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Influence of cross-section geometry and wire orientation on the phonon shifts in ultra-scaled Si nanowires

Abhijeet Paul, Mathieu Luisier, and Gerhard Klimeck
School of Electrical and Computer Engineering, Network for Computational Nanotechnology, Purdue University, West Lafayette, Indiana 47907, USA

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Engineering the cross-section shape and size of ultra-scaled Si nanowires (SiNWs) provides an attractive way for tuning their structural properties. The acoustic and optical phonon shifts of the free-standing circular, hexagonal, square, and triangular SiNWs are calculated using a modified valence force field (MVFF) model. The acoustic phonon blue shift (acoustic hardening) and the optical phonon red shift (optical softening) show a strong dependence on the cross-section shape and size of the SiNWs. The triangular SiNWs have the least structural symmetry as revealed by the splitting of the degenerate flexural phonon modes and these show the minimum acoustic hardening and the maximum optical hardening. The acoustic hardening, in all SiNWs, is attributed to the decreasing difference in the vibrational energy distribution between the inner and the surface atoms with decreasing cross-section size. The optical softening is attributed to the reduced phonon group velocity and the localization of the vibrational energy density on the inner atoms. While the acoustic phonon shift shows a strong wire orientation dependence, the optical phonon softening is independent of wire orientation.


I. INTRODUCTION

Silicon nanowires (SiNWs) have the potential to become the next generation solution for improved (1) complementary-metal-oxide-semiconductor (CMOS) transistors with higher channel drive currents, (2) thermoelectric (TE) devices, (3) rechargeable batteries, (4) compact non-volatile memories, (5) solar cells, and (6) explosive and bio-sensors. A lot of vital information about their structural properties can be optimized for maximum technological benefits in SiNWs.

Engineering the Si nanowire structural properties based on their cross-section size has been studied extensively. However, the impact of cross-section shape has not been completely addressed yet. Experimentally, the impact of semiconductor (GaAs, GaP, ZnS, etc.) nanowire shape on their structural properties has been observed. Motivated by these experiments, we theoretically explore the effect of the cross-section geometry of ultra-scaled SiNWs on their structural properties like phonon shifts. We furthermore provide analytical expressions for the variation of these physical quantities with size and shape thus, enabling (1) physical insights and (2) a compact modeling representation of the structural properties.

The determination of size and stability of SiNWs is crucial for their usage in different applications. Raman spectroscopy provides a valuable, non-destructive method to analyze the physical properties of nanostructures (NS) like cross-section size, degree of crystallinity, dimensionality of confinement, etc. Raman spectroscopy utilizes the amount of phonon spectrum shift and line width broadening to obtain useful structural information. The first satisfactory theoretical model for explaining Raman shifts and line width broadening was proposed by Richter et al. and improved by Campbell and Fauchet. These phenomenological continuum models are based on the choice of the phonon weighting function as well as the boundary conditions of the phonon vibrations which are chosen rather arbitrarily and hence do not provide correct phonon shift in nanostructures. Arora et al. experimentally reported that phonon shifts are very different from bulk in nanostructures with size less than 20 nm. Tanaka et al. also pointed out the failure of continuum models to predict the Raman shift in nanostructures with size <7.5 nm due to the arbitrary parameter sets used in continuum models. While continuum models can match the experimental Raman spectroscopy data using fitting parameters, they lack the predictive capability for estimating the phonon shifts and line widths in nanostructures with different shapes and compositions.

The evident inability of the continuum models to properly explain and predict the structural properties in nanostructures demands for methods which can automatically take into account the effects of structural miniaturization like geometrical confinement, orientation effects, cross-sectional shape, and surface-to-volume ratio effects.

Many efforts to explain the phonon shifts in nanostructures have been reported. They are based on models like the VFF approach, partial density approach, bond charge model (BCM), bond order model, etc. In all these approaches, the importance of taking into account the atomic positions and the atomic surrounding to understand the Raman spectroscopy data using fitting parameters, they lack the predictive capability for estimating the phonon shifts and line widths in nanostructures with different shapes and compositions.
shift has been stressed which most of the continuum models lack.23,24

We utilize a modified valence force field (MVFF) phonon model30–32 to study the physical properties of SiNWs. This MVFF model (1) is relatively straightforward to understand and implement, (2) explains the experimental phonon and elastic properties of zinc-blende materials very well,28,30,31,33 and (3) is computationally very efficient which allows for expanding the simulation domain easily to few million atoms.34 However, frozen phonon models like the MVFF one do not integrate thermodynamics which forbids the correct calculation of many physical properties such as low-temperature volume thermal expansion. Yet these models give a good insight into the physical processes governed by the lattice under ambient conditions.

The paper is organized as follows. Section II provides a brief introduction about the MVFF model for the calculation of phonons in SiNWs and about the method to extract the phonon shifts in these nanostructures (Sec. II B). The results section (Sec. III) discusses the effect of cross-section shape and size on the phonon spectra (Sec. III A) and presents experimental benchmarking of the phonon shifts using the MVFF model (Sec. III B). Furthermore, the trends of the acoustic phonon shift (Sec. III C) and the optical phonon shift (Sec. III D) are discussed along with wire orientation dependence (Sec. III E). Conclusions are provided in Sec. IV.

II. THEORY AND APPROACH

A. Phonon model

In the MVFF model, the frequencies of the phonon modes are calculated from the forces acting on atoms induced by finite displacements of the atoms from their equilibrium positions in a crystal.35 To calculate the restoring force(F), first, the total potential energy of the solid (U) is estimated. For the MVFF model, U is approximated as,31

\[
U \approx \frac{1}{2} \sum_{i \in N_A} \left[ \sum_{j \in m(i)} U_{ij}^{bb} + \sum_{j,k \in m(i)} (U_{ijk}^{bb} + U_{ijk}^{bb} + U_{ijk}^{bb}) + \sum_{j,k \in COP_i} U_{ijkl}^{bb} \right],
\]

where \(N_A\), \(nn(i)\) and \(COP_i\) represent the total number of atoms in one unit cell, the number of nearest neighbors for atom “I,” and the coplanar atom groups for atom “I,” respectively. The first two terms \(U_{ij}^{bb}\) and \(U_{ijk}^{bb}\) represent the elastic energy coming from bond stretching and bending between the atoms connected to each other as given in the original Keating VFF model.36 The terms \(U_{ijk}^{bb}\) represent the cross bond stretching,30 cross bond bending-stretching,33 coplanar bond bending interactions, respectively. The detailed procedure for obtaining the phonon spectra in Si bulk and NWs are provided in Refs. 31 and 32. In the following sections, the method to extract the acoustic and optical phonon shifts and the types of SiNWs used in this study are discussed.

B. Phonon shift in Si nanowires

The vibrational spectra of the nanostructures are strongly influenced by (1) the finite size of the nanostructures, (2) the mismatch with the matrix material (the surrounding atoms), or (3) defects.12,20,22 The optical and the acoustic phonon energies are shifted compared to the bulk values (around \(q \approx 0\)) in these geometrically confined structures. Raman spectroscopy reveals the decrease of the optical frequency with down-scaling of the nanostructures (called the optical softening or optical red shift)27,37 and the increase of the acoustic frequency (called the acoustic hardening or acoustic blue shift).12,27 These phonon shifts are estimated using the following relation:14,27,29

\[
\Delta \omega_0^{ac/\text{opt}} = \omega_0^{ac/\text{opt}} - \omega_0^{ac/\text{bulk}},
\]

where \(\omega_0^{ac/\text{bulk}}\) is the bulk acoustic (optical) phonon frequency at the \(\Gamma\) point. The phonon shifts show the following functional dependence on the nanostructure cross-section size (W),11,27,29

\[
\Delta \omega_0^{ac/\text{opt}} = A_{ac/\text{opt}} (\frac{d_0}{W})^{d_{ac/\text{opt}}} [\text{cm}^{-1}],
\]

where \(d_0\) is the lattice constant of the material. For \(A > 0\), the phonon shift is positive (or blue shift) and for \(A < 0\), the shift is negative (or red shift).27 The exponent value “d” indicates the dimensionality of the geometrical confinement. For 1D nanowires/nanorods, a variety of “d” values has been reported in the literature like 0.67,29 0.95,8 1.44,11 etc.

Using a series of Raman spectroscopy measurement for a sample of nanostructures, the size and the dimensionality of the nanostructures can be predicted.15,22,27 The phonon shifts observed in Raman spectroscopy can be predicted using the phonon spectrum. Atomistic phonon modeling correctly takes surface boundary conditions into account depending on the cross-section shape of the wire which reflects in the overall phonon spectrum. The surface and inner atomic movements vary with different cross-section shapes and, therefore, affect the phonon shifts. Equation (3) captures the nanostucture size effect in the exponent value “d” and the shape effect in the pre-factor “A.” Thus, a combination of A and d can be useful for the determination of size and shape of the SiNWs.

C. Si Nanowire details

Four cross-section shapes for [100] oriented SiNWs have been considered in this study, (a) circular, (b) hexagonal, (c) square, and (d) triangular cross-section shapes (Fig. 1). SiNWs with [110] and [111] channel orientation studied here are of square cross-section only. The feature size is determined by the width parameter W. The value of W is varied from 2 to 6 nm. The surface atoms are allowed to vibrate freely without any passivating species. The wires are still assumed to have a tetrahedral geometry. It has been shown that wires with diameter below 2 nm tend to lose the tetrahedral structure due to surface pressure and internal strain.
III. RESULTS AND DISCUSSION

In this section, the effect of cross-section on the phonon dispersion and phonon shifts of [100] SiNWs are discussed. There is a lack of proper channel orientation information in the literature. However, Adu et al.\textsuperscript{40} reported [100] channel orientation due to which we chose [100] SiNWs for shape study. Furthermore, we also investigate the impact of channel orientation on the phonon shifts in square SiNWs.

A. Phonon dispersion

The phonon dispersion of SiNWs for all the cross-section shapes with [100] channel are shown in Fig. 2. While the full phonon dispersion extends up to $\omega_{q=0} \approx q^2$, phonon modes till 9 meV energy range are shown for clarity. All the wires exhibit two flexural branches\textsuperscript{32} ($\omega_{q=0} \approx q^2$). These modes are double degenerate in all the shapes except the triangular wire. In the triangular wires, these modes split due to the reduced structural symmetry (Fig. 2(d)). The next two phonon branches in all the structures show $\omega_{q=0} \approx q$. These branches determine the sound velocity in these structures\textsuperscript{32} (Table I). The triangular wire has the lowest longitudinal and transverse sound velocity ($V_{snd,l}$) whereas other shapes have very similar sound velocities. The splitting of the degenerate flexural modes and the reduced sound velocity show that triangular wires have the least structural symmetry.

B. Experimental benchmark

Before using the MVFF model to calculate phonon frequency shifts, it is important to compare the theoretical MVFF results with experimental data. Both the experimental acoustic and optical phonon shifts in Si nanocrystals are compared with other experimental data and theoretical models.

1. Acoustic shift

Acoustic phonon shift obtained in square [111] SiNWs using the MVFF model compares very well with other theoretical values\textsuperscript{14,41} as shown in Fig. 3. The acoustic shift is caused due to the geometrical confinement present in SiNWs which breaks the crystal symmetry\textsuperscript{27} providing frequency shifts between 20 to 100 cm$^{-1}$. Similar acoustic hardening is also reported in Ref. 41 for [111] SiNWs utilizing the Keating VFF model\textsuperscript{36} (Si-1, Si-2 in Fig. 3) and in Ref. 14 which uses the bond charge model (Si-3 in Fig. 3). The phonon shifts calculated using MVFF show a power law of $W^{0.78}$ which is close to the BCM result of $W^{0.71}$ for square SiNWs.\textsuperscript{14} Thus, the acoustic phonon shifts from the MVFF model compare well with other theories.

2. Optical shift

The optical phonon shift is experimentally measured using Raman spectroscopy.\textsuperscript{15} With decreasing cross-section size, the optical red-shift increases.\textsuperscript{27} The theoretical optical phonon shift is calculated for free-standing [100] circular SiNWs using the MVFF model (Si-8 in Fig. 4). The theoretical values of the optical shift agree well with the experimental data\textsuperscript{15} (Si-2 in Fig. 4). Comparison of the MVFF calculation (Si-8) with other theoretical models (see Fig. 4) like the Si-1 result based on BCM from Ref. 14, Si-3 (Ref. 27) based on bond order length strength correlation method (BOLS), Si-4 (Ref. 42) obtained by empirical fitting using Gaussian function,\textsuperscript{24} Si-5 (Ref. 11) based on bond polarizability model (BPM), Si-6 (Ref. 43) based on theoretical size

<table>
<thead>
<tr>
<th>Shape</th>
<th>$V_{snd,l}$ (km/s)</th>
<th>$V_{snd,t}$ (km/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Circular</td>
<td>6.23</td>
<td>4.50</td>
</tr>
<tr>
<td>Hexagon</td>
<td>6.18</td>
<td>4.37</td>
</tr>
<tr>
<td>Square</td>
<td>6.26</td>
<td>4.37</td>
</tr>
<tr>
<td>Triangular</td>
<td>5.79</td>
<td>3.12</td>
</tr>
</tbody>
</table>
dependence of root-mean-square average amplitude of atomic thermal vibration, and Si-7 (Ref. 44) obtained from a modified phonon confinement model (Heisenberg’s uncertainty principle), is very good. The mismatch in the phonon shifts at extremely small dimensions (W /C^2 = 2 nm) may be due to the structural relaxation in small cross-section wires (38,39) which is not taken into account in this study. Hence, the MVFF model correctly captures the optical phonon shifts in SiNWs for W = 2 nm. However, for W < 2 nm, the MVFF phonon values without structural relaxation are not very accurate. Though the optical shift is well captured by the Richter model (23) (Si-4 in Fig. 4), the fitting parameters are chosen arbitrarily which removes the predictive capability from the model.

In the next few sections, we will discuss the structural properties of ultra-scaled SiNWs with different cross-section shapes and sizes.

C. Acoustic phonon shift in SiNWs

1. Influence of cross-section shape and size

The acoustic phonon shifts are calculated using the MVFF model for different cross-section shaped SiNWs. All the wire geometries show a blue shift of the acoustic mode (this mode closely resembles the “radial breathing mode” observed in perfectly circular wires (41)) as the wire cross-section size is reduced (Fig. 5(a)). There is a clear cross-section shape dependence of the blue shifts where the blue shift follows the order D_x^tri < D_x^sq < D_x^hex < D_x^cir. The power exponent (d_ac), for the SiNWs in this study, varies between 0.6 and 0.87 (Table II). The order of the pre-factor (A_ac) in Eq. (2) value (Table II) also shows the order of the acoustic blue shift for [100] SiNWs.

Similar trends for acoustic blue shift are observed in other theoretical works (14,41). The power exponent and the pre-factor are shown in Table II. The values of d_ac and A_ac for Si-1 and Si-2 indicate that the SiNWs used in Ref. 41 are almost circular which is indeed the case as presented in that work. Similarly, the d_ac and A_ac values obtained for Si-3 (based on BCM) represent a square SiNW which is corroborated by the structure shape used in Ref. 14. Thus, the combination of d_ac and A_ac values can clearly correlate to the shape of the SiNWs and these combinations are very well calculated using the MVFF model.

With the increase in wire cross-section size, two important things happen, (1) the geometric confinement on the phonons reduces and (2) the vibrational energy deviation between the surface and the inner atoms decreases (Fig. 5). First point explains the reduction in the blue shift with increase in cross-section size for all the SiNWs while the second point explains the order of blue-shift with shape.

As the SiNW cross-section is reduced, lots of low velocity phonon sub-bands start to appear above the acoustic branches (Fig. 2) which are normally absent in bulk. These relatively flat bands cause phonon confinement. These zone center low energy phonon sub-bands cause acoustic blue shift. The surface atom vibrations become comparable to the...
The spatial vibrational energy density can be calculated as 

\[ D = \frac{1}{NA} \sum_{i,j} [F_{BE}(\omega_{i,j}) + 0.5]R_{ij} \phi_{i,q,j} \phi_{i,q,j} \tag{4} \]

where \( NA \) is the total number of atoms in the unit cell, \( \omega_{i,j} \) is the phonon sub-band, \( q \) is the phonon wave-vector, \( j \) is the polarization, \( F_{BE} \) is Bose-Einstein distribution for phonon population, \( \phi_{i,q,j} \) is the phonon eigen frequency for sub-band \( i \) and wave-vector \( q \), and \( \phi_{i,q,j} \) is the phonon eigen vibration mode.

Figure 5(b) shows that the triangular wire exhibits the maximum difference between the surface and inner atom vibrational energy density for \( W = 2 \) nm and 4 nm, followed by the square, the hexagonal, and the circular wire. Figure 6 shows the spatial distribution of the energy density for the acoustic phonon branch for 2 nm cross-section SiNWs. The surface atoms vibrate more intensively compared to the inner atoms. In circular and hexagonal nanowires, all atoms vibrate with a similar intensity as indicated by the small \( \Delta E \) value. However, in square and triangular wires, the surface atoms vibrate more compared to the inner atoms leading to a larger \( \Delta E \) value.

The low frequency acoustic phonon modes are very similar to the breathing mode found in larger circular wires. These eigen frequencies follow a \( 1/W^2 \) law (Fig. 5), with \( d = 1 \) for a perfectly concentric circular wire. The value of “d” deviates from 1 as the cross-section shape deviates from the ideal circular geometry.

D. Optical phonon shift in SiNWs

1. Influence of cross-section shape and size

For optical phonon shift, the MVFF model predicts a width exponent factor \( d_{opt} \) between 1.8 and 2 (Table III) for all the cross-section shapes. The [100] triangular SiNWs show the maximum optical red shift (\( d_{opt} = 1.795 \)) whereas the square SiNWs show the minimum optical red shift (\( d_{opt} = 2.06 \), close to the prediction in Ref. 14) (Fig. 7). Furthermore, with decreasing cross-section size (\( W \)), all the wires show an increasing optical red-shift (Fig. 7).

The \( d_{opt} \) and \( A_{opt} \) values for optical phonon frequency shift in SiNWs from other experimental data and theoretical models are provided in Table III. The combination (\( d_{opt} \) and \( A_{opt} \)) for Si-1 indicates a roughly square SiNW which is indeed the structure used in Ref. 14. The (\( d_{opt} \) and \( A_{opt} \)) combination for Si-2 directs towards triangular SiNWs. Experimentally, the cross-section shapes are not very clear since the fabricated SiNWs are all bunched up together. The value of \( d_{opt} \) and \( A_{opt} \) for Si-3,27 Si-5,11 and Si-6 (Ref. 43) are smaller compared to the values obtained from MVFF model. This can be due to the use of (1) surface reconstruction (neglected in present study) and (2) bulk phonon dispersion in these theoretical models. The \( d_{opt} \) and \( A_{opt} \) combination for Si-7 indicates a square SiNW which is indeed the case as provided in Ref. 44. Thus, the optical coefficients provide a good correlation to the SiNW shapes as corroborated from other theoretical and experimental works. Hence, MVFF provides a reliable indicator for the SiNW shapes using the optical phonon red-shift.

![Diagram](image_url)
Many explanations have been reported in the literature for the optical red-shift in nanostructures like, the increasing SVR,\textsuperscript{21,27} compressive strain,\textsuperscript{26} surface defects,\textsuperscript{46} and optical phonon confinement.\textsuperscript{21,23,24,47} In the present study of free-standing SiNWs, the observed shape and size dependence can be explained using the vibrational energy density\textsuperscript{45} of the optical mode as well as the optical phonon group velocity ($V_{\text{ph}}^{\text{grp}}$).\textsuperscript{32}

Figure 8 shows the spatial distribution of the vibrational energy density for the optical mode in SiNWs with $W = 4$ nm. The structure with the maximum spatial spread of the energy density has the most active optical modes\textsuperscript{27} since surface atom vibrations contribute to the optical modes. The symbols in Fig. 8 show the full width half maximum (FWHM) extent of the energy density. The square wire has the maximum energy spread while the triangular wire has the minimum energy spread which explains the highest red-shift in the triangular wires (least active optical modes). As the SiNW dimensions decrease, the energy spread also decreases which increases the red shift for all the shapes.

Another reason for the red-shift can be attributed to the phonon group velocity. Figure 9 shows that the triangular wire has the smallest group velocity whereas the square wire has the highest group velocity. A smaller group velocity implies higher phonon confinement.\textsuperscript{37} Thus, the phonon group velocity gives the following order of optical phonon confinement; triangular $>$ circular $>$ hexagonal $>$ square. Higher phonon confinement results in more red-shift. This again explains the observed shape dependence of optical red-shift in [100] SiNWs.

**E. Orientation effect on phonon shifts**

Along with the shape and size of the SiNWs, the wire axis direction can also produce different phonon shifts. This indicates that the confined phonon dispersion is anisotropic. For brevity, we present the orientation effects for square SiNWs only, however, these trends are also valid for other shapes. The acoustic phonon shift and the optical phonon shifts are shown in Figs. 10(a) and 10(b), respectively. The acoustic phonon blue shift exhibits a strong anisotropy (Fig. 10(a)), however, the optical red shift has a very weak orientation dependence (Fig. 10(b)). This observed behavior of phonon shift can be explained by the phonon dispersion anisotropy in Si. In Si, the maximum phonon frequency of the
TABLE IV. Width parameters for acoustic and optical phonon shift in square SiNWs with different orientations.

<table>
<thead>
<tr>
<th>Channel Or</th>
<th>$A_{ac}$ (cm$^{-1}$)</th>
<th>$d_{ac}$</th>
<th>$A_{opt}$ (cm$^{-1}$)</th>
<th>$d_{opt}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>[100]</td>
<td>210.4</td>
<td>0.79</td>
<td>-74.62</td>
<td>2.06</td>
</tr>
<tr>
<td>[110]</td>
<td>196.7</td>
<td>0.89</td>
<td>-66.47</td>
<td>2.00</td>
</tr>
<tr>
<td>[111] (Si-4, Fig. 3)</td>
<td>201.4</td>
<td>0.81</td>
<td>-57.17</td>
<td>1.97</td>
</tr>
</tbody>
</table>

acoustic branch along [100], [110], and [111] directions are highly anisotropic, whereas the maximum frequency of the optical branches are isotropic (~519.3 cm$^{-1}$). The acoustic blue shift show the following behavior $\Delta \omega_{100}^{ac} > \Delta \omega_{111}^{ac} > \Delta \omega_{110}^{ac}$. The cross-section size dependence for both kind of phonon shifts are provided in Table IV. The acoustic phonon shift exponent of [110] wires is 0.89 which compares reasonably to the exponent of 0.95 observed for [110] SiNWs in Ref. 8 (see Fig. 3).

F. Discussion

The phonon spectrum shift in SiNWs with shape, size, and orientation is useful in understanding the experimental Raman shifts. The analytical expressions for the shifts can provide a good idea about the structure of the SiNWs which can be helpful in determining properties such as phonon-photon interactions. The evolution of the phonon shifts with increasing size also reflects the size (Wlim) at which the shape effects may be no more distinguishable using Raman spectroscopy. From the expressions of the phonon shifts (Eq. (2)), the Wlim value for acoustic blue shift comes out to be roughly 7 nm and for optical shifts this value is 10 nm. The analytical expressions are well suited for calculating the vibrational energy shifts depending on different physical aspects of the SiNWs.

IV. CONCLUSION

We have used a MVFF model to calculate the acoustic and optical phonon shifts in SiNWs. The theory agrees quite well with the experimental Raman shift data. At the nanometer scale, the acoustic phonon shift is quite sensitive to the (1) wire cross-section size and shape and (2) wire channel orientation whereas the optical phonon shift is mainly controlled by the wire cross-section shape and size. The different width exponents and the pre-factors from the acoustic and optical phonon shifts can become a useful tool in predicting the size and shape of the SiNWs. Triangular wires show the highest optical phonon confinement and the least structural symmetry. Analytical expressions for the shape and size dependence of the phonon shifts are useful for compact modeling of physical properties of ultra-scaled SiNWs.

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