

ECE 661: Homework 6
Mridul Gupta
Email: gupta431@purdue.edu

Theory Question

1. Otsu thresholding works really well for images with bimodal histograms. It is very fast method because it just finds one threshold for an entire image but that also makes it very noisy. In iterative Otsu, we will get better result with each iteration only if the foreground image from previous iteration also has bimodal histogram.
2. This method requires good markers. If the markers are not good, the method doesn't work very well. Overall, its a less noisy process than otsu thresholding. Due to oversegmentation, extracted objects might not be good but variations of the algorithm have been proposed to reduce oversegmentation.

Section 3

1. Otsu's Algorithm

It divides the image into 2 classes , foreground and background. w_0 , w_1 are the probabilities of the two classes. Histogram frequencies are normalized and are represented by p_i for gray value i . μ_0 is the mean of class 0 and μ_1 is the mean of class 1. Between-class variance is given by $\sigma_b^2 = w_0w_1(\mu_0 - \mu_1)^2$. We have to maximize this between-class variance to get the threshold value. We consider each gray pixel value i as a threshold, n_i represents the number of pixels with gray value i and N is the total number of pixels.

$$w_0 = \sum_{k=0}^{i-1} p_i = \sum_{k=0}^{i-1} \frac{n_i}{N}$$
$$w_1 = 1 - w_0$$
$$\mu_0 = \sum_{k=0}^{i-1} \frac{kp_i}{w_0} = \frac{\sum_{k=0}^{i-1} kn_i}{\sum_{k=0}^{i-1} n_i}$$
$$\mu_1 = \frac{\mu_T - w_0\mu_0}{w_1}$$

where μ_T is the mean over the entire image. Over all possible thresholds, we keep track of the threshold which maximizes the between-class variance.

2. Pixel-value based segmentation

We run Otsu's method on each channel separately. We have the option to run Otsu' method multiple times while keeping track if the foreground class is above or below the computed threshold.

- (a) For cat image, only the Red channel of the image was used for thresholding and the foreground was the class with higher pixel values and only 1 iteration was run.
- (b) For pigeon image, all channels of the image were used for thresholding and the foreground was the class with higher pixel values and only 1 iteration was run for each channel.
- (c) For fox image, only blue channel of the image was used for thresholding and the foreground was the class with higher pixel values and only 2 iterations were run for each channel.

3. Texture-based segmentation

There are multiple ways of calculating texture value for a pixel but we use the sliding window approach. We use three window sizes for each image. For each window size, we calculate the variance of neighbors of a pixel in that window. We treat the variance values at each pixel location as a feature value for that pixel and run Otsu thresholding on this new variance image.

- (a) For cat image, only the Red channel of the image was used for thresholding and the foreground was the class with lower variance values and 6 iterations were run. window sizes were 3, 5 and 7 and the final target mask was inverted.
- (b) For pigeon image, all channels (RGB) of the image were used for thresholding and the foreground was the class with lower variance values and 6, 3 and 3 iterations were run respectively. window sizes were 7, 9 and 11 and the final target mask was not inverted.
- (c) For fox image, all channels (RGB) of the image were used for thresholding and the foreground was the class with lower variance values and 1, 1 and 3 iterations were run respectively. window sizes were 3, 5 and 7 and the final target mask was inverted.

4. Contour Extraction

Contours are basically formed by the pixels that form the edges. Dilation and erosion were performed to connect missing edges and remove small dots from the image respectively. A pixel forms an edge if out of its 9 neighbors, at least 1 pixel belongs to the background i.e. it has the value 0.

- (a) For RGB segmentation based foreground mask:
 - i. Cat image - eroded then dilated once with kernel of size 3×3 .
 - ii. Pigeon image - eroded then dilated once with kernel of size 3×3 .
 - iii. Fox image - dilated then eroded 5 and 6 times respectively with kernel of size 3×3 .
- (b) In cat image, foreground mask was eroded - 3 iterations, with kernel size of 3×3 . It was then dilated - 6 iterations with the same kernel size.
- (c) Other images were neither eroded nor dilated.

Results



Figure 1: RGB - Cat channel 1 foreground and the final foreground mask



Figure 2: RGB - Cat foreground

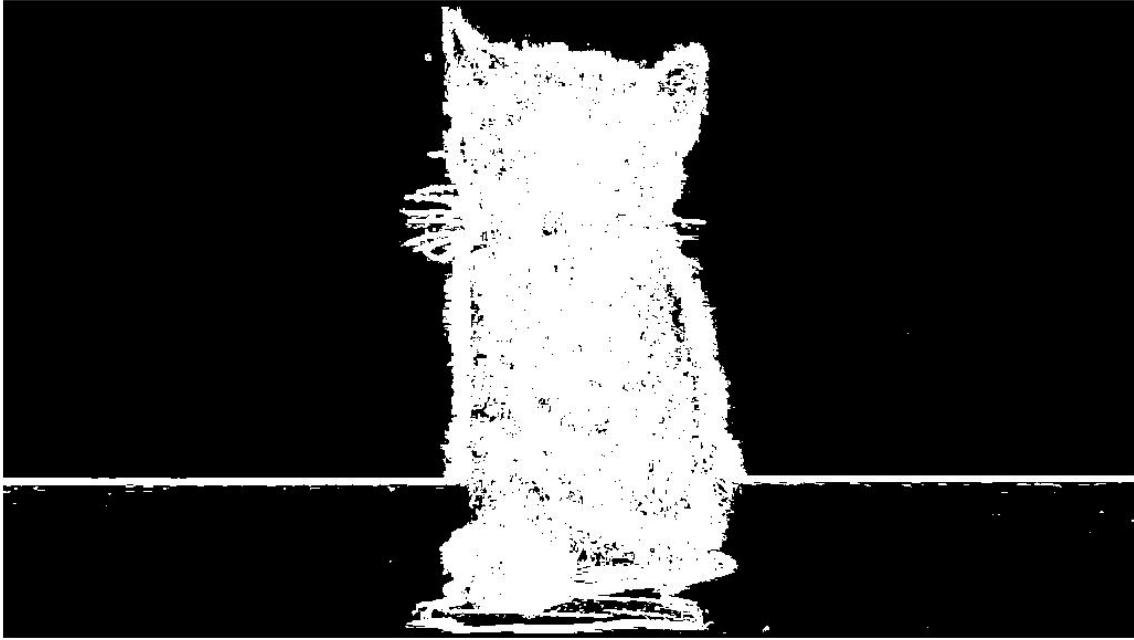


Figure 3: Texture - Cat foreground mask



Figure 4: Texture - Cat foreground

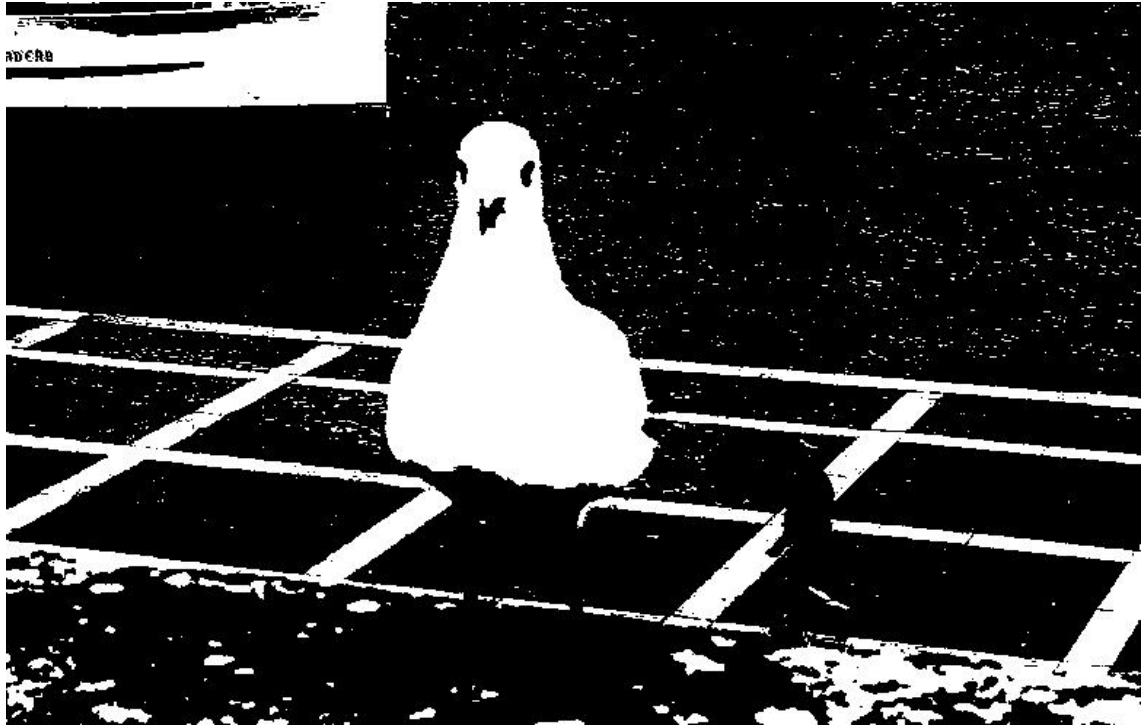


Figure 5: RGB - Pigeon channel 1 foreground mask

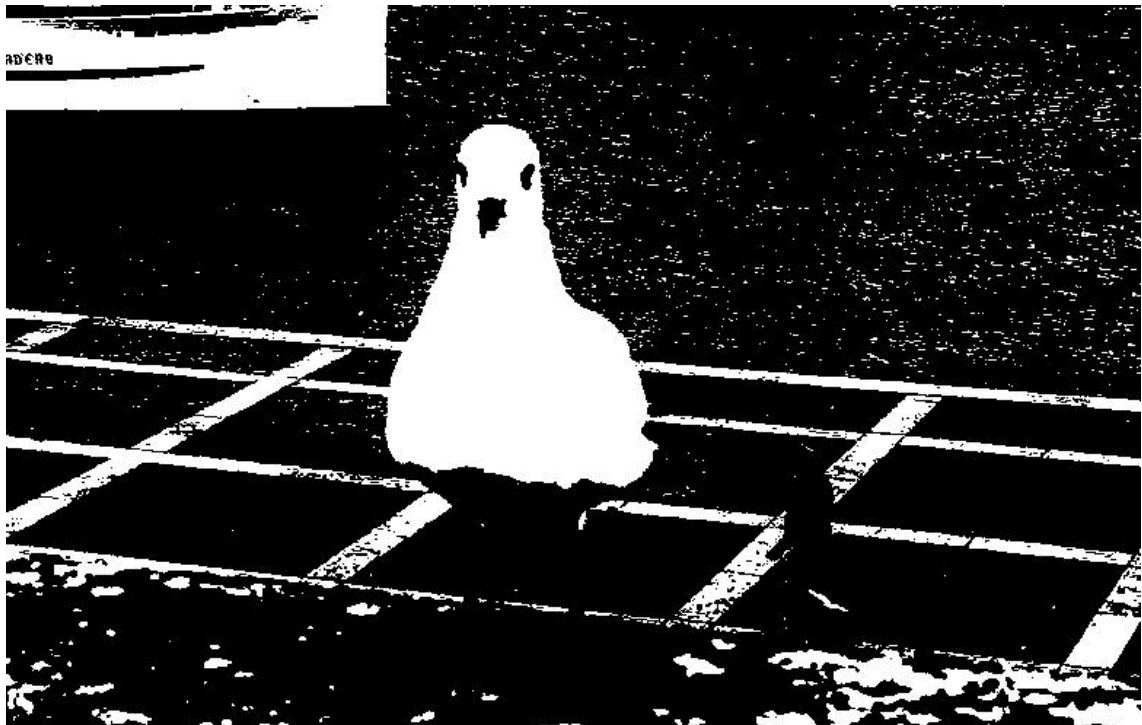


Figure 6: RGB - Pigeon channel 2 foreground mask

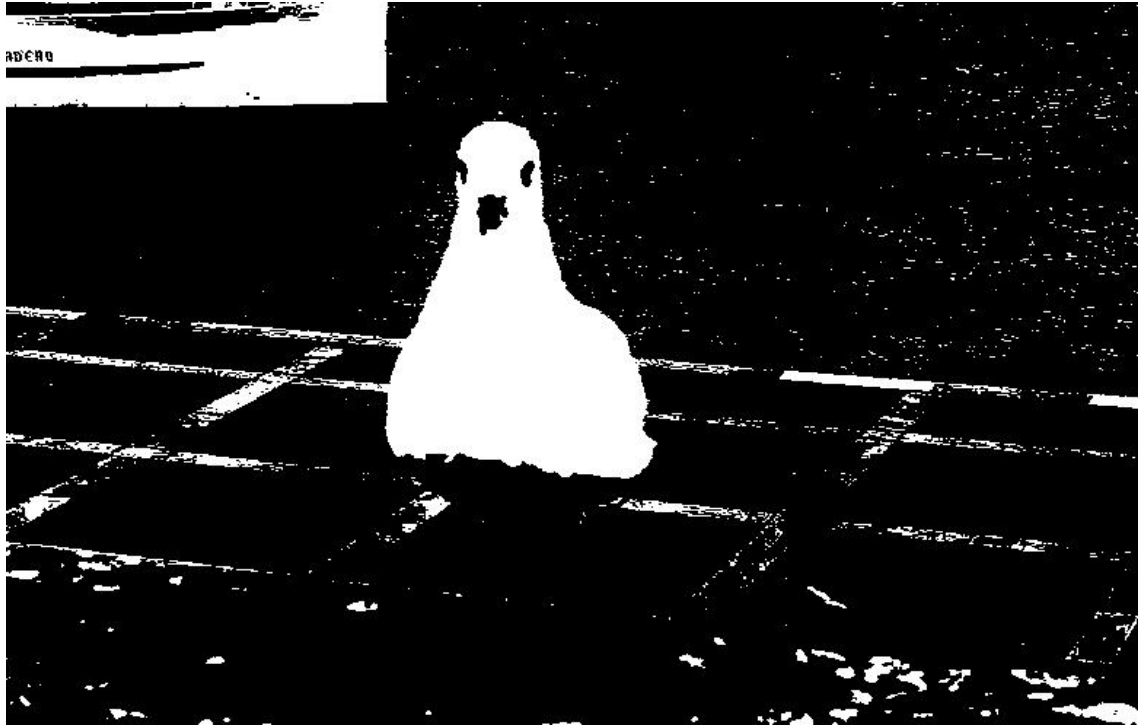


Figure 7: RGB - Pigeon channel 3 foreground mask



Figure 8: RGB - Pigeon final foreground mask



Figure 9: RGB - Pigeon final foreground



Figure 10: Texture - Pigeon foreground mask



Figure 11: Texture - Pigeon foreground



Figure 12: RGB - Fox channel 3 foreground and the final foreground mask



Figure 13: RGB - Fox foreground

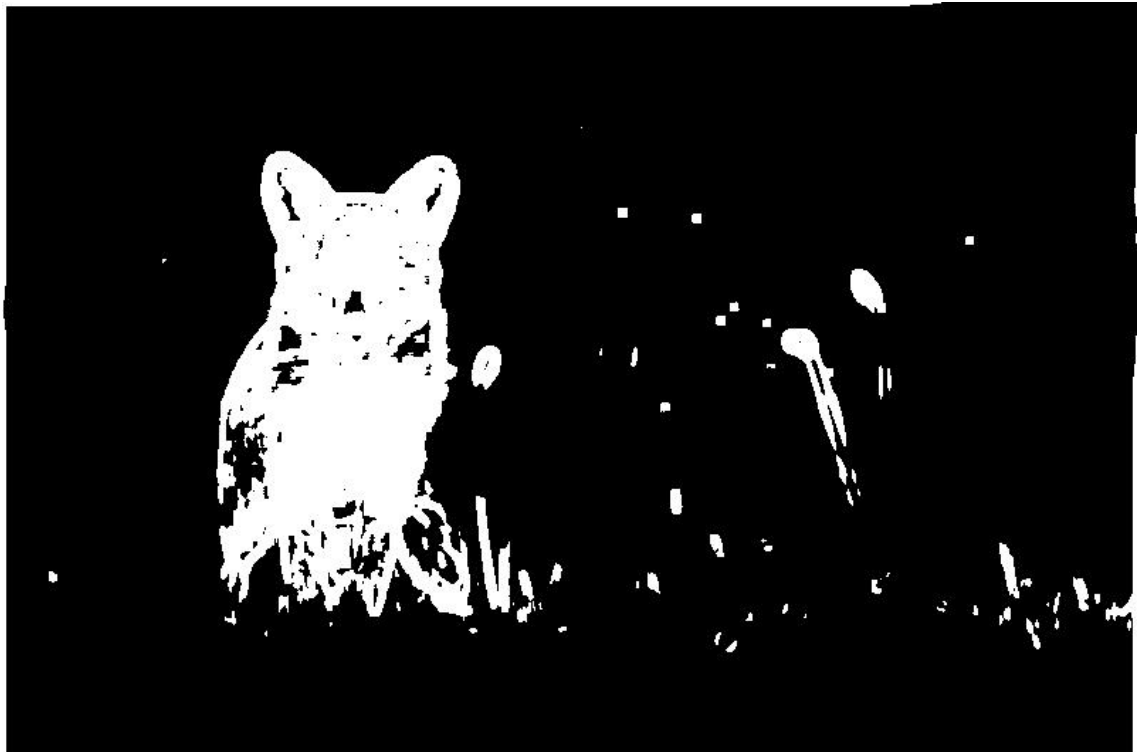


Figure 14: Texture - Fox foreground mask



Figure 15: Texture - Fox foreground

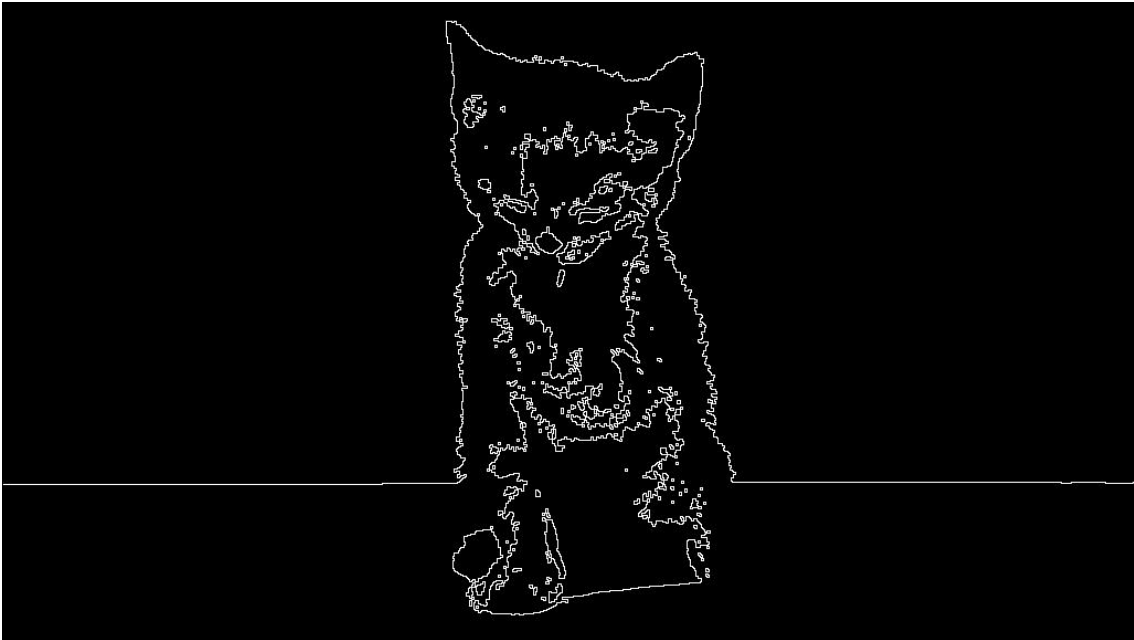


Figure 16: RGB - Cat Contour



Figure 17: Texture - Cat Contour



Figure 18: RGB - Pigeon Contour

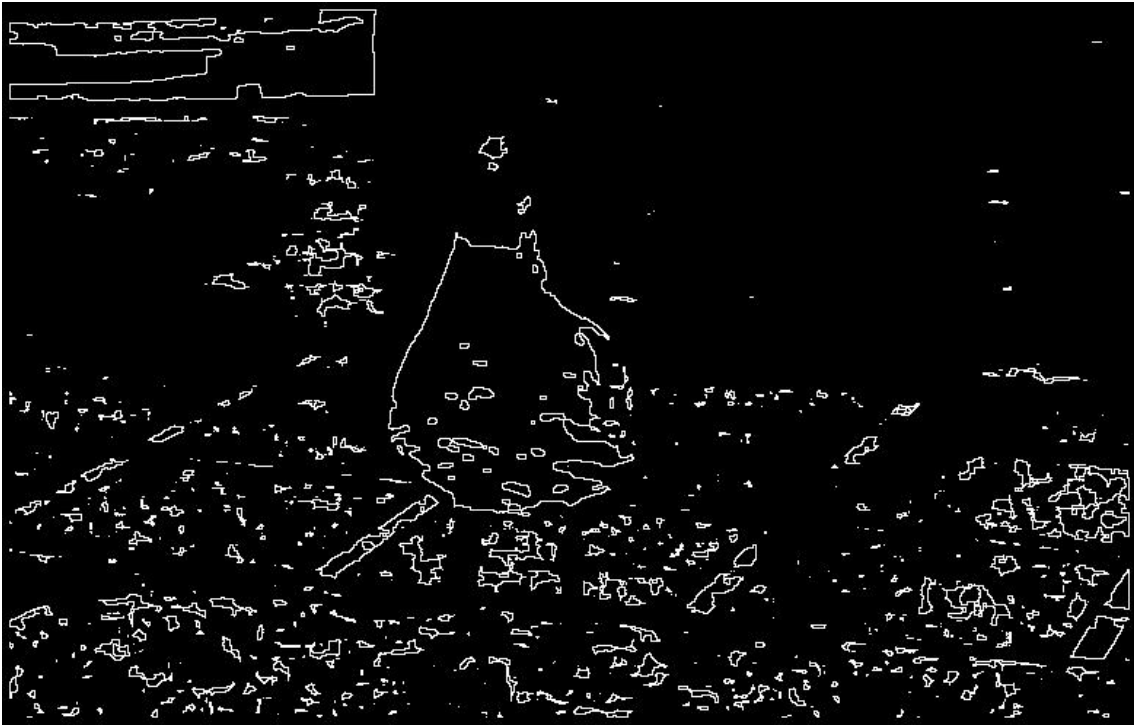


Figure 19: Texture - Pigeon Contour



Figure 20: RGB - Fox Contour

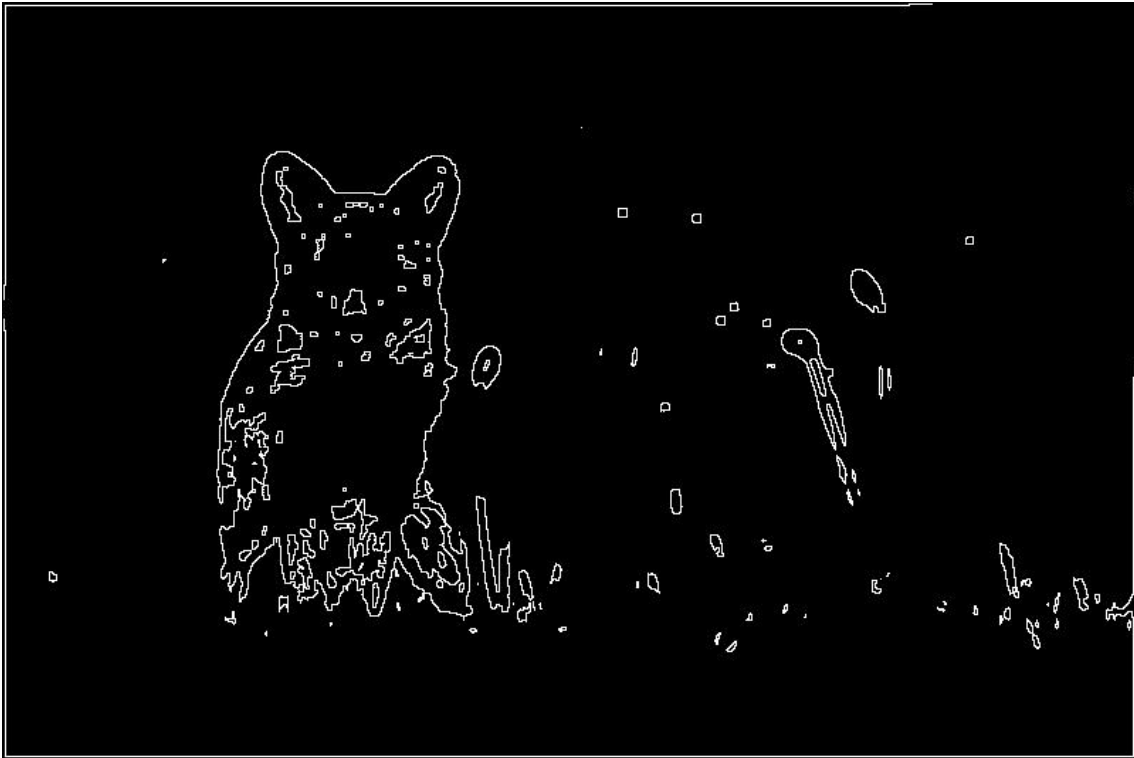


Figure 21: Texture - Fox Contour

Observation

1. For the cat image, table has a color very close to the cat, so RGB-based segmentation does not work very well and texture based segmentation does really well.
2. For pigeon image, RGB based method is not able to separate pigeon from the boat because they have the same color but does much better than texture based method. Texture based method is able to keep pigeon in the foreground but there are quite a lot of false positives especially the ground tiles which have slightly different color than the pigeon.
3. For fox image, both methods did quite well, but RGB based method missed some portion of the legs of the fox whereas texture based method did not. With other post-processing techniques, it might have been possible to make the foreground mask better.
4. I think both the methods perform really well overall but texture based method probably has an edge over RGB based method since it can deal with similar colors comparatively easily.

```
1  ### ECE 661 - HW 6
2  ### Otsu thresholding
3
4  import numpy as np
5  import cv2
6  from matplotlib import pyplot as plt
7  import copy
8
9
```

```

10
11
12 def otsu_threshold(img, iterations = 1, invert=0):
13     ### img is grayscale image, for RGB, send one channel at a time
14     ### returns mask for the image
15     output_mask = np.ones(img.shape)
16     if(len(img.shape)==3):
17         print("Error- " + str(img.shape[2])+" channel image is the
18             input to otsu threshold method")
19         return -1
20
21     for i in range(iterations):
22         cur_for = img[output_mask!=0]
23         hist, bins = np.histogram(cur_for, bins= np.unique(cur_for))
24
25         ### normalize histogram
26
27         hist = hist/float(len(cur_for))
28         #     print(np.sum(hist))
29         #     print(bins)
30
31         ##define variables for calculation of threshold
32         w0 =0
33         mu0= 0
34         total_weighted_avg = np.mean(cur_for)
35         otsu_t=-1
36         max_siglab2 = 0
37         sum1=0
38
39         #     ##siglab2 + siglab2 = constant so we dont need to
40         calculate siglab2
41         count=-1
42         for th in bins[:-2]:
43             count+=1
44             w0+=hist[count]
45             w1 = 1-w0
46             sum1 += th*hist[count]
47             mu0=sum1/w0
48             if w1==0:
49                 break
50             mu1 = (total_weighted_avg-sum1)/w1
51             siglab2 = w0*w1*np.square(mu0-mu1)
52             if siglab2>max_siglab2:
53                 max_siglab2 = siglab2
54                 otsu_t = th
55
56         print(otsu_t)

```

```

56         if invert==0:
57             output_mask = img>otsu_t
58         else:
59             output_mask = img<otsu_t
60     return (output_mask!=0)
61
62
63 # In[149]:
64
65
66 def get_variance(img,k):
67     ##avoids nested loops for variance calculation
68     k = int(k/2)
69     img_new = np.zeros((img.shape[0]+2*k,img.shape[1]+2*k))
70     img_new[k:img.shape[0]+k,k:img.shape[1]+k] = img
71     neighbours = []
72     for i in range(k,img.shape[0]+k):
73         for j in range(k,img.shape[1]+k):
74             neighbours.append(img_new[i-k:i+k+1,j-k:j+k+1].
75                             flatten())
76     neighbours = np.array(neighbours)
77     print(neighbours.shape)
78     variances = np.int32(np.var(np.array(neighbours,dtype = np.
79                                 float32),axis=1))
80
81     variances = variances.reshape(img.shape[0],img.shape[1])
82
83     print(variances.shape)
84     return variances
85
86 # In[128]:
87
88 def texture_otsu(img,N=[3,5,7],iterations=[1,1,1],invert = [0,0,0]):
89     ### function for texture based segemenation
90     gray = cv2.cvtColor(img, cv2.COLOR_RGB2GRAY)
91
92     ###place a window of N*N at each pixel location
93     masks = np.zeros(im.shape)
94     for i in range(len(N)):
95         ##this is the new channel values
96         var = get_variance(gray,N[i])
97
98         temp = otsu_threshold(var.flatten(),iterations[i], invert[i
99             ])
100         masks[:, :, i] = temp.reshape((img.shape[0],img.shape[1]))
101     ##product of the three masks

```

```

101     final_mask = np.multiply(np.multiply(masks[:, :, 0], masks[:, :, 1]),
102                               masks[:, :, 2])
103     final_mask = final_mask!=0
104     return final_mask
105
106
107 # In[75]:
108
109
110 def get_contour(mask):
111     ## checks if any neighbour is not a part of the foreground to
112     compute contours
113     contour = np.zeros(mask.shape)
114     for i in range(1,mask.shape[0]-1):
115         for j in range(1,mask.shape[1]-1):
116             if mask[i][j]==0:
117                 continue
118             if np.sum(mask[i-1:i+2,j-1:j+2])<9:
119                 contour[i][j]=1
120     return contour
121
122 # In[361]:
123
124 ###Parameters for the three images
125
126 ##cat image
127 # iterations=[1,0,0]
128 # invert = [0,0,0]
129
130 ##pigeon image
131 iterations=[1,1,1]
132 invert = [0,0,0]
133
134 ##fox image
135 # iterations=[0,0,2]
136 # invert = [0,0,0]
137
138 name= 'pigeon'
139 im = np.uint8(cv2.imread(name+'.jpg')[...,::-1])
140
141 plt.imshow(im)
142 masks = np.zeros(im.shape)
143 for i in range(3):
144
145     im1 = copy.deepcopy(im[:, :, i])
146

```



```

147     temp = otsu_threshold(im1.flatten(), iterations[i], invert[i])
148     masks[:, :, i] = temp.reshape((im.shape[0], im.shape[1]))
149
150
151
152
153 # In[362]:
154
155
156 for i in range(1,4):
157     # plt.imshow(masks[:, :, 2], cmap='gray')
158     plt.imsave(name+'foreground_mask_channel'+str(i)+'.jpg', masks
159              [:, :, i-1], cmap='gray')
160
161 foreground = np.multiply(np.multiply(masks[:, :, 0], masks[:, :, 1]),
162                          masks[:, :, 2])
163 plt.imshow(foreground, cmap='gray')
164 plt.imsave(name+'foreground_mask.jpg', foreground, cmap='gray')
165 ##save masked image
166 fore_img = np.zeros(im.shape)
167 for i in range(3):
168     fore_img[:, :, i] = np.multiply(im[:, :, i], foreground)
169 plt.imsave(name+'foreground.jpg', np.uint8(fore_img))
170
171
172 # In[365]:
173
174
175 ##so we have a foreground mask at this point
176 ## we will erode and dilate the mask to get rid of single pixel
177     peaks and make image smooth
178
179 ##cat erode - dilate 1
180 ##pigeon erode - dilate 1
181 ## fox dil5 -erode6
182 kernel = np.ones((3,3))
183 ero_fore = cv2.erode(np.float32(foreground), kernel, iterations =1)
184 dil_fore = cv2.dilate(ero_fore, kernel, iterations =1)
185
186 plt.imshow(ero_fore, cmap='gray')
187
188 # In[366]:
189
190
191 ##now we will extract the contours

```

```

192 cnt = get_contour(ero_fore)
193 plt.imshow(cnt, cmap='gray')
194 plt.imshow(name+'contour_RGB.jpg', cnt, cmap='gray')
195
196
197 # In[367]:
198
199
200 ##now texture based otsu
201
202 ###Parameters for the three images
203
204 ##cat image
205 # iterations=[6,0,0]
206 # invert = [1,1,1]
207 # N=[3,5,7]
208 # invert_mask=1
209
210 ##pigeon image
211 iterations=[6,3,3]
212 invert = [1,1,1]
213 N=[7,9,11]
214 invert_mask=0
215
216 ##fox image
217 # iterations=[1,1,3]
218 # invert = [1,1,1]
219 # N=[3,5,7]
220 # invert_mask=1
221
222 im1 = copy.deepcopy(im)
223
224 temp = texture_otsu(im1, N, iterations, invert)
225 mask = temp.reshape((im.shape[0], im.shape[1]))
226 if invert_mask==1:
227     mask=(mask==0)
228 plt.imshow(mask, cmap='gray')
229
230
231 # In[368]:
232
233
234 plt.imshow(name+'texture_foreground_mask.jpg', mask, cmap='gray')
235 fore_img = np.zeros(im.shape)
236 for i in range(3):
237     fore_img[:, :, i] = np.multiply(im[:, :, i], mask)
238 plt.imshow(name+'texture_foreground.jpg', np.uint8(fore_img))
239

```

```

240
241 # In[369]:
242
243
244 ##so we have a foreground mask at this point
245 ## we will erode and dilate the mask to get rid of single pixel
    peaks and make image smooth
246 ##cat dilation = 5, erosion = 1, kernel = 3*3
247 ##pegion nothing
248 ##fox nothing
249
250 kernel1 = np.ones((5,5))
251 kernel2 = np.ones((3,3))
252
253 dil_fore = cv2.dilate(np.float32(mask),kernel2,iterations =5)
254 ero_fore = cv2.erode(np.float32(dil_fore),kernel1,iterations = 1)
255
256 plt.imshow(dil_fore,cmap='gray')
257
258
259 # In[370]:
260
261
262 ##now we will extract the contours
263 cnt = get_contour(dil_fore)
264 plt.imshow(cnt,cmap='gray')
265 plt.imshow(name+'contour_texture.jpg',cnt,cmap='gray')

```