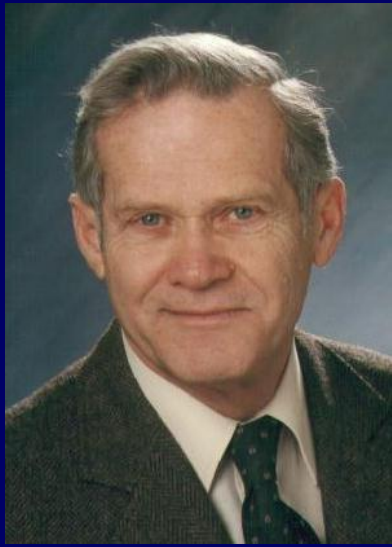


*20<sup>th</sup> Gerald A. Leonards Lecture, Purdue University, April 12, 2024*

# **Seismic Design Considerations for Tailings Dams**

**Jonathan D. Bray, PhD, PE, NAE**

*Faculty Chair in Earthquake Engineering Excellence  
University of California, Berkeley  
jonbray@berkeley.edu*



## Prof. Leonards Focused on Details

- Depositional environment should be considered
- Thin layers can govern site performance
- Importance of continuous sampling

***“Just one more FE analysis,”*** which was #17. I performed 44 analyses before project was over to explore fully details that might matter

***“Students do not mind hard work if they feel they are learning something.”***  
I learned much from Prof. Leonards.

# **SEISMIC DESIGN CONSIDERATIONS FOR TAILINGS DAMS**

## **OUTLINE**

- 1. Tailings Storage Facilities**
- 2. Observed Performance of Tailings Dams**
- 3. Flow Failure Potential**
- 4. Seismic Slope Displacement**
- 5. Summary**

# Tailings Storage Facility (TSF)



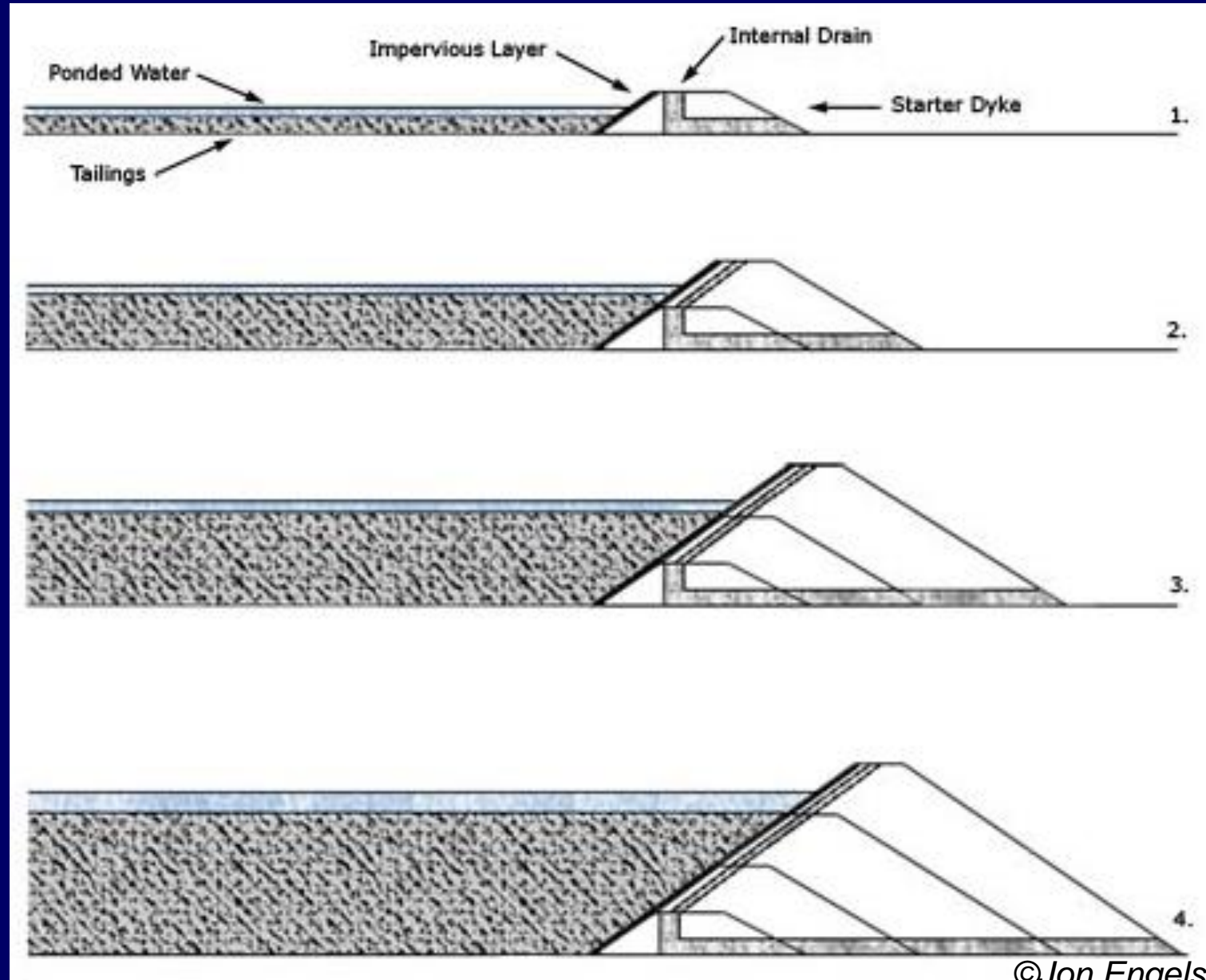
*Akyem Mine TSF Cell 1 (background)  
and TSF Cell 2 (foreground) in Ghana*

*Photo courtesy of Kim Morrison, Newmont Corp.*



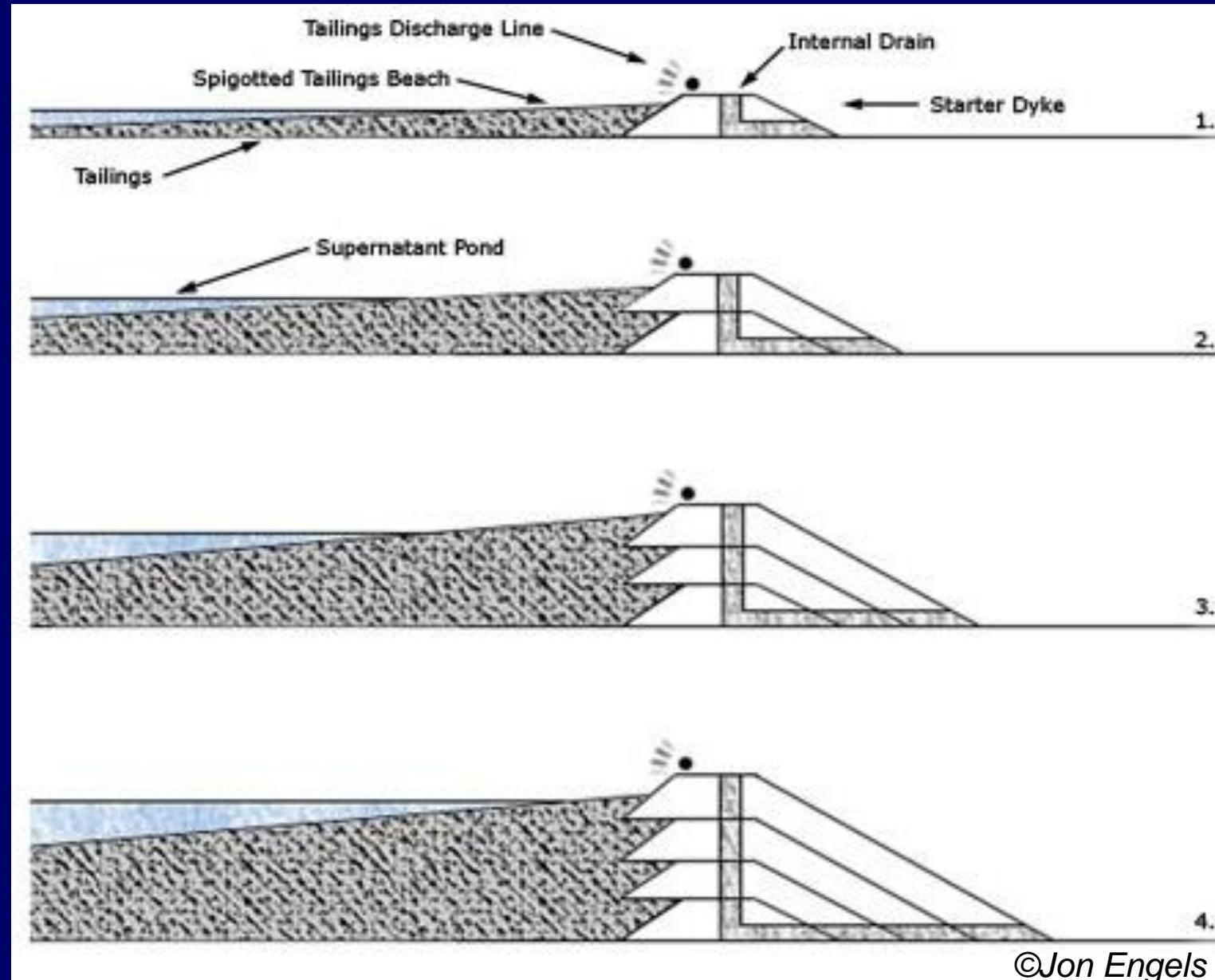
# Types of TSF Design

- *Downstream*
- *Centerline*
- *Upstream*



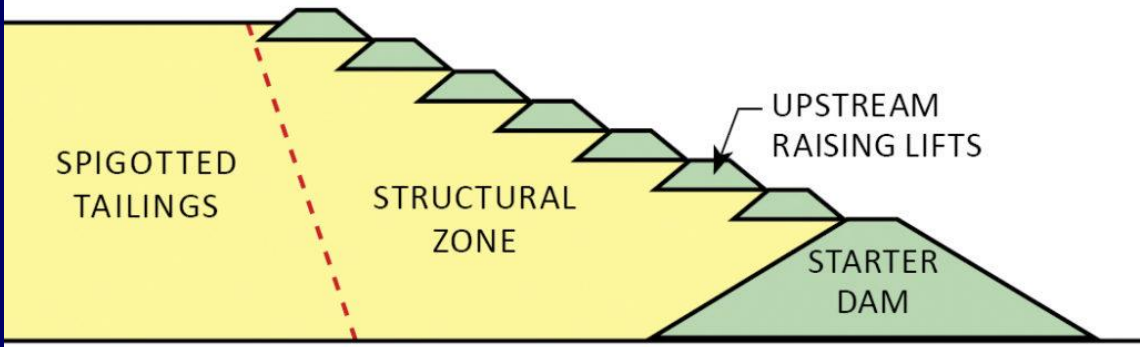
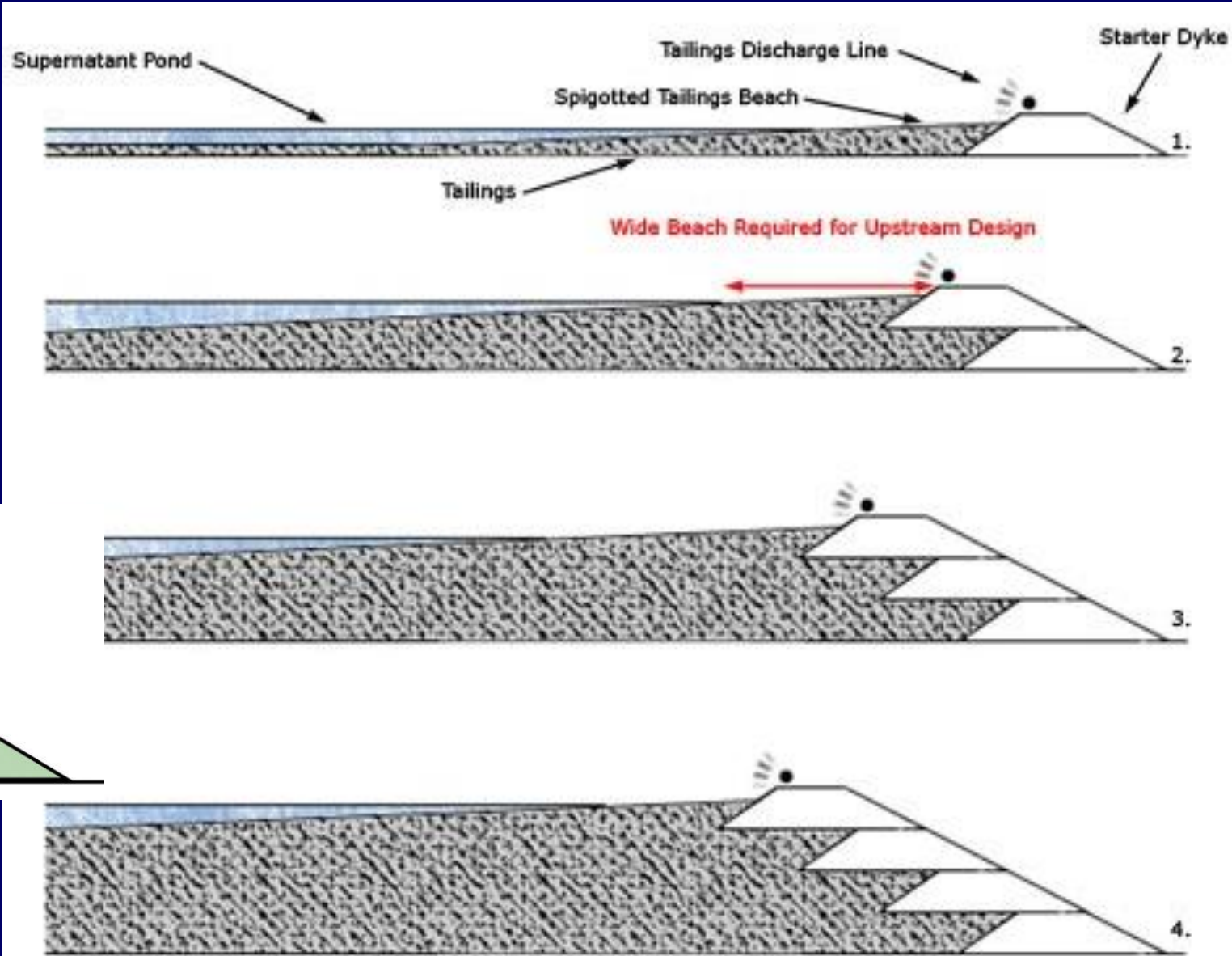
# Types of TSF Design

- *Downstream*
- *Centerline*
- *Upstream*



# Types of TSF Design

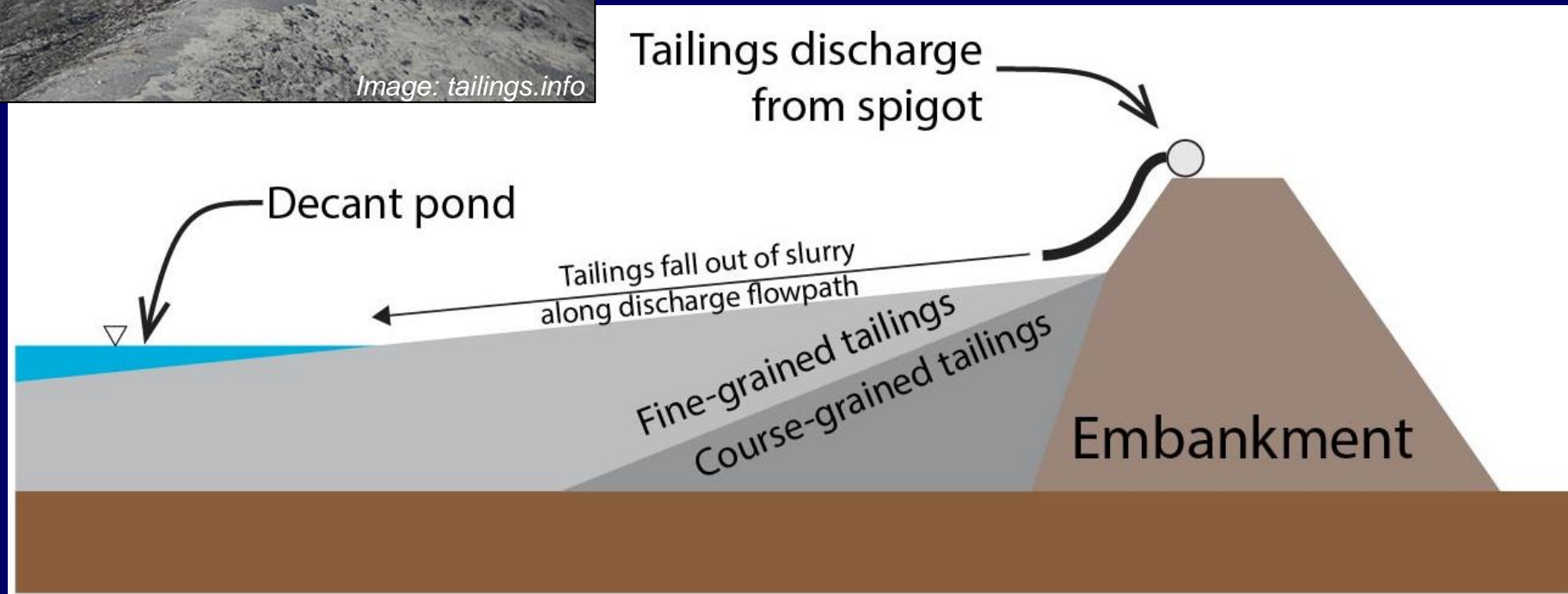
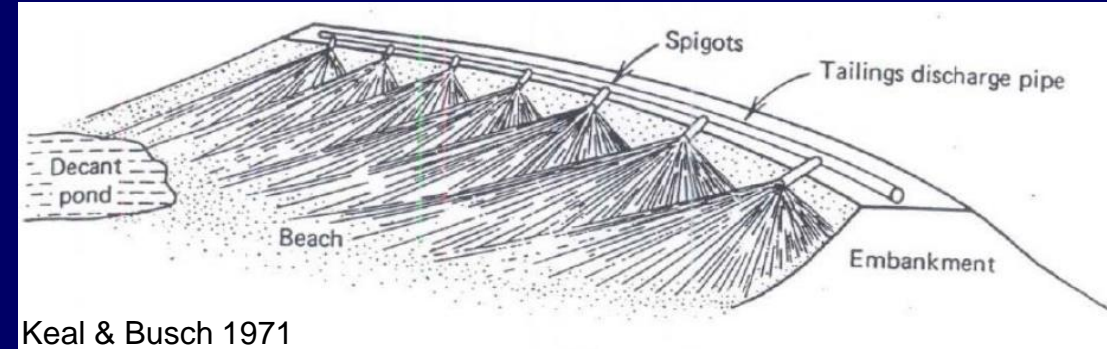
- *Downstream*
- *Centerline*
- *Upstream*



[Best Practices for Tailings Dam Design - KCB \(kohn.com\)](http://kohn.com)



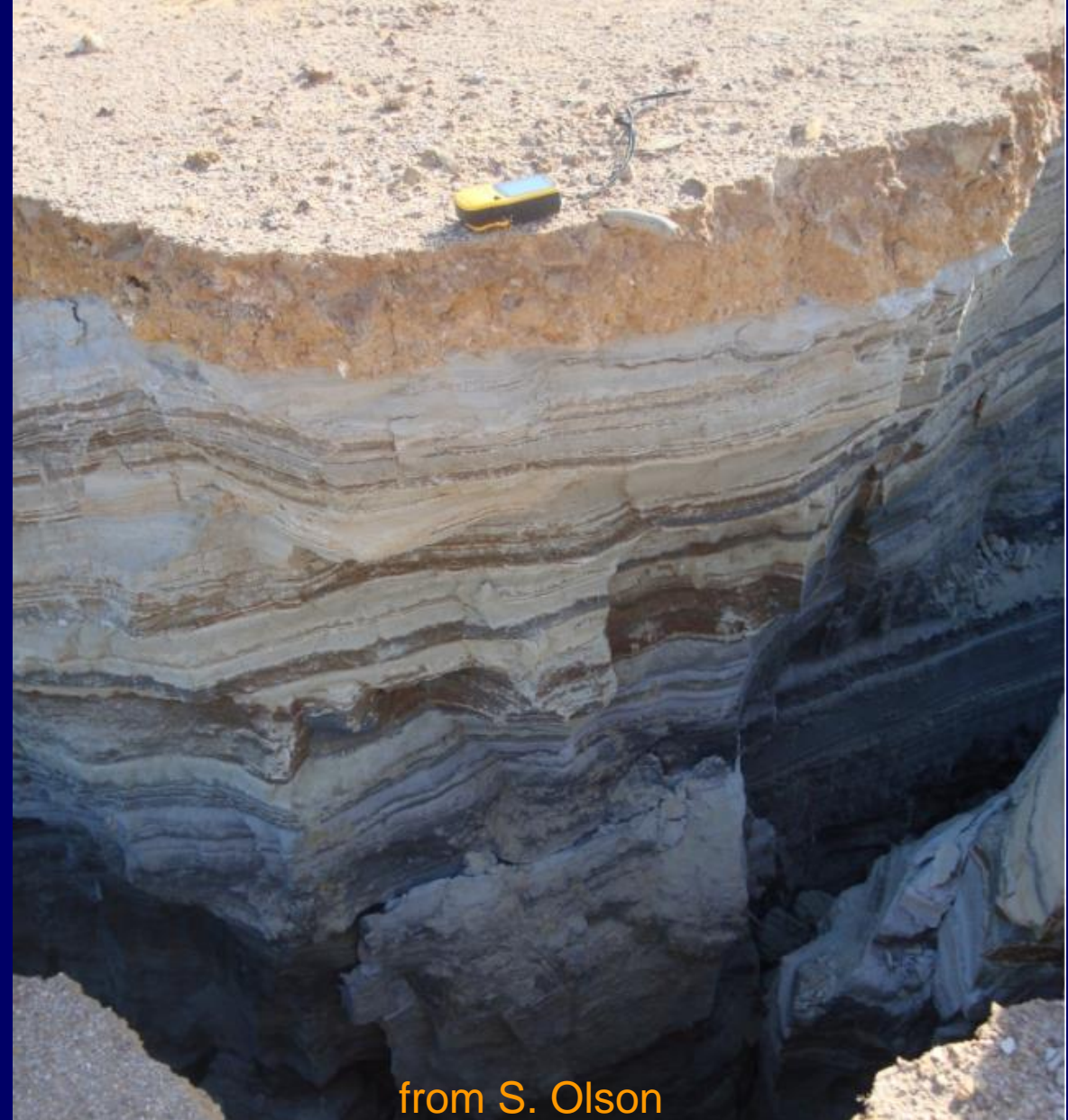
# Spigot Discharge & Hydraulic Deposition





# Hydraulic Filling Creates Layered System

- Composite response
- Anisotropic properties
- Drainage
- Instrumentation
- Calibration

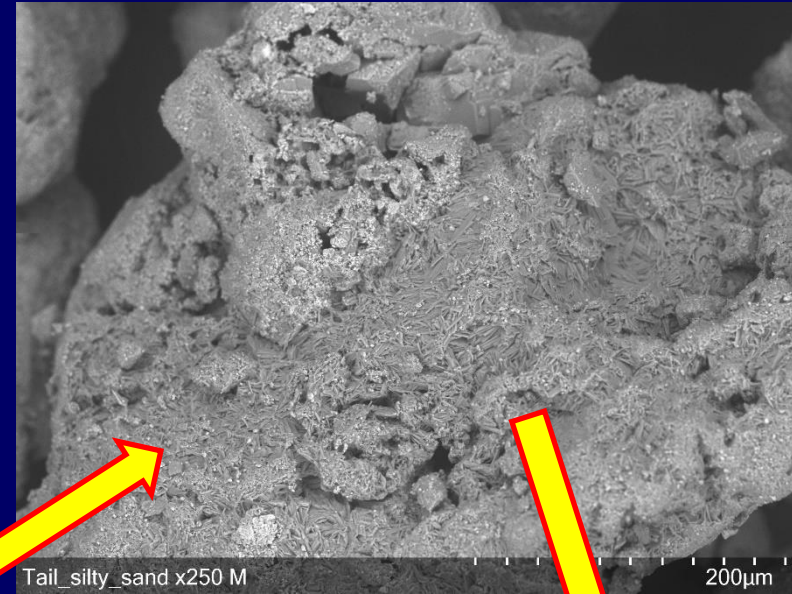
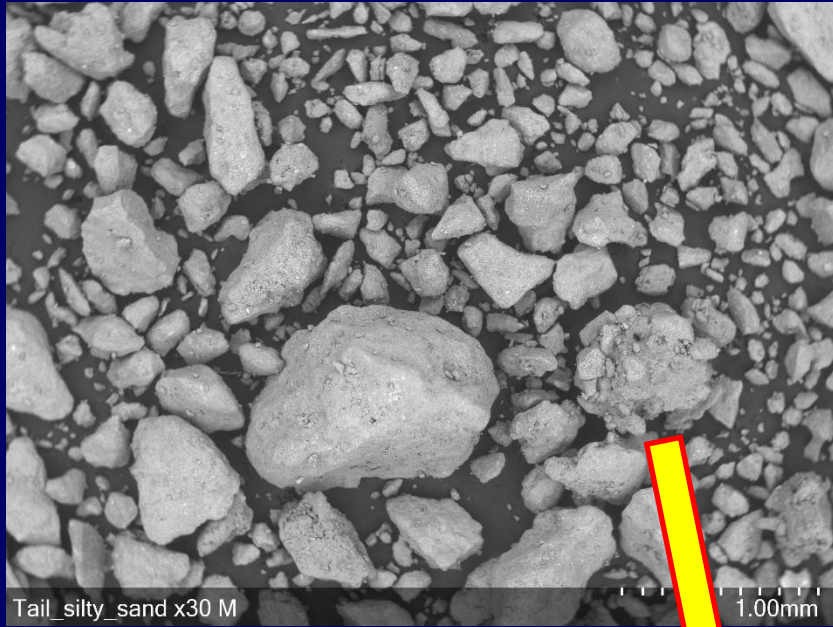


from S. Olson

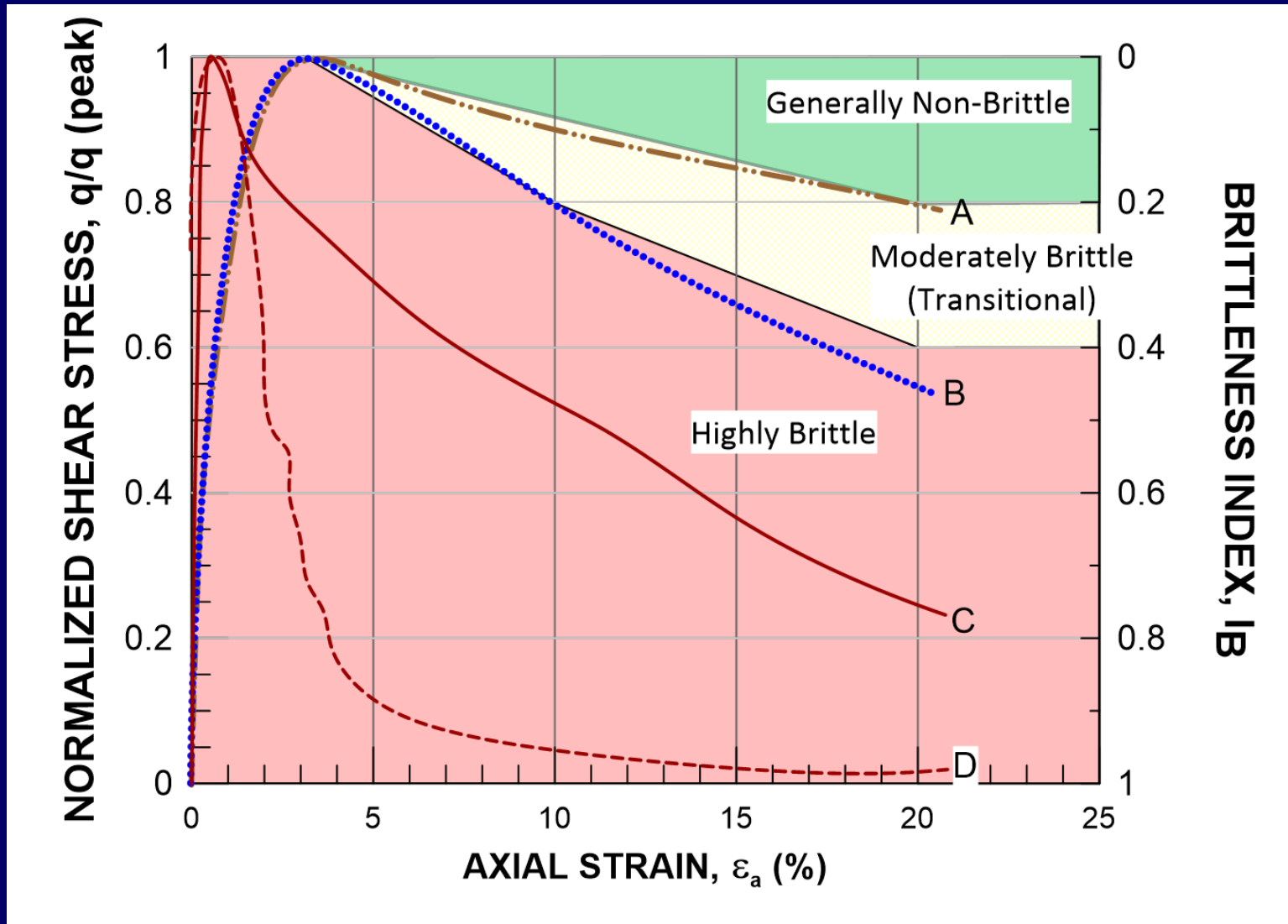


# SEM Allows One to See Tailings Particles

(tailings material in Peru, Olaya & Bray, in progress)



# Focus on Materials with Contractive Response with Brittle Strain-Softening



**Brittleness Index,  $I_B$**   
 (Bishop 1967, 1973)

$$I_B = 1 - S_r / S_{u\_peak} = 1 - 1 / S_t$$

$$S_t = S_{u\_peak} / S_r$$

If  $S_r = 0.2 S_{u\_peak}$  (i.e.,  $S_t = 5$ )  
 Then  $I_B = 0.8$

# **SEISMIC DESIGN CONSIDERATIONS FOR TAILINGS DAMS**

## **2. Observed Performance of Tailings Dams**



# Feijao Tailings Dam 1 ( $H = 80\text{ m}$ )

25/01/2019 12:28:22 Sex

(Robertson et al. 2019)



B1 - CAM1 - Barragem

**270 deaths**



# Recent Failures

Jagersfontein Tailings Dam Failure  
South Africa, 11 September 2022



(after Torres-Cruz, 2022)

**17 Fatalities**



Copler Heap Leach Failure  
Turkey, 13 February 2024



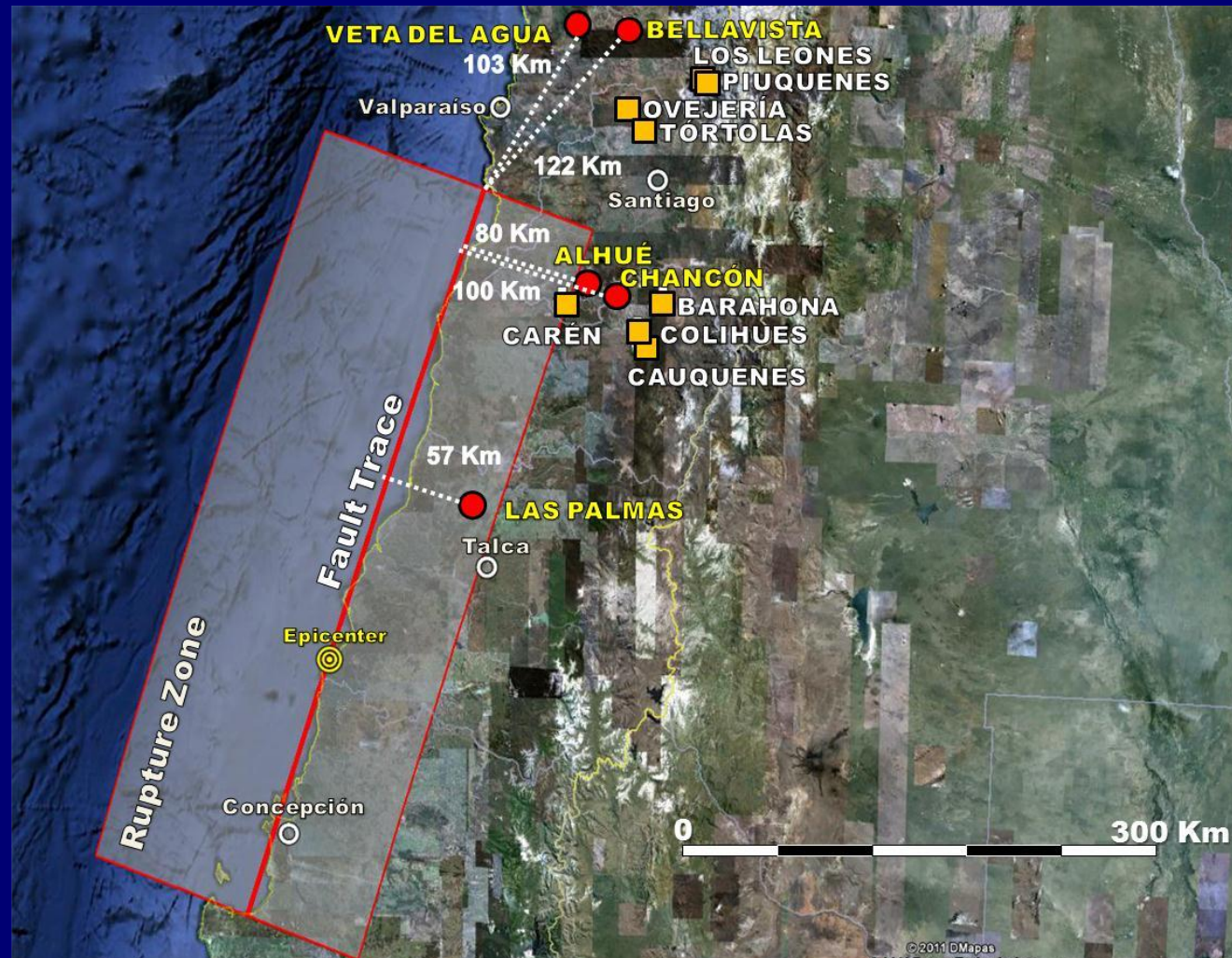
(from P. Repetto)

**9 Fatalities**





# Observed Seismic Performance of Tailings Dams 2010 $M_w$ 8.8 Maule, Chile EQ

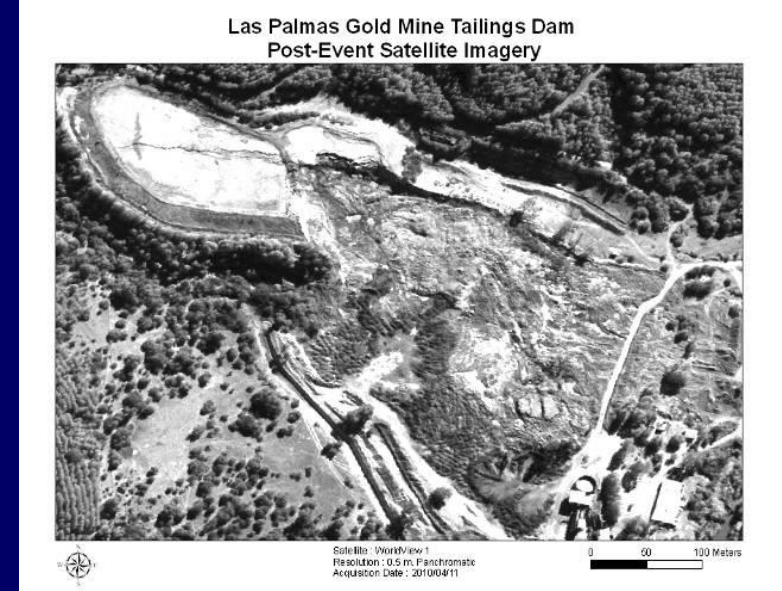
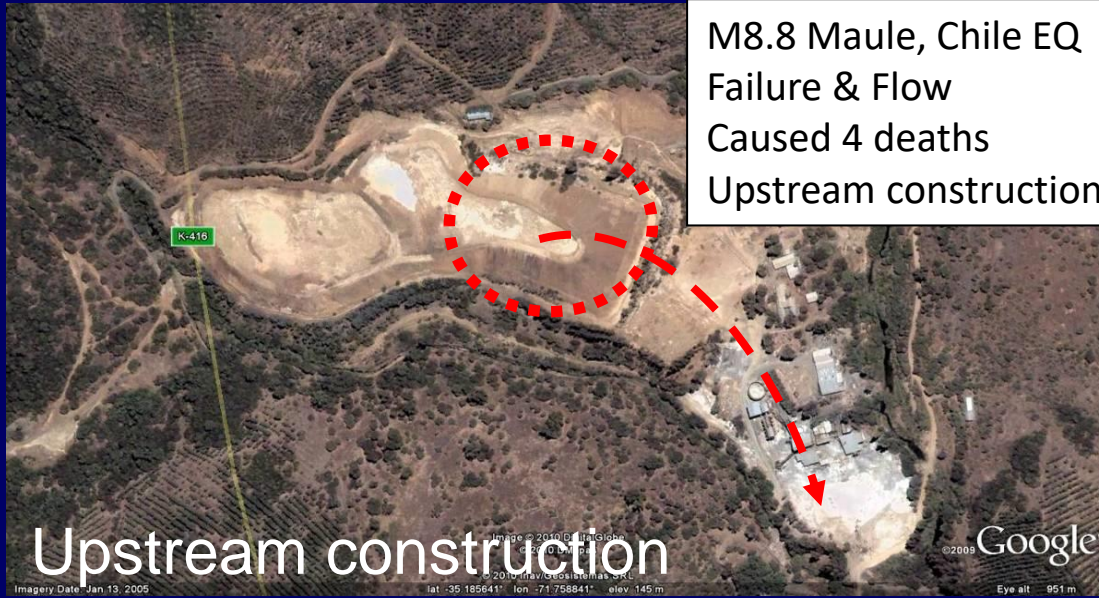


- Large tailings dams that performed well
- Tailings dams that performed poorly





# Las Palmas Gold Mine Tailings Dam EQ-Induced Failure



Bray & Frost 2010



View across scarp



View from scarp looking downstream



Ejecta near toe of flow debris



# Seismic Performance of Tailings Dams

(Upstream Construction Dams, M8.8 Maule, Chile EQ )



Bellavista

Dike No. 1

(Ramirez, 2010)

Veta del Agua

Dike No. 5

(Prof. R. Espinace)



Verdugo et al. 2012

# **SEISMIC DESIGN CONSIDERATIONS FOR TAILINGS DAMS**

## **3. Flow Slide Potential**

# Two Critical Issues

1. Are there materials that can lose significant strength due to cyclic loading?

If Post-Cyclic Static Slope Stability  $FS \leq \approx 1$ ,  
Flow Slide is Possible

2. If not, will the system undergo significant deformations that may jeopardize its performance?

If  $FS > 1$ , Estimate Seismic Slope Displacement



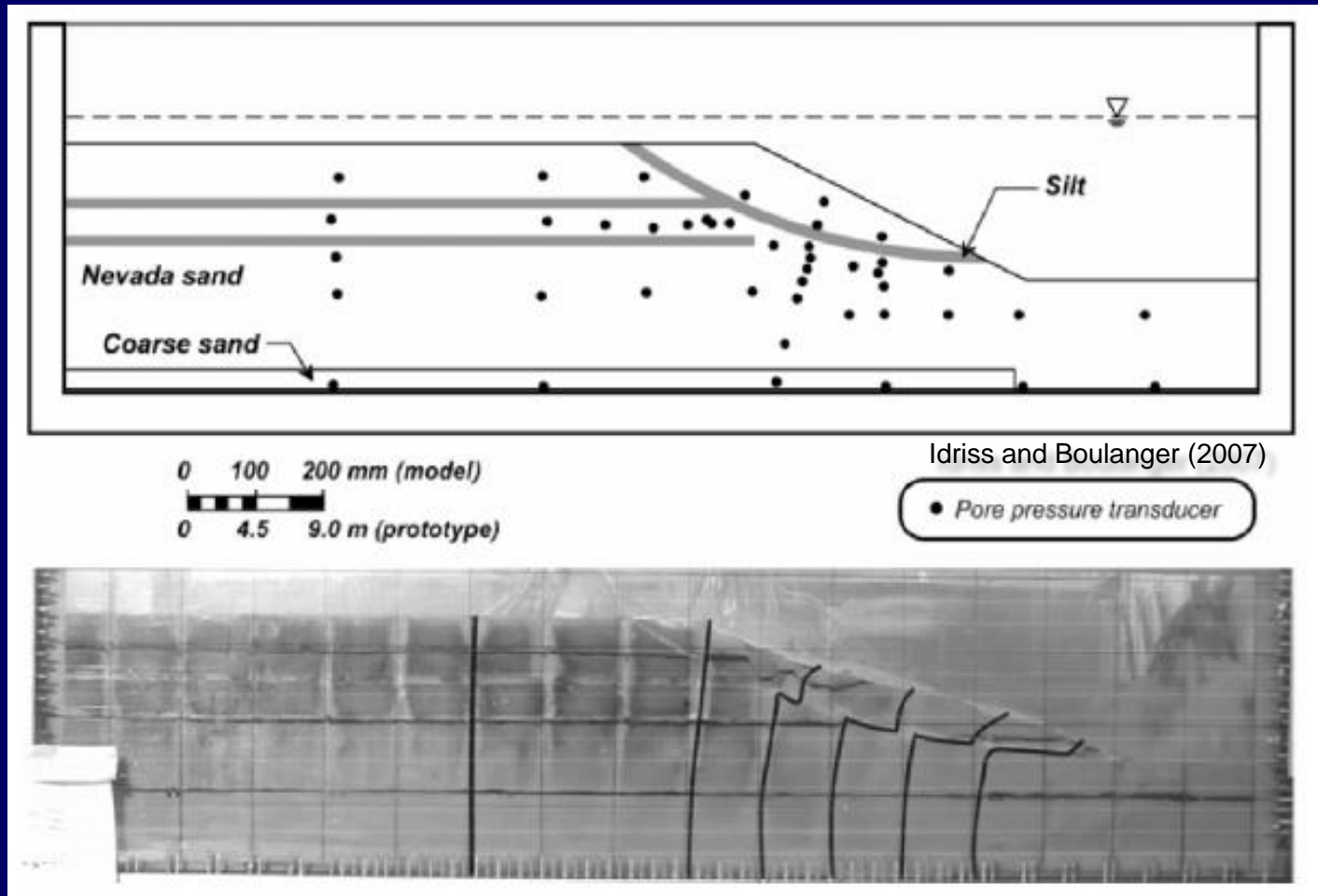
# Post-Liquefaction Residual Strength ( $S_r$ ) is a System Property



Lower San Fernando Dam Instability in 1971 EQ (H. B. Seed)



# VOID REDISTRIBUTION



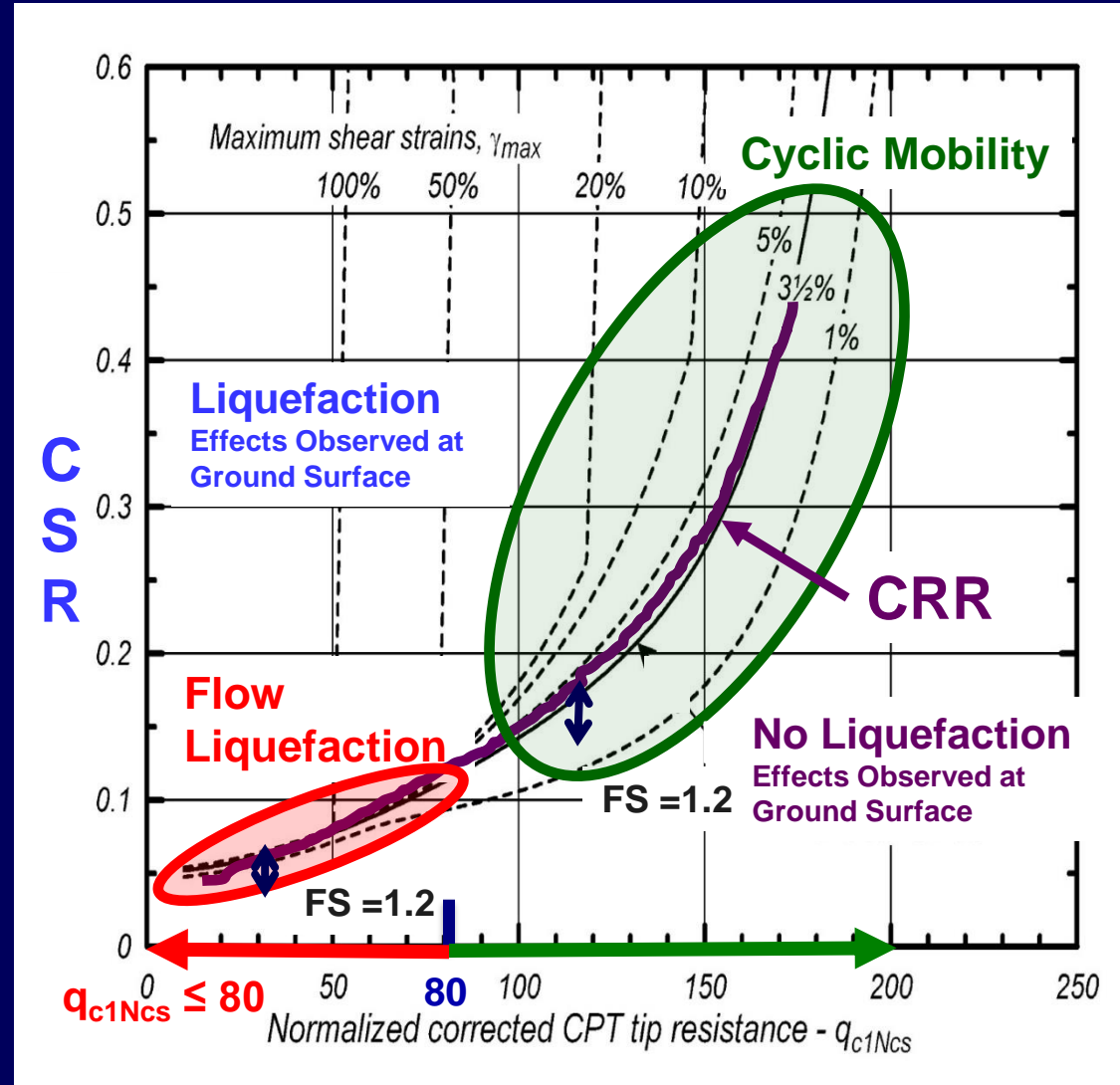
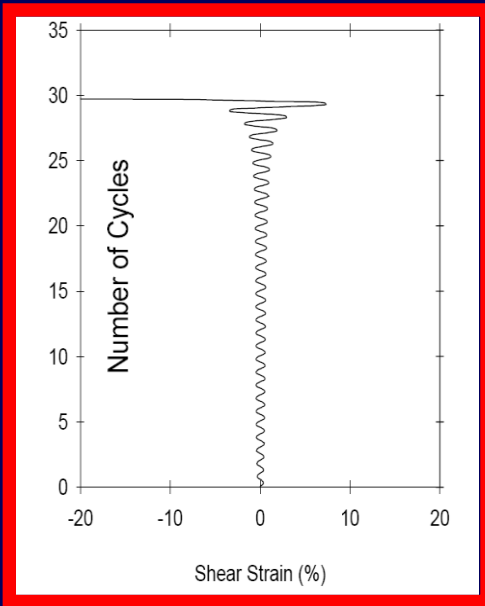
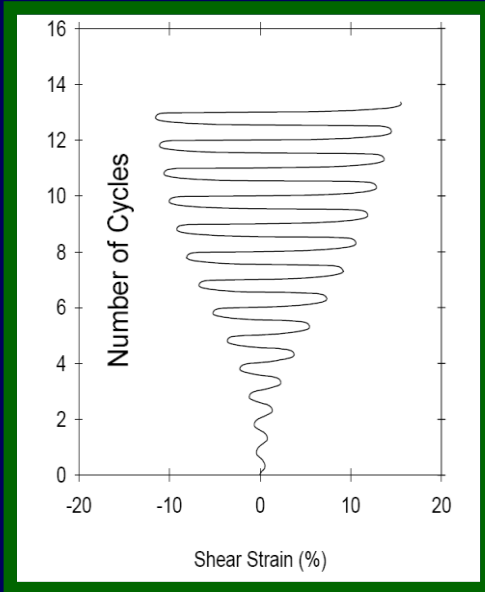
Porewater accumulated beneath silt layer

Local void ratio increases & strength decreases

Failure occurred on discrete surface

Slope failed after shaking ended

# LIQUEFACTION EFFECTS

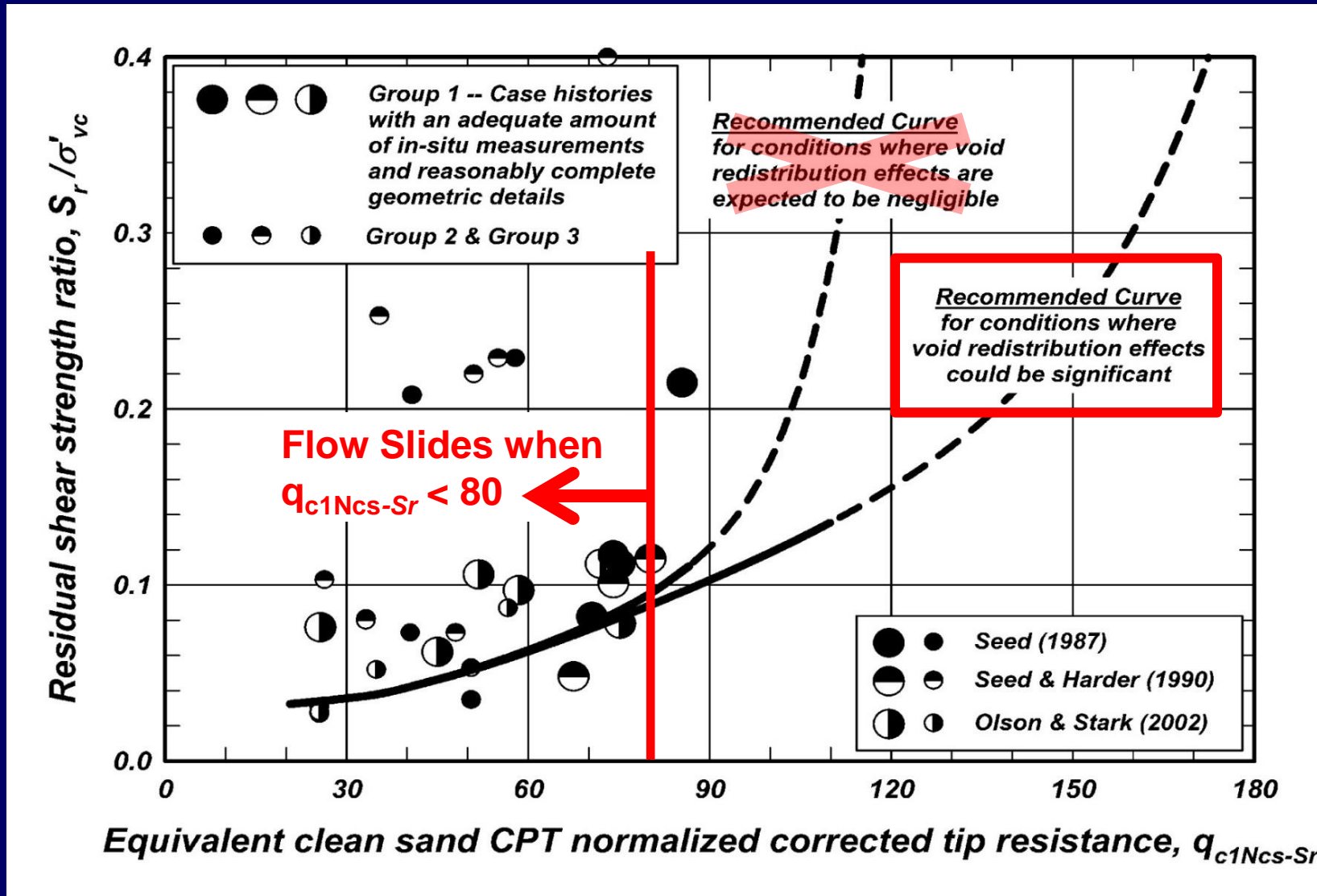


$$FS = CRR / CSR$$

Idriss & Boulanger 2008

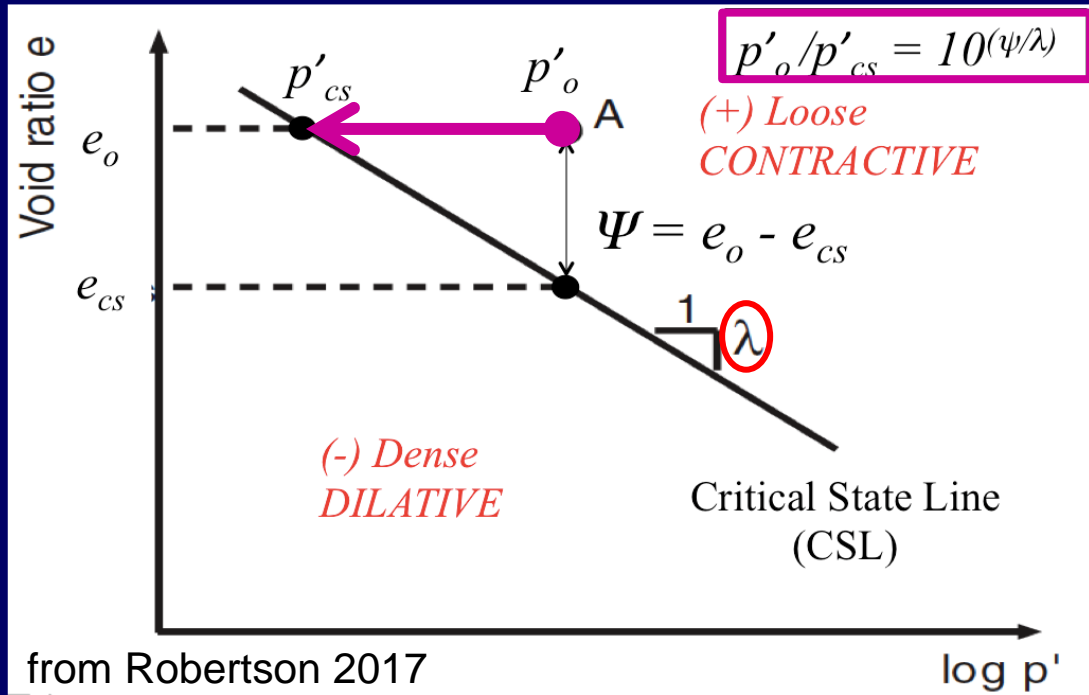


# Post-Liquefaction Residual Strength



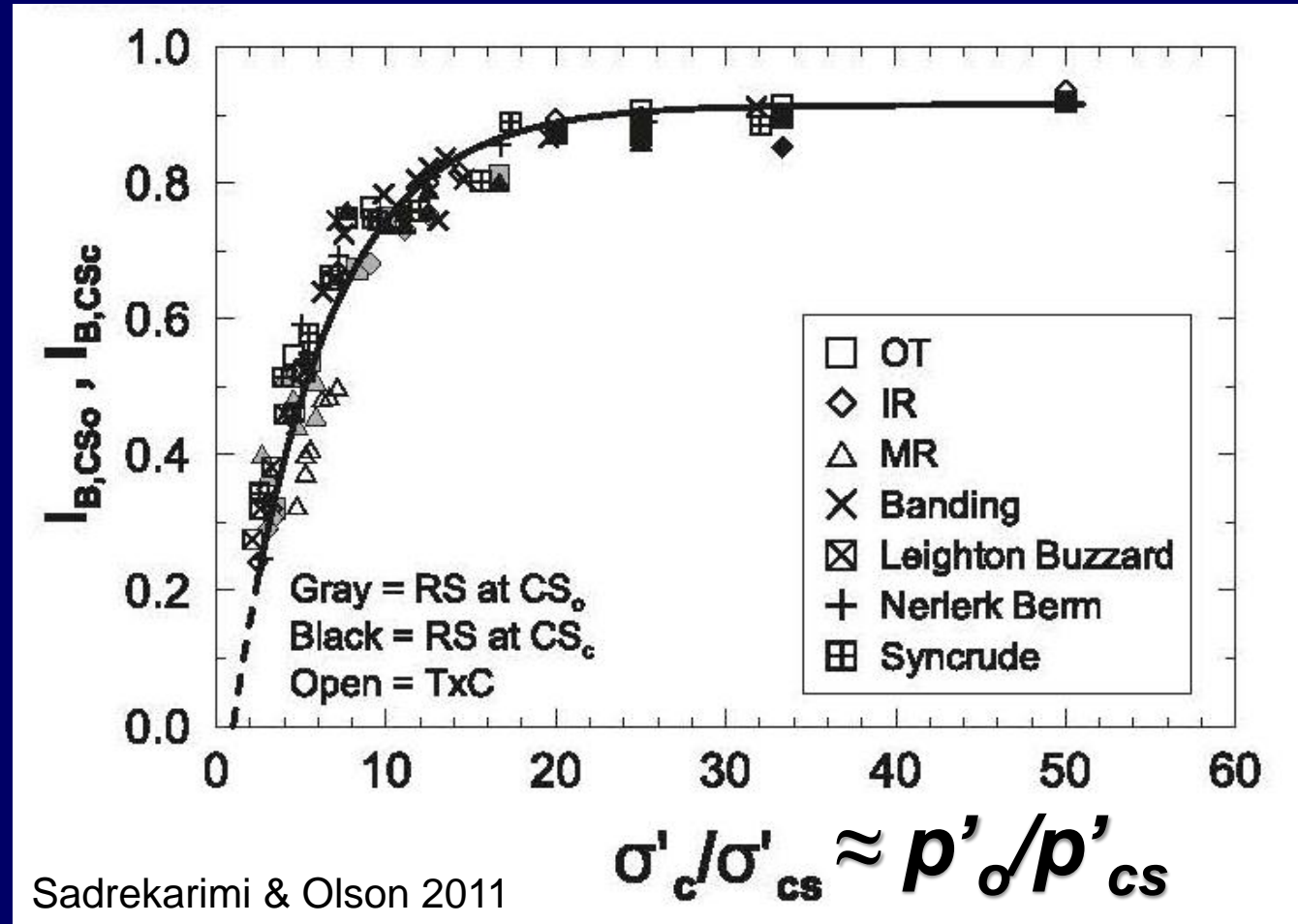
Idriss & Boulanger 2008

# INITIAL STRESS RATIO ( $p'_o/p'_{cs}$ )



**Brittleness Index (Bishop 1967):**

$$I_B = 1 - S_r / S_{peak}$$

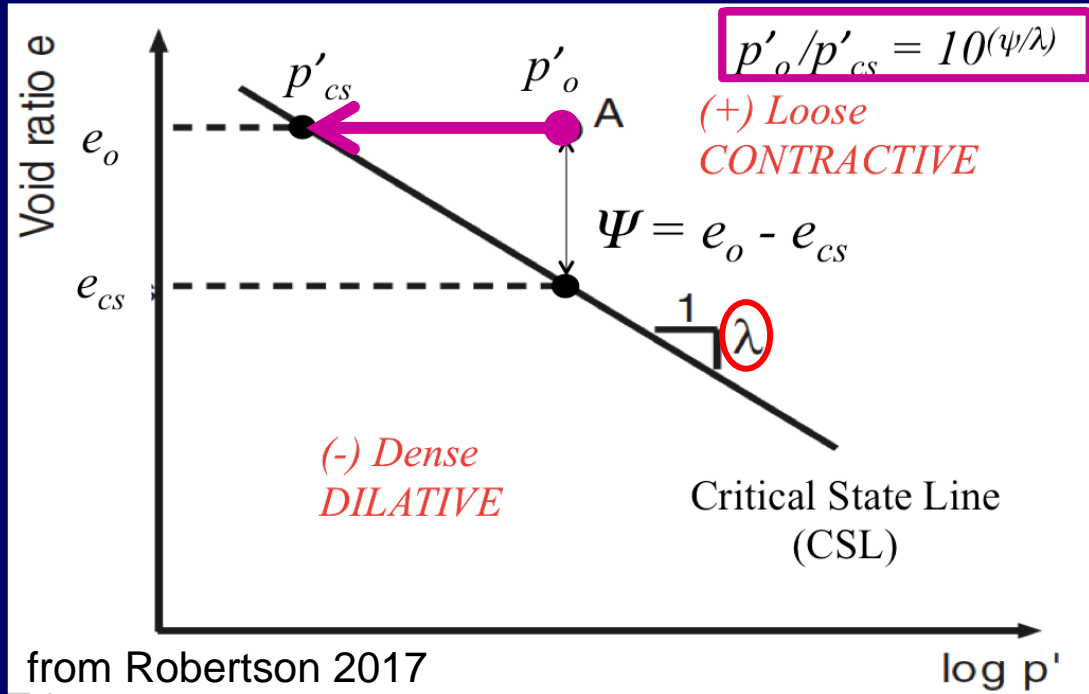


**Brittleness increases as initial stress ratio increases**



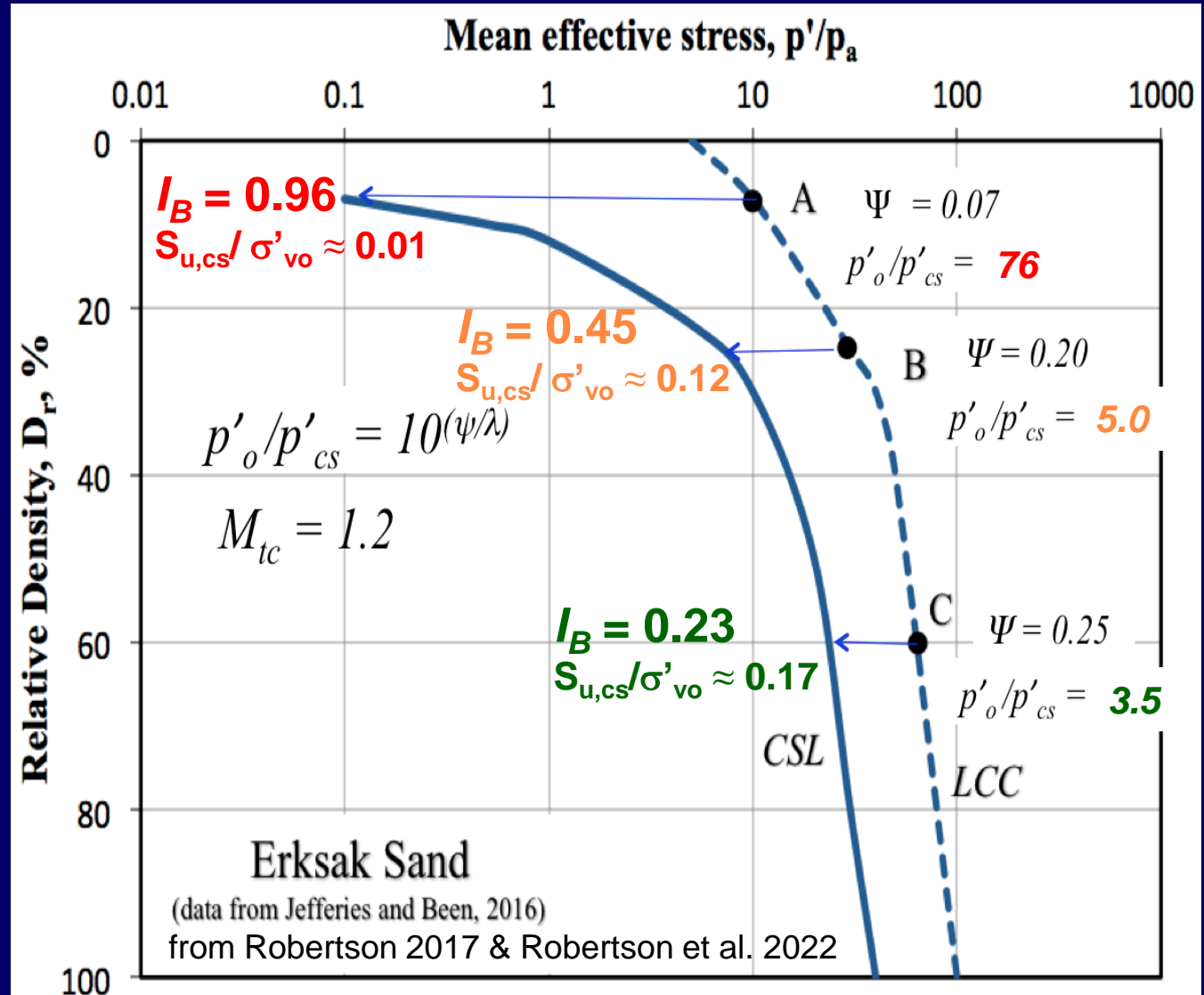
# INITIAL STRESS RATIO ( $p'_o/p'_{cs}$ )

OVER LARGE STRESS RANGE

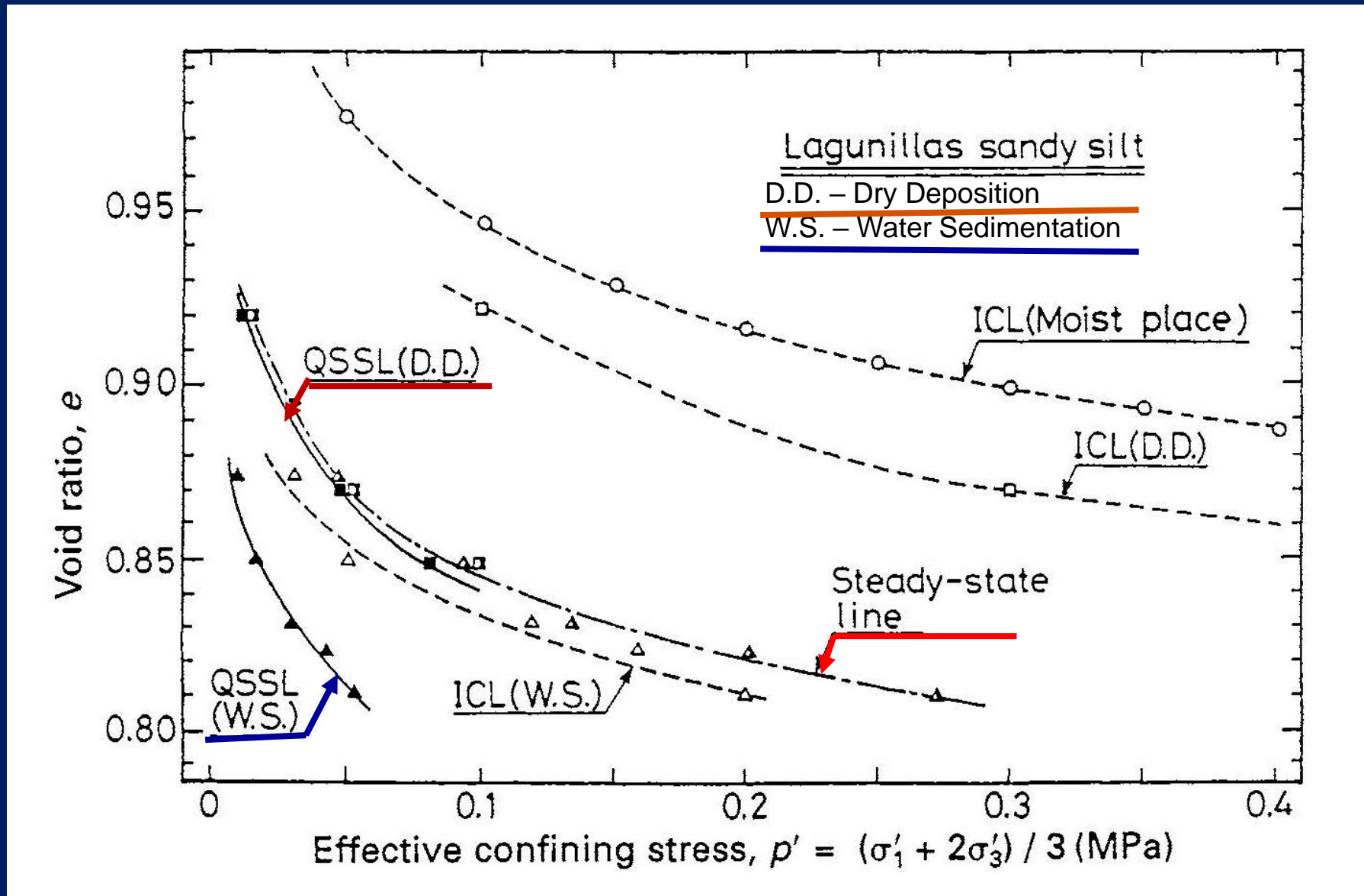


Brittleness Index (Bishop 1967):

$$I_B = 1 - S_r / S_{peak}$$



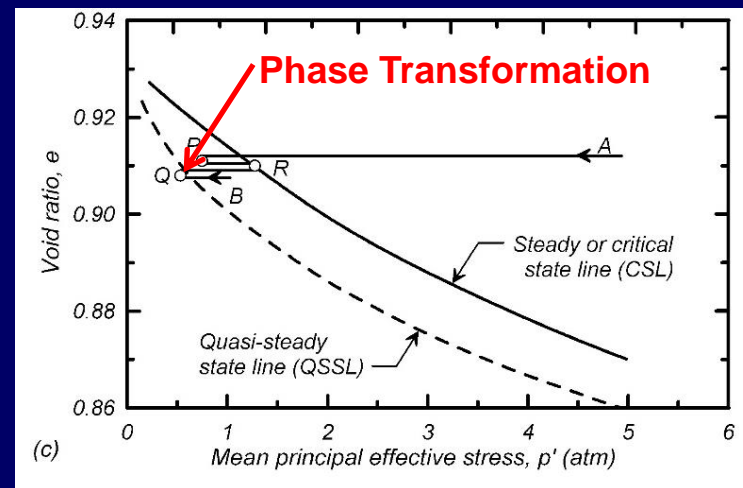
# QSSLs & SSL with ICLs of Lagunillas Sandy Silt





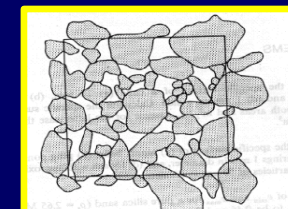
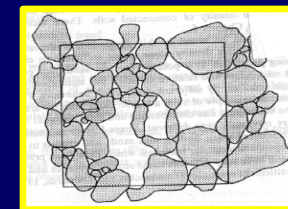
# QUASI-STEADY STATE LINE

(affected by soil fabric, i.e. depositional history)

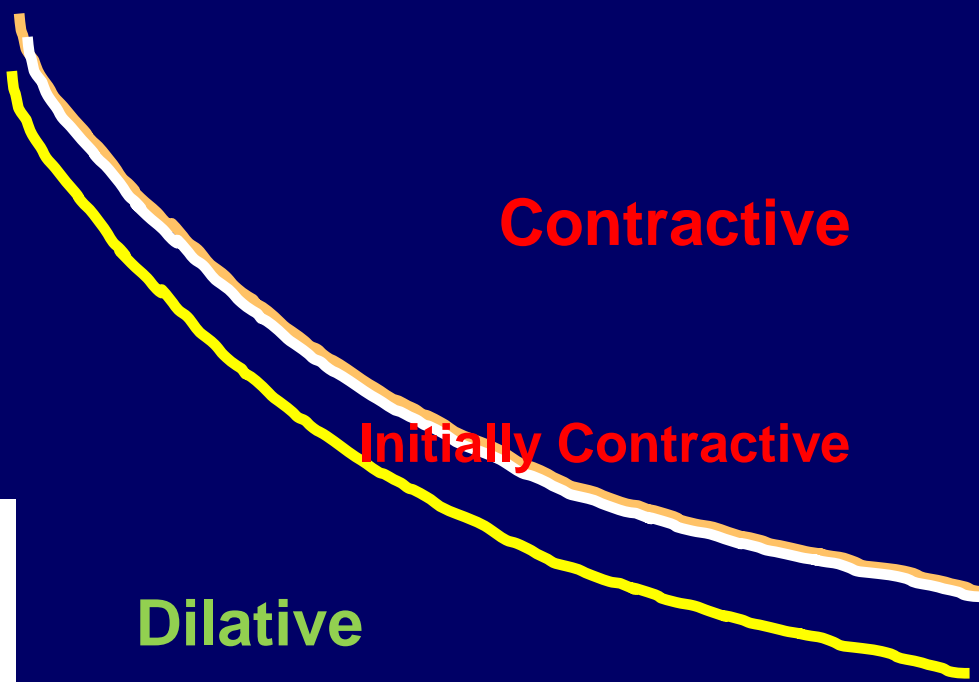


Data from Ishihara 1993

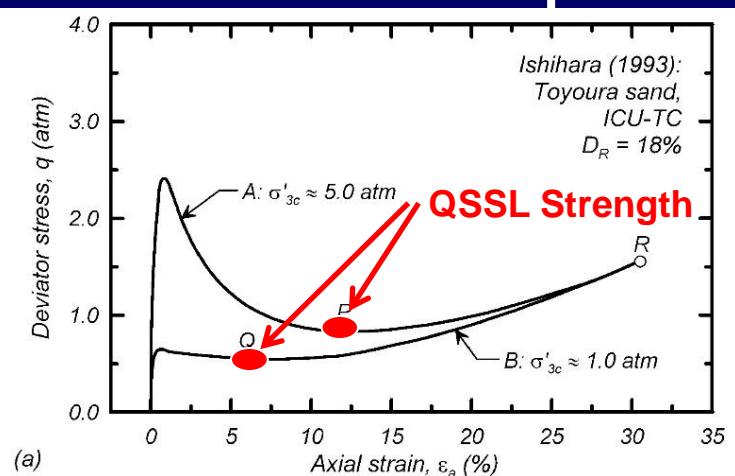
CSL } Independent of  
 SSL } initial state or fabric  
 QSSL } Dependent on fabric



e



p'



Ishihara (1993):  
 Toyoura sand,  
 ICU-TC  
 $D_R = 18\%$

QSSL Strength

# SILT LIQUEFACTION AFTER 1999 KOCAELI & CHI-CHI EQs

**Silt can liquefy**

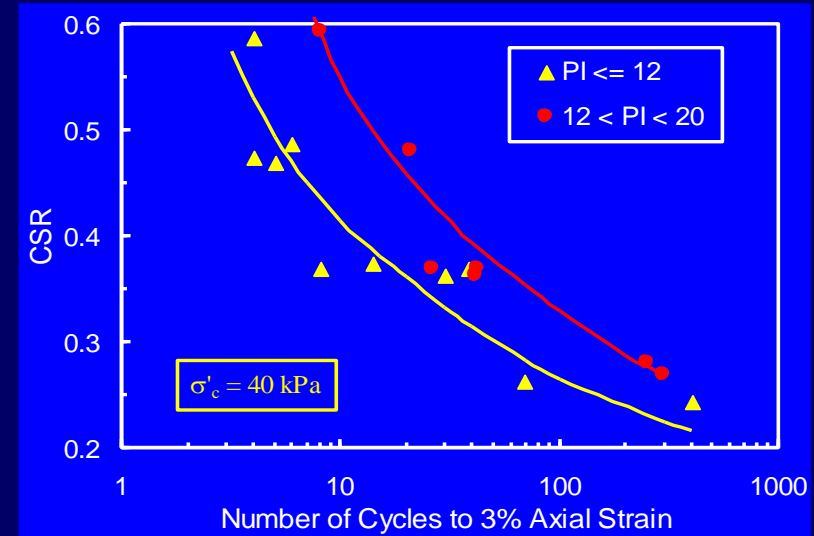
**Do not use Chinese criteria because  
% clay-size criterion is not reliable**

**Focus on mineralogy & sensitivity:**

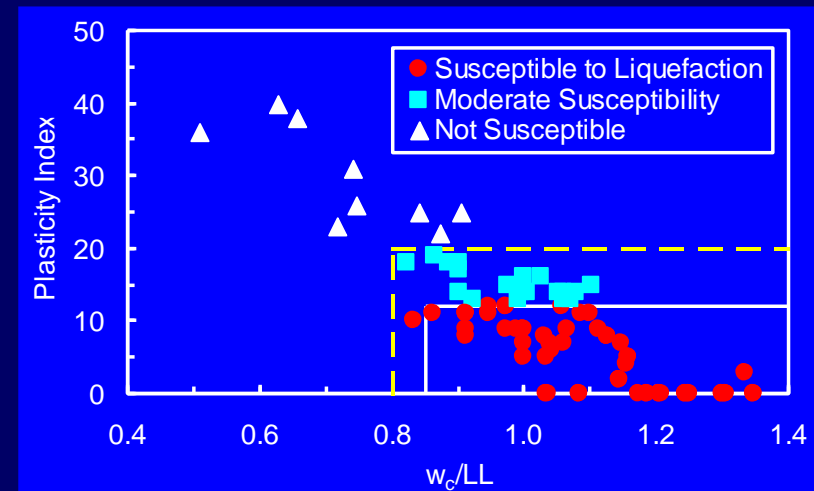
**Use  $PI \leq 12$  &  $w_c/LL \geq 0.85$**

**Under intense shaking, consider using:**

**$PI \leq 18$  &  $w_c/LL \geq 0.80$**



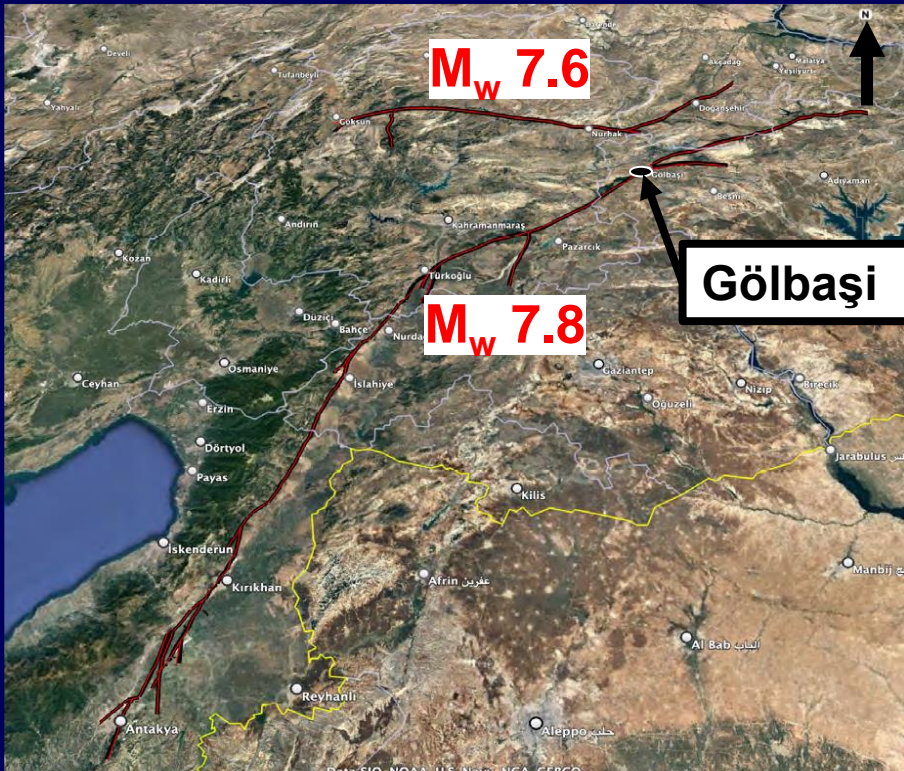
**Silt CTX Testing (Bray & Sancio 2006)**



**Bray & Sancio 2006 Susceptibility Criteria**



# Sediment Ejecta in Gölbaşı – 2023 Turkey EQs



Ejecta (30MAR2023;  
37.7877N, 37.6430E)

8 free-field ejecta samples collected after EQs

“Top-Down” procedure (Youd pers. com, 1999)

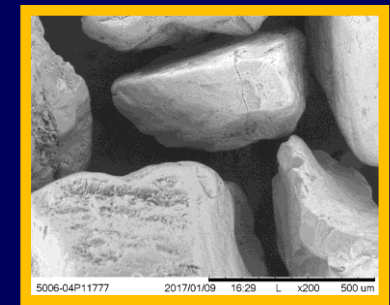
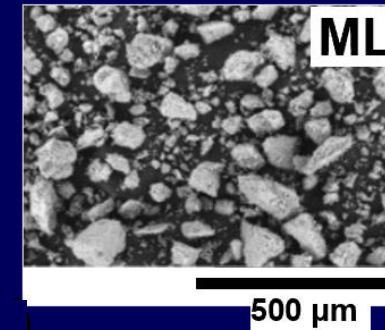
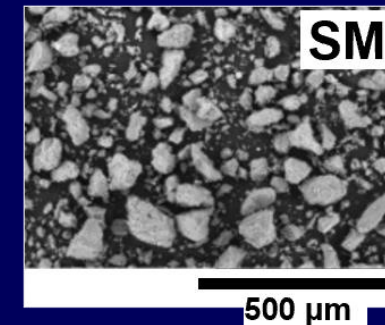
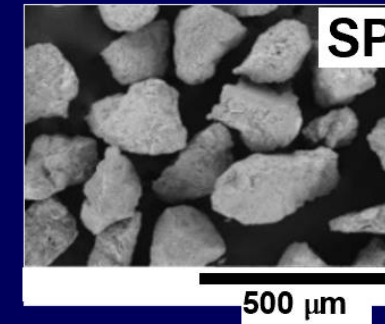
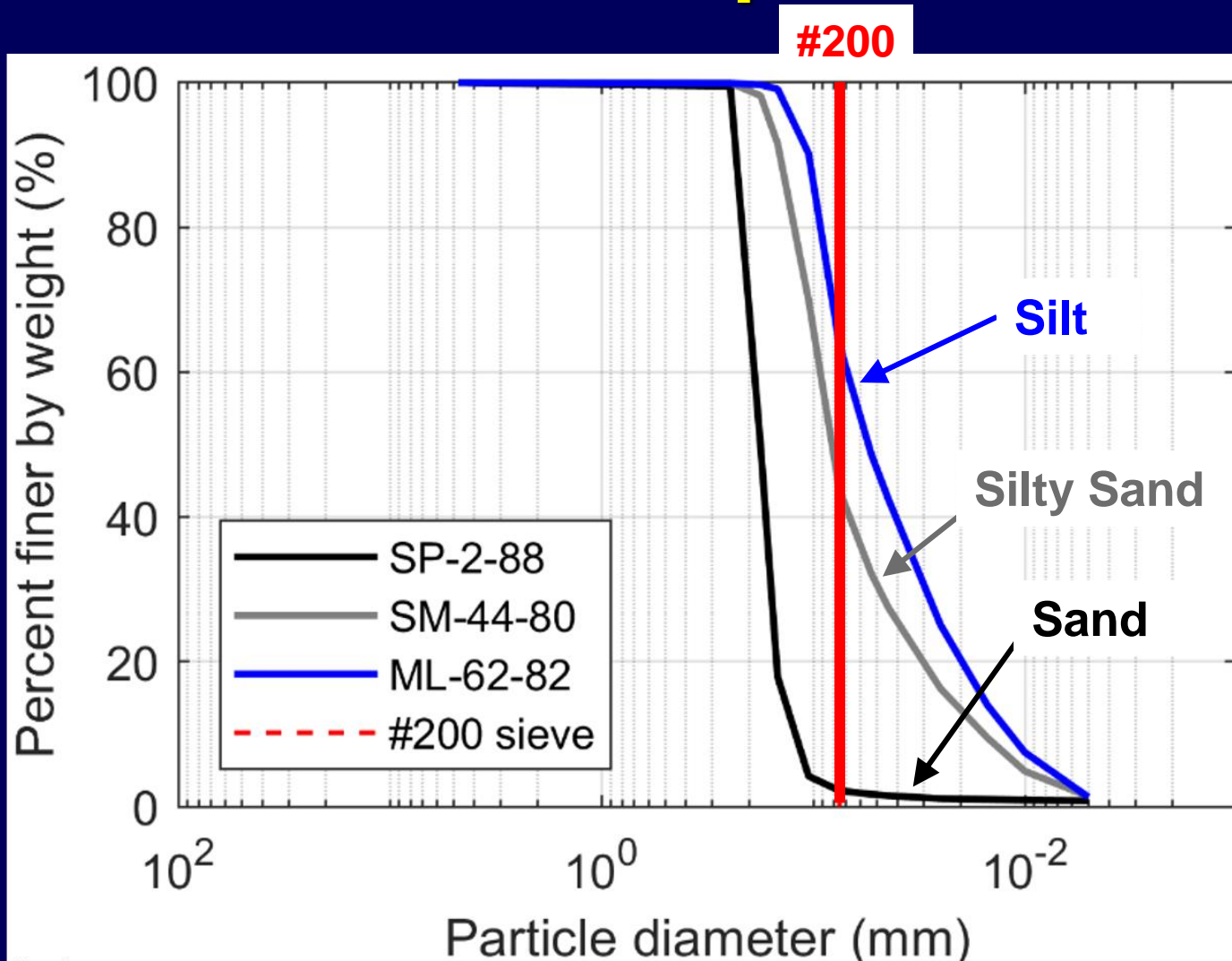
**ASTM PI = 9 – 14**

(Moug et al. 2023 GEER Report)





# Grain-Size of Liquefiable Christchurch Soils



Classic Testing SP

Monterey 0/30  
FC=0%  
x200

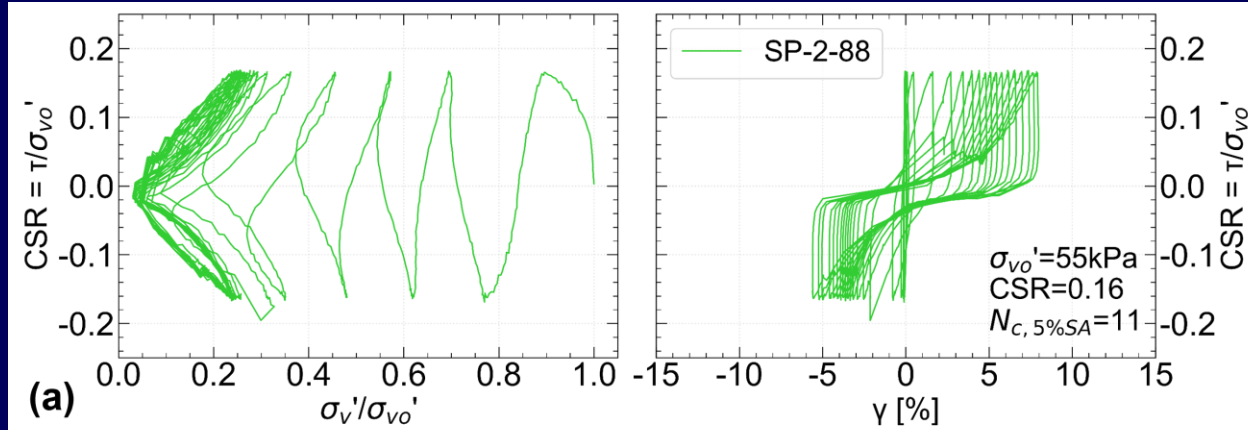
Mijic et al. (2021)

Does soil 'know' the #200 sieve exists?

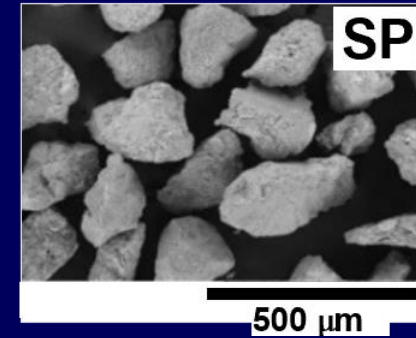


# Cyclic Simple Shear Tests of “Undisturbed” Christchurch Soil

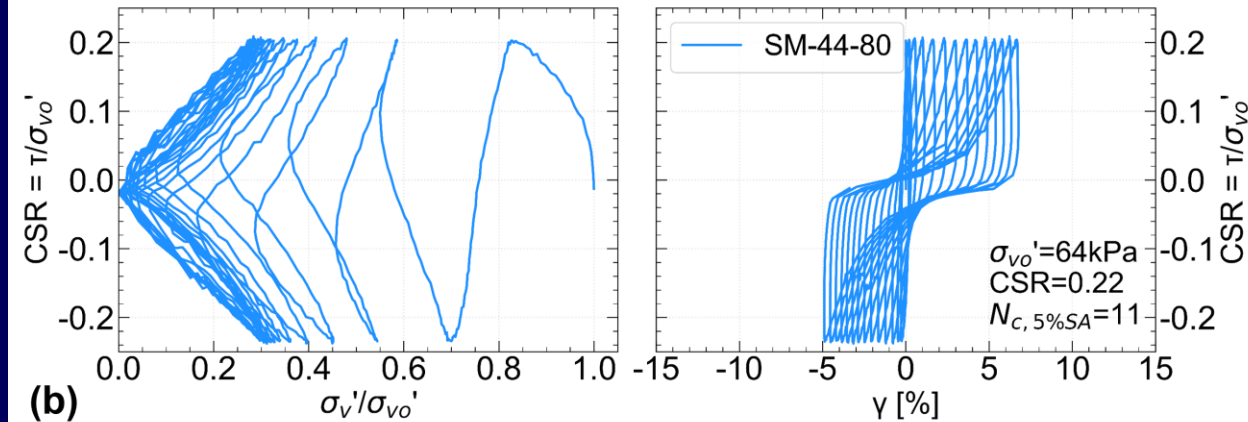
**SP**



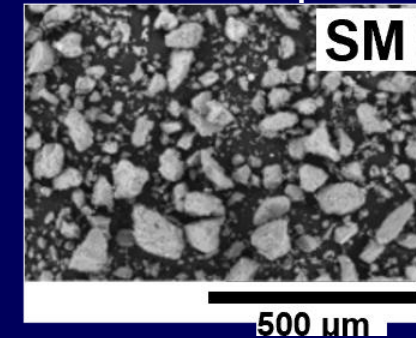
**FC = 2%,  $D_r = 88\%$**



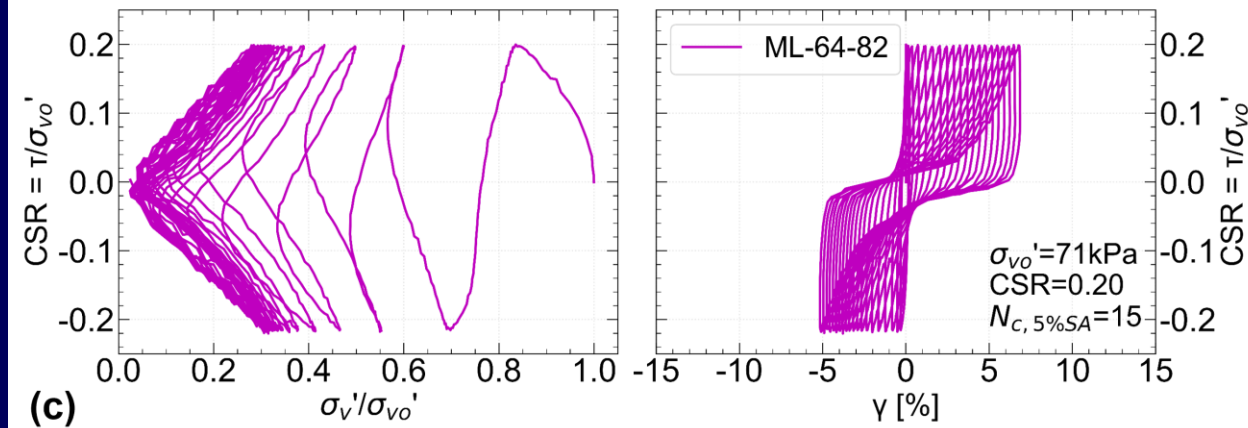
**SM**



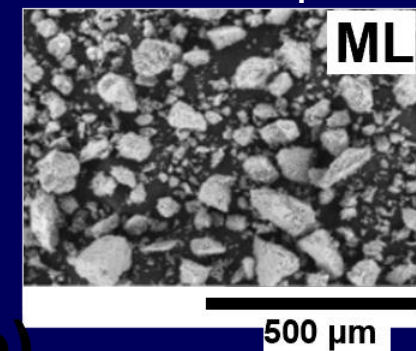
**FC = 44%,  $D_r = 80\%$**



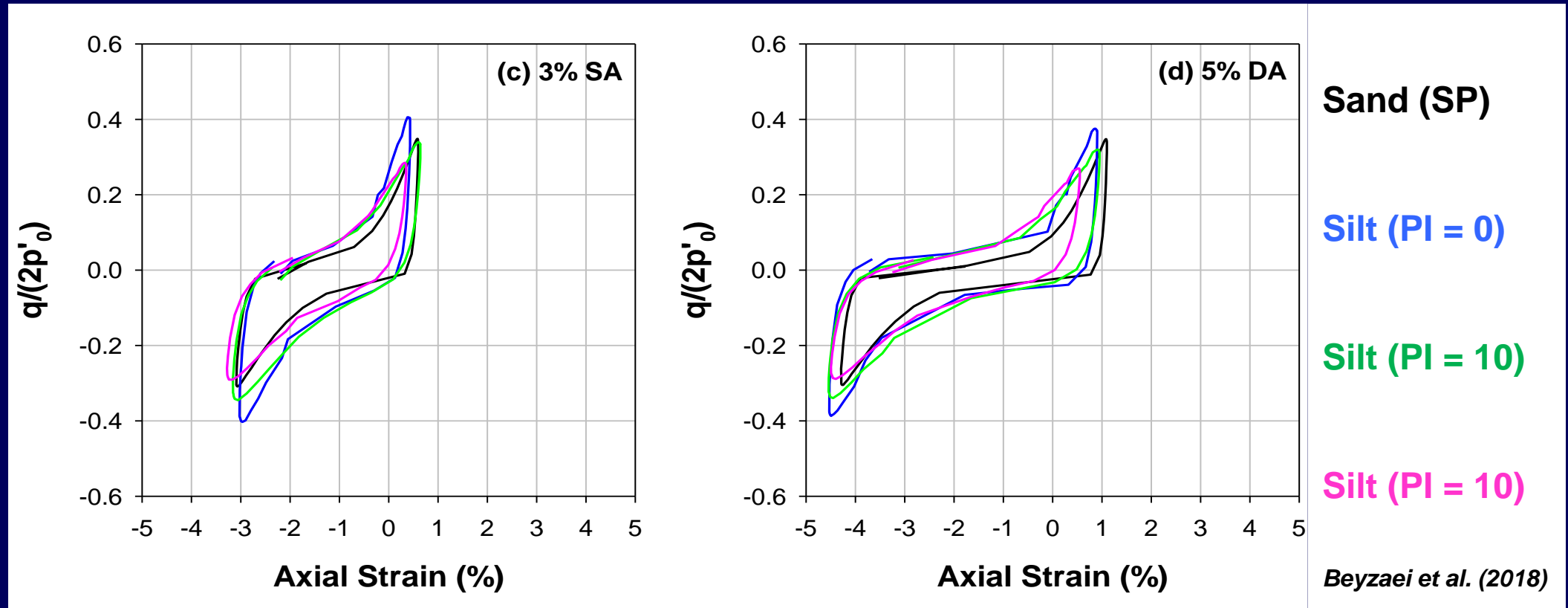
**ML**



**FC = 64%,  $D_r = 82\%$**



# Cyclic Triaxial Tests Performed on Christchurch Soil



Bray & Sancio 2006 criteria based on engineering response & consequences of material

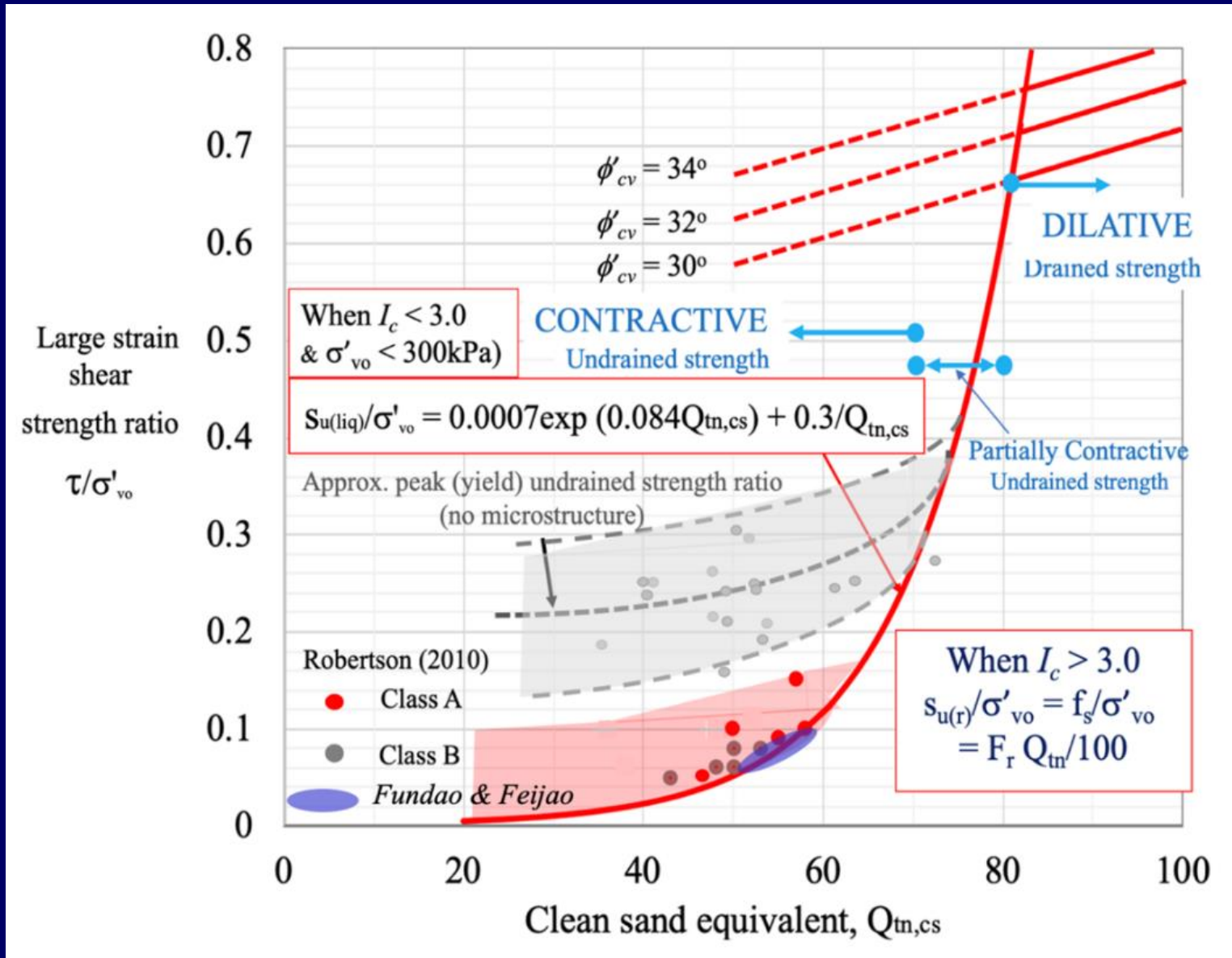
- “cyclic performance assessment” criteria

Perform cyclic testing on high FC soil to assess seismic response characteristics  
(they can be sampled effectively)





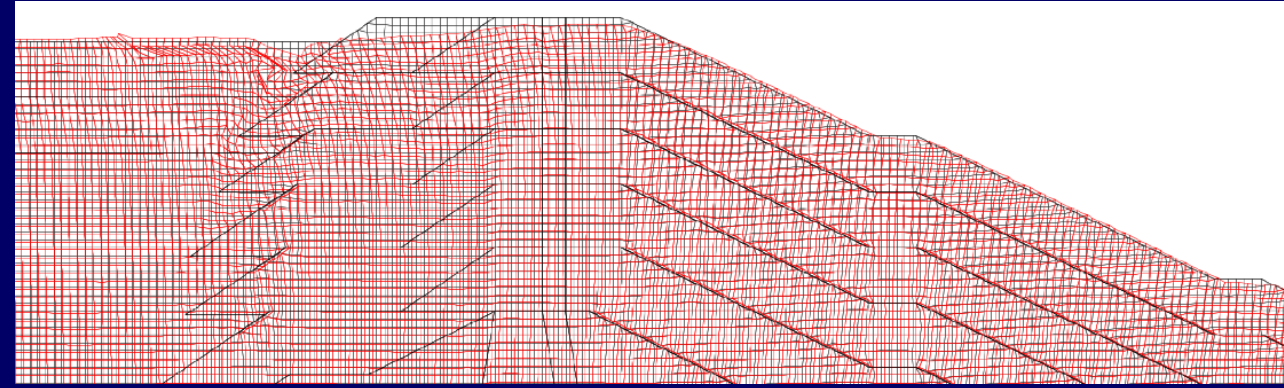
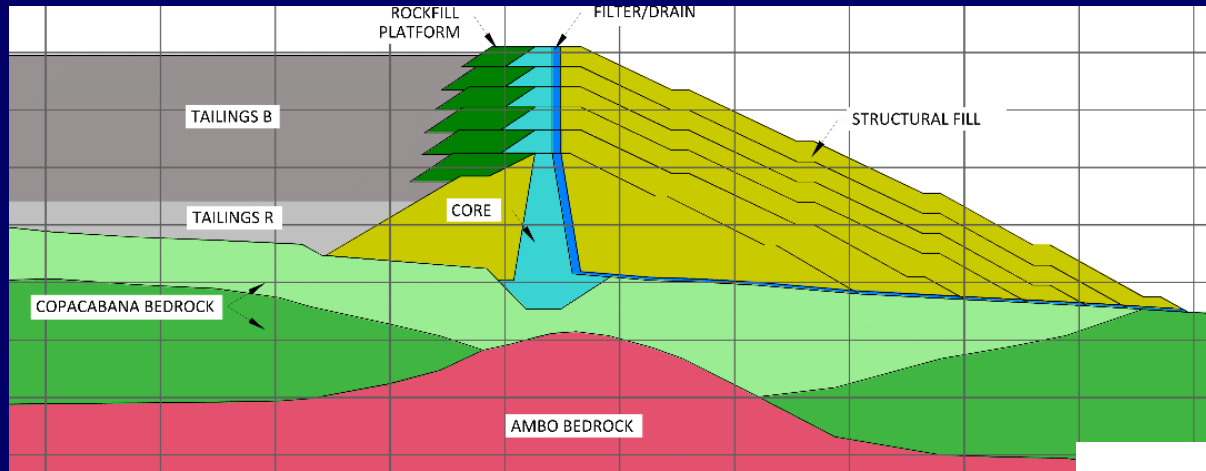
# Post-Liquefaction Residual Strength



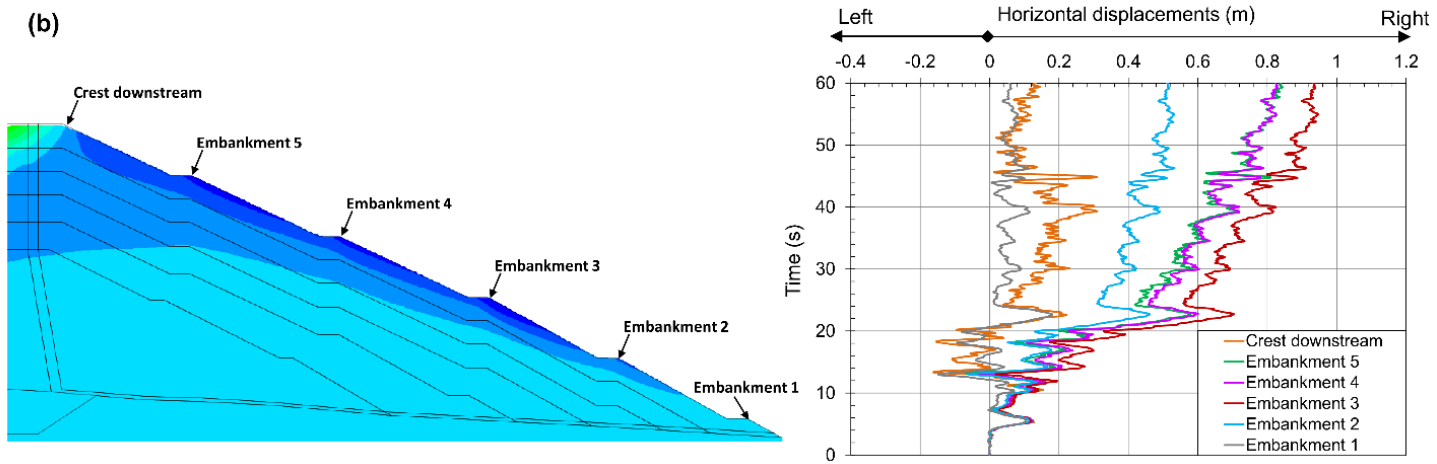
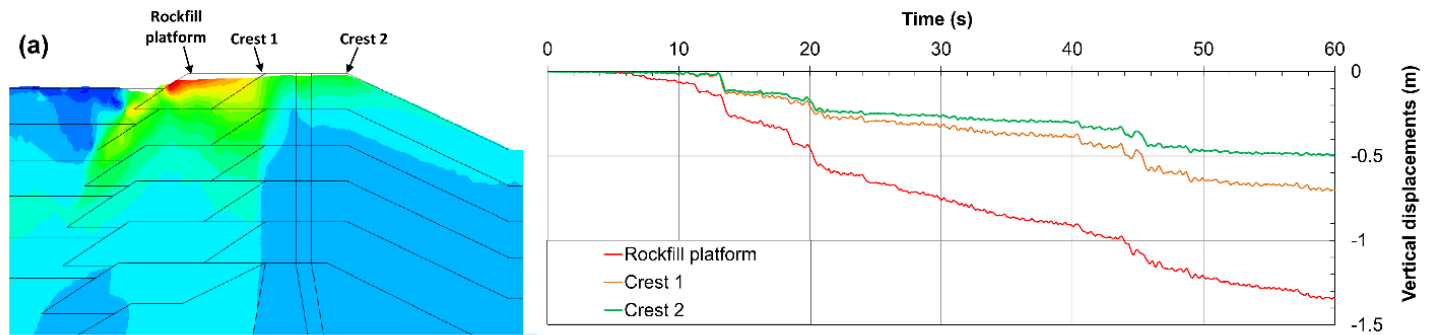
# **SEISMIC DESIGN CONSIDERATIONS FOR TAILINGS DAMS**

## **4. Seismic Slope Displacement**

# Finite Difference Analysis of a Centerline Tailings Dam



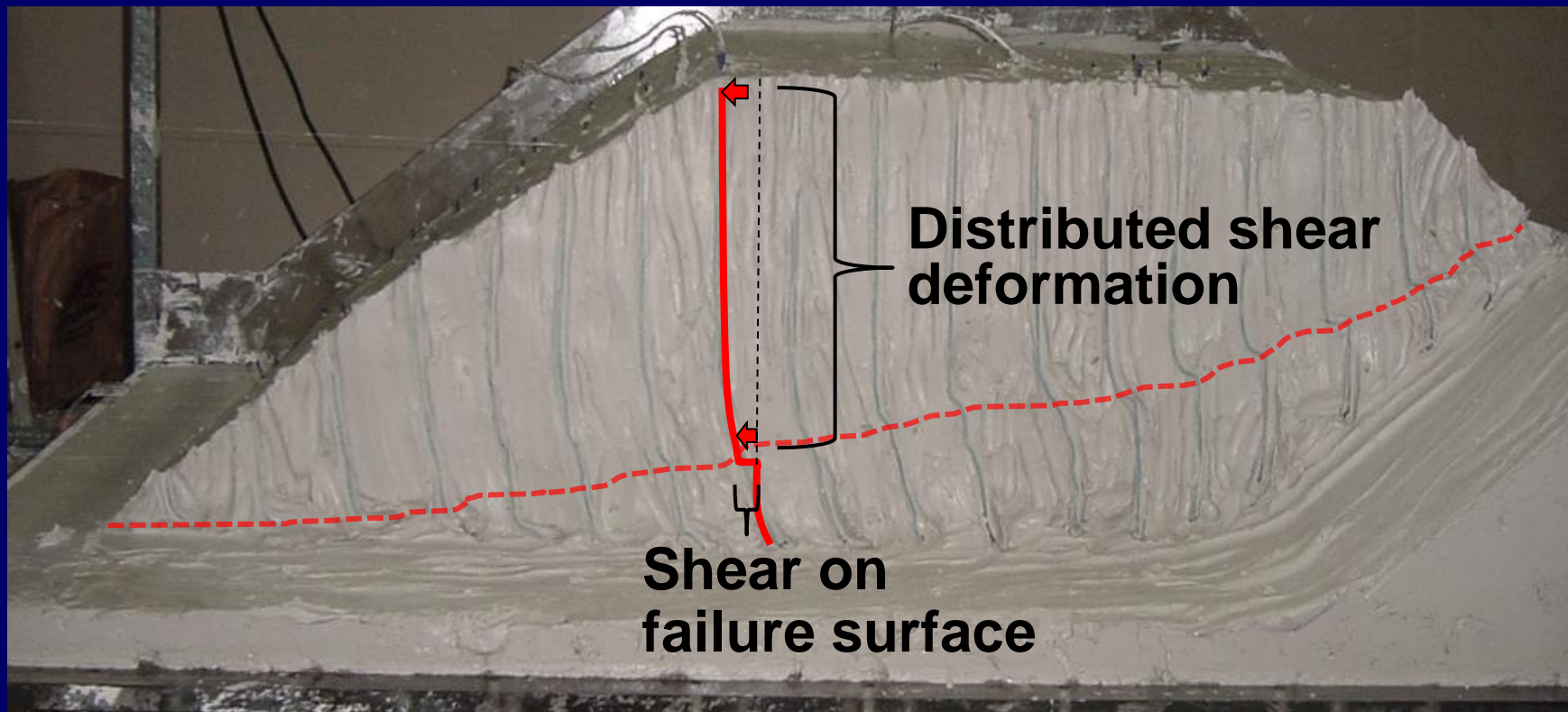
“Dynamic effective stress analysis of a centreline tailings dam under subduction earthquakes”  
by Macedo et al. 2022





# Seismic Slope Displacement

- Shear on Failure Surface
  - Distributed Shear Deformation
- Newmark-type seismic displacement
- Shear**
- Add Volumetric-Induced Deformation, when appropriate

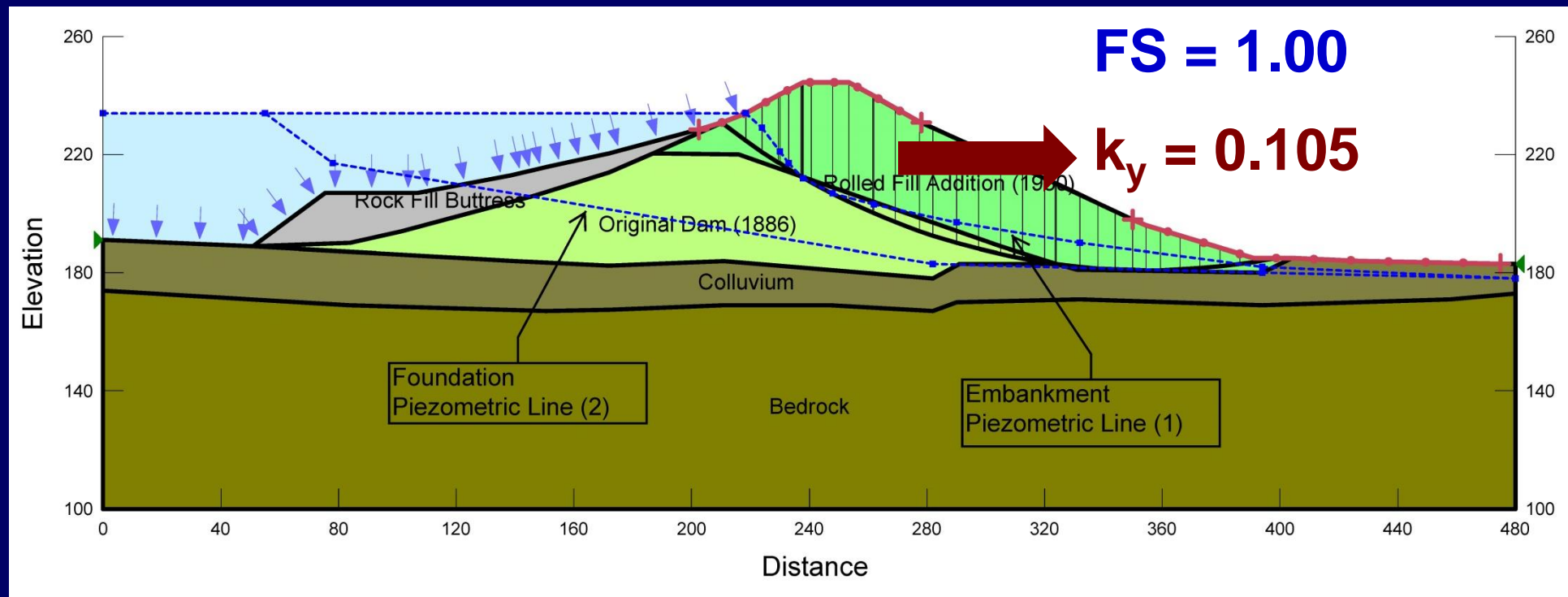


# **Key Components of Seismic Slope Displacement Analysis**

- a. Dynamic Resistance**
- b. Earthquake Ground Motion**
- c. Dynamic Response**
- d. Seismic Displacement Calculation**

# a. Dynamic Resistance

***Yield Coefficient ( $k_y$ ):*** seismic coefficient that results in FS=1.0 in pseudostatic stability analysis



Use method that satisfies all three conditions of equilibrium and focus on **soil strength**, water pressures, and unit weight



# Peak Dynamic Undrained Shear Strength of Clay

Chen et al. (2006)

- $S_{\text{dynamic, peak}} = S_{\text{static, peak}} (C_{\text{rate}}) (C_{\text{cyc}}) (C_{\text{prog}}) (C_{\text{def}})$
- Rate of loading:  $C_{\text{rate}} > 1$
- Cyclic Degradation:  $C_{\text{cyc}} < 1$
- Progressive failure:  $C_{\text{prog}} < 1$
- Distributed deformation:  $C_{\text{def}} < 1$

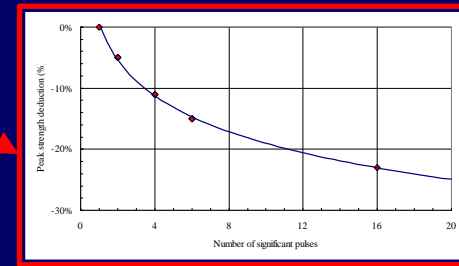
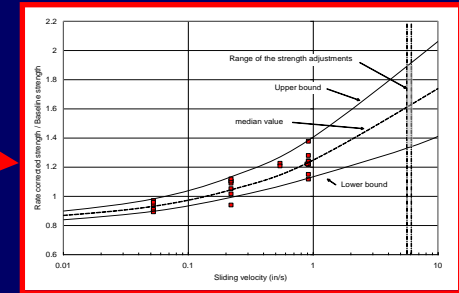
Typical values often lead to:

$$S_{\text{dynamic, peak}} \approx S_{\text{static, peak}} (1.4) (0.85) (0.9) (0.9) \approx S_{\text{static, peak}}$$

But  $S_{\text{dynamic, peak}}$  varies with loading, i.e., EQ motion:

Near-Fault Pulse:  $S_{\text{dynamic, peak}} \approx S_{\text{static, peak}} (1.4)(1.0)(1.0)(0.9) \approx 1.2 S_{\text{static, peak}}$

Long Duration:  $S_{\text{dynamic, peak}} \approx S_{\text{static, peak}} (1.4)(0.7)(0.9)(0.9) \approx 0.8 S_{\text{static, peak}}$



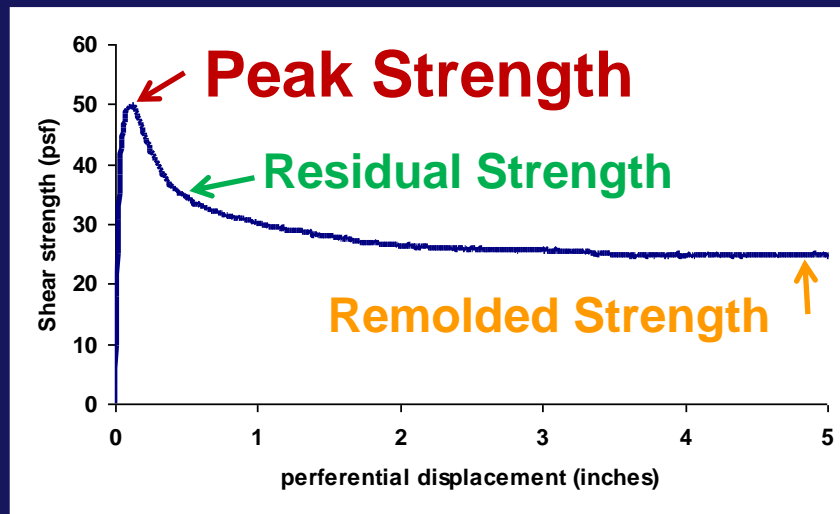
# Dynamic Shear Strength of Clay

Chen et al. (2006)

Peak dynamic strength is used for strain-hardening soil or limited displacement

As EQ-induced strain exceeds failure strain, dynamic strength reduces for strain-softening soil

Thus,  $S_{\text{dynamic}}$  &  $k_y$  are also a function of displacement

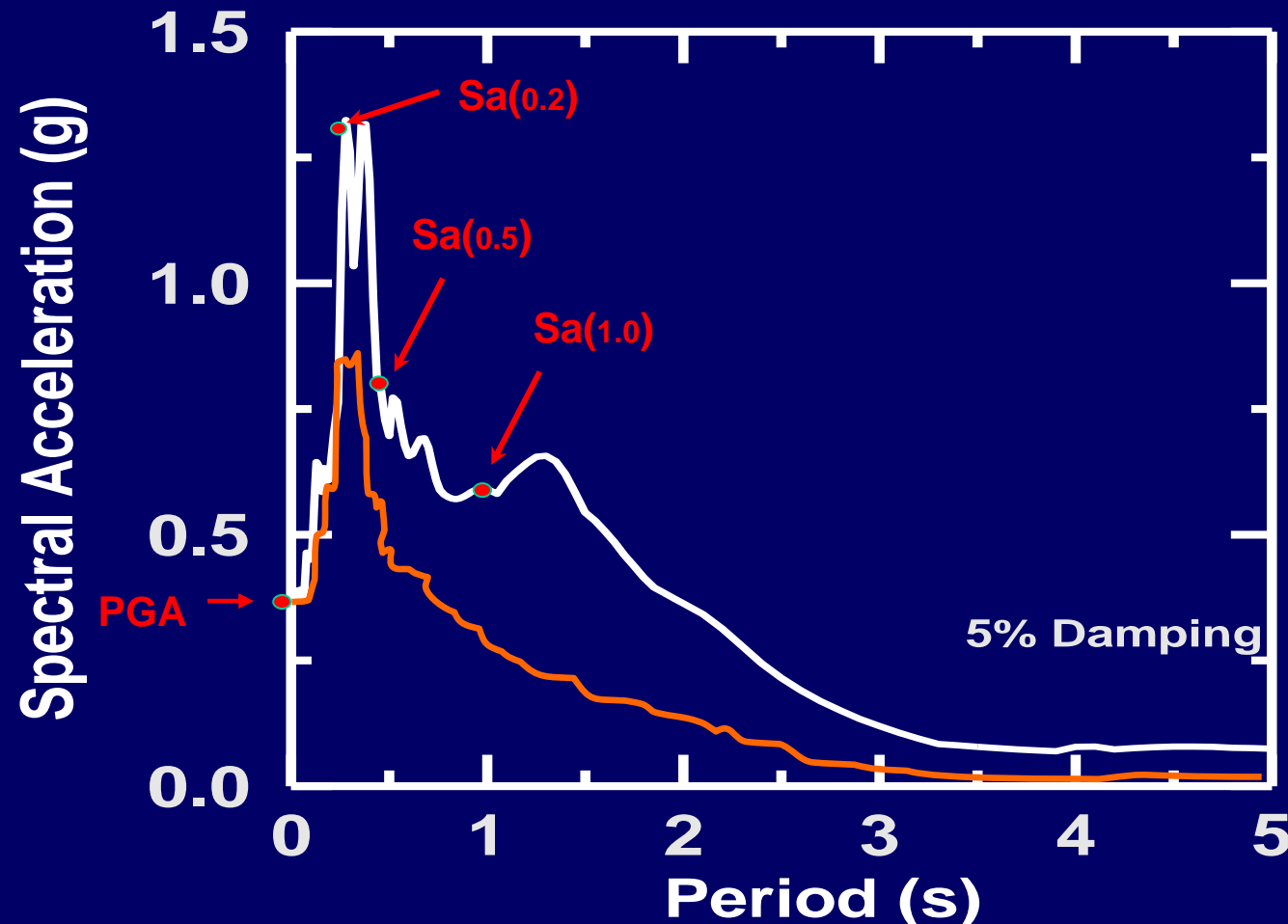


Field Vane Shear Test (FVST) [ASTM D2573]



## ***b. Earthquake Ground Motion:***

### **Acceleration Response Spectrum**



provides response of SDOF of different periods at 5% damping

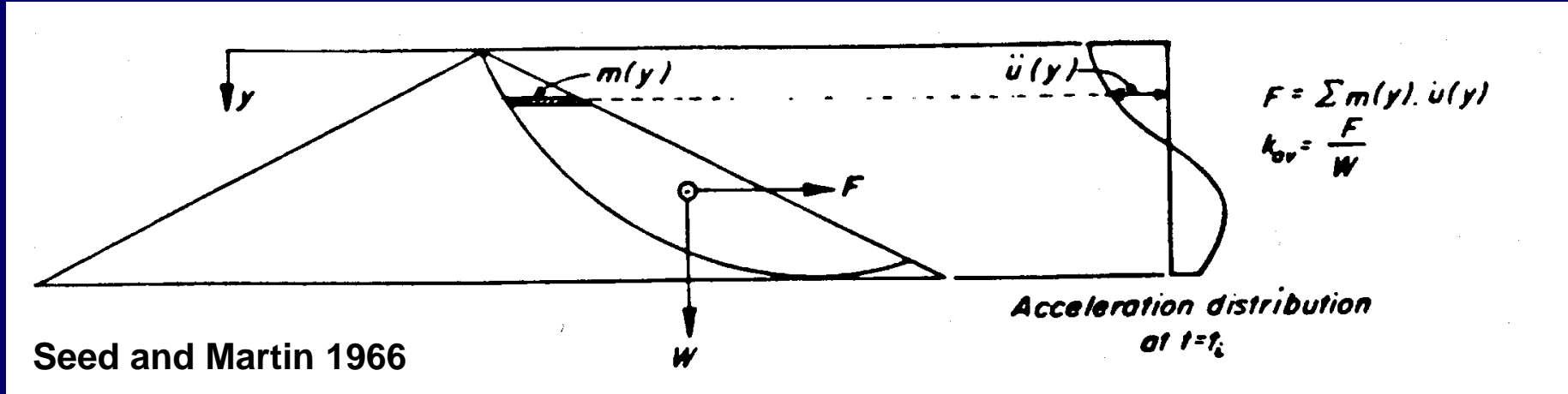
indicates intensity and frequency content of ground motion below sliding mass

ground motion characteristics greatly affect slope displacement



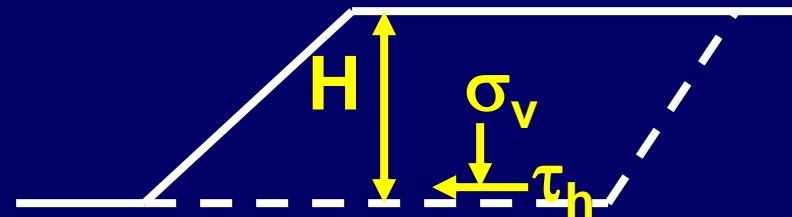
# c. Dynamic Response of Sliding Mass

## Equivalent Acceleration Concept

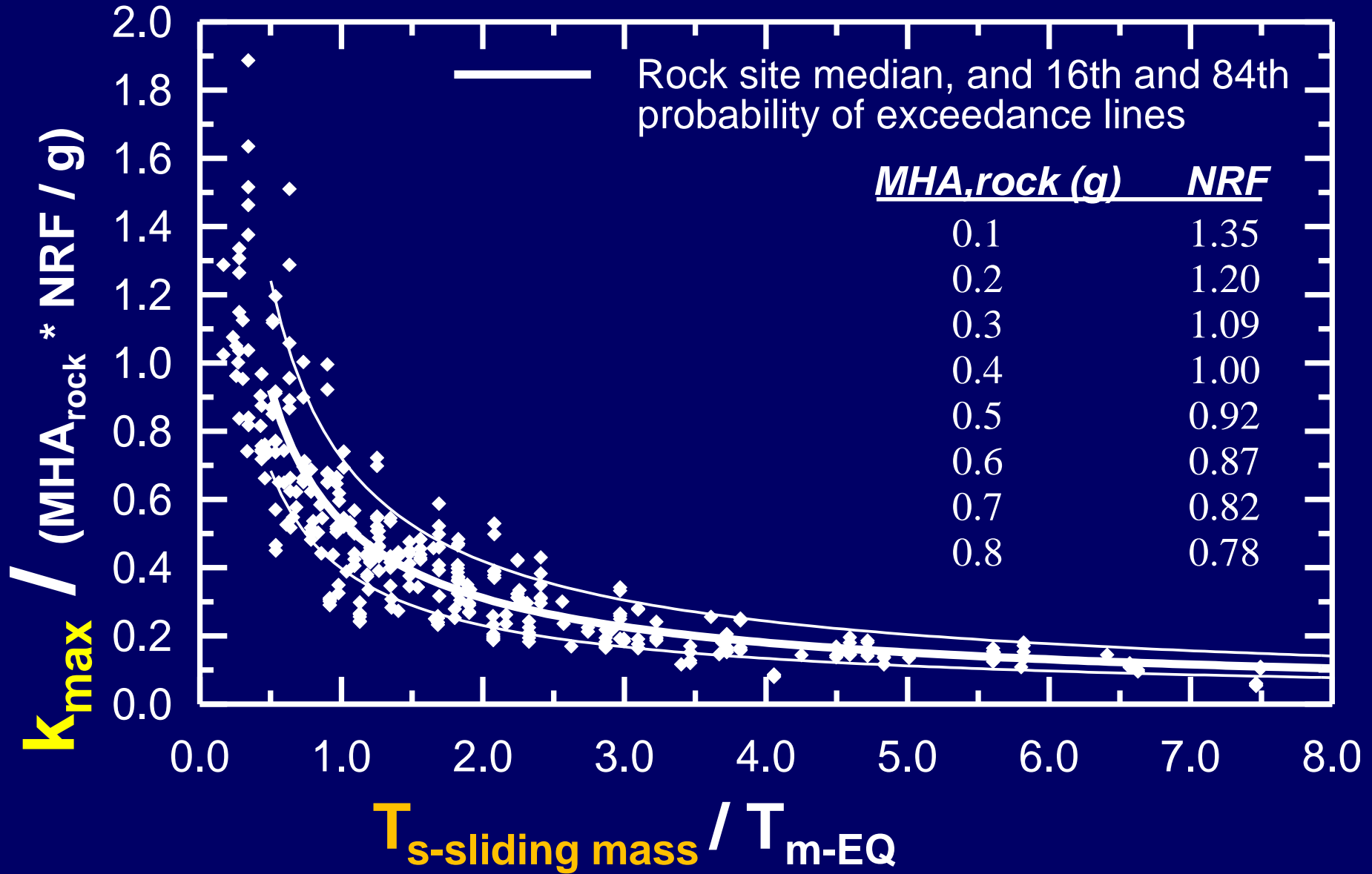


accounts for cumulative effect of incoherent motion in deformable sliding mass

- Horz. Equiv. Accel.:  $HEA(t) = (\tau_h(t) / \sigma_v) g$
- $k_{max} = \max. HEA / g$



# FACTORS AFFECTING MAXIMUM SEISMIC LOADING



(Bray & Rathje 1998)

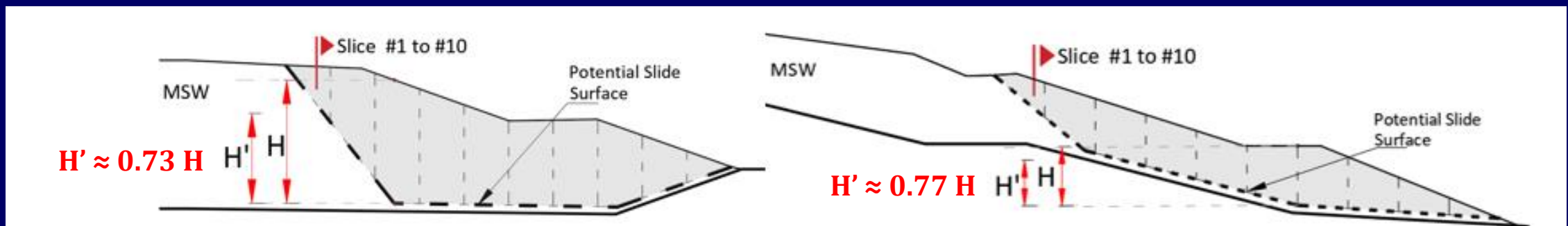
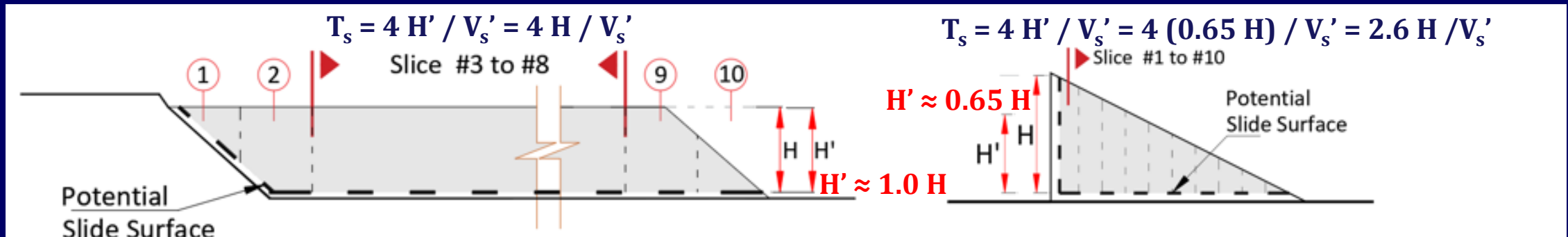
# Fundamental Period of Sliding Mass ( $T_s$ )

$$T_s = 4 H' / V_s'$$

$T_s$  = Initial Fundamental Period of Sliding Mass

$V_s'$  = Average Shear Wave Velocity of Sliding Mass ( $V_s' = \Sigma[(V_{si})(m_i)] / \Sigma(m_i)$ )

$H'$  = Effective Height of Sliding Mass ( $H' = (\text{mass-weighted-}T_s) V_s' / 4$ )



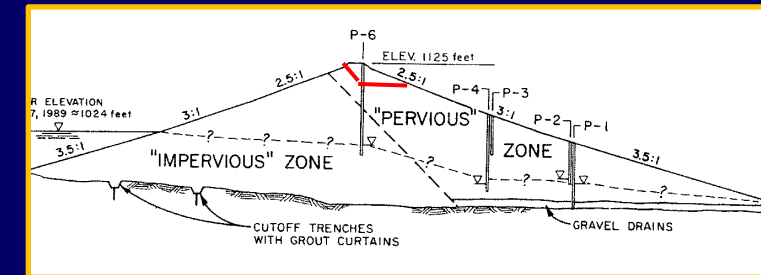
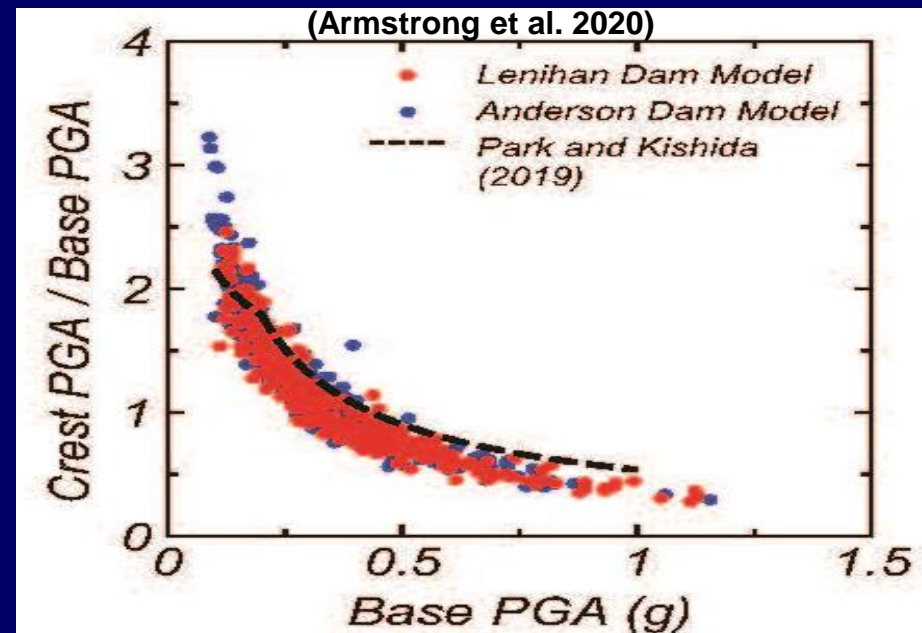
$H' \approx 0.65 H$  to  $1.0 H$  (Bray & Macedo 2021)



# Topographic Amplification of PGA for Shallow Sliding

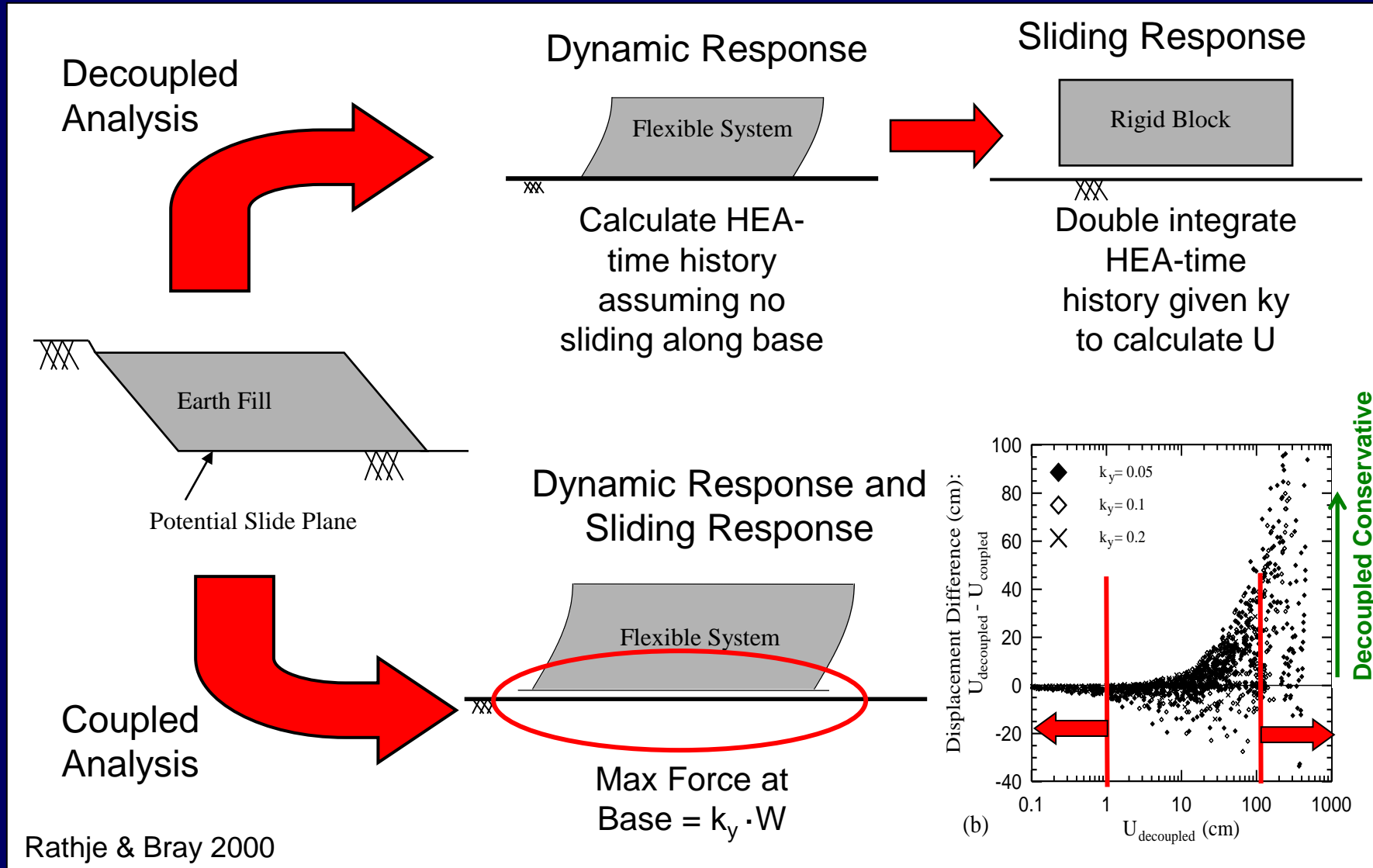
- Steep Slope (>60°):**  $PGA_{crest} \approx 1.5 PGA_{1D}$   
 (Ashford and Sitar 2002)
- Moderate Slope (<45°):**  $PGA_{crest} \approx 1.3 PGA_{1D}$   
 (Rathje and Bray 2001)
- Dam Crest:**  $PGA_{crest} \approx \exp(-0.62 + 0.254 \ln(PGA_{rock}))$   $PGA_{rock} > 0.2 g$   
 (Park & Kishida 2019)  $PGA_{crest} \approx \exp(0.147 + 0.731 \ln(PGA_{rock}))$   $PGA_{rock} \leq 0.2 g$

*In addition to  
1D Site Effects*



# d. Seismic Displacement Calculation

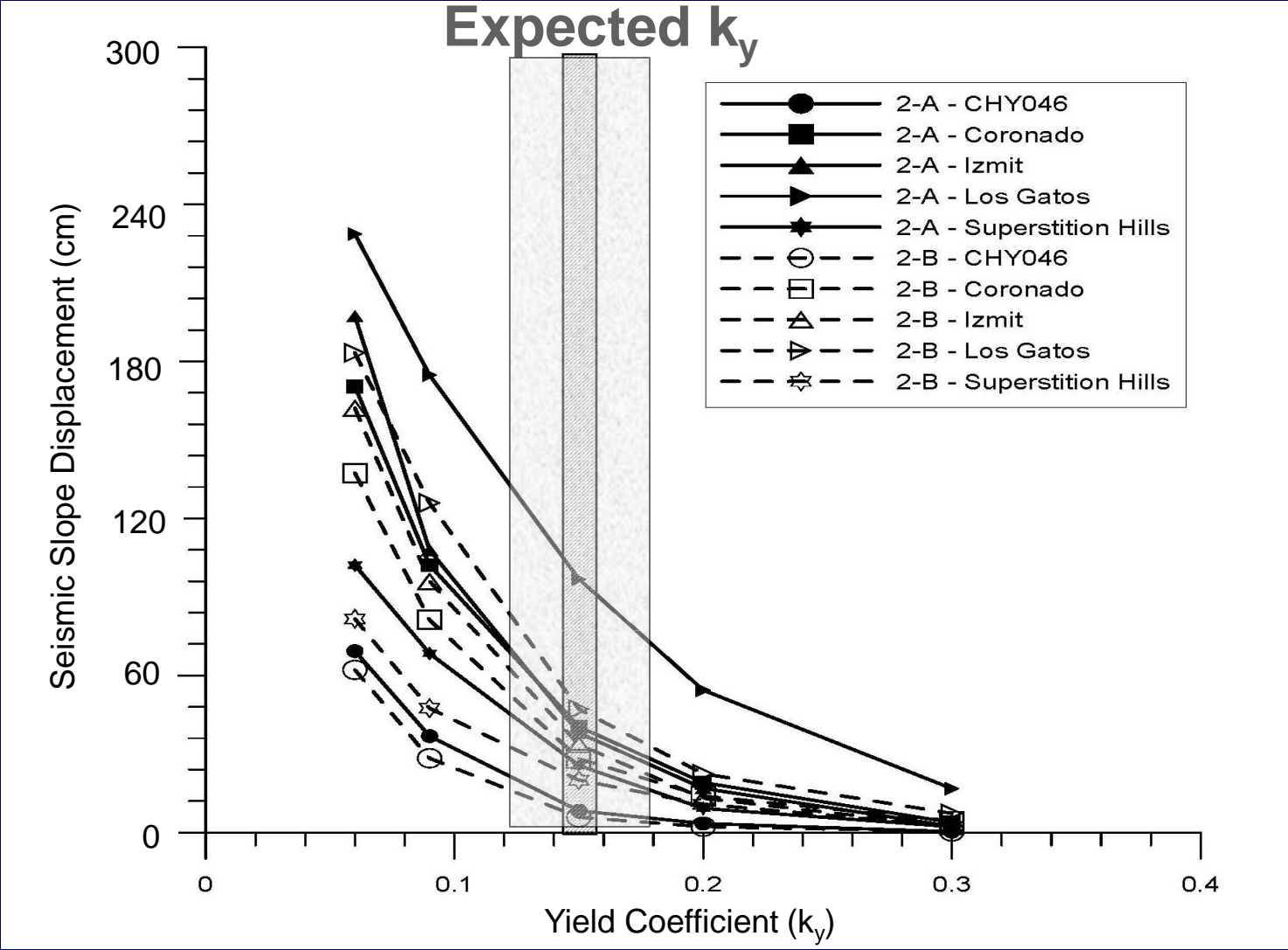
## Modified Newmark Sliding Block Analysis



$$FS_{\text{static}} > 1.0$$

$$k_y > 0$$

# Calculated Seismic Slope Displacement (D)

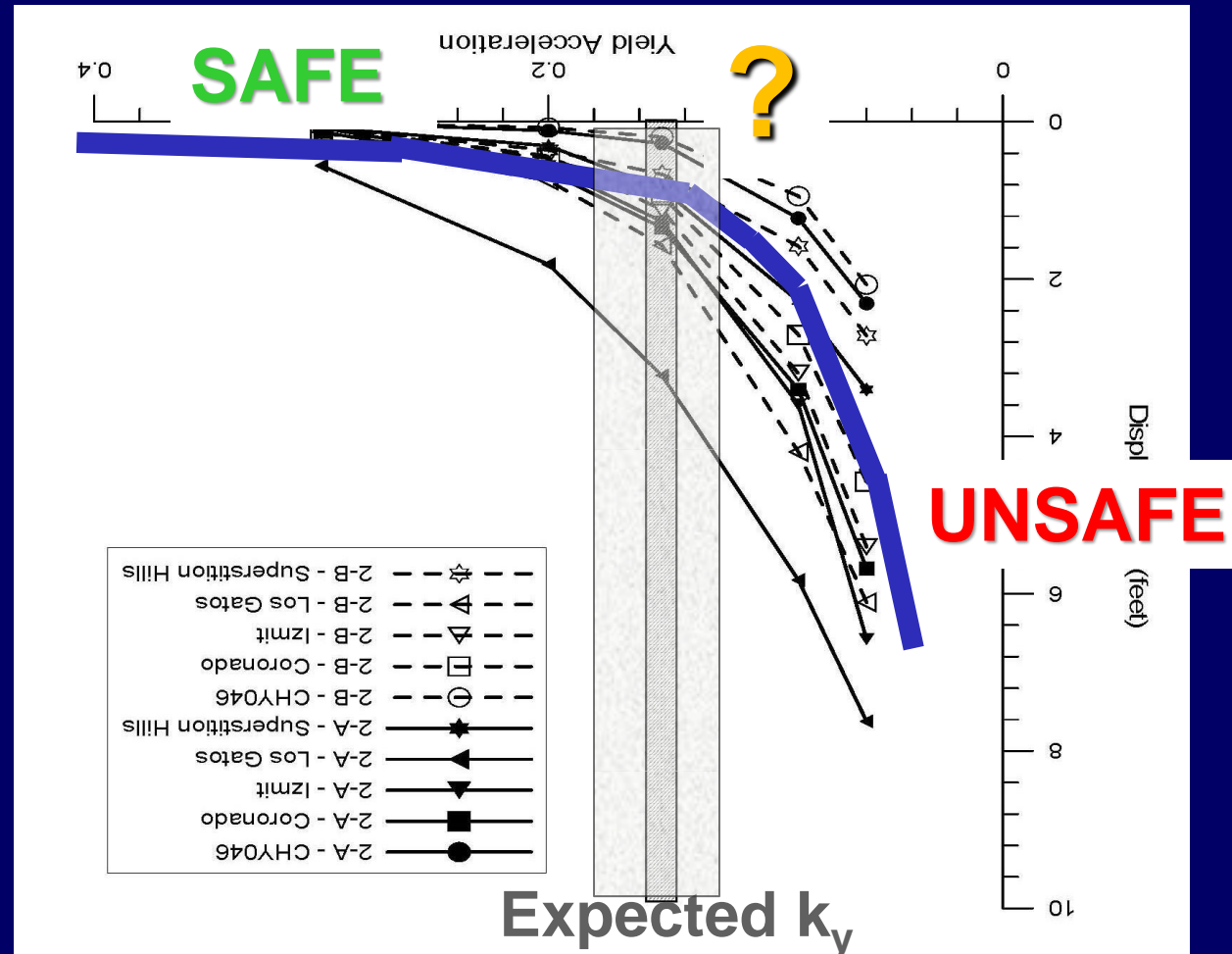


Use programs such as SLAMMER by Jibson et al. (2013)



# Think About It as a “Cliff”

Calculated Seismic Displacement is an *Index* of Performance



# Evaluate Seismic Performance

Given seismic displacement estimates:

- Minor (e.g.,  $D < 30$  cm)
- Major (e.g.,  $D > 1$  m)

Evaluate the ability of the tailings dam to accommodate the estimated level of deformation

Consider:

- Brittleness of materials
- Consequences of failure and conservatism of hazard assessment and stability analyses
- Defensive measures that provide redundancy, e.g., filters, chimney drain, more freeboard, wider crest

# Bray & Macedo (2019) Seismic Slope Procedure

update to Bray & Travasarou (2007) which was based on NGA-West-1

## 1. SLOPE MODEL

nonlinear soil response  
fully coupled deformable stick-slip  
stiffness ( $T_s$ ) & strength ( $k_y$ )  
13  $T_s$  values & 10  $k_y$  values

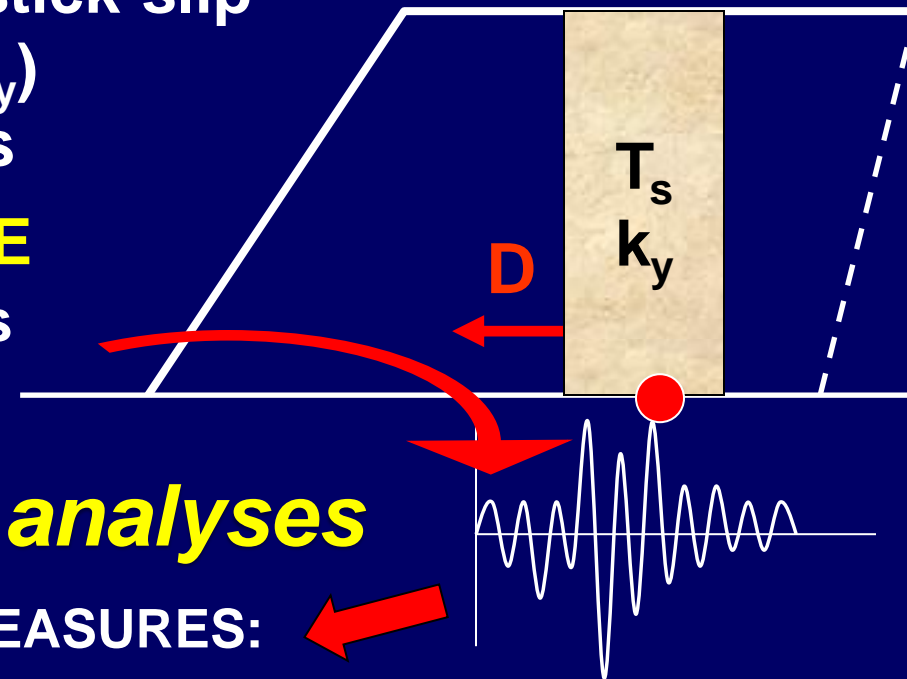
## 2. EARTHQUAKE DATABASE

6711 two-component records  
NGA-West-2: crustal EQs

**Nearly 3000000 analyses**

OPTIMAL INTENSITY MEASURES:

$S_a(1.3 T_s)$  &  $M_w$  of outcropping motion below slide



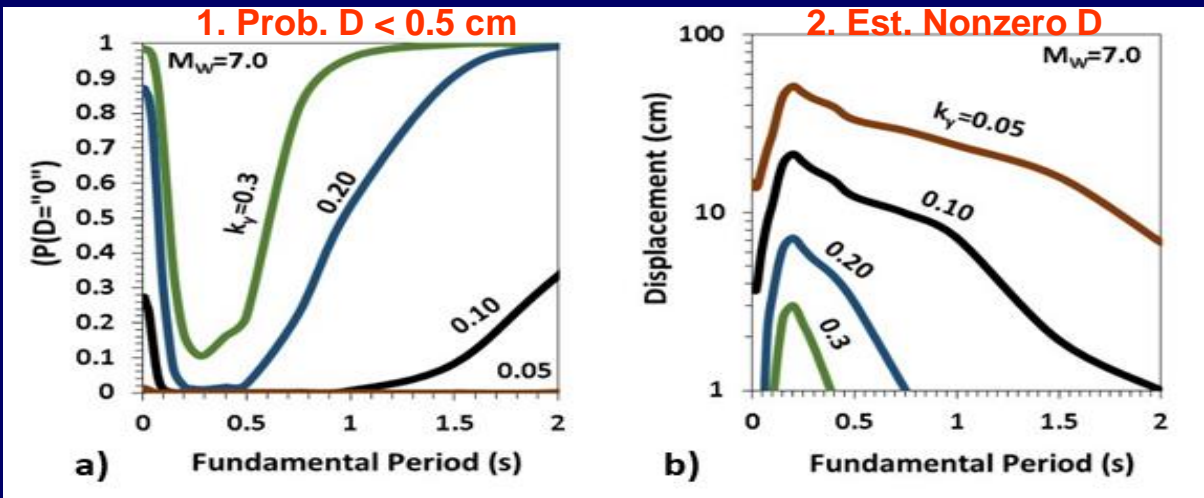
## 3. VALIDATION

13 case histories

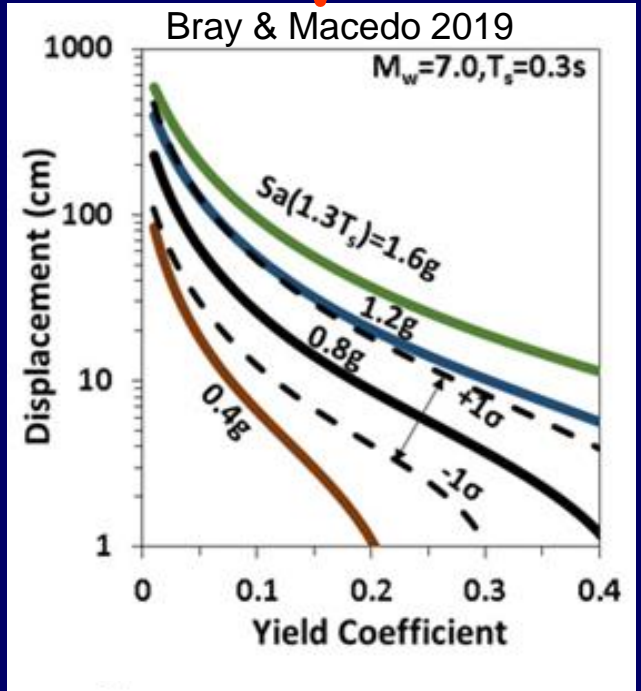


# Mixed Random Variable Approach

$$P(D_0 = '0') = f(k_y, S_a(1.3T_s), T_s)$$



$$D = f(k_y, S_a(1.3T_s), T_s, M_w) \pm \epsilon$$



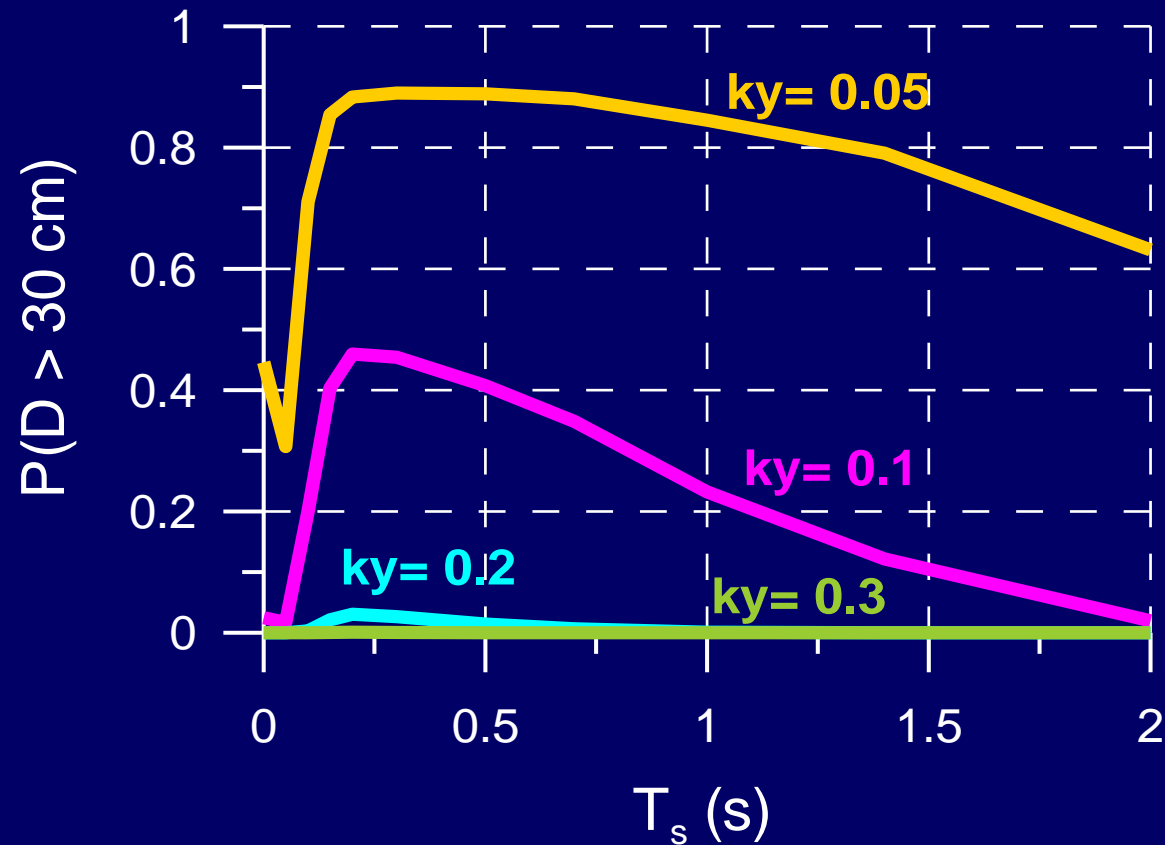
Use Spreadsheet:  
<https://ce.berkeley.edu/people/faculty/bray>

Case	OrdinaryGM (EQ2&3)	Select Ordinary or Pulse or Combined Equations	Dependence on $k_y$
8	Yield Coefficient ( $k_y$ ) <sup>16</sup>	0.10	$k_y$
9	Initial Fundamental Period ( $T_1$ ) <sup>16</sup>	0.50	seconds
10	Degraded Period ( $1.3T_1$ )	0.65	seconds
11	Moment Magnitude ( $M_w$ )	7.0	
12	Spectral Acceleration ( $S_a(1.3T_1)$ ) <sup>16</sup>	0.70	g
13	PGV Information	PGV is not used in this case, enter 1 below	
14	Peak Ground Velocity (PGV) <sup>16</sup>	1.0	cm/s
15	Percentile (if Pulse ground Motion) <sup>16</sup>	No Pulse	

	$P(D=0)$	$D$ (cm)	$D_{median}$ (cm)	$D_{-84\%}$ (cm)	$D_{-16\%}$ (cm)
17	0.00	0.000	166.4	340.5	81.3
18	0.00	0.000	71.7	71.7	35.0
19	0.00	0.000	47.5	47.5	23.2
20	0.00	0.000	28.9	28.9	14.4
21	0.00	0.001	15.2	15.2	7.4
22	0.00	0.008	9.2	9.1	4.4
23	0.00	0.112	4.2	3.8	1.3
24	0.00	0.371	2.3	1.28	0.5

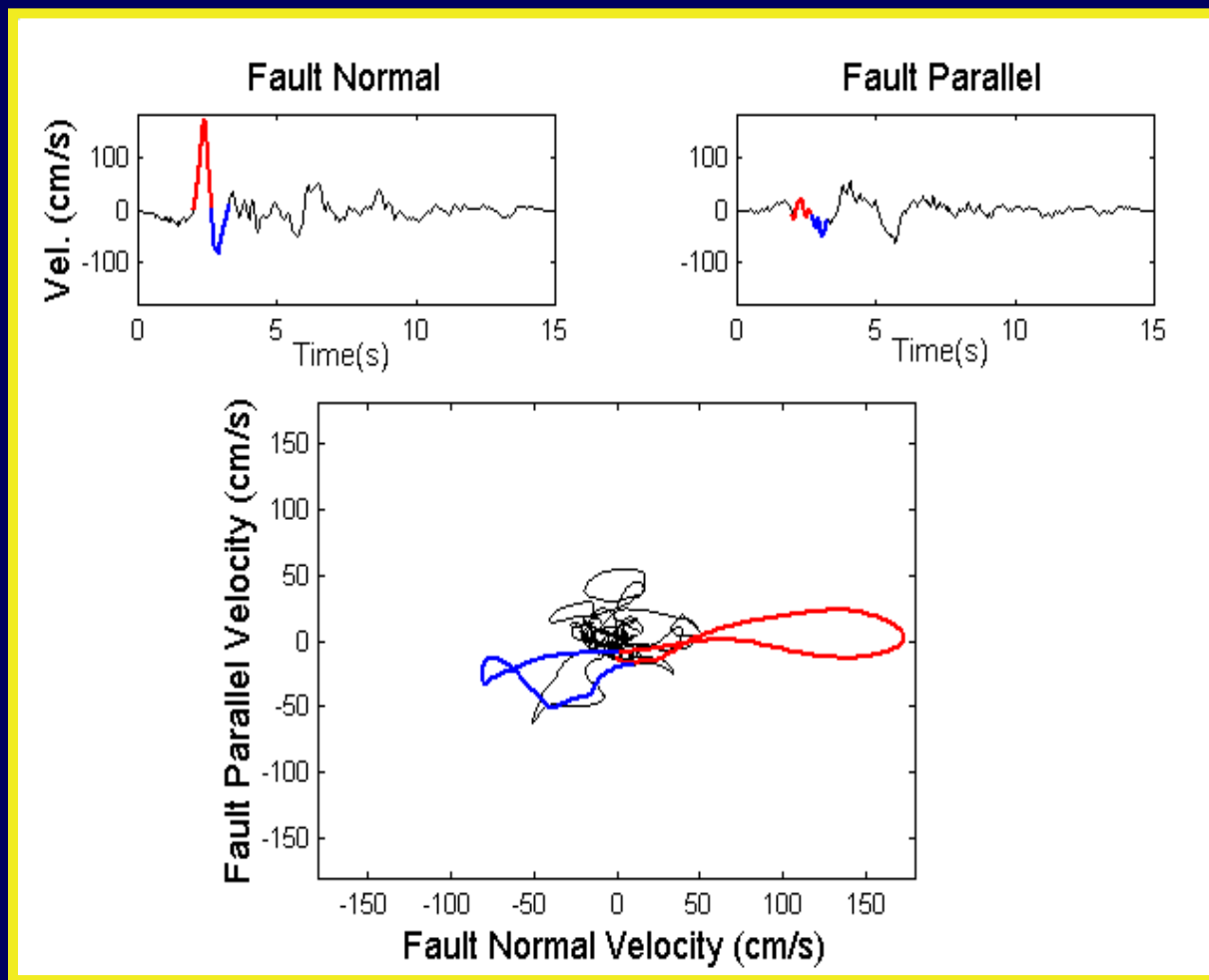
# PROBABILITY OF EXCEEDANCE OF DISPLACEMENT THRESHOLD



Scenario Event: M 7 at 10 km "Soil" – SS fault

# Forward-Directivity Fault-Normal & Fault-Parallel Velocity Pulses

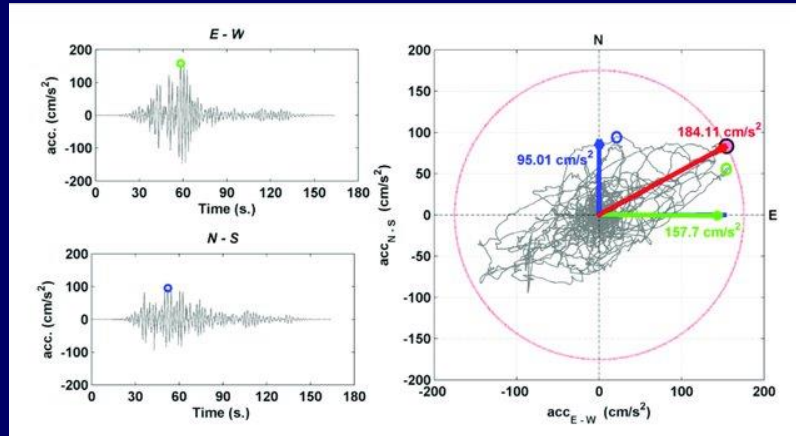
Rinaldi Receiving Station (1994 Northridge EQ)





# Bray & Macedo (2019) Near-Fault Pulse Model

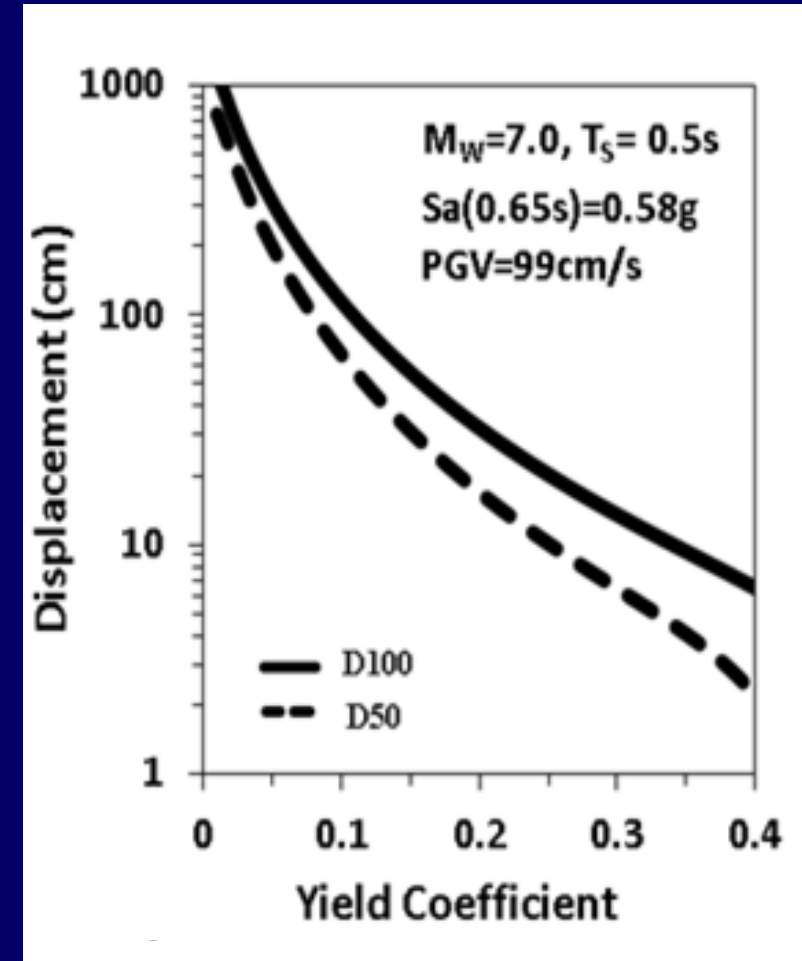
$$D = f(k_y, S_a(1.3T_s), T_s, M_W, PGV)$$



**D100: Max D Component**

**D50: Median D Component**

Horz. components of each near-fault recording rotated in 1° increments to calculate D100 & D50



**Use D100 for Fault-Normal & D50 for Fault-Parallel Orientations**

# Validation of Bray & Macedo (2019) Simplified Procedure

System	EQ	Obs. $D_{max}$ (cm)	<u>Bray &amp; Macedo 2019</u>	
			P (D = "0")	Est. Disp (cm)
Guadalupe LF	LP	Minor	0.96	0
Pacheco Pass LF	LP	None	1.0	0
Austrian Dam	LP*	50	0.0	33 - 98
Lexington Dam	LP*	15	0.0	22 - 65
Chiquita Canyon D LF	NR*	30	0.0	15 - 44
Sunshine Canyon LF	NR*	30	0.0	17- 50

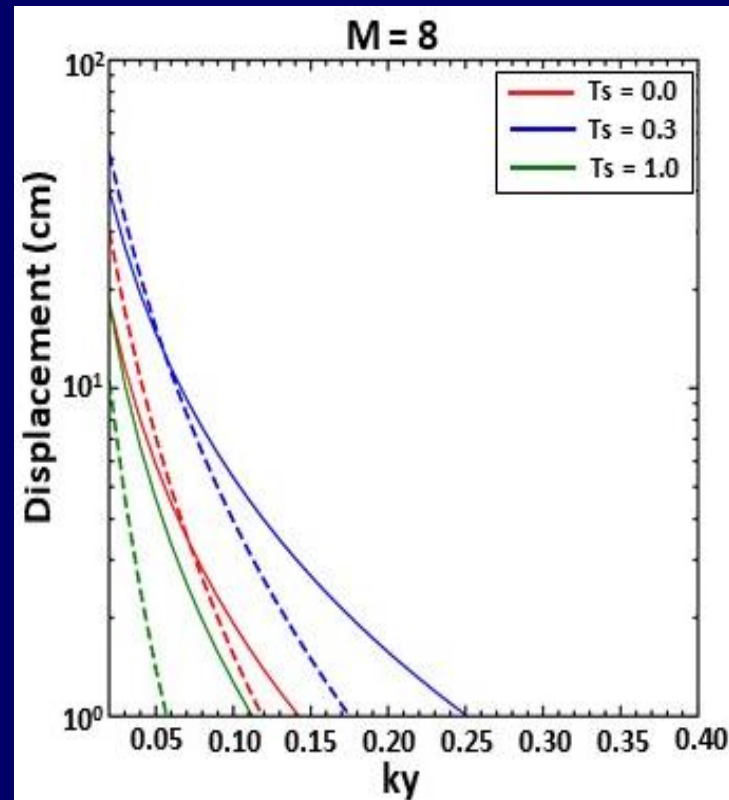
\*Denotes Pulse Motion

**Bray & Macedo (2019) used 13 well documented case histories in validation**

# Subduction Zone Earthquakes

*Macedo et al. (2023)*

- 6240 Interface Subduction Zone EQ Two-Component Recordings ( $M_w$  from 4.8 to 9.1)  
*Bray et al. (2018) used 810 two-component recordings ( $M_w$  from 7.0 to 9.1)*
- 8299 Intraslab Subduction Zone EQ Two-Component Recordings ( $M_w$  from 4.0 to 7.8)

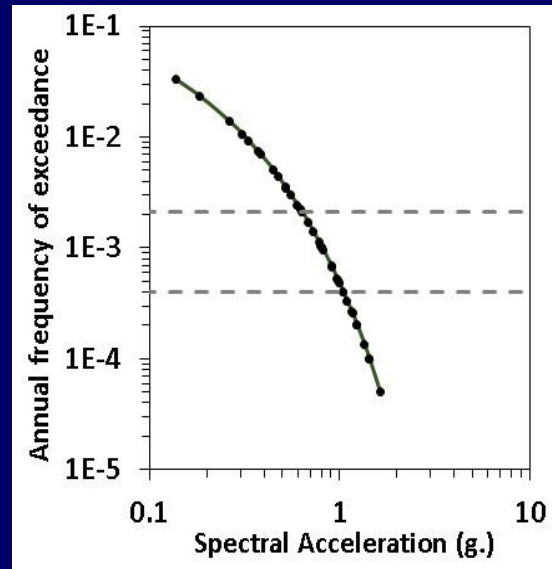


Solid Lines: Intraslab EQ Model

Dashed Lines: Interface EQ Model

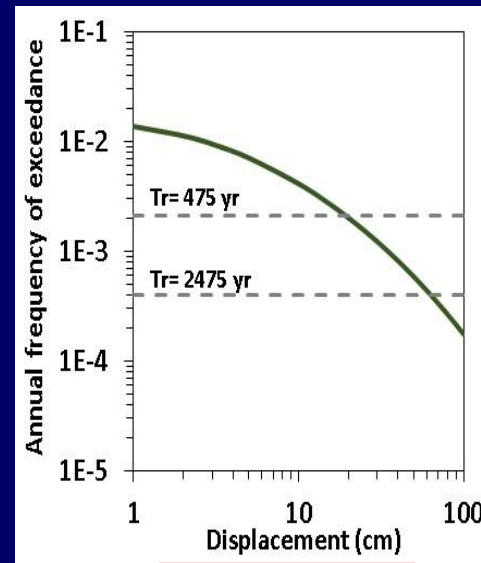
Ground motions processed uniformly  
(PEER NGA-Sub Database, Bozorgnia & Stewart 2020)

# Performance-Based Probabilistic Approach



$$D = f(k_y S_a T_s M_w)$$

- *Include variability of  $S_a$  &  $D$*
- *Include variability of  $k_y$  &  $T_s$*



Mean Seismic  
Slope Displacement  
Hazard Curve



# Capture Epistemic Uncertainty

Fault 1:

Magnitude pdf: delta function at M

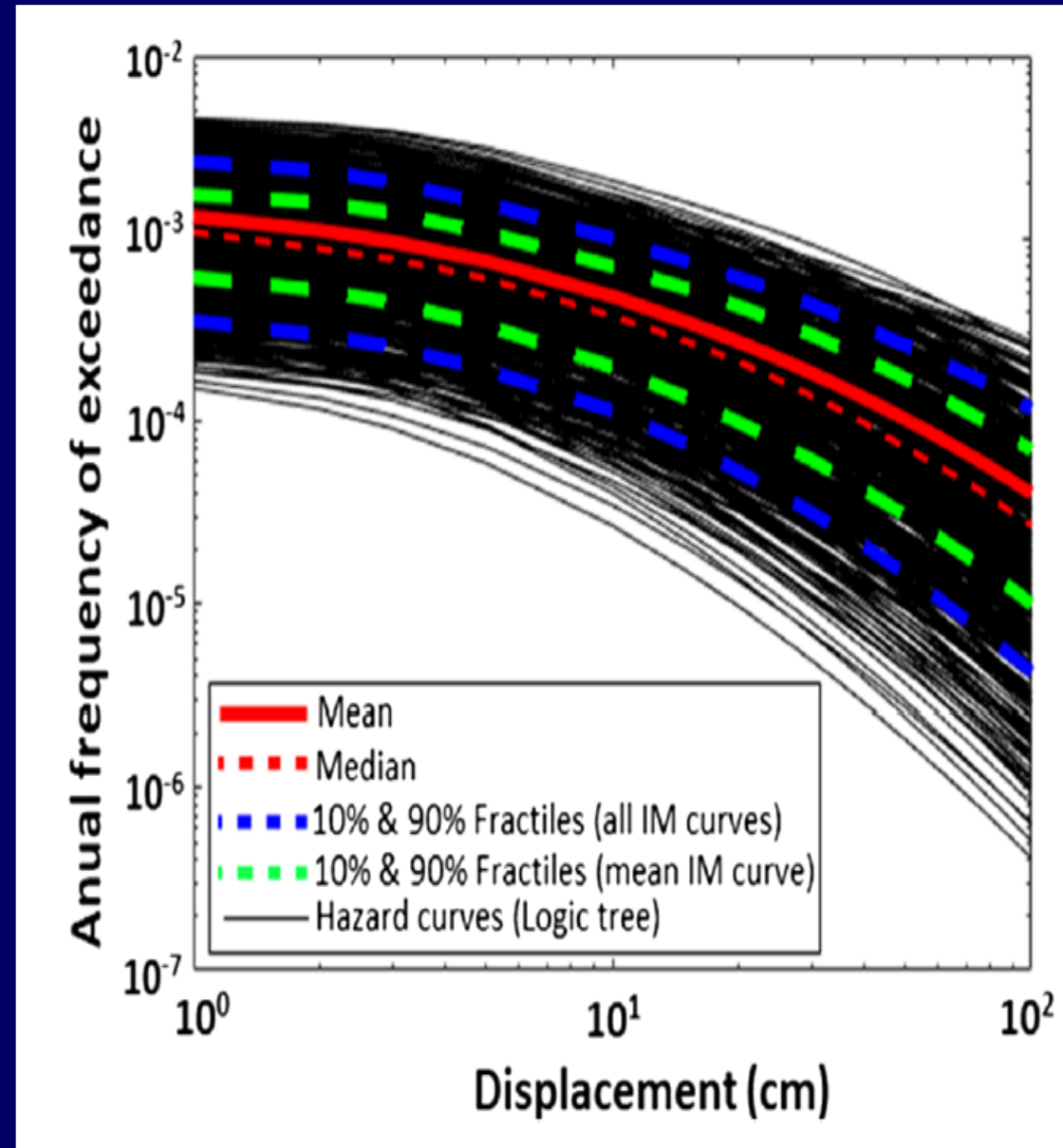
Distance pdf (rupture location): delta function at 30 km

FLT 1:

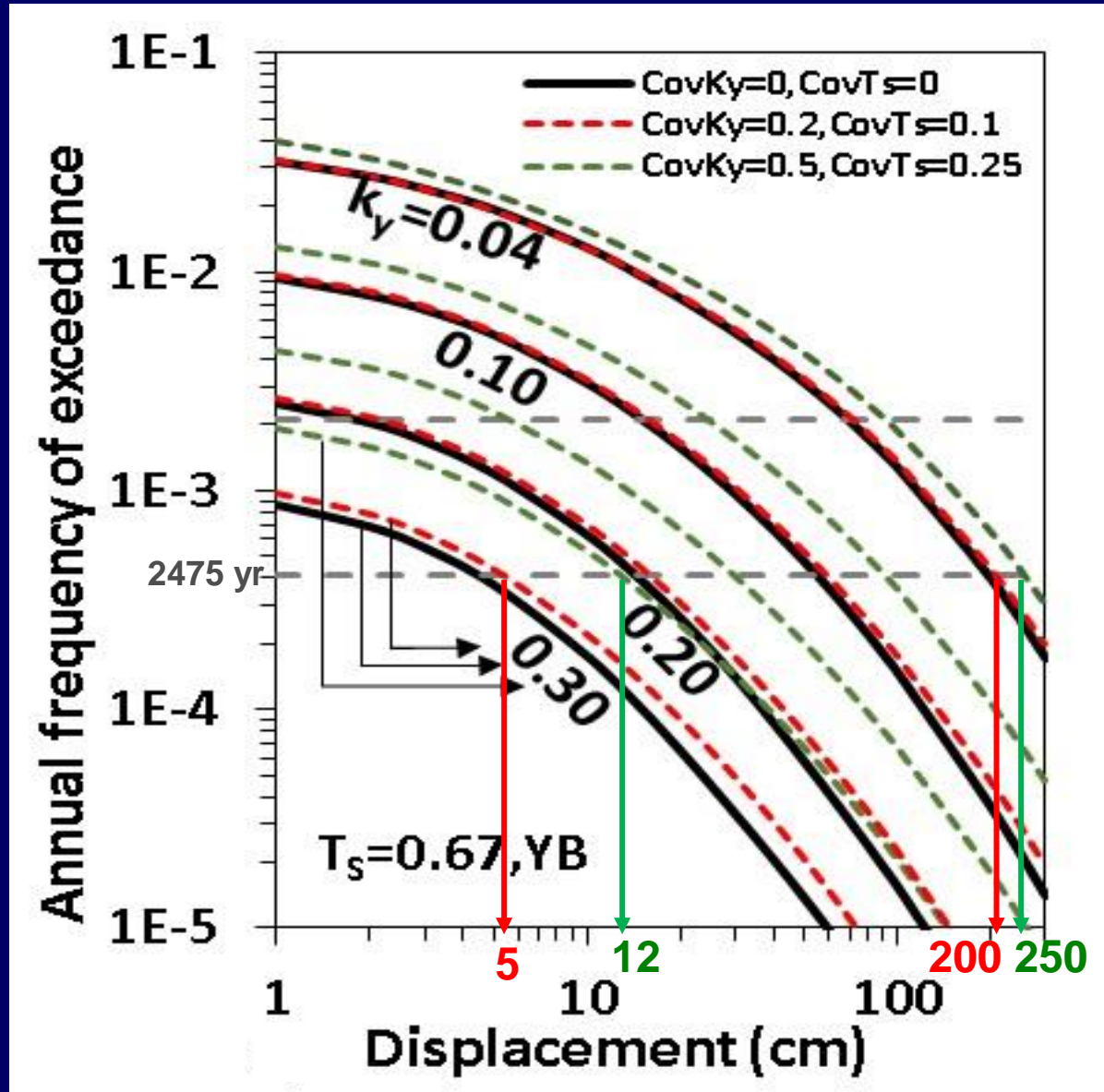


Weighting factor GMPE1: 0.6, GMPE2: 0.4

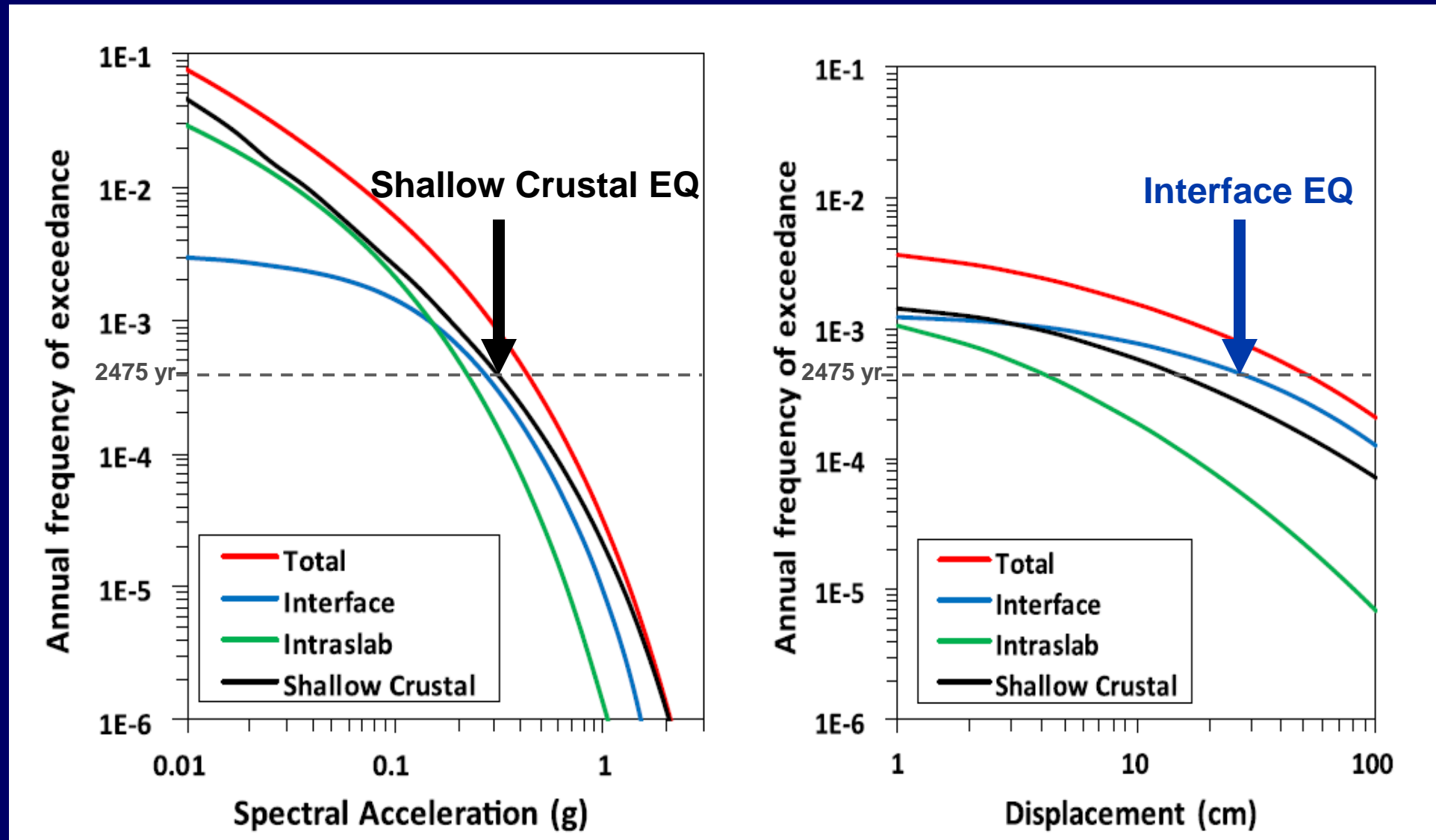
**Logic Trees for:**  
**M, R, Rate, GMMs &**  
 **$k_y$ ,  $T_s$ , D-models**



# Comparison of Variability due to $k_y$ & $T_s$



# Contributions of Different Tectonic Settings (Seattle Site)



# Summary

- **First focus on severe strength loss potential: Flow Liquefaction**
- **Clayey Silt can liquefy - perform monotonic & cyclic tests**
- **Consider depositional environment (Fabric)**
- **Estimate  $S_r$  from back-analyses of flow slides - a system property**
- **Deformable sliding block displacement procedure provides useful insights when  $FS_{\text{static}} > 1$ ; follow with FDA on high-risk dams**
- **Use Bray & Macedo (2019) for Shallow Crustal EQs and Macedo et al. (2023) for Interface & Intraslab Subduction Zone EQs**
- **PBEE seismic slope displacement approach captures uncertainty**



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