

Lecture Summary – Combination

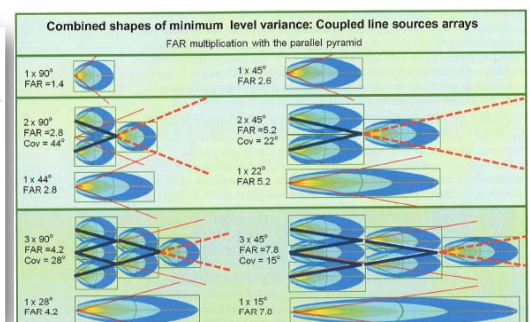
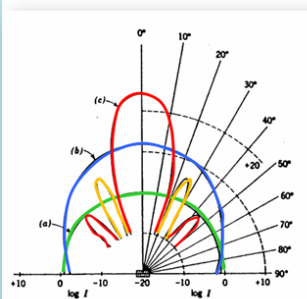
Chapter 9

- **array building**
 - two principal beamwidth shapes suitable for array building
 - 2nd order “plateau” type that flattens out in the high frequencies (“constant directivity”) – provides consistent unity splay angle → applications in both H and V planes (but in limited quantities)
 - highly sloped 3rd order elements useful in highly overlapped coupled array configurations (no consistent unity splay angle) – foremost application is creation of asymmetrical arrays → leader in vertical applications
 - (1st order speakers best suited for “standalone” applications → best for horizontal coverage applications
- **role of overlap as a “shaping tool”**
 - can range from half as wide to twice as wide
 - decisive factor: percentage overlap
 - control of overlap
 - angular (point in different directions)
 - displacement (moving elements apart)
 - low overlap: elements retain much of their individual character (yet merge to create “sculpted shapes” unique to arrays)
 - high overlap: individual elements disappear and merge into combined shape of “new and different” single speaker
 - overlap is the “shaping tool”
- **limitations of combined shapes**
 - will use aspect ratio icons to visualize individual contributions
 - *beam concentration and ripple variance aspect of combined response are not apparent in simple icon representation*
- **role of asymmetry as a “shaping tool”**
 - what asymmetries are available to the array designer
 - why are asymmetries necessary
 - which asymmetries are static and which are dynamic
- **coupled line source arrays – basic idea**
 - stack “aspect ratio icons” end-to-end (for side-by-side speakers)
 - combined shape of coupled line source visualized as forward extension by means of simple additions of aspect ratio shapes

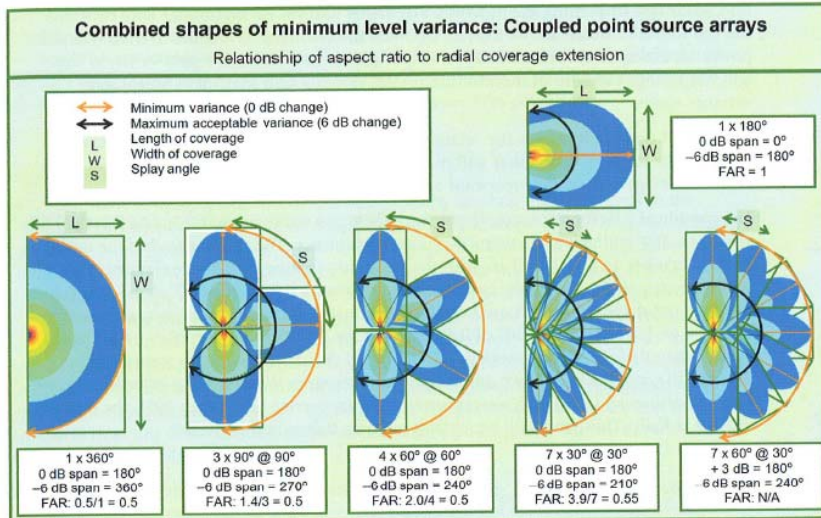
Recall: Beamwidth of a single speaker approaches 90° when the transmitted λ equals the radiating cone size (blue line in figure). Beamwidth is wider if $\lambda >$ cone size (green line) and narrower if $\lambda <$ cone size (red line).

For a coupled line source, vertical coverage is 72° when the transmitted λ equals the line length (e.g. beamwidth for a 2m long array will be 72° at 170 Hz).

Note that equations relating line length to beamwidth assume omnidirectional (“point”) sources.



- coupled point source arrays – basic idea
 - arrange aspect ratio icons side-by-side around a virtual point source (unity splay angle)
 - combined shape will strongly resemble radial spread of individual FAR patterns

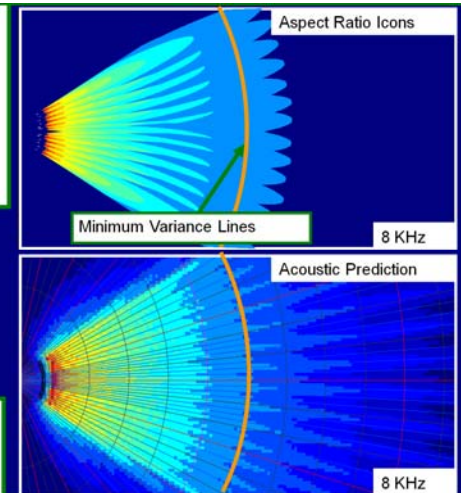


Shapes of Minimum Level Variance

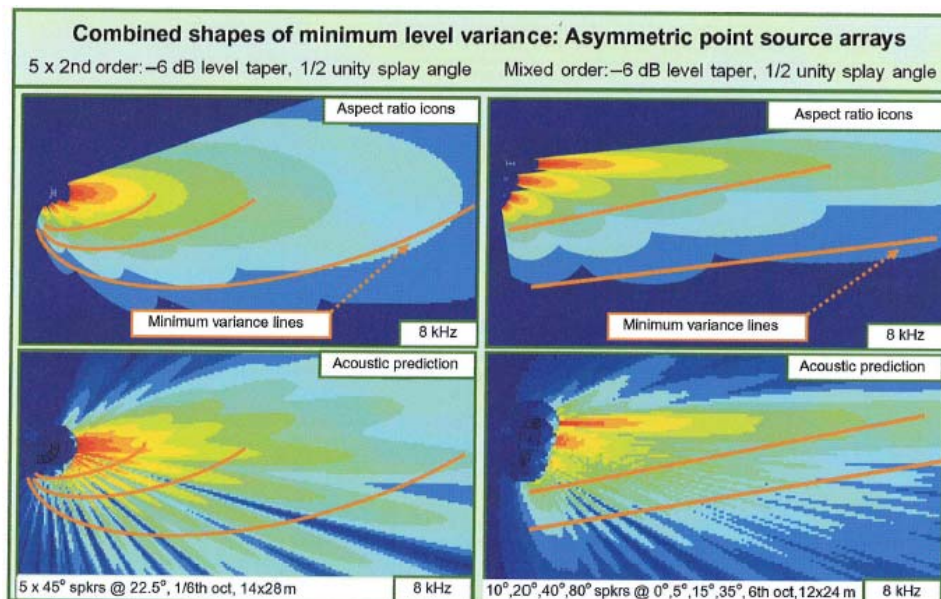
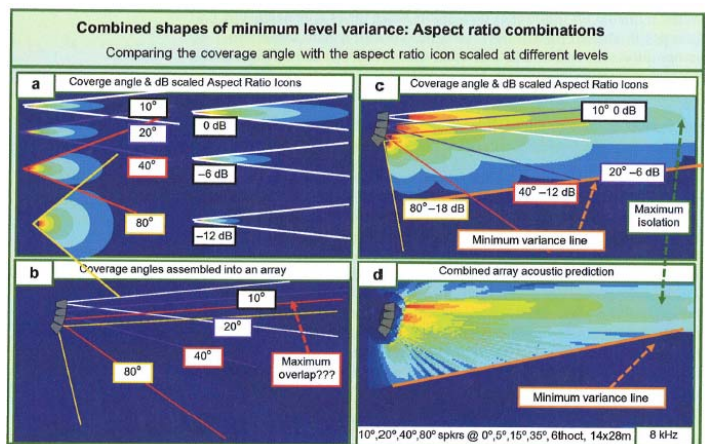
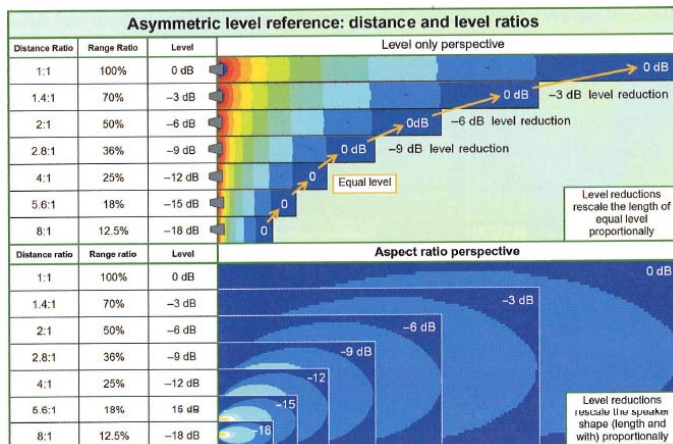
Coupled Point Source Arrays

Comparison of individual aspect ratio icons and the combined acoustic prediction

16 x 3rd order (15) @ 4 deg
1 octave, 34 x 80m

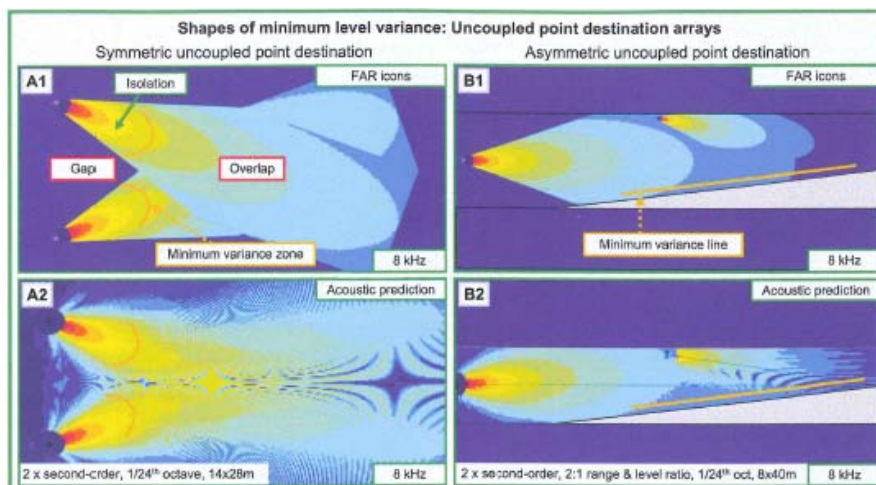
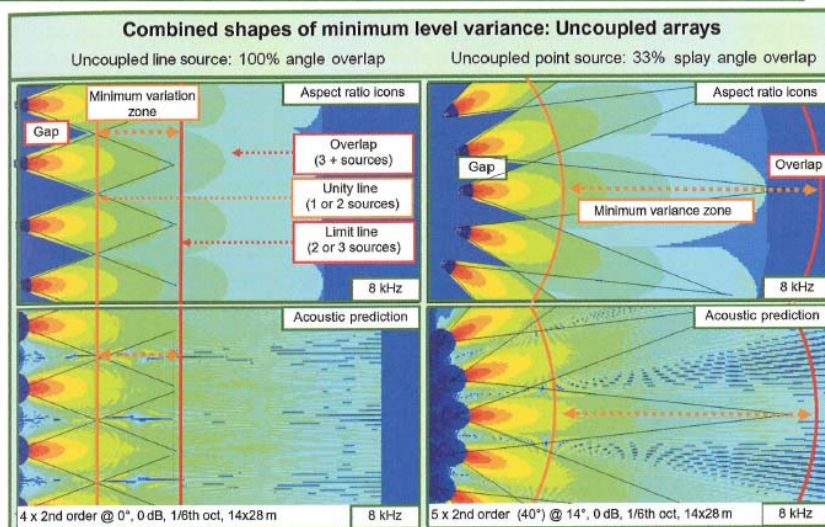
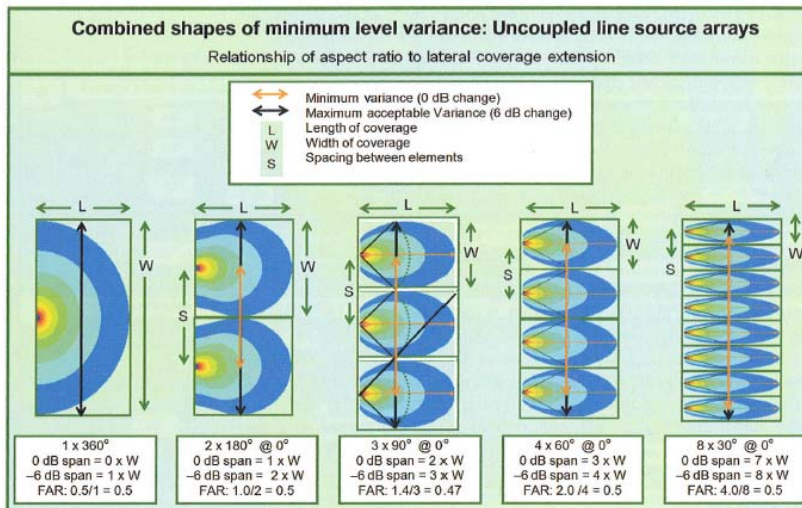


- asymmetric level scaling – size of icon reduced 50% for each reduction in level by 6 dB

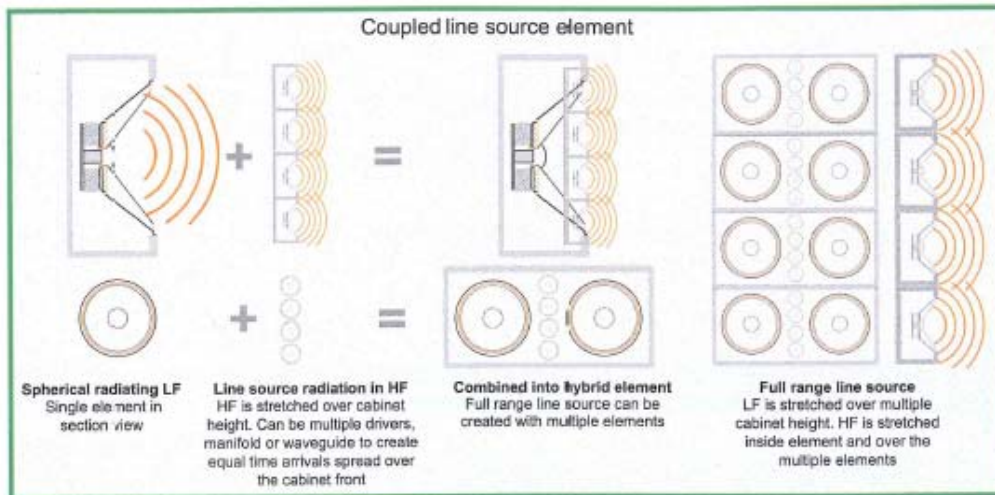


- uncoupled arrays – basic idea

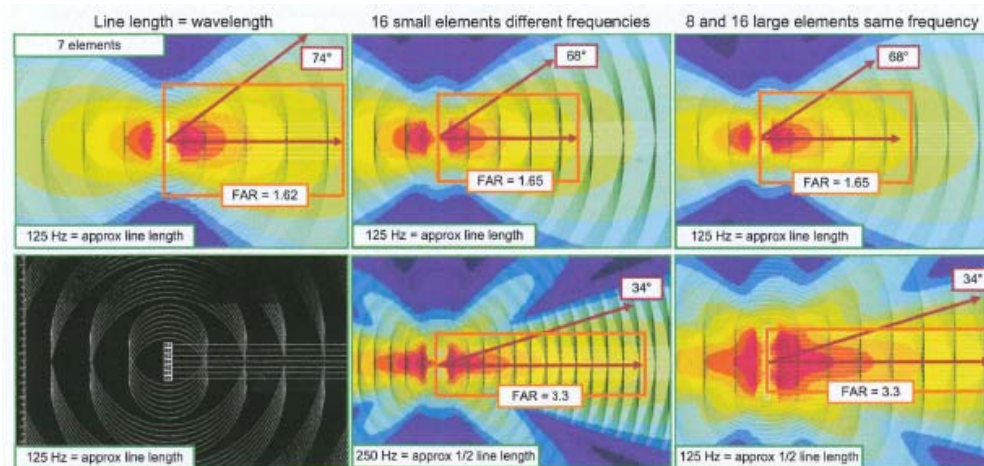
- best way to deal with overly wide coverage shapes
- combined shape can be seen as lateral extension by means of simple stacking of aspect ratio shapes
- combined aspect ratio becomes wider (while not becoming longer) and therefore lower in number
- FAR found by dividing the single element FAR by the number of elements



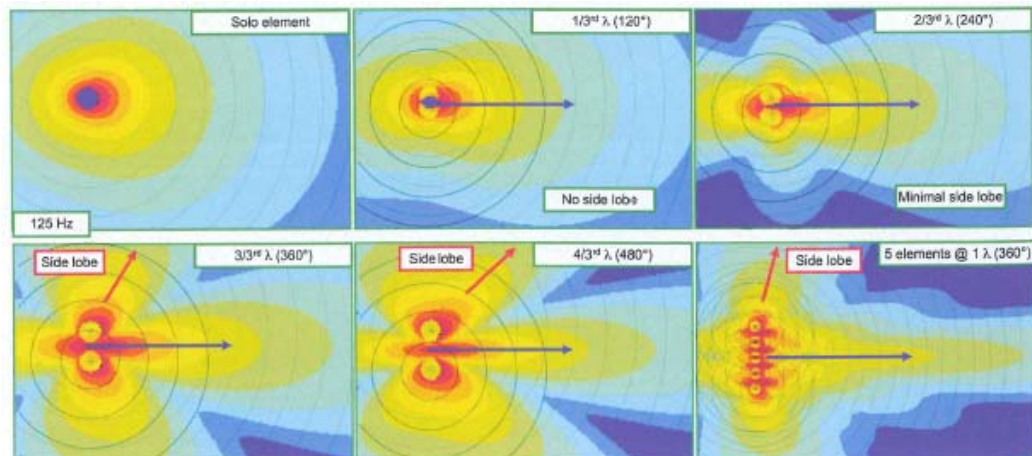
- spectral variance of coupled arrays
 - possible outcomes of beam combinations
 - concentration/power addition (coupling zone)
 - spreading (isolation zone)
 - “passing through each other” (combing zone)
- spectral variance of coupled line source arrays
 - representative line source element



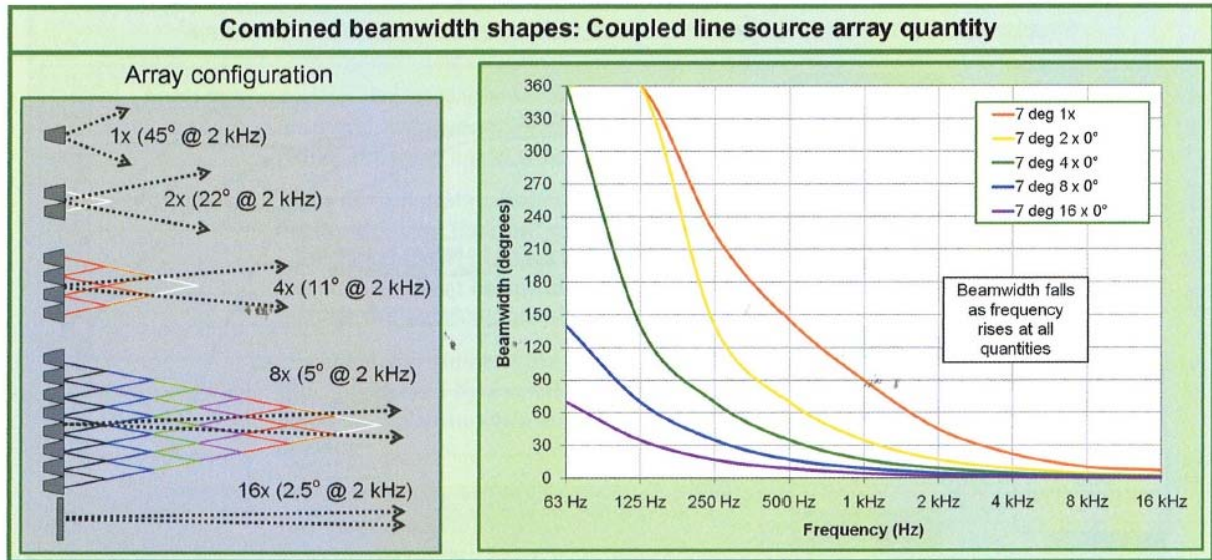
- coupled line source length effects



- coupled line source element spacing effects

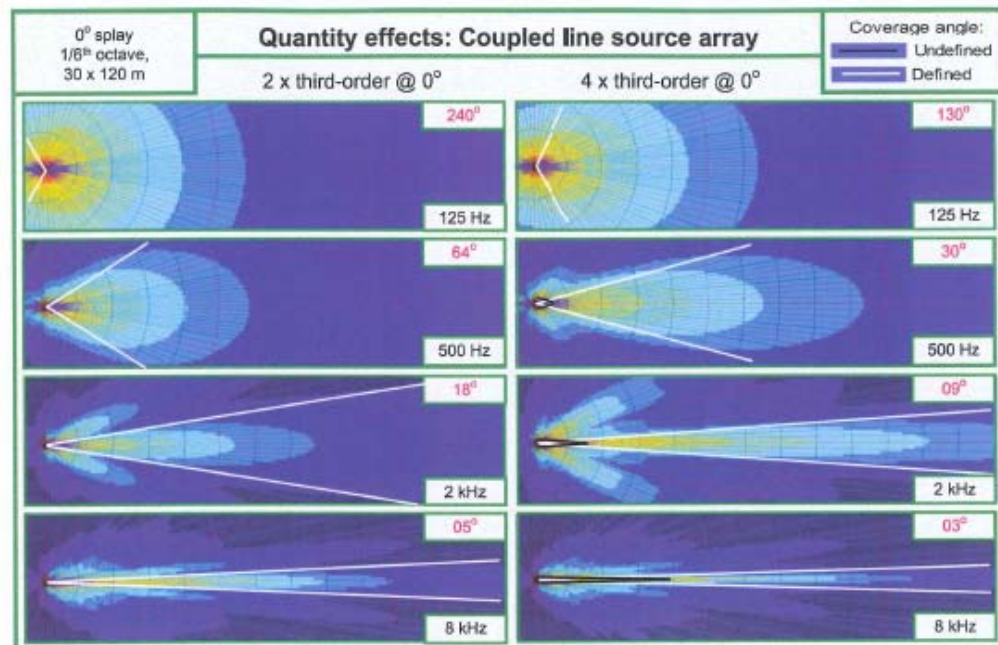


○ coupled line source element beamwidth shapes

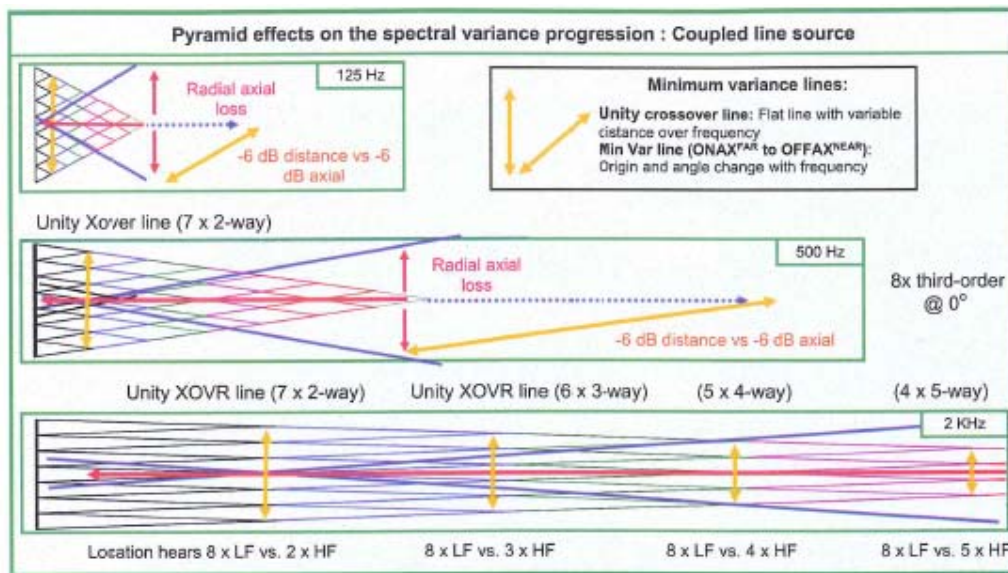


○ coupled line source element quantity effects

- coverage pattern narrows as quantity rises
- ratio of spectral variance unchanged by quantity
- beam concentration is primary driving force
- larger quantities give appearance of reduced spectral variance **if range of viewing does not extend far enough** for coupling to occur over the **full frequency range**



- coupled line source pyramid effects



- coupled line source speaker order effects

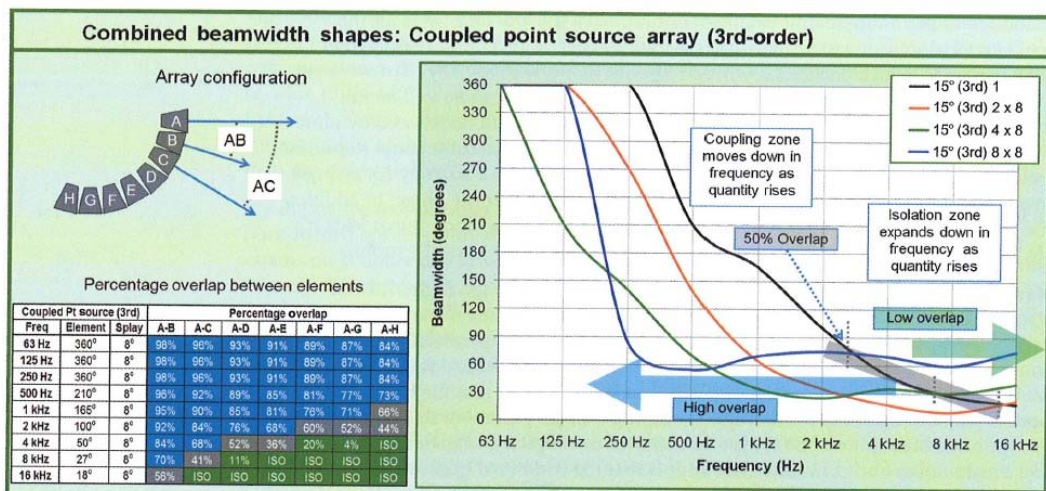
- line length is dominate force at lower frequencies (where line length $\geq \lambda/2$)
- side lobes vary with speaker order but main lobes are still matched at mid frequencies
- at high frequencies, low-order array coverage degenerates into ripple, while high-order array maintains focus

- coupled line source level tapering effect

- effectively reduces number of elements contributing to the “pyramid”
- behavior mimics an array of shorter length
- (aside – frequency dependent amplitude tapering not considered in text, nor is delay tapering – accomplished using DSP)

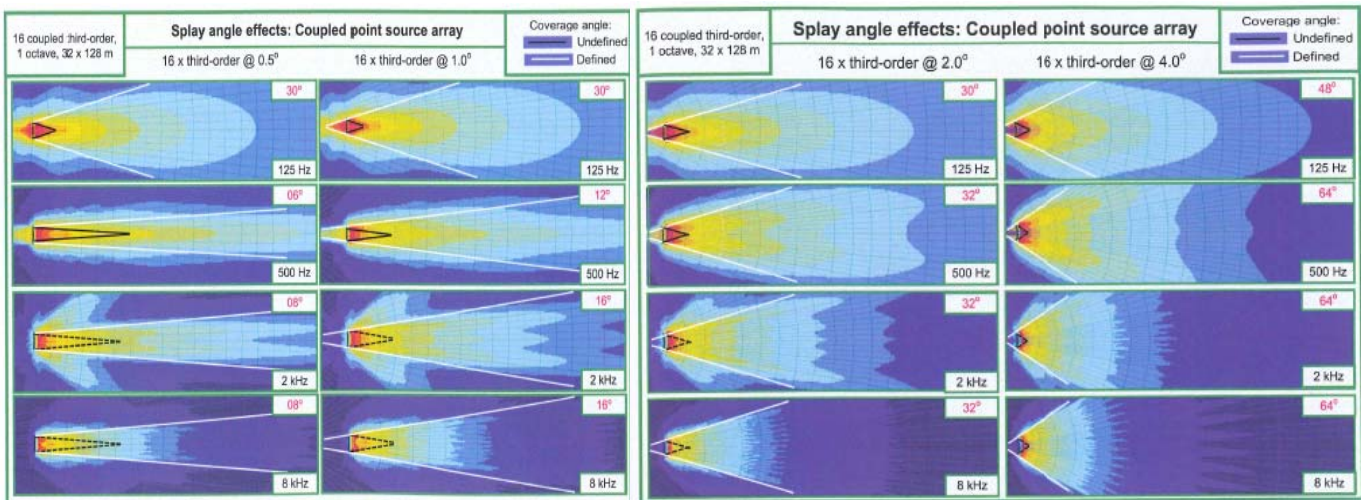
- spectral variance of coupled point source arrays

- beamwidth shapes



- **splay angle effects**

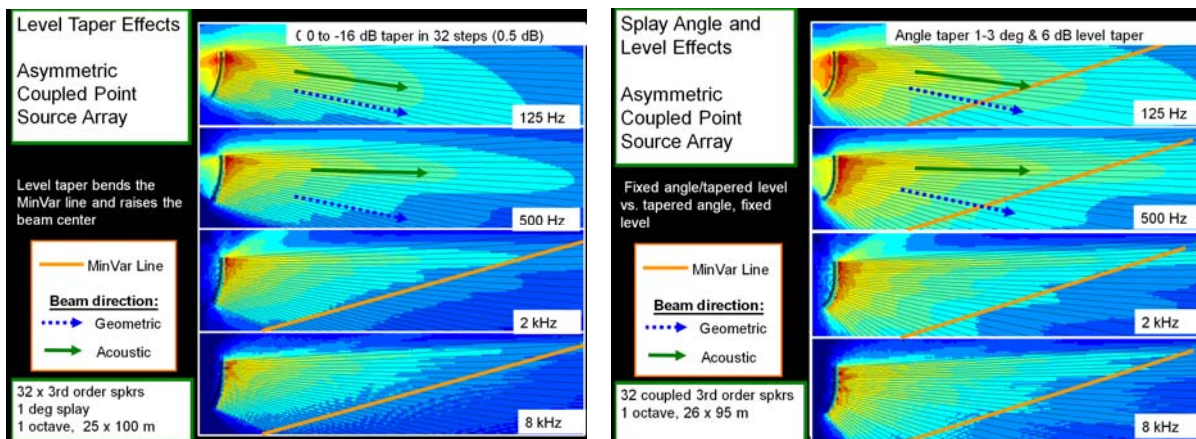
- even a small splay angle creates an opportunity for reduced spectral variance (that cannot be found in a coupled line source...*unless DSP techniques are used*)
- isolation (even in small measure) will counteract pattern narrowing



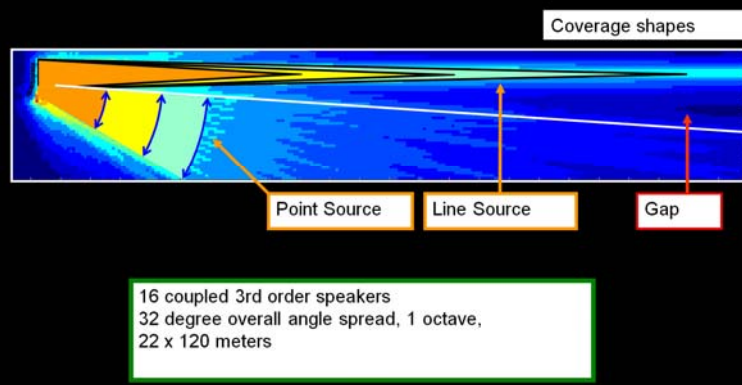
- **asymmetry (symmetry percentage) – ratio of angular coverage above and below center**

- level taper
- splay (angle) taper
- mixed loudspeaker orders
- lateral spacing/level offsets
- forward spacing/level offsets
- hybrid coupled line/point source arrays

Level tapering bends the minimum variance line and raises the beam center



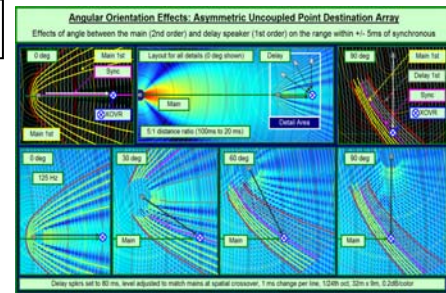
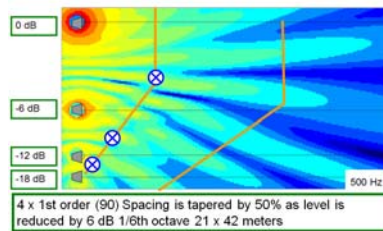
Hybrid Coupled Line/Point Source Array



Where would a “gap” in the coverage shape be useful?

- **uncoupled arrays**
 - line source
 - point source
 - point destination
- **conclusions**
 - **1st order speakers**
 - most suitable for single-element applications with a low proximity ratio
 - least suitable for angular overlap
 - least suitable for combination (power addition)
 - beamwidth must not widen as frequency rises (once plateau reached must remain constant)
 - should be arrayed at or near unity splay angle based on beamwidth plateau
 - **2nd order speakers**
 - most suitable for single-element applications with a medium proximity ratio
 - suitable for combination (power addition) on a limited basis
 - no beamwidth reversal (widening as frequency increases)
 - should be arrayed at or near unity splay angle based on beamwidth plateau
 - **3rd order speakers**
 - least suitable for single-element applications
 - most suitable for angular overlap
 - suitable for combination (power addition)
 - constant downward beamwidth slope (with no reversals) as frequency increases
 - should be arrayed at an angle greater than 0° (relative)
 - **power capability**
 - coupled arrays can increase concentrated power capability beyond a single element while maintaining minimum variance over long distances
 - the coupled point source has the highest ratio of increased power to variance over the widest frequency span and spatial area
 - the coupled line source can provide “unlimited” power but is incapable of minimum spectral variance over the space
 - asymmetric level tapering will decrease the overall power capability at the geometric center of the array but provide the opportunity for minimum variance over an asymmetric space
 - uncoupled arrays can increase distributed power capability beyond a single element while maintaining minimum variance, but only over a very limited distance
 - **minimum variance coverage shapes**
 - rectangle: individual speaker
 - arc: symmetric point source
 - right triangle: asymmetric coupled point source
 - **minimum variance principles**
 - single speakers
 - position the speakers with the lowest possible proximity ratio to the audience in at least one plane
 - use speakers that have minimum beamwidth ratio over frequency (1st or 2nd order)

Lateral Spacing and Level Effects



- match the properties of symmetry (symmetric orientation for symmetric shapes, asymmetric orientation for asymmetric shapes)
 - match speaker aspect ratio to audience coverage shape
 - if speaker coverage pattern overlap on to room surfaces is too strong, use an array instead
- minimum variance principles, continued...
 - symmetric point source coupled arrays
 - fill the arc angle required to fit the shape of the audience area (number of elements required will depend on speaker order)
 - low-order speakers must have minimal overlap
 - high-order speakers can be overlapped for power addition
 - beam spreading will shape (widen) the HF coverage
 - beam concentration will shape (narrow) the LF coverage
 - apply these principles to make shapes meet in the mid-range
 - uncoupled arrays
 - achieve isolation by angular offset and/or displacement
 - as angular offset falls, the usable depth range falls as well
 - uncoupled array depth is initiated by overlap
 - before overlap, response is as a single element
 - after overlap begins, array behavior and ripple variance begin
 - uncoupled array depth is limited by overlap – multiple overlap provides the ending limit for depth
 - uncoupled arrays can be scaled by relative level to appropriate depth

