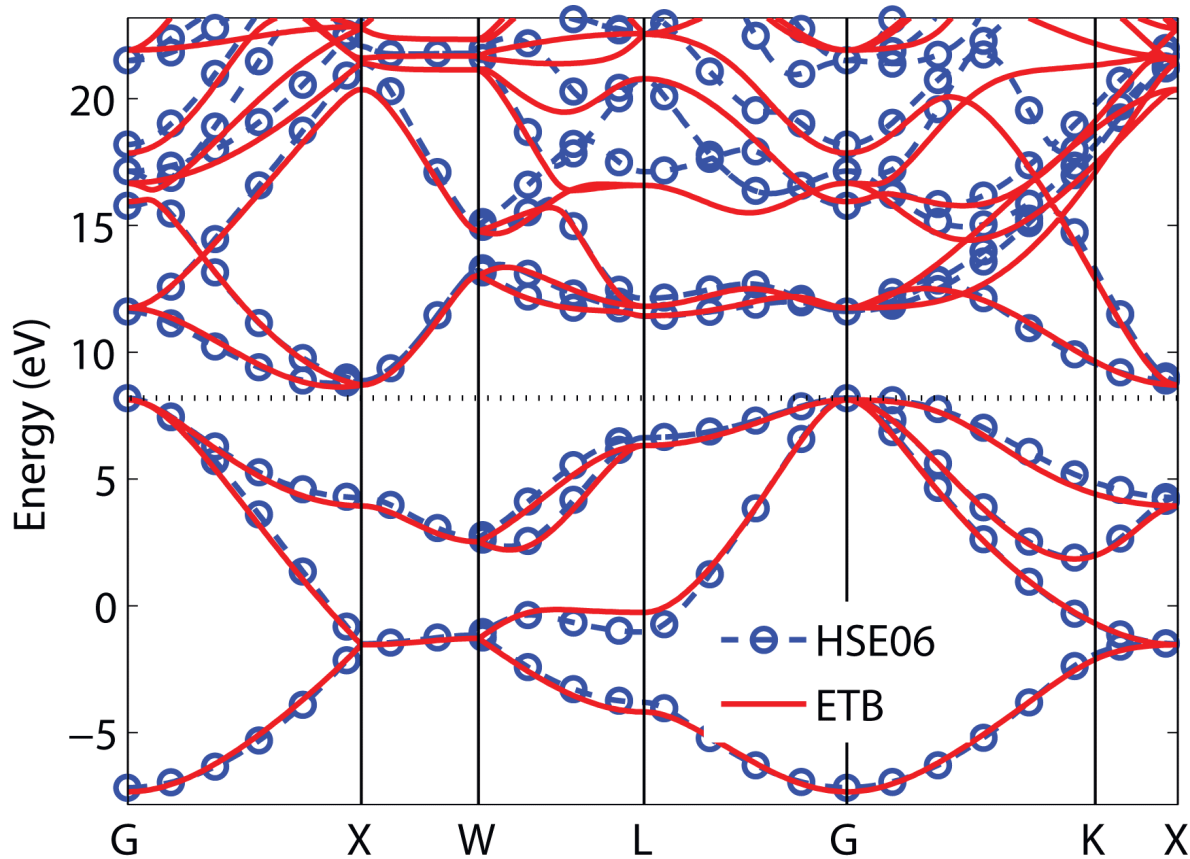


ETB model in this work

→ **Environment dependent Hamiltonian**

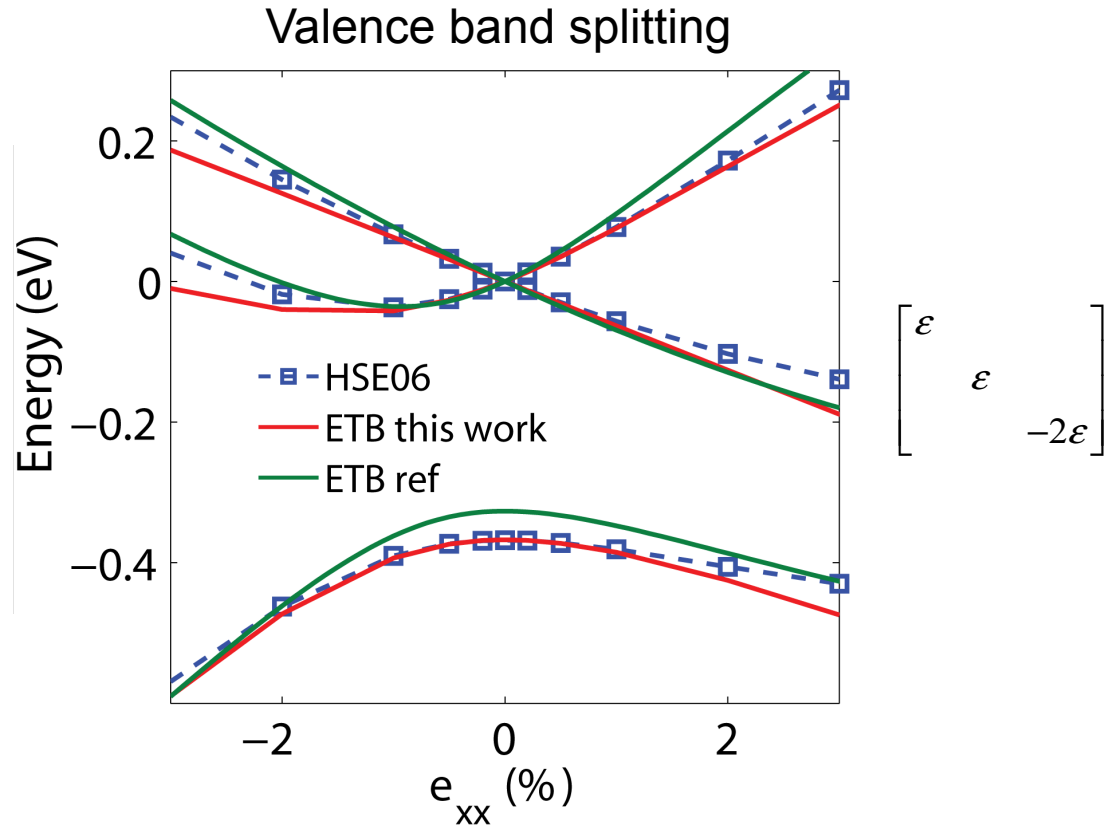
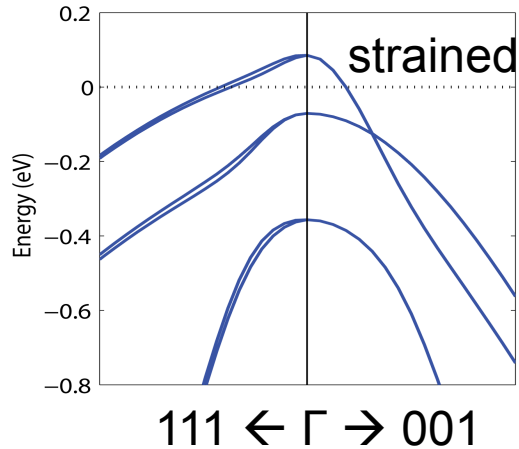
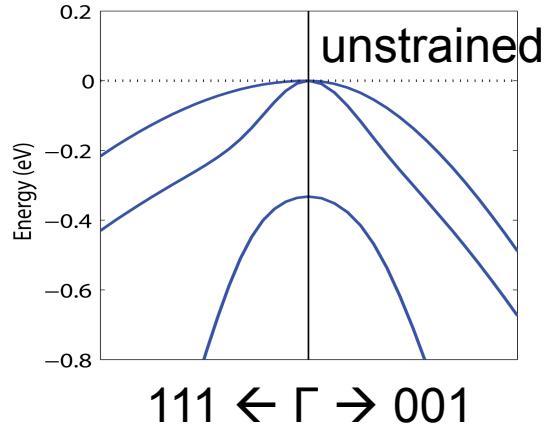
- strains
- Interfaces

Si, $a_0 = 5.0$ Angstrom



With hydrostatic strain:
 ➤ Band gaps will change;
 ➤ Indirect gap \rightarrow direct gap.

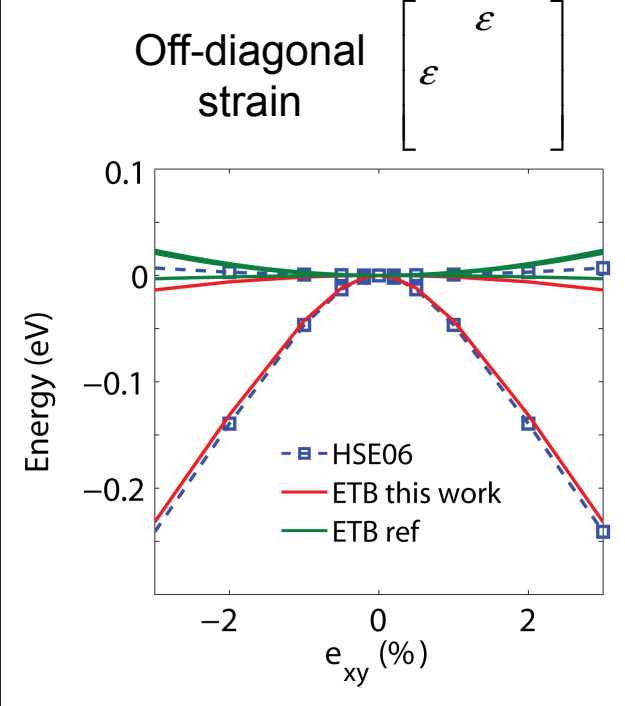
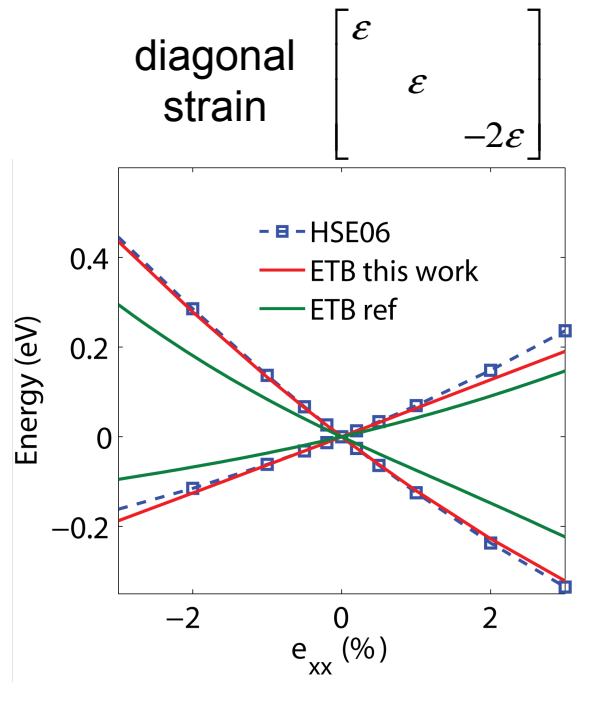
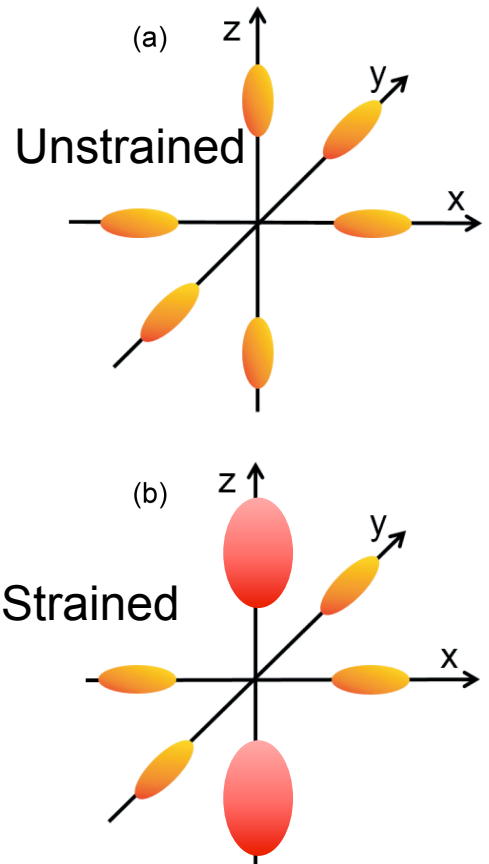
The TB model in this work can be applied to hydrostatic strain cases



ETB ref : T. Boykin et al.
PRB 66, 125207 (2002).

ETB model in this work reproduce the strain valence bands.

Band edge of X valleys



ETB model by this work show better result than existing TB model for conduction bands

ETB ref : T. Boykin et al. PRB 66, 125207 (2002).

ETB model in this work reproduce the strain behavior of CB(X valleys).

Solutions and applications

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2 Application to unstrained bulk

3 Application to ultra thin bodies (UTBs)

4 **Environment dependent strain model**

5 Transferability to interface

Solutions and applications

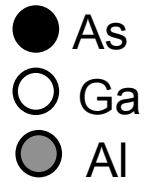
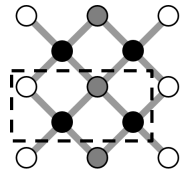
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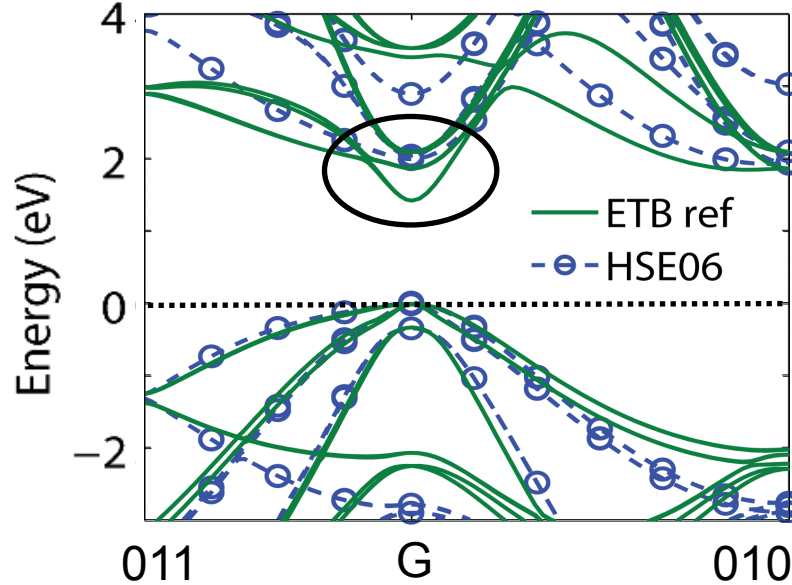
3 Application to ultra thin bodies (UTBs)

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5 **Transferability to interface**

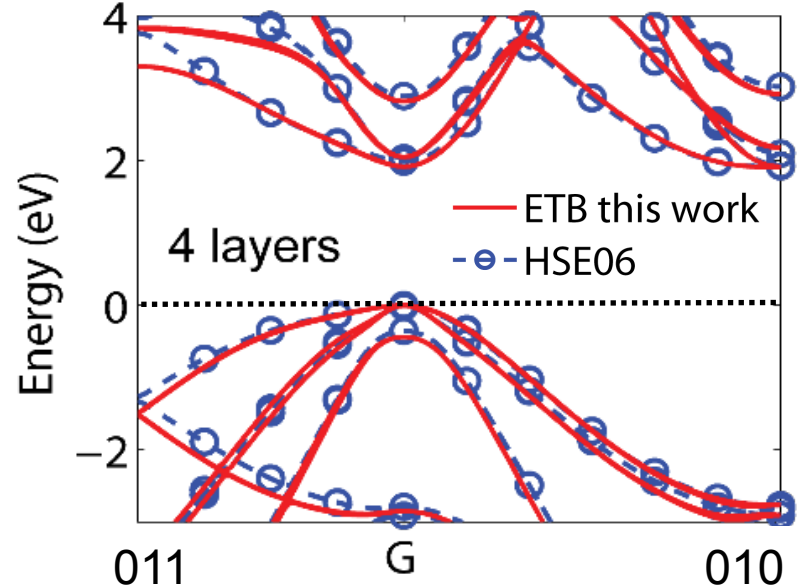


Existing ETB

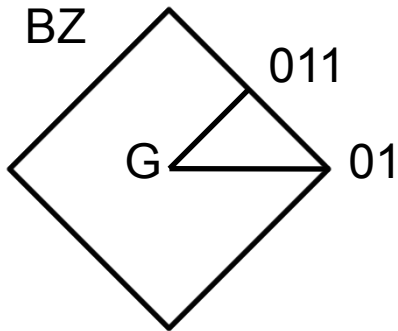
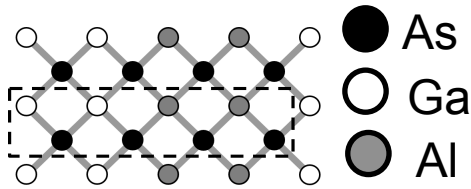


ETB ref : T. Boykin et al. PRB 66, 125207 (2002).

ETB This work

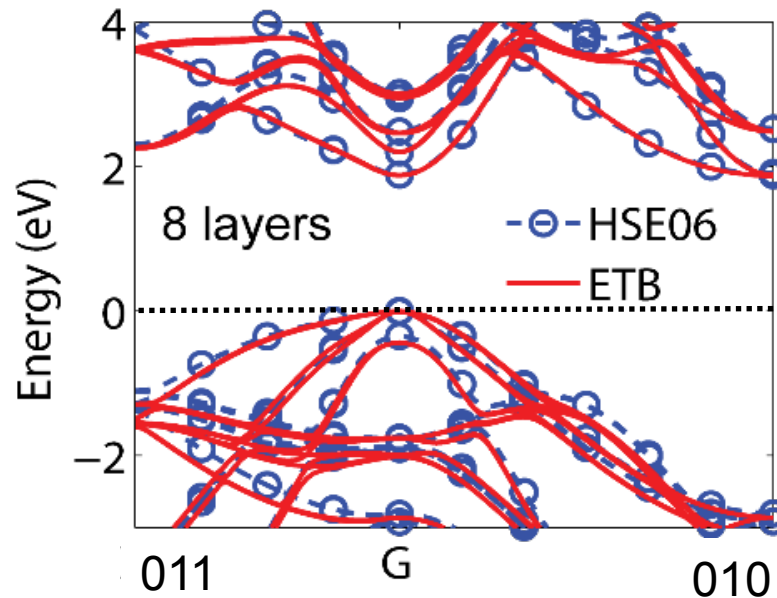


Existing ETB model shows significant differences in a GaAs/AlAs superlattice

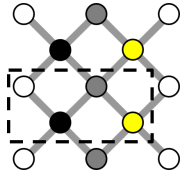


ETB calculations in this work :

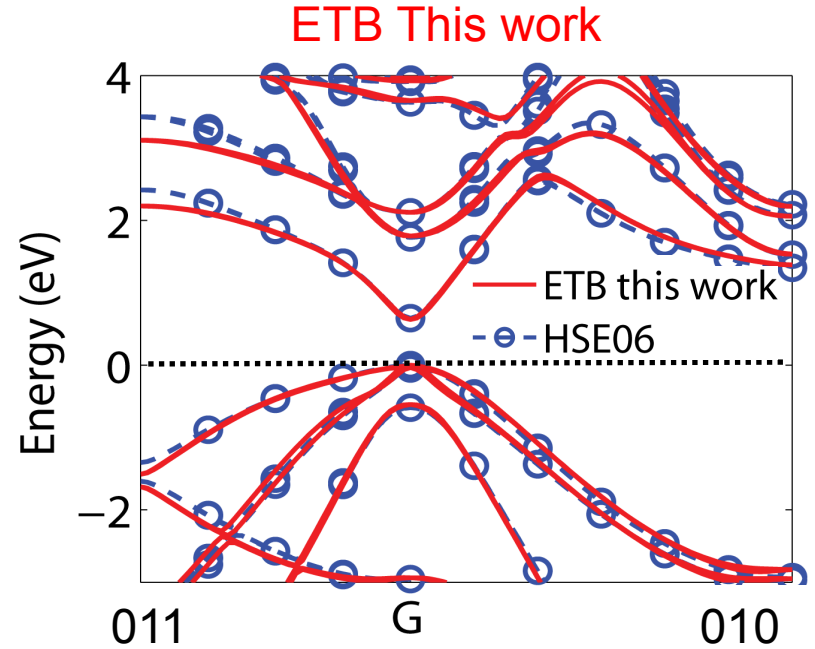
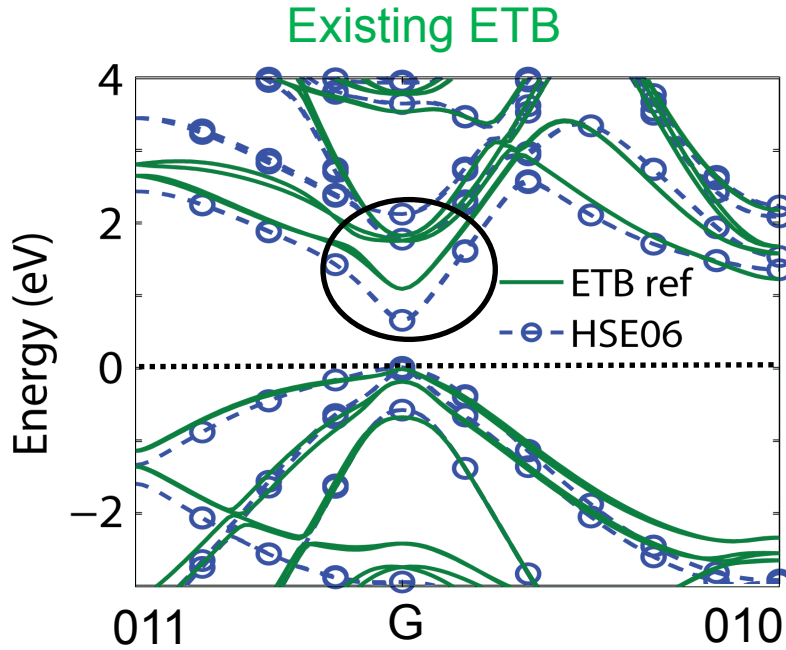
- $sp^3d^5s^* + SO$
- 1st nearest neighbor interaction
- Negligible built-in potential



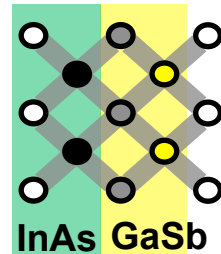
ETB in this work can accurately calculate band structure of GaAs/AlAs superlattices



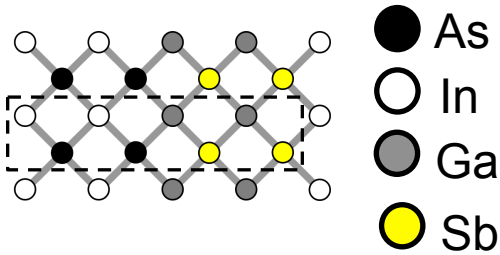
- As
- In
- Ga
- Sb



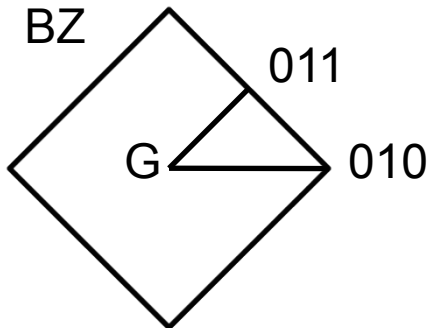
ETB ref : J. Jancu, et al. PRB, 57, 6393 (1998).



Existing ETB model shows significant differences in a InAs/GaSb superlattice

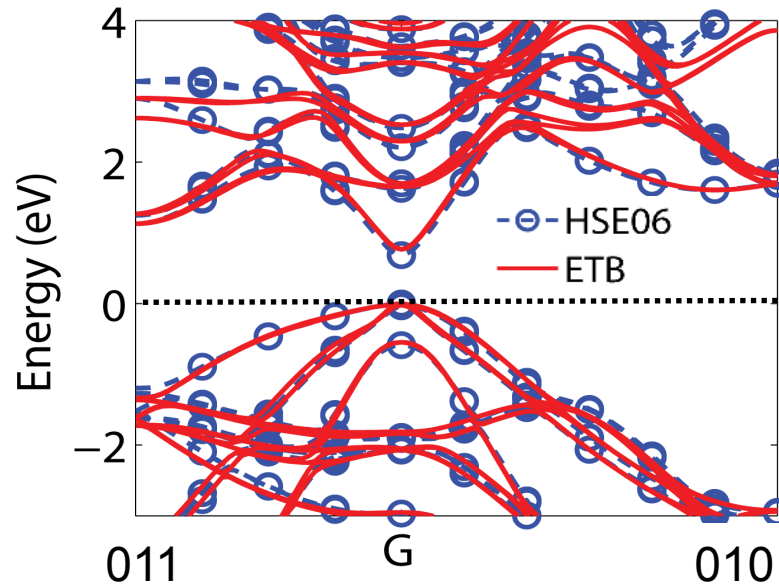


Bonds involved:
In-As,
Ga-Sb,
In-Sb,
Ga-As



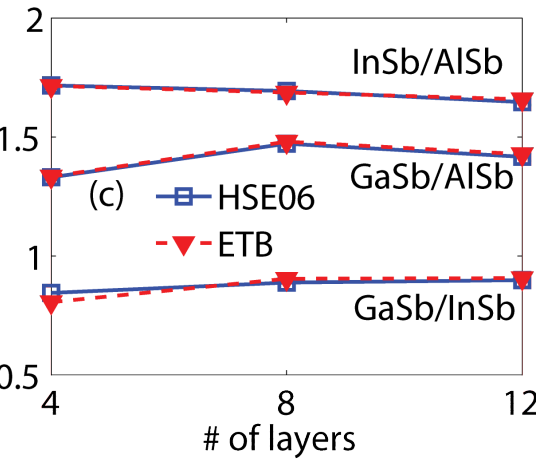
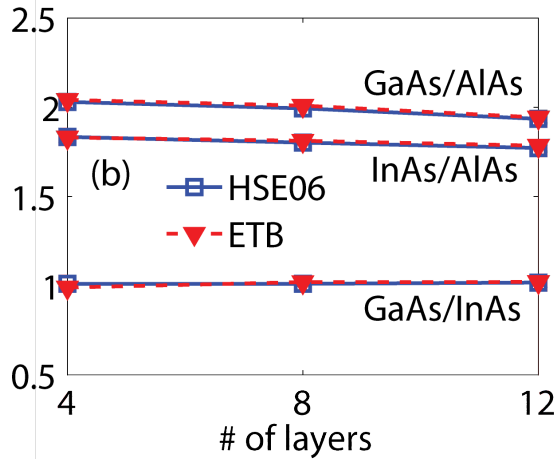
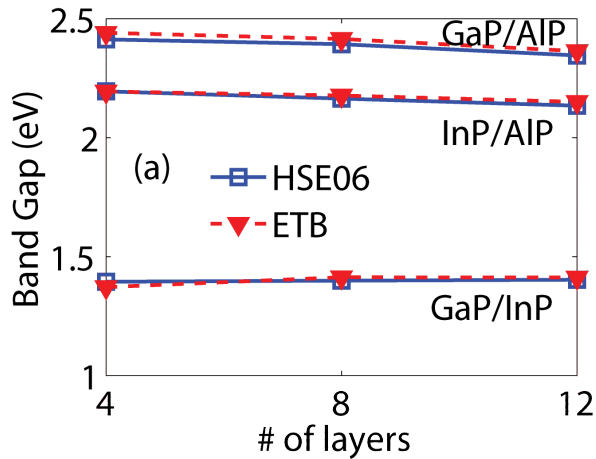
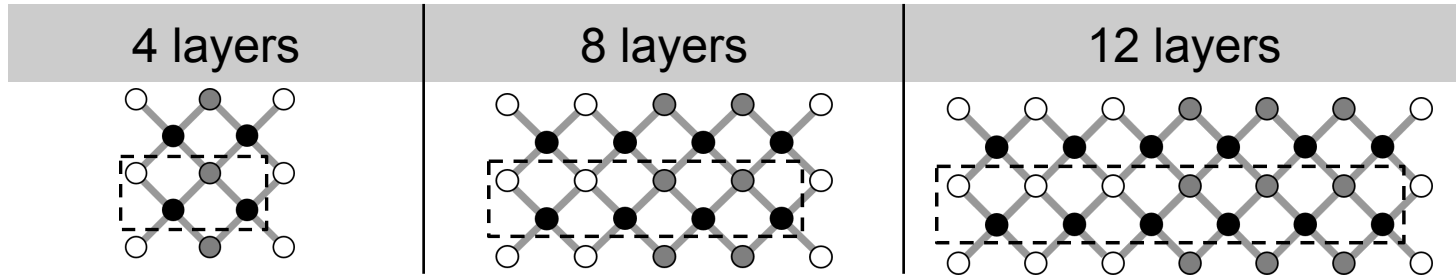
ETB calculations in this work:

- $sp^3d^5s^* + SO$
- 1st nearest neighbor interaction
- Negligible built-in potential



ETB in this work can accurately calculate band structure of InAs/GaSb superlattices

Superlattices with common anions



Band gaps of different superlattices by ETB agree with HSE06 calculations.

Summary & Outlook

- Traditional tight binding parameterization has problems;
- Tight binding parameterization from *ab-initio* calculations is developed in this work;
- ETB parameters with better transferability and explicit ETB basis functions are obtained;
- Application to unstrained and strained materials → good agreement with *ab-initio* bands is achieved;
- Application to nanostructures (UTBs and superlattice) → good transferability can be achieved with 1st nearest neighbor ETB models.

Motivation:

- *Ab-initio* calculations usually assume zero temperature.
- But device simulations require room temperature tight binding parameters.

Approach:

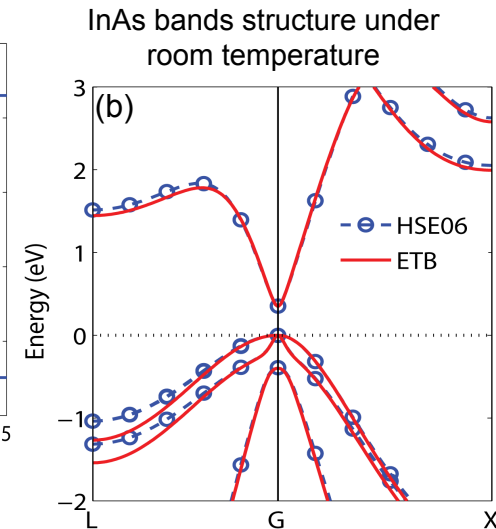
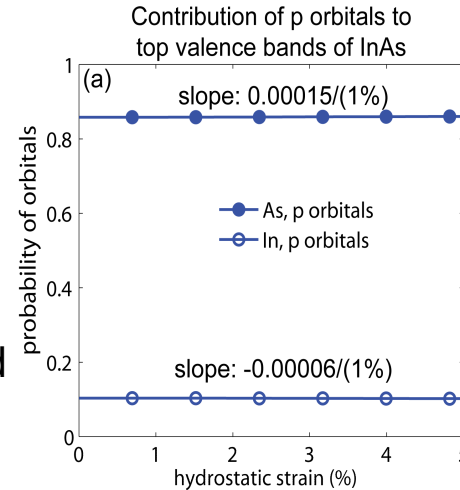
- Effect of room temperature is approximated by hydrostatic strain.

$$E(k, T) \approx E(k, \delta a_0)$$

- Environment dependent strain ETB model
- *Ab-initio* mapping algorithm to extract ETB parameters.

Results:

- *Ab-initio* band structures matching room temperature experimental results are obtained.
- introduce of strain only change wave function slightly
- ETB parameters for room temperature are obtained.



Impact:

TB parameters for room temperature materials are available. Devices under room temperature is enabled.

Motivation:

- 2D materials like MoS₂ are interested in recent device design, but TB parameters for device level simulation is required.
- Extract TB parameters from DFT results (DFT energy bands & eigenfunctions)

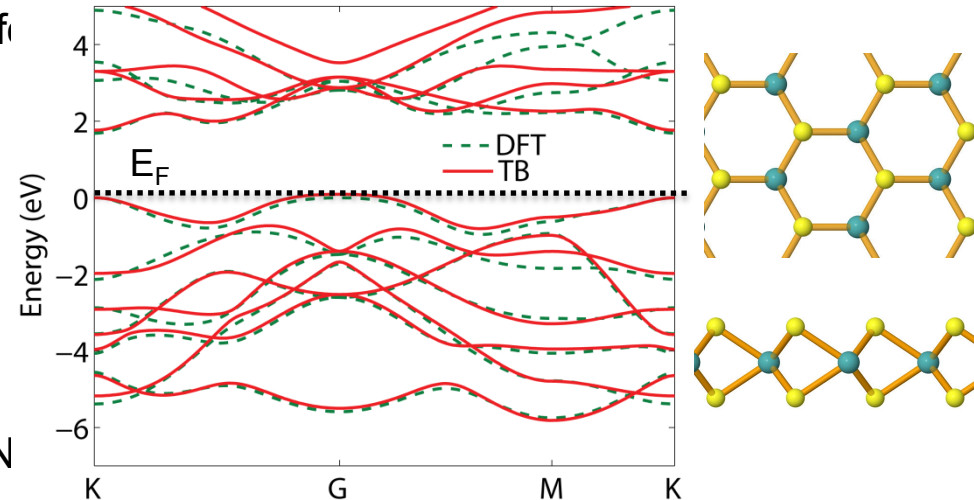
Approach:

- Basis transformation:
Plane waves → localized orbitals
- TB model: orthogonal TB model with 1st N Interactions;
- optimize TB orbitals and parameters to match *ab-initio* results.
targets: *ab-initio* bands & wave functions.

Results:

- Reasonable parameters and band structure is obtained;

Single layer MoS₂ band structure



Impact:

TB parameters for TMDs are obtained, device level calculations of TMD transistors are enabled.

Objective:

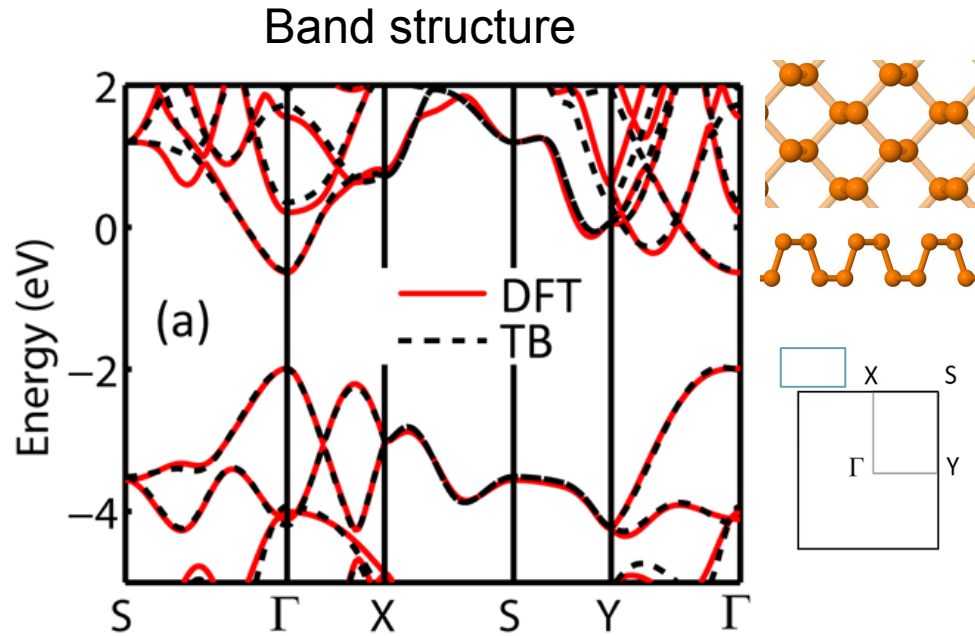
- Existing four-band tight binding model underestimates band splitting \rightarrow might affect charge distribution especially if scattering exists.

Method:

- Ten-band ETB model considering 2NN interactions.
- Harrison's scaling law for bond length dependence of parameters.
- One parameter set for in-plane, one parameter set for inter-layer.
- Optimize parameters by fitting to DFT, for monolayer, bilayer, and bulk.

Results:

- Tight binding parameters for black Phosphorus.
- TB bandstructure well reproduce DFT



Impact:

- Atomistic modeling for black Phosphorus transistors are enabled.

Objective:

- Investigate the Si UTB/SiO₂ interface and evaluate the normally used hydrogen atom passivation treatment.

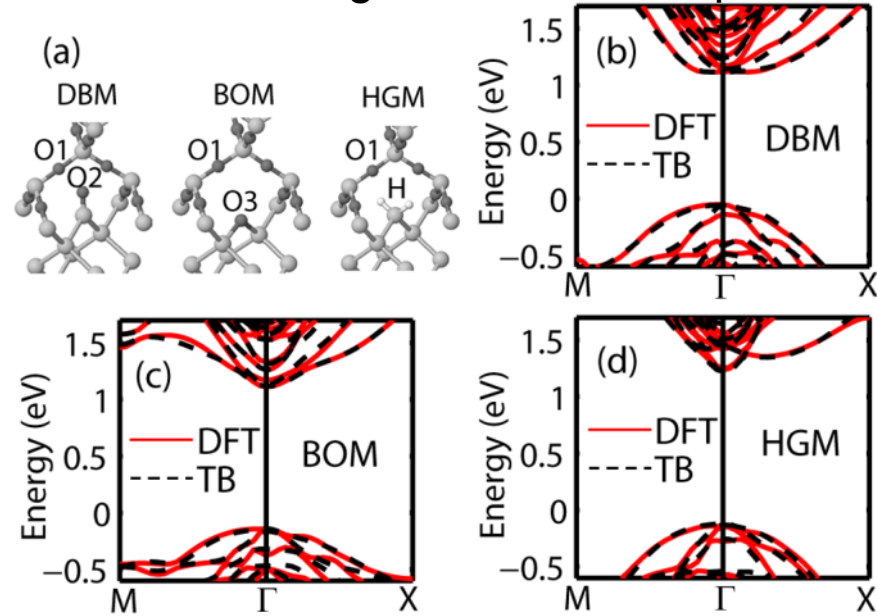
Method:

- Passivation for three relevant oxidation configurations are parameterized.
- Parameters are optimized by fitting TB dispersions to DFT-HSE06 calculations.

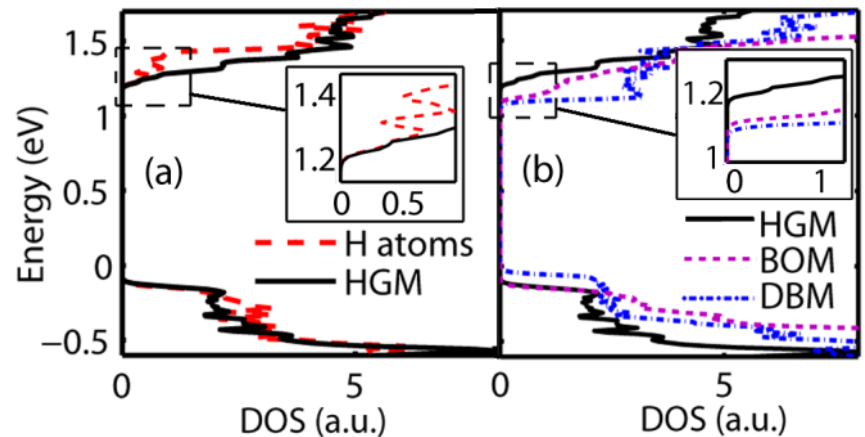
Impact:

- UTB band structures of TB match well with DFT calculations.
- HGM gives higher DOS compared to hydrogen atom passivation.
- Oxidation configurations involved more oxygen atoms contribute higher DOS.
- DBM and BOM configurations are not well confined, which are suggested to be avoided in experiment.

oxidation configurations and dispersions

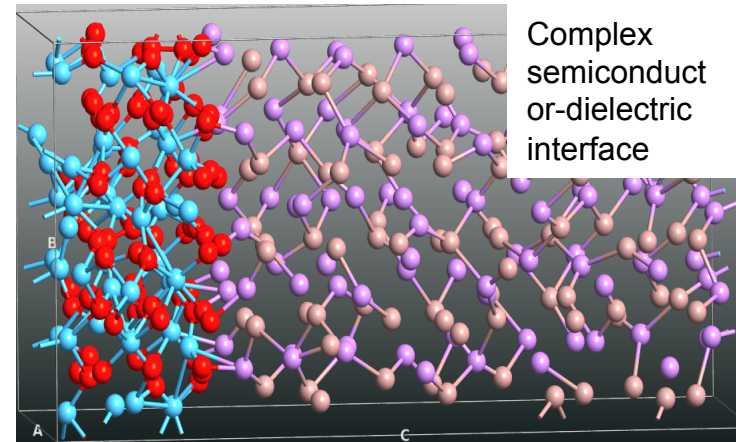


DOS for the oxidation configurations



InAs Parameterization

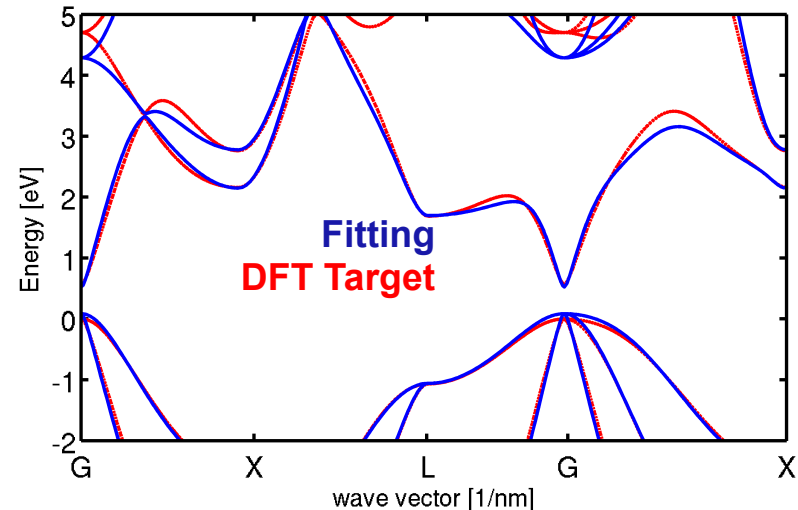
- Transferable parameters for semiconductors are needed to model disordered systems and interfaces
- Extended Hückel model gives natural treatment of these systems



HfO₂, InAs interface. Strain, rearrangement requires high transferability

Parameterization Technique

- InAs fit to $E(k)$ and wavefunction targets from HSE06 calculations
- Work underway to produce bulk parameterizations with more accurate strain behavior than published parameterizations



Motivation:

- Extract TB parameters from DFT results (DFT energy bands & eigenfunctions)
- MgO is interested in spintronic devices, but no TB parameters for device level simulation.

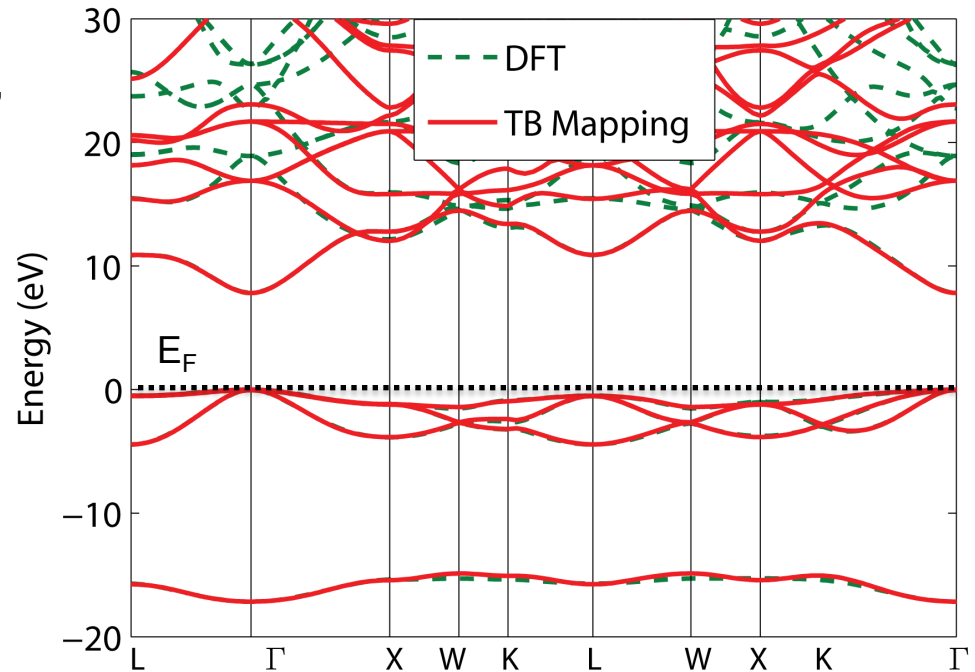
Approach:

- Low rank approximation:

$$H_{DFT} \rightarrow H_{TB}$$
- constraint:
 - 2st NNs Interactions,
 - unity overlap matrix;
- optimize the TB basis functions to get reasonable TB parameters. targets: HSE06 bands.

Results:

- Reasonable parameters and band structure is obtained by mapped TB Hamiltonian;



Impact:

TB parameters for complicated material MgO are obtained, device level calculations of MgO based spintronics Transistor are enabled.

Motivation:

- Extract TB parameters from DFT results (DFT energy bands & eigenfunctions)
- Complicated exotic material SmSe is interested in Piezoelectronic Transistor design, but no TB parameters for device level simulation.

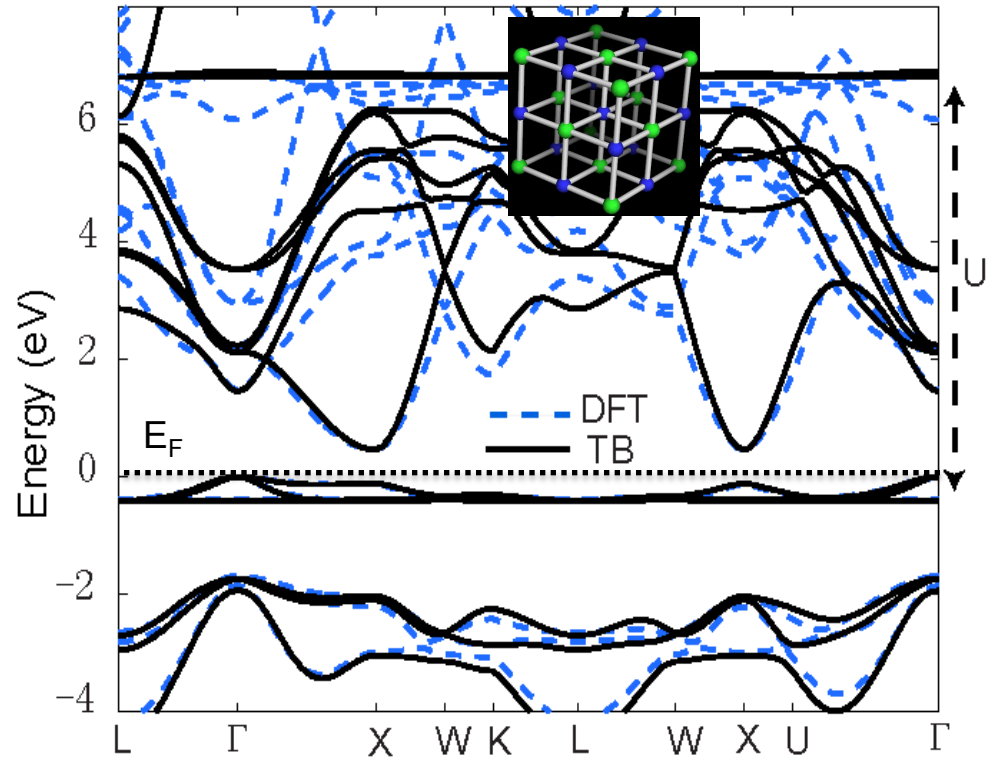
Approach:

- Low rank approximation:

$$H_{DFT} \rightarrow H_{TB}$$
- constraint:
 - 1st NNs Interactions,
 - unity overlap matrix;
- optimize the TB basis functions to get reasonable TB parameters. targets: LDA+U bands.

Results:

- Reasonable parameters and band structure is obtained by mapped TB Hamiltonian;



Impact:

TB parameters for complicated material SmSe are obtained, device level calculations of SmSe based piezoelectronic Transistor are enabled.

Motivation:

Topological insulators like (CdTe/HgTe/CdTe QW) are new group of materials.

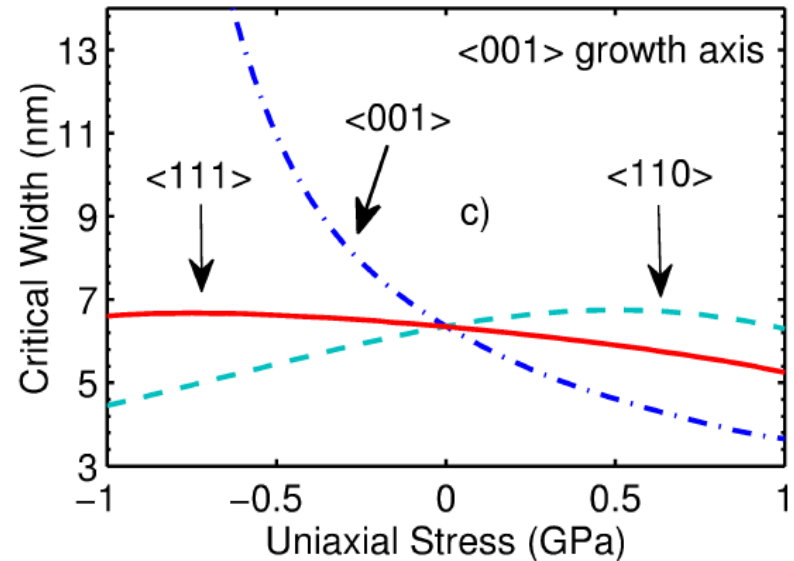
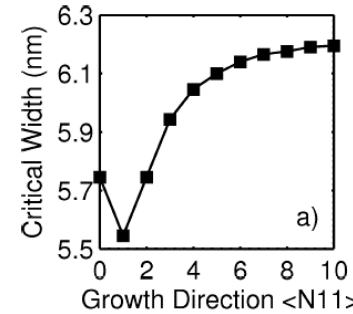
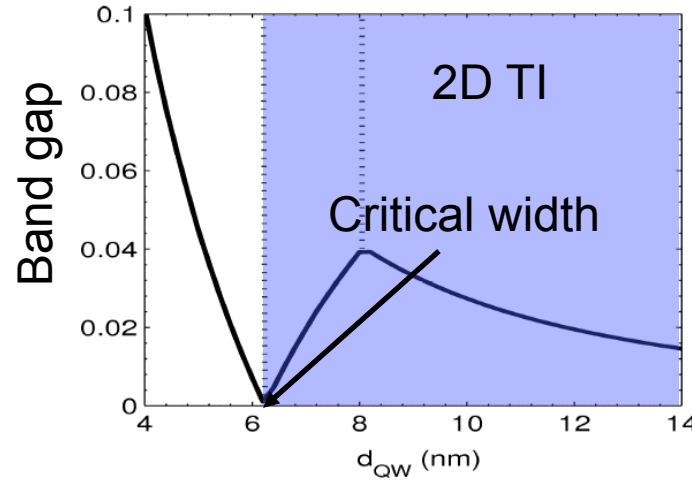
The behavior of topological insulator in device environment is not clear.

Approach:

- 8 band strained k.p model for CdTe and HgTe
- Finite differential method for CdTe/HgTe/CdTe quantum wells.

Results:

- Topological states in CdTe/HgTe/CdTe can be modulated by strain/crystal orientation/vertical electric field.



Committee member:

Prof. Klimeck, Prof. Strachan, Prof. Povolotskyi, Prof. Lundstrom,
Prof . Boykin (UAH)

Prof. Kubis, Prof. R. Rahman, Dr. J. Huang, Dr. J. Fonseca, Dr.
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S. Lee, Dr. H. Ryu.

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H. Ilatikhameneh, K. Wang, Y. Chu, T. Ameen, C. Chen, P.
Sarangapani, H. Sahasrabudhe, S. Perez, S. Mukherjee, Dr. X.
Wang, Dr. Y. Gao and all other NCN students

NCN Staff members:

V. Johnson, C. Heins, L. Schumacher, A. Byrne, A. Buckles

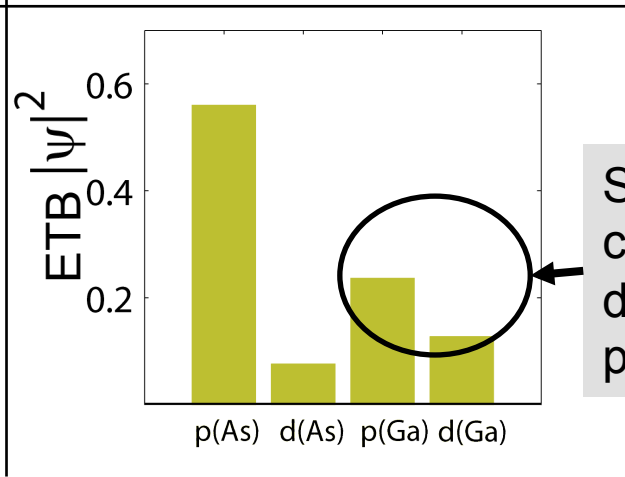
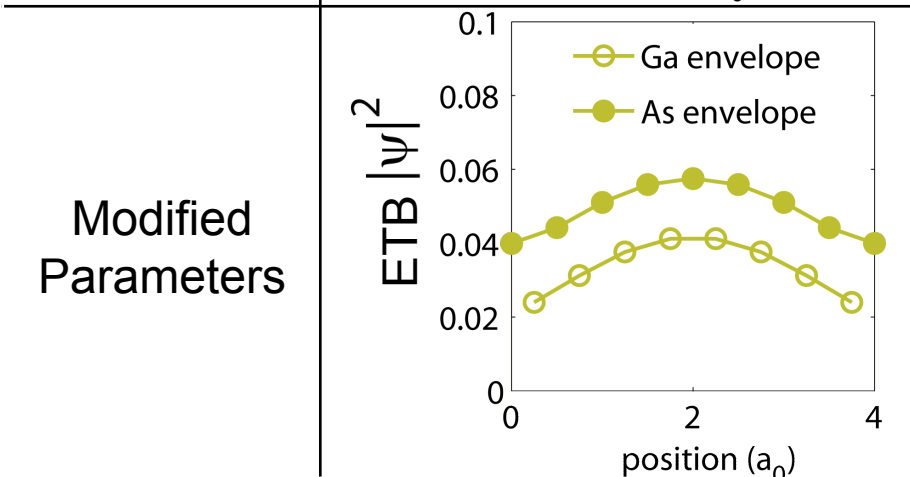
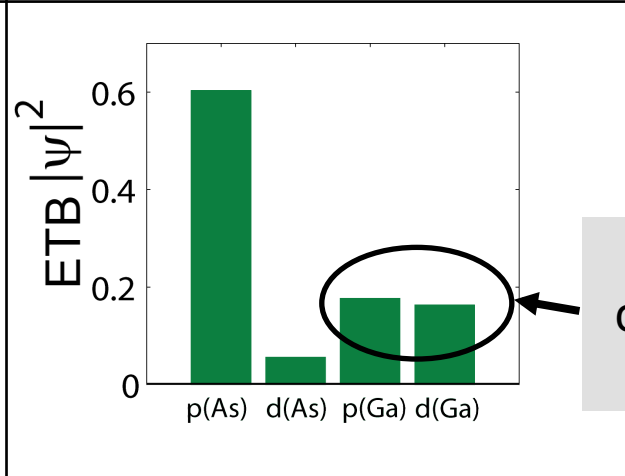
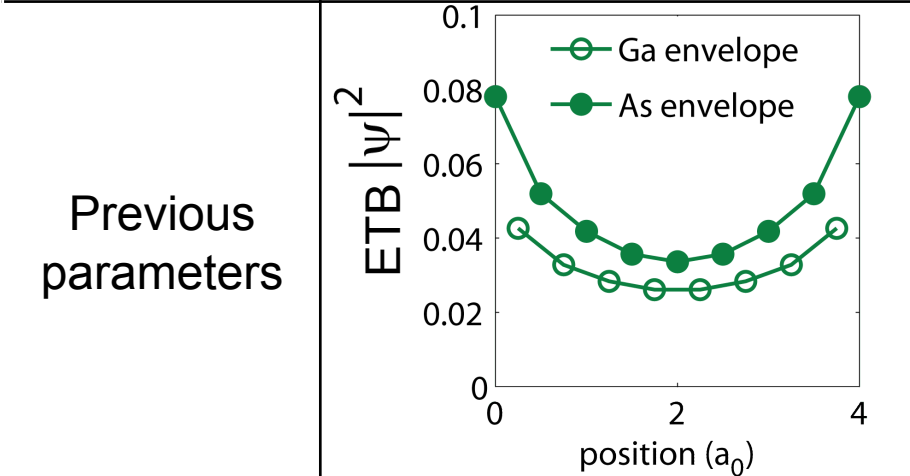
Thank you!

Related Publication list

- **Y. Tan**, M. Povolotskyi, T. Kubis, T. Boykin, G. Klimeck, 'Transferable tight binding model for strained group IV and III-V heterostructures' to be submitted to Phys. Rev. B
- **Y. Tan**, M. Povolotskyi, T. Kubis, T. B. Boykin, G. Klimeck, 'Tight Binding analysis of Si and GaAs ultra-scaled transistors with subatomic wave-function resolution' Phys. Rev. B 92, 085301 (2015)
- **Y. Tan**, M. Povolotskyi, T. Kubis, Y. He, Z. Jiang, G. Klimeck, T. B. Boykin, 'Empirical tight binding parameters for GaAs and MgO with explicit basis through DFT mapping', Journal of Computational Electronics 12 (1), 56-60 (2013)
- Y. He, **Y. Tan**, Z. Jiang, M. Povolotskyi, G. Klimeck, T. Kubis, 'Surface Passivation in Empirical Tight Binding', submitted to IEEE Trans. Elect. Dev.
- Z. Jiang, M. Kuroda, **Y. Tan**, D. News, M. Povolotskyi, T. Boykin, T. Kubis, G. Klimeck, G. Martyna, 'Electron transport in nano-scaled piezoelectronic devices', Applied Physics Letters 102 (19), 193501 (2013)
- H. Ilatikhameneh, **Y. Tan**, B. Novakovic, G. Klimeck, R. Rahman, J. Appenzeller, 'Tunnel Field-Effect Transistors in 2D Transition Metal Dichalcogenide Materials', IEEE Journal on Exploratory Solid-State Computational Devices and Circuits, 1,12,(2015)
- P. Sengupta, T. Kubis, **Y. Tan**, M. Povolotskyi, G. Klimeck, 'Design principles for HgTe based topological insulator devices', Journal of Applied Physics 114 (4), 043702 (2013)
- Y. Hsueh, H. Büch, **Y. Tan**, Y. Wang, L. Hollenberg, G. Klimeck, M. Simmons, and R. Rahman, "Spin-Lattice Relaxation Times of Single Donors and Donor Clusters in Silicon", Phys. Rev. Lett. 113, 246406 (2014)
- F. Chen, L. Jauregui, **Y. Tan**, M. Manfra, G. Klimeck, Y. Chen, T. Kubis, 'In-surface confinement of topological insulator nanowire surface states', Appl. Phys. Lett. 107, 121605 (2015)

Backup slides

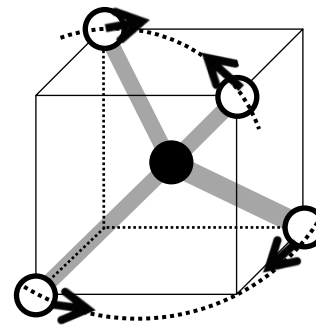
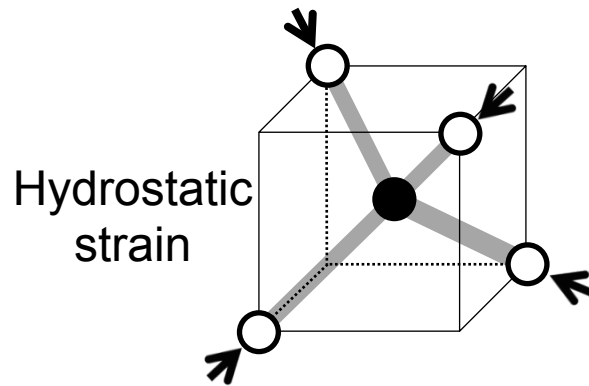
	UTB wave functions	Bulk wave functions
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Smaller d-contribution due to modified parameters also eliminate unphysical states

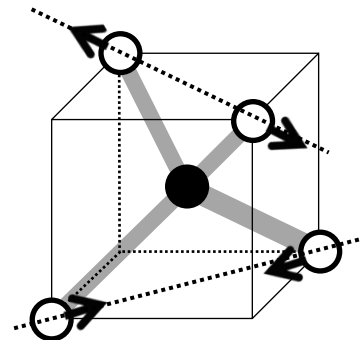
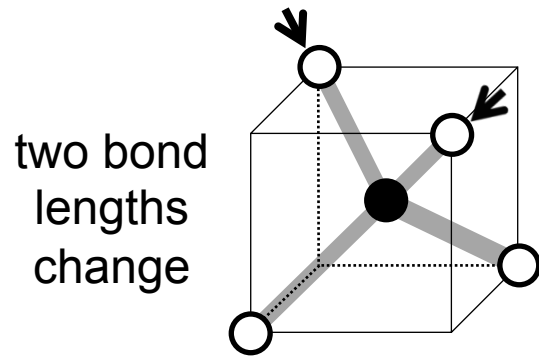
Special distorted systems considered in fitting:

- Four kinds of atom displacements
- Assume no missing nearest neighbor



Diagonal strains

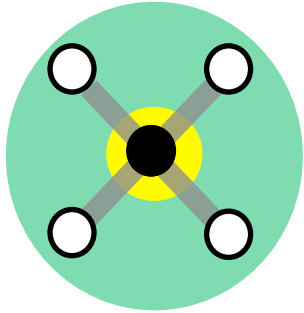
$$\begin{bmatrix} \varepsilon & & \\ & \varepsilon & \\ & & -2\varepsilon \end{bmatrix}$$



Off-diagonal strains

$$\begin{bmatrix} & \varepsilon & \\ \varepsilon & & \end{bmatrix}$$

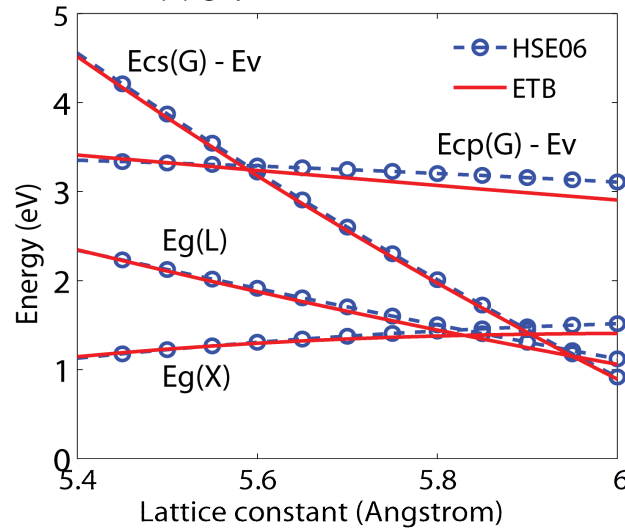
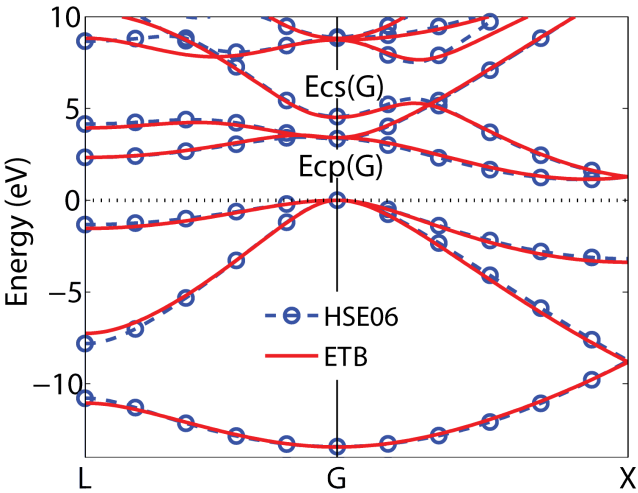
Onsite element:



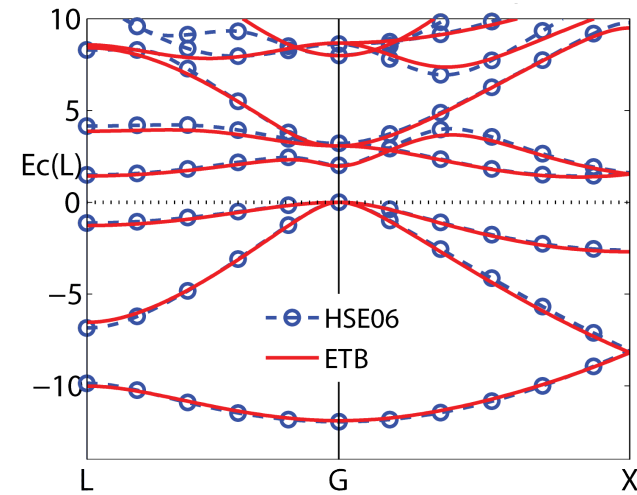
$$H_{\alpha_i, \alpha_i}^{(0)} = E_{\alpha_i} + \underbrace{\sum_{j \in \text{NNs}} I_{\alpha_i, j}(d_{ij}) + \sum_{j \in \text{NNs}} O_{i, j}(d_{ij})}_{\text{Environment dependent terms: Sum over nearest neighbors}}$$

Environment dependent terms:
Sum over nearest neighbors

Lattice const = 5.4 Angstrom



Lattice const = 5.8 Angstrom



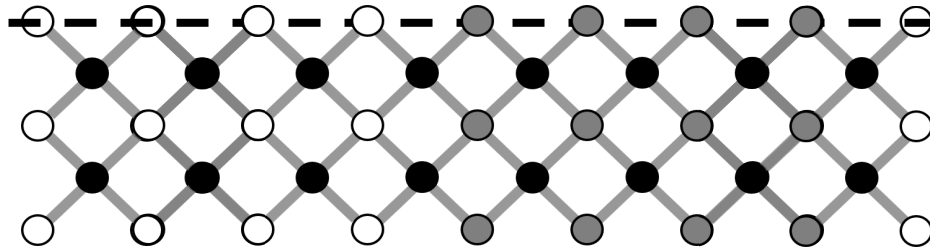
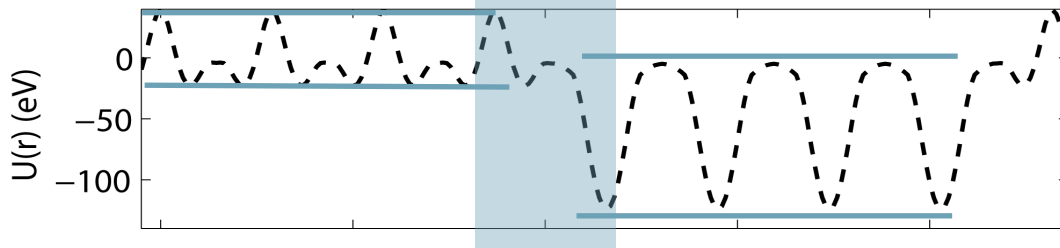
With hydrostatic strain:

- Band gaps will change;
- Gap of X, L and Γ points change at different ratio;
- Transition from indirect gap to direct gap happens;

The TB model in this work can be applied to hydrostatic strain cases

What is proper interaction radius of TB model?

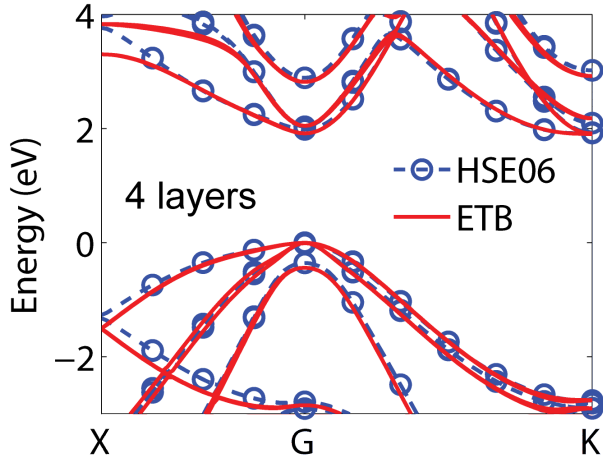
Observation: Ab-initio potential at III-V interface varies over the range of first nearest neighbor



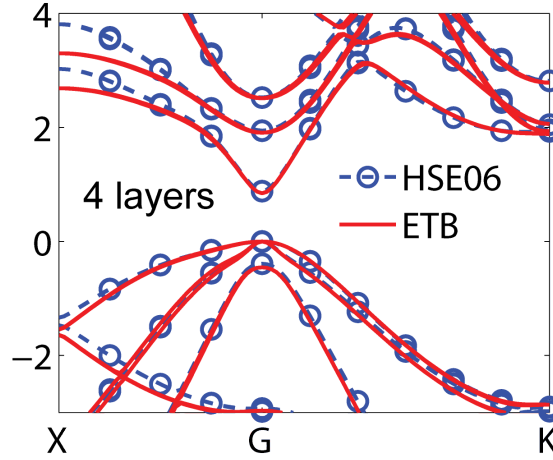
ab-initio local potential of GaAs/InAs superlattice

Is 1st nearest neighbor interaction enough for III-V hetero structures?

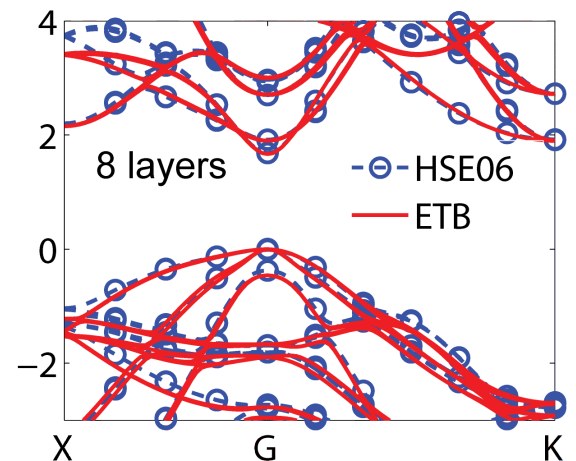
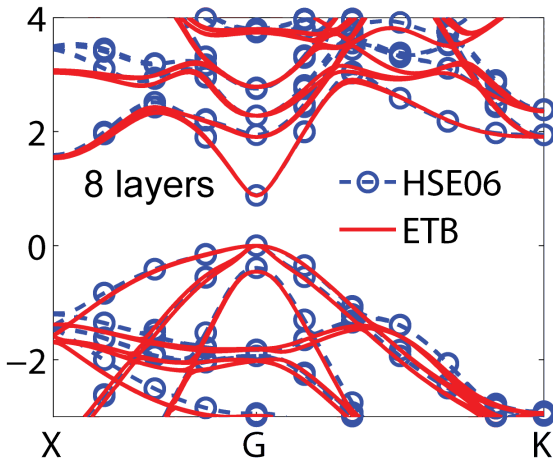
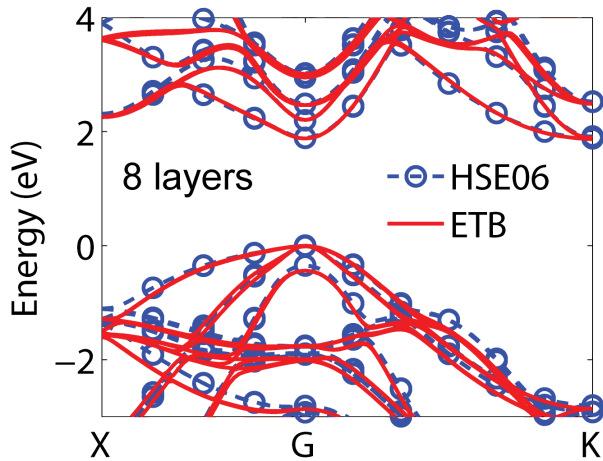
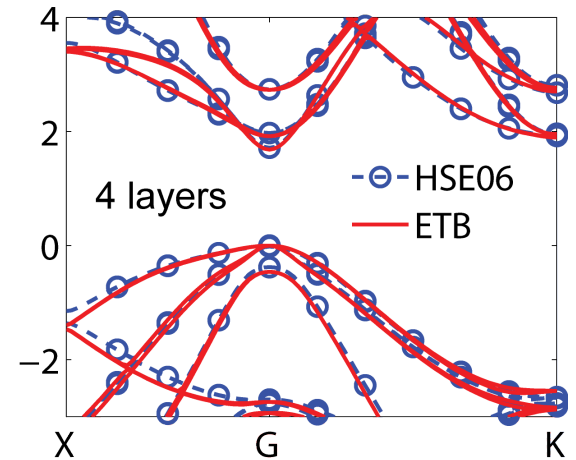
GaAs/AlAs



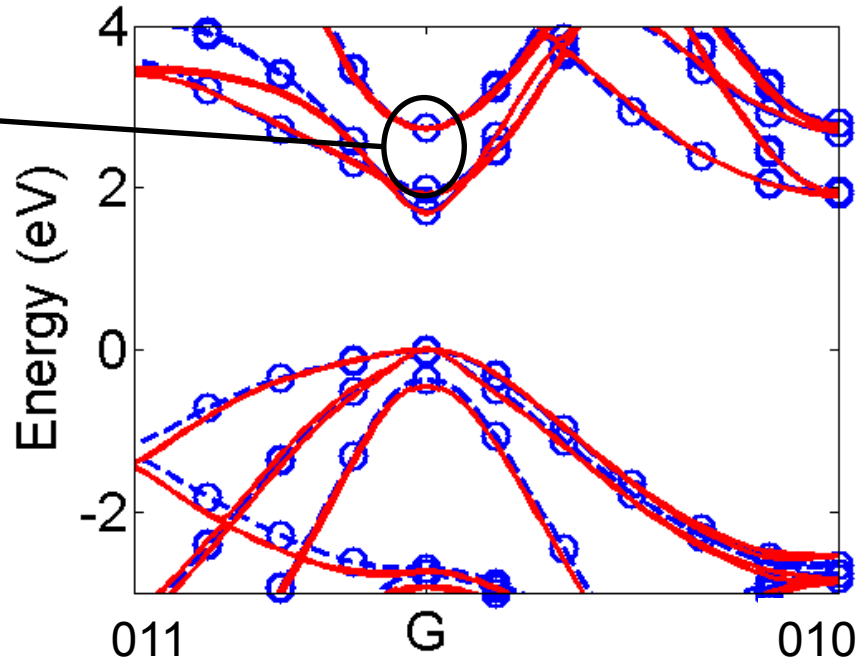
GaAs/InAs



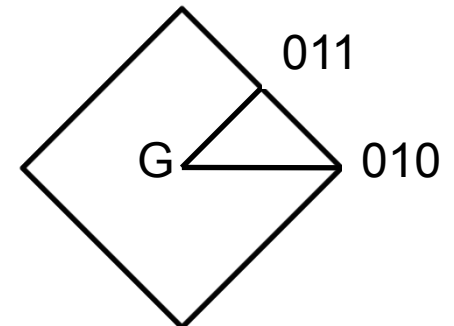
InAs/AlAs



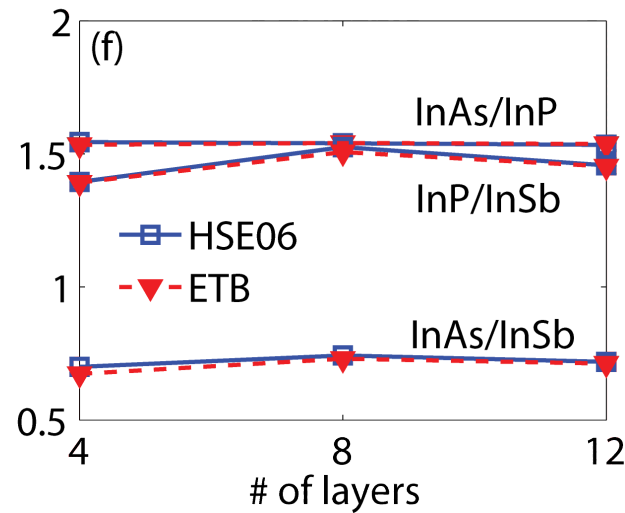
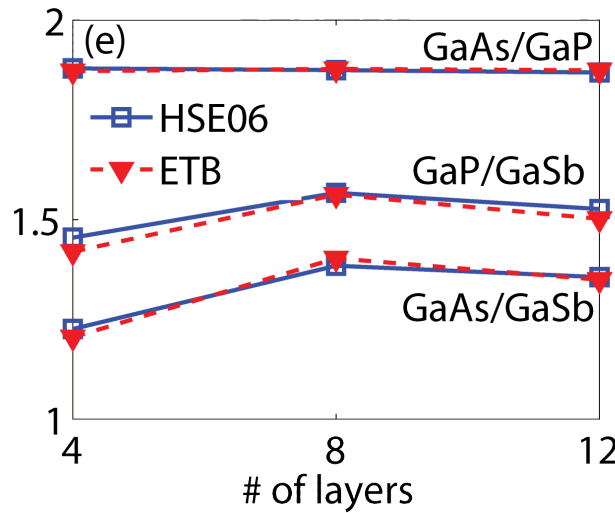
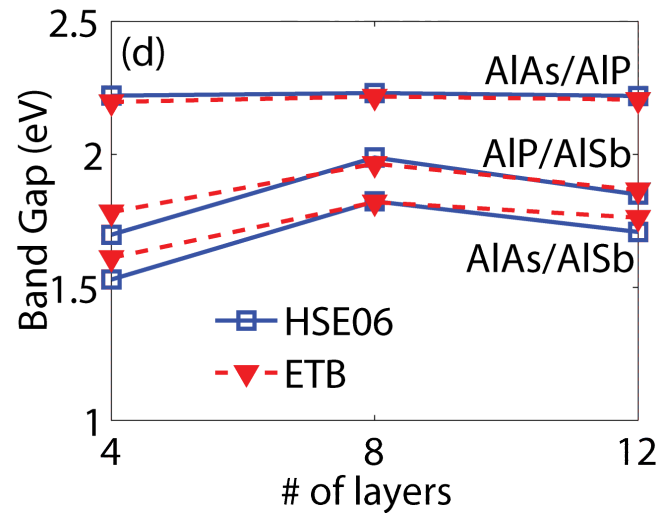
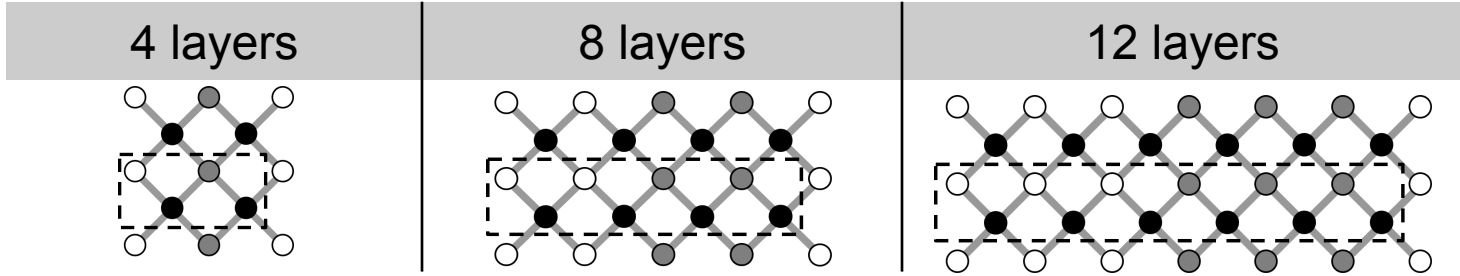
Folded bands originate from X valleys



Lowest few conduction bands originate from Γ and X valleys in the fcc BZ



Superlattices with common cations



Band gaps of different superlattices by TB agree with HSE06 calculations.

Type III superlattice? →
confinement opens the band gap

