

ECE59500NL Lecture 16: Parsing—II

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Some Abstractions

```
(define rule-lhs first)
(define rule-rhs1 third)
(define rule-rhs2 fourth)
(define entry-word first)
(define entry-category second)

(define (empty? word-string) (null? word-string))

(define (singleton? word-string)
  (= (length word-string) 1))

(define (head word-string) (first word-string))

(define (tail word-string) (rest word-string))

(define (ith-word word-string i)
  (list-ref word-string i))

(define (lookup word lexicon)
  (define (lookup lexicon)
    (when (null? lexicon) (fail))
    (if (string-ci=? word (entry-word (first lexicon)))
        (either (entry-category (first lexicon))
                 (lookup (rest lexicon)))
        (lookup (rest lexicon))))
  (lookup lexicon))
```

Top Down Recognizer

FAILIFNOTPHRASE(w, c)

- ▶ Base case: w contains a single word
 - ▶ fail if $\text{CATEGORY}(w) \neq c$
- ▶ Inductive case: w contains more than one word
 - ▶ choose a rule $A \rightarrow BC$ where $A = c$
 - ▶ split w into lr
 - ▶ FAILIFNOTPHRASE(l, B)
 - ▶ FAILIFNOTPHRASE(r, C)

Top Down Recognizer in Lisp

```
(define (split word-string)
  (define (split left right)
    (when (null? right) (fail))
    (either (list left right)
             (split (append left (list (first right)))
                    (rest right)))))
  (when (null? word-string) (fail))
  (split (list (first word-string)) (rest word-string)))

(define (top-down:is-sentence? word-string rules lexicon)
  (define fail-if-not-phrase
    (lambda (word-string category)
      (cond
        ((singleton? word-string)
         (unless (eq? (lookup (head word-string) lexicon)
                          category)
          (fail)))
        (#t)
        (else (let ((rule (a-member-of rules)))
                  (unless (eq? (rule-lhs rule) category)
                    (fail))
                  (let ((word-strings (split word-string)))
                    (fail-if-not-phrase (first word-strings)
                                         (rule-rhs1 rule))
                    (fail-if-not-phrase (second word-strings)
                                         (rule-rhs2 rule))))))))))
  (one-value (fail-if-not-phrase word-string 's) #f))
```

Recursive Descent Recognizer

$\text{PEEL}(w, c)$

- ▶ fail if w is empty
- ▶ either
 - ▶ base case
 - ▶ fail if first word of w not of category c
 - ▶ return tail of w
 - ▶ inductive case
 - ▶ choose a rule $A \rightarrow BC$ with $A = c$
 - ▶ let $w' = \text{PEEL}(w, B)$
 - ▶ return $\text{PEEL}(w', C)$

Recursive Descent Recognizer in Lisp

```
(define (recursive-descent:is-sentence?
      word-string rules lexicon)
  (define peel
    (lambda (word-string category)
      (when (empty? word-string) (fail))
      (either
        (begin
          (unless (eq? (lookup (head word-string) lexicon)
                        category)
            (fail))
          (tail word-string))
        (let ((rule (a-member-of rules)))
          (unless (eq? (rule-lhs rule) category) (fail))
          (peel (peel word-string (rule-rhs1 rule))
                (rule-rhs2 rule))))))
  (one-value (begin (unless (null? (peel word-string 's))
                        (fail))
                    #t)
    #f))
```

Shift Reduce Recognizer

SHIFTREDUCE

- ▶ Termination Condition
 - ▶ fail unless buffer is empty and stack has a single entry
 - ▶ return top of stack
- ▶ Shift
 - ▶ fail if buffer is empty
 - ▶ pop off first word in buffer and push its category on the stack
 - ▶ SHIFTREDUCE
- ▶ Reduce
 - ▶ fail if stack has less than two entries
 - ▶ choose a rule $A \rightarrow BC$ where B = next of stack and C = top of stack
 - ▶ pop off top two entries from stack
 - ▶ push A on the stack
 - ▶ SHIFTREDUCE

Shift Reduce Recognizer in Lisp

```
(define (shift-reduce:is-sentence?
      word-string rules lexicon)
  (define shift-reduce
    (lambda (stack word-string)
      (either (begin
                (unless (and (empty? word-string)
                              (= (length stack) 1))
                  (fail))
                (first stack))
              (begin (when (empty? word-string) (fail))
                      (shift-reduce
                       (cons (lookup (head word-string)
                                     lexicon)
                             stack)
                       (tail word-string))))))
    (begin
      (when (< (length stack) 2) (fail))
      (let ((rule (a-member-of rules)))
        (unless (and (eq? (rule-rhs1 rule) (second stack))
                      (eq? (rule-rhs2 rule) (first stack)))
          (fail))
        (shift-reduce
         (cons (rule-lhs rule) (rest (rest stack)))
         word-string))))))
  (one-value
   (begin (unless (eq? (shift-reduce '() word-string) 's)
                   (fail))
           #t)
   #f))
```


Complexity of Top Down Recognizer

OBSERVATION: Halts since length of `word-string` decreases at each recursive call and can never be less than zero.

Let $p(n)$ be the number of recursive calls to `fail-if-not-phrase` needed to process a `word-string` of length n .

$$\begin{aligned}p(1) &= 1 \\p(n) &= 1 + \sum_{i=1}^{n-1} p(i)p(n-i)\end{aligned}$$

Exponential in n .

Recognition vs. Parsing

- ▶ Recognizer returns TRUE/FALSE
- ▶ Parser returns a parse tree
- ▶ Any recognizer can be turned into a parser
independent of strategy, memoization, partial evaluation, . . .

Top Down Recognizer \Rightarrow Parser

FAILIFNOTPHRASE(w, c)

- ▶ Base case: w contains a single word
 - ▶ fail if CATEGORY(w) $\neq c$
- ▶ Inductive case: w contains more than one word
 - ▶ choose a rule $A \rightarrow BC$ where $A = c$
 - ▶ split w into lr
 - ▶ FAILIFNOTPHRASE(l, B)
 - ▶ FAILIFNOTPHRASE(r, C)

\Downarrow

APARSEOF(w, c)

- ▶ Base case: w contains a single word
 - ▶ fail if CATEGORY(w) $\neq c$
 - ▶ otherwise return
- ▶ Inductive case: w contains more than one word
 - ▶ choose a rule $A \rightarrow BC$ where $A = c$
 - ▶ split w into lr
 - ▶ let t_1 be APARSEOF(l, B)
 - ▶ let t_2 be APARSEOF(r, C)
 - ▶ return

c
|
 w

A
└─┬─
 t_1 t_2

Recursive Descent Recognizer \Rightarrow Parser

PEEL(w, c)

- ▶ fail if w is empty
- ▶ either
 - ▶ base case
 - ▶ fail if first word of w not of category c
 - ▶ return tail of w
 - ▶ inductive case
 - ▶ choose a rule $A \rightarrow BC$ with $A = c$
 - ▶ let $w' = \text{PEEL}(w, B)$
 - ▶ return $\text{PEEL}(w', C)$

\Downarrow

PEEL(w, c)

- ▶ fail if w is empty
- ▶ either
 - ▶ base case
 - ▶ fail if first word of w not of category c
 - ▶ return $\langle \text{TAIL}(w), t \rangle$ where t is
 - ▶ inductive case
 - ▶ choose a rule $A \rightarrow BC$ with $A = c$
 - ▶ let $\langle w', t_1 \rangle = \text{PEEL}(w, B)$
 - ▶ let $\langle w'', t_2 \rangle = \text{PEEL}(w', C)$
 - ▶ return $\langle w'', t \rangle$ where t is

c
|
 w

A
└─┬─
 t_1 t_2

Shift Reduce Recognizer \Rightarrow Parser

SHIFTREDUCE

- ▶ Termination Condition
 - ▶ fail unless buffer is empty and stack has a single entry
 - ▶ return top of stack
- ▶ Shift
 - ▶ fail if buffer is empty
 - ▶ pop off first word in buffer and push its category on the stack
 - ▶ SHIFTREDUCE
- ▶ Reduce
 - ▶ fail if stack has less than two entries
 - ▶ choose a rule $A \rightarrow BC$ where B = next of stack and C = top of stack
 - ▶ pop off top two entries from stack
 - ▶ push A on stack
 - ▶ SHIFTREDUCE

\Downarrow

SHIFTREDUCE

- ▶ Termination Condition
 - ▶ fail unless buffer is empty and stack has a single entry
 - ▶ return top of stack
- ▶ Shift
 - ▶ fail if buffer is empty
 - ▶ pop off first word w in buffer and push $\langle c, t \rangle$ on the stack where c is the category of w and t is

$$\begin{array}{c} c \\ | \\ w \end{array}$$

- ▶ SHIFTREDUCE
- ▶ Reduce
 - ▶ fail if stack has less than two entries
 - ▶ pop $\langle c, t_2 \rangle$ off the stack
 - ▶ pop $\langle b, t_1 \rangle$ off the stack
 - ▶ choose a rule $A \rightarrow BC$ where $B = b$ and $C = c$
 - ▶ push $\langle A, t \rangle$ on the stack where t is

$$\begin{array}{c} A \\ \wedge \\ t_1 \quad t_2 \end{array}$$

- ▶ SHIFTREDUCE