

# 1<sup>st</sup> Memorial Gerald A. Leonards Lecture

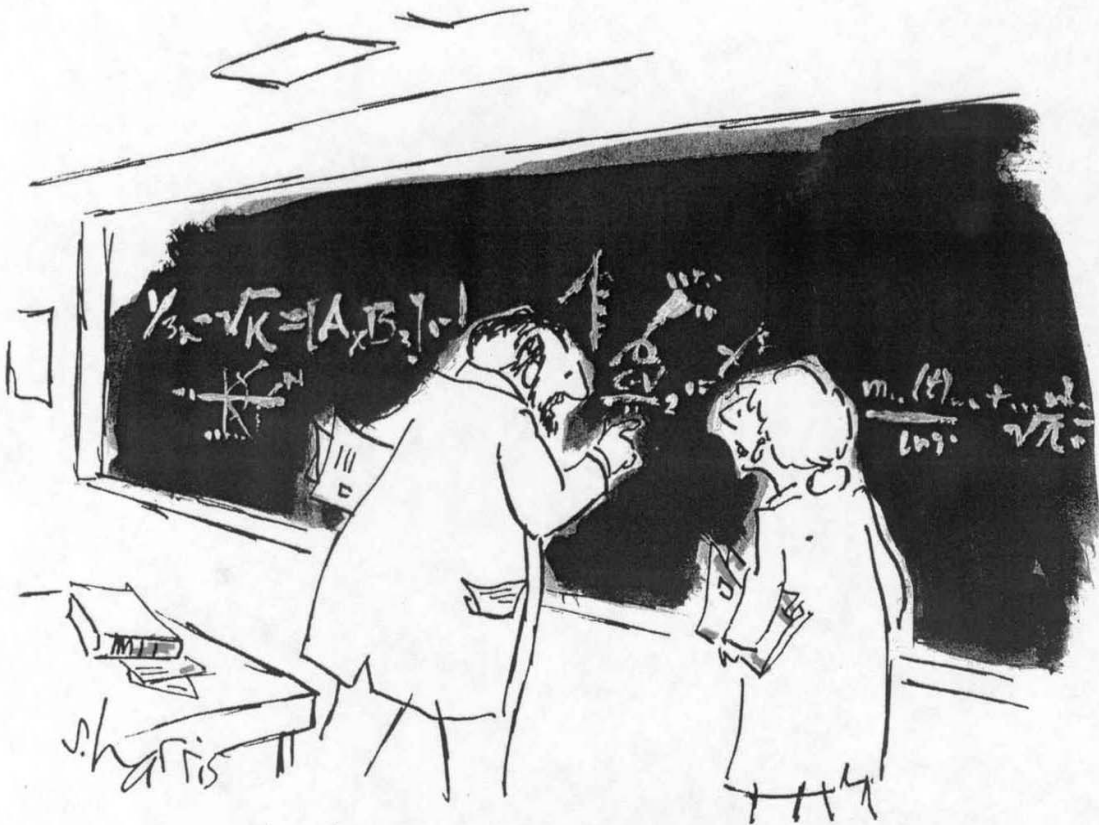
## *"The Fountain"*

by

**Professor Emeritus Milton Harr**

School of Civil Engineering  
Purdue University

May 22, 2003



**“AT THIS POINT, THE  
SHORT ATTENTION  
SPANS DROP OUT.”**

-COURTESY UMR ENGINEER & OTHERS-

1. ACTON'S LAW: Power tends to corrupt; absolute power corrupts absolutely.
2. ALBRECHT'S LAW: Social innovations tend to the level of minimum tolerable well-being.
3. ALLEN'S AXIOM: When all else fails, read the instructions.
4. BOWIE'S THEOREM: If an experiment works you must be using the wrong equipment.
- U.B. → 5. CARLSON'S CONSOLATION: Nothing is ever a complete failure; it can always serve as a bad example.
6. CLARKE'S THIRD LAW: Any sufficiently advanced technology is indistinguishable from magic.
7. COHN'S LAW: The more time you spend in reporting on what you are doing the less time you have to do anything. Stability is achieved when you spend all your time reporting on the nothing you are doing.
8. CORRESPONDENCE COROLARY: An experiment may be considered a success if no more than half your data must be discarded to obtain correspondence with your theory.
9. CROPP'S LAW: The amount of work done varies inversely with the amount of time spent in the office.
10. CUTLER WEBSTER'S LAW: There are two sides to every argument, unless a person is personally involved, in which case there is only one.
11. DOW'S LAW: In a hierarchical organization, the higher the level, the greater the confusion.
12. FINAGLE'S LAWS:
  - (1) Once a job is fouled up, anything done to improve it makes it worse.
  - (2) No matter what results are expected someone is always willing to fake it.
  - (3) No matter what the result someone is always eager to misinterpret it.
  - (4) No matter what occurs, someone believes it happened according to his pet theory.
13. GUMPERSON'S LAW: The probability of a given event occurring is inversely proportional to its desirability.
14. GOVERNMENT'S LAW: There is an exception to all laws.
15. HARVARD LAW: Under the most carefully controlled conditions of pressure, temperature, volume, humidity, and other variables, the organism will do as it damn well pleases.
16. HUEBARD'S LAW: Don't take life too seriously; you won't get out of it alive.
17. JERKINSON'S LAW: It won't work.
18. LARKINSON'S LAW: All laws are basically false.
19. LAW OF CONTINUITY: Experiments should be reproducible. They should all fail the same way.

20. LAW OF THE PERVERSITY OF NATURE: You cannot determine beforehand which side of the bread to butter.

21. LAW OF THE TOO SOLID GOOF: In any collection of data, the figures that are obviously correct beyond all need of checking, contain the errors.

corollary 1: No one you ask for help will see the error either.

corollary 2: Any nagging intruder, who stops by with unsought advice will spot it immediately.

22. MAY'S LAW: The quality of correlation is inversely proportional to the density of control. (The fewer the data points, the smoother the curves.)

23. MENCKEN'S LAW: There is always an easy answer to every human problem - neat, plausible, and wrong.

24. MURPHY'S LAWS:

(1) In any field of scientific endeavor, anything that can go wrong, will go wrong.

(2) Left to themselves, things always go from bad to worse.

(3) If there is a possibility of several things going wrong, the one that will go wrong, is the one that will do the most damage.

(4) Nothing is as easy as it looks.

(5) Everything takes longer than you think it will.

(6) If everything seems to be going well, you have obviously overlooked something.

(7) Nature always sides with the hidden flaw.

25. PARKINSON'S LAW: Work expands to fill the time available for its completion.

26. PARKINSON'S LAW, MODIFIED: The junk you have will expand to fill the available space.

27. PETER'S PRINCIPLE: In every hierarchy, each employee tends to rise to the level of his incompetence.

28. PUDDER'S LAW: Anything that begins well will end badly. (note: The converse of Pudder's law is not true.)

29. RUDIN'S LAW: In a crises that forces a choice to be made among alternative courses of action, people tend to choose the worst possible course.

30. RYAN'S LAW: Make three correct guesses consecutively and you will establish yourself as an expert.

31. SATTLINGER'S LAW: It works better if you plug it in.

32. THYME'S LAW: Everything goes wrong at once.

33. UNNAMED LAW: If it happens, it must be possible.

34. WEILER'S LAW: Nothing is impossible for the man who doesn't have to do the work.

35. WHITEHEAD'S LAW: The obvious answer is always overlooked.

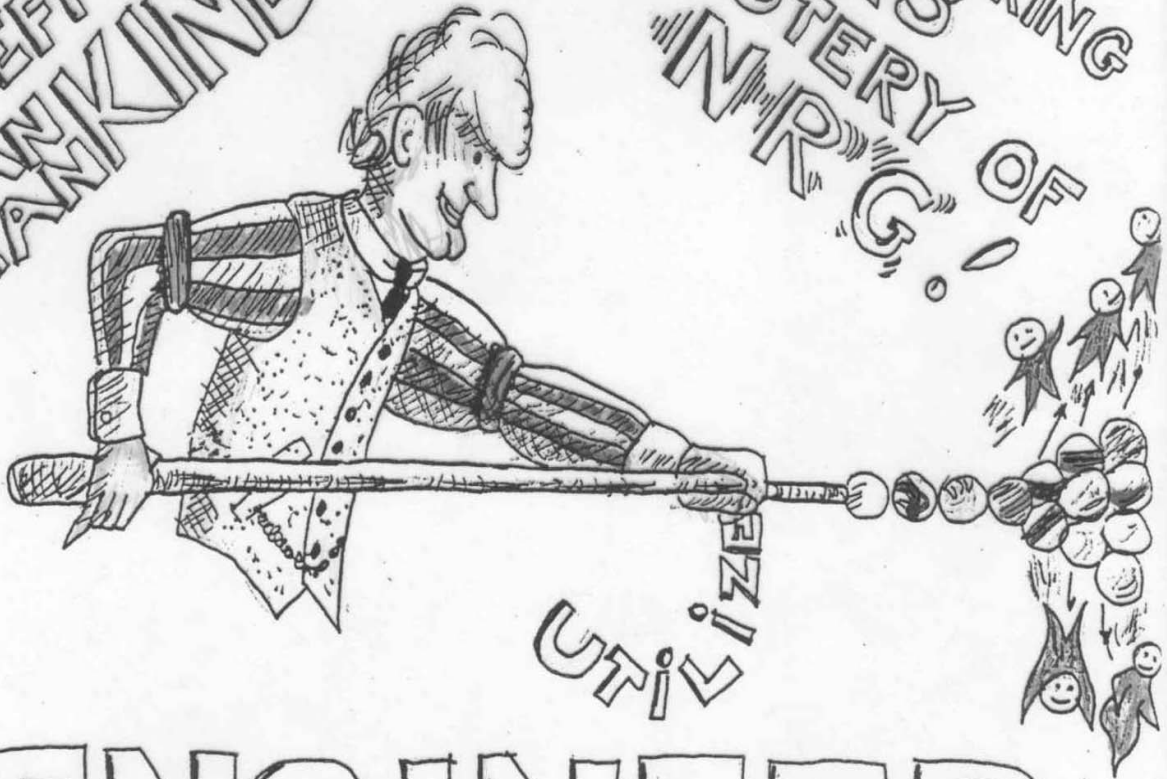
36. WILCOX'S LAW: A pat on the back is only a few centimeters from a kick in the pants.

37. WOODWARD'S LAW: A theory is better than its explanation.



BENEFIT  
MANKIND  
WOMANKIND

ENGINEERING  
SEEKS  
MASTERY OF  
NRG!



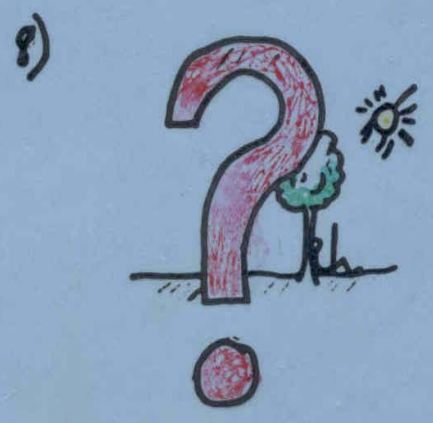
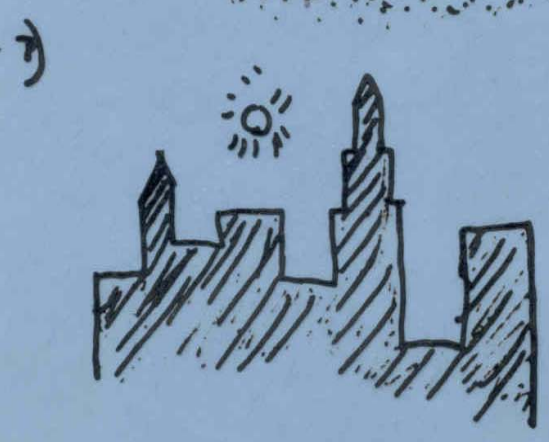
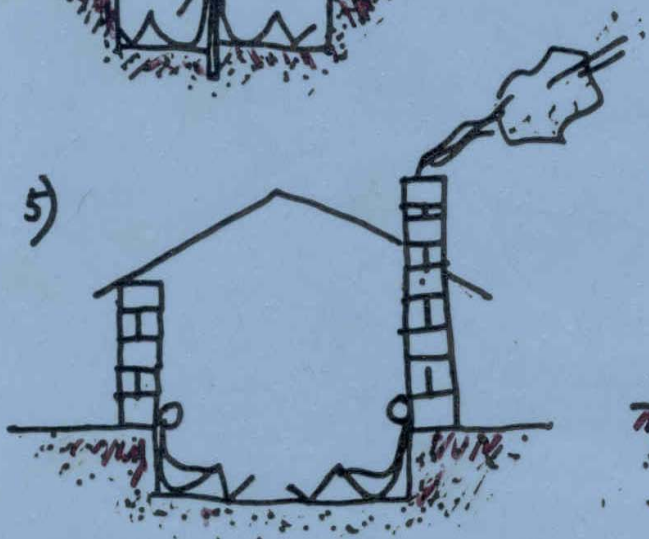
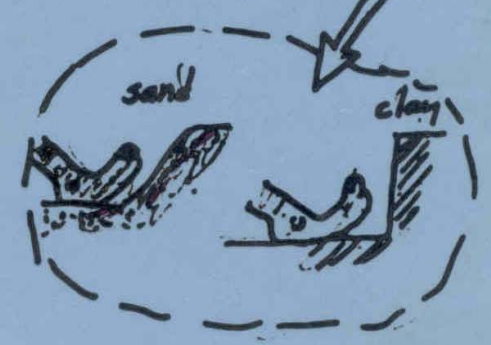
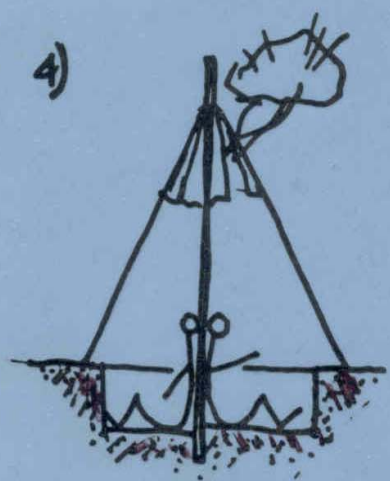
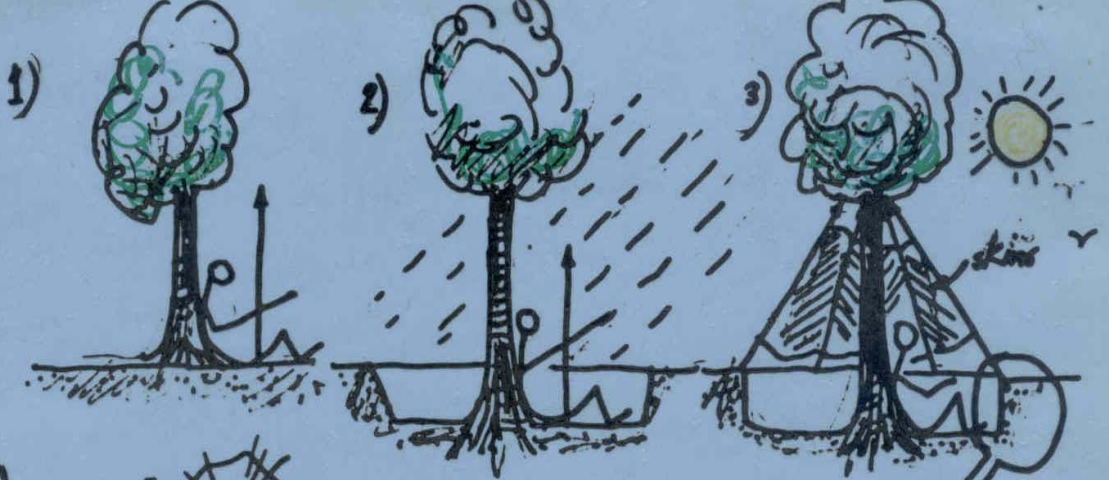
ENGINEERS  
CONTROL  
ENERGY

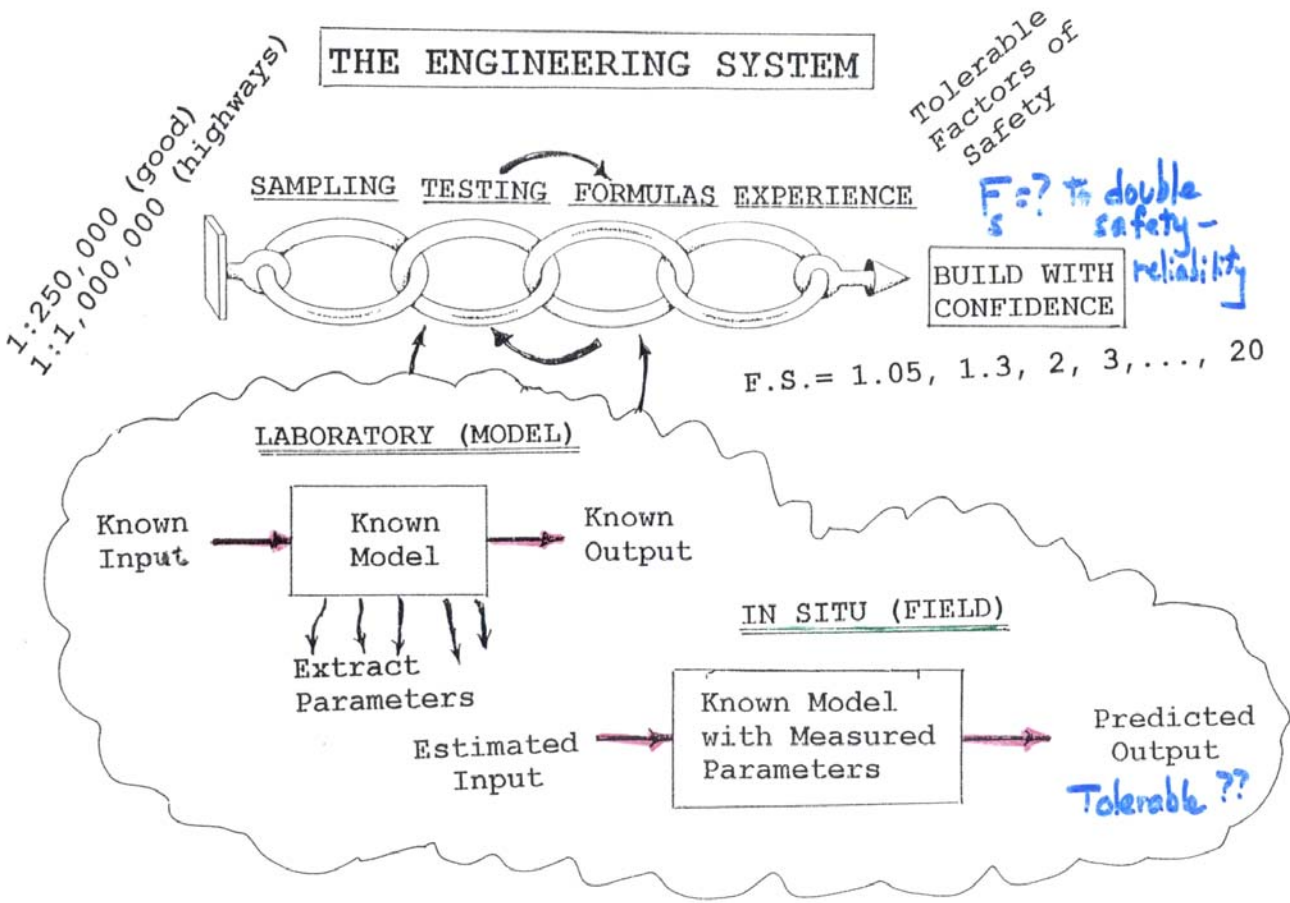
HARNESSES

ENGINEERING

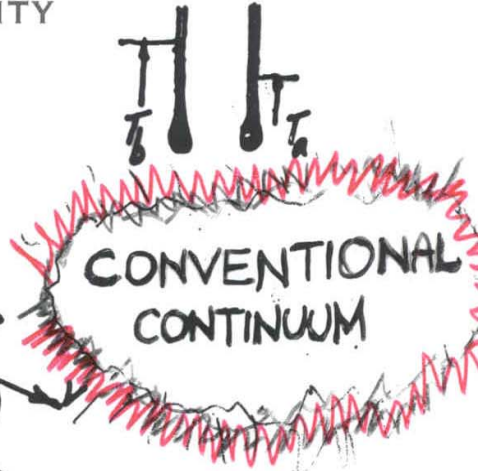
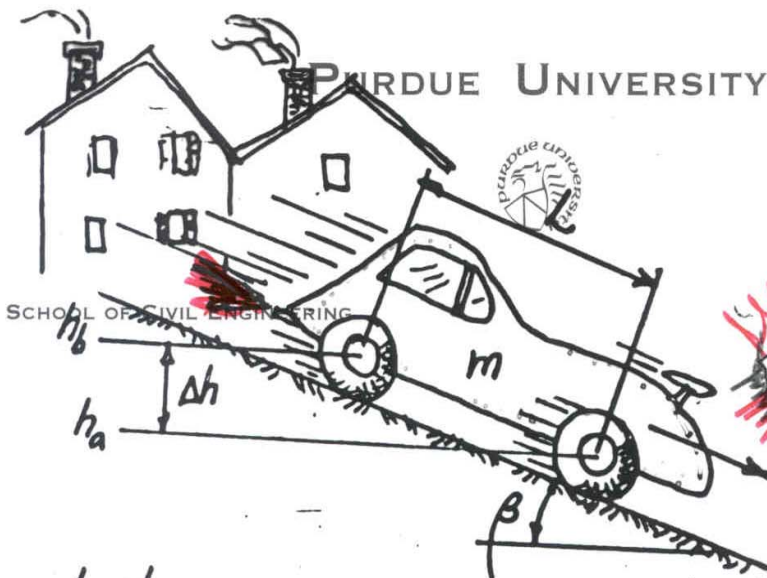
HOW WAS KNOWLEDGE ACQUIRED???

From observing successes and building one  
brick higher.









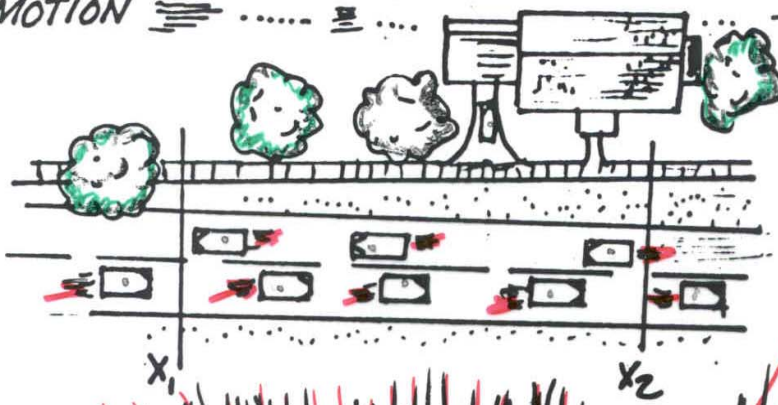
(A)

- velocity ..... gradient;  $v \propto (h_b - h_a)$
  - current ..... voltage drop;  $i \propto (V_b - V_a)$
  - heat flow ..... difference in temperature;  $q \propto (T_b - T_a)$
  - flow rate ..... pressure difference;  $w \propto (P_b - P_a)$
  - force ..... change in velocity;  $F \propto (V_b - V_a)$
- PROPORTIONAL TO**

MOTION

CHANGE IN ENERGY!!!

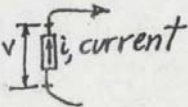

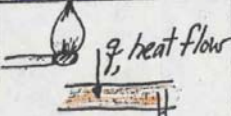
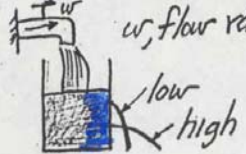
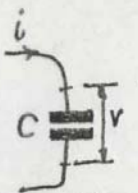



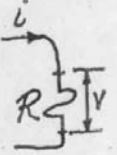
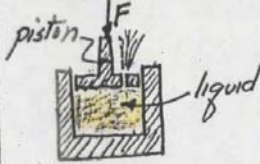

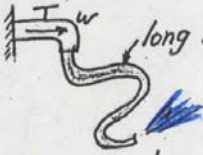
(B)



**LAW OF CONSERVATION OF CARS**

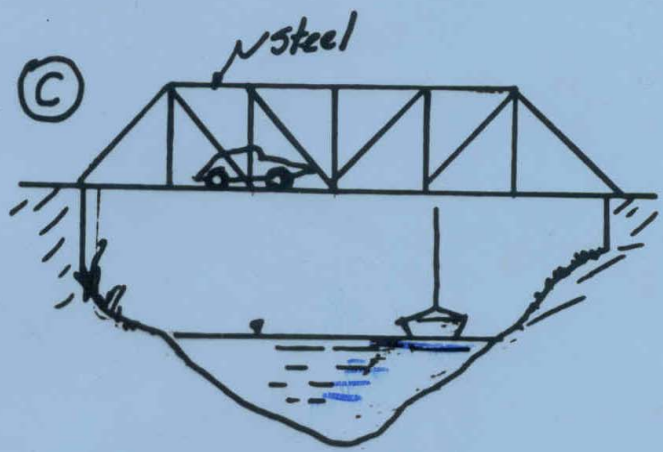
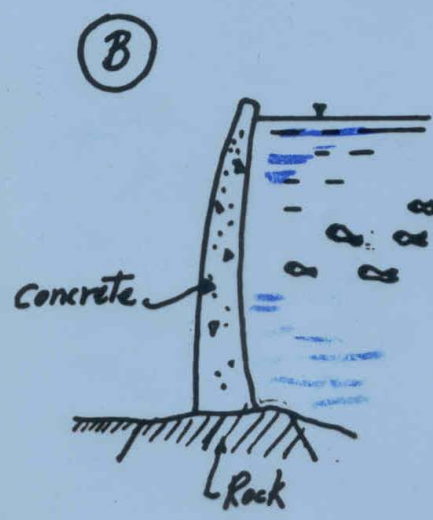
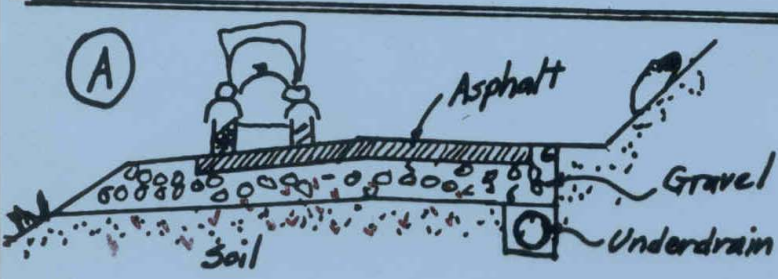
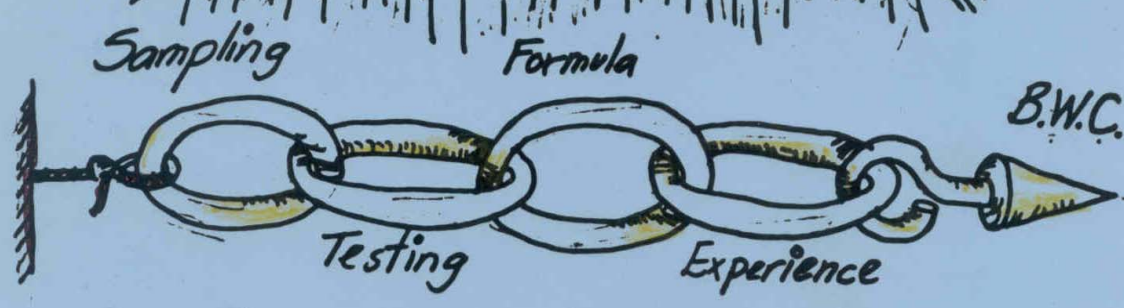
The net change in the number of vehicles on the section of highway between  $x_1$  and  $x_2$ , during any time interval, is the difference between the number entering and leaving that section!!!

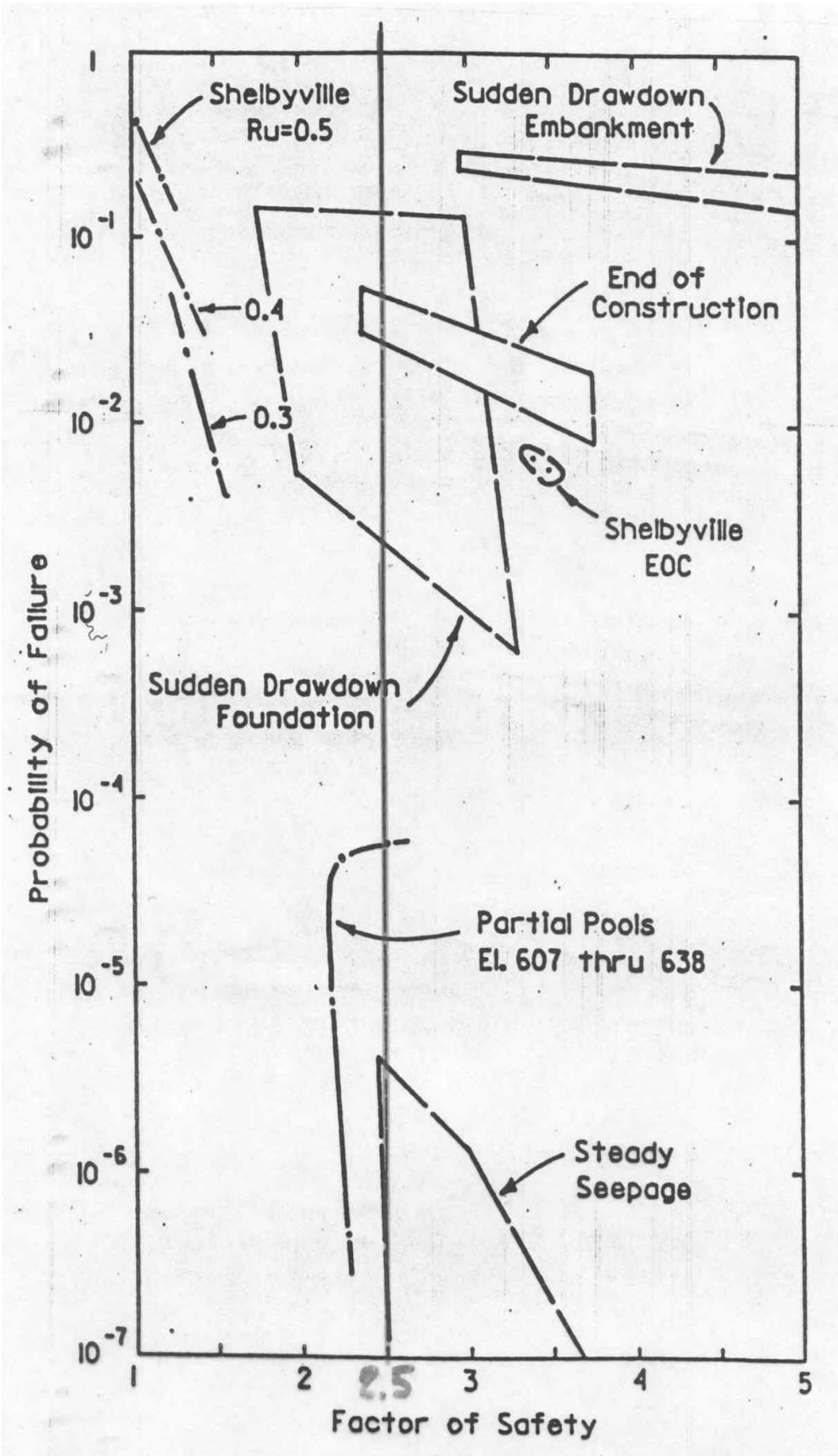


Electrical	Mechanical	Thermal	Fluid
 <p><math>v</math>, <math>V</math>, <u>Voltage drop</u></p>	 <p><math>F</math>, force <math>v = D/t</math>, <u>Velocity</u></p>	 <p><math>q</math>, heat flow <u>Temperature</u>, <math>T</math></p>	 <p><math>w</math>, flow rate low high <u>pressure</u>, <math>p</math></p>
 <p><u>capacitor</u></p>	 <p><math>m</math>, <u>Mass</u></p>	 <p><u>Heat capacity</u></p>	 <p><u>Liquid storage</u></p>
 <p><u>Resistor</u></p>	 <p><u>Damper</u></p>	 <p><u>Heat resistance</u></p>	 <p><u>Liquid resistance</u></p>
ohm's law	Newton's law	Fourier's law	Darcy's law

AT A POINT!

# THE SYSTEM

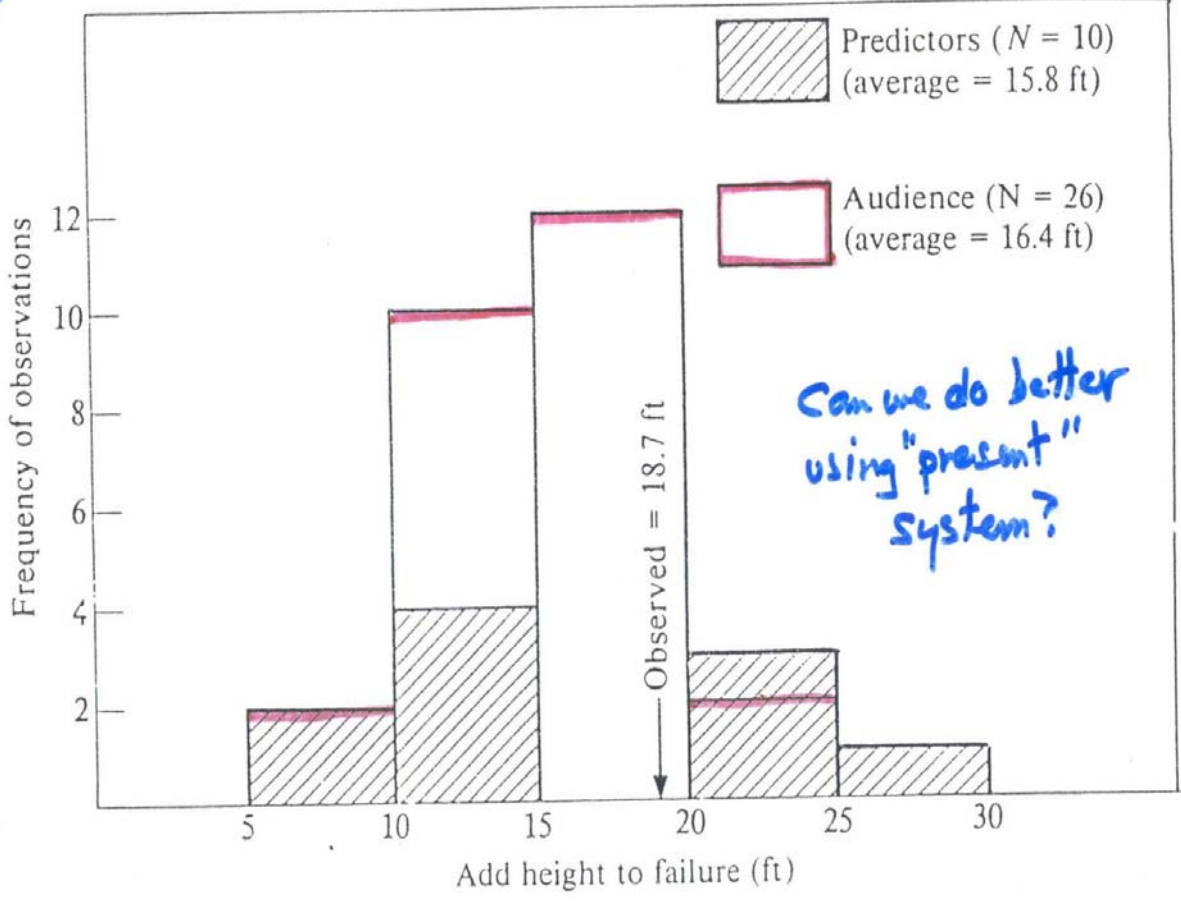


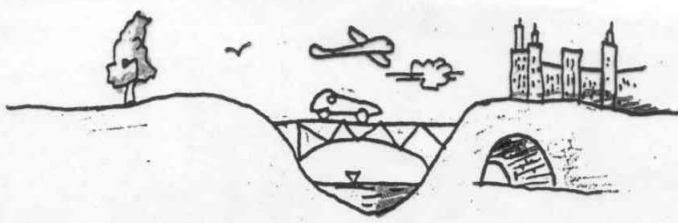




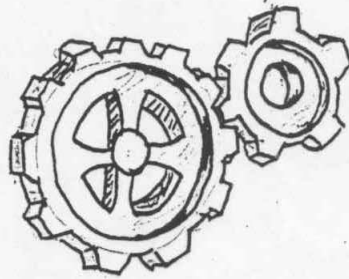
MIT 1974

# Predictions vs. Design?





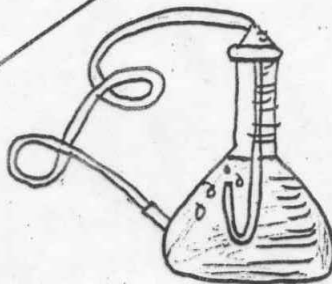
H.T.P.T.P.O.T.N.Y.D.



OPTIMIZE



\$ SAFETY ?



FOOTPRINTS IN THE SAND

**BUILD**

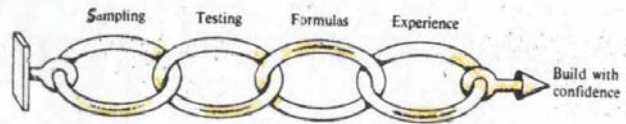
**WITH**

**CONFIDENCE**

VS

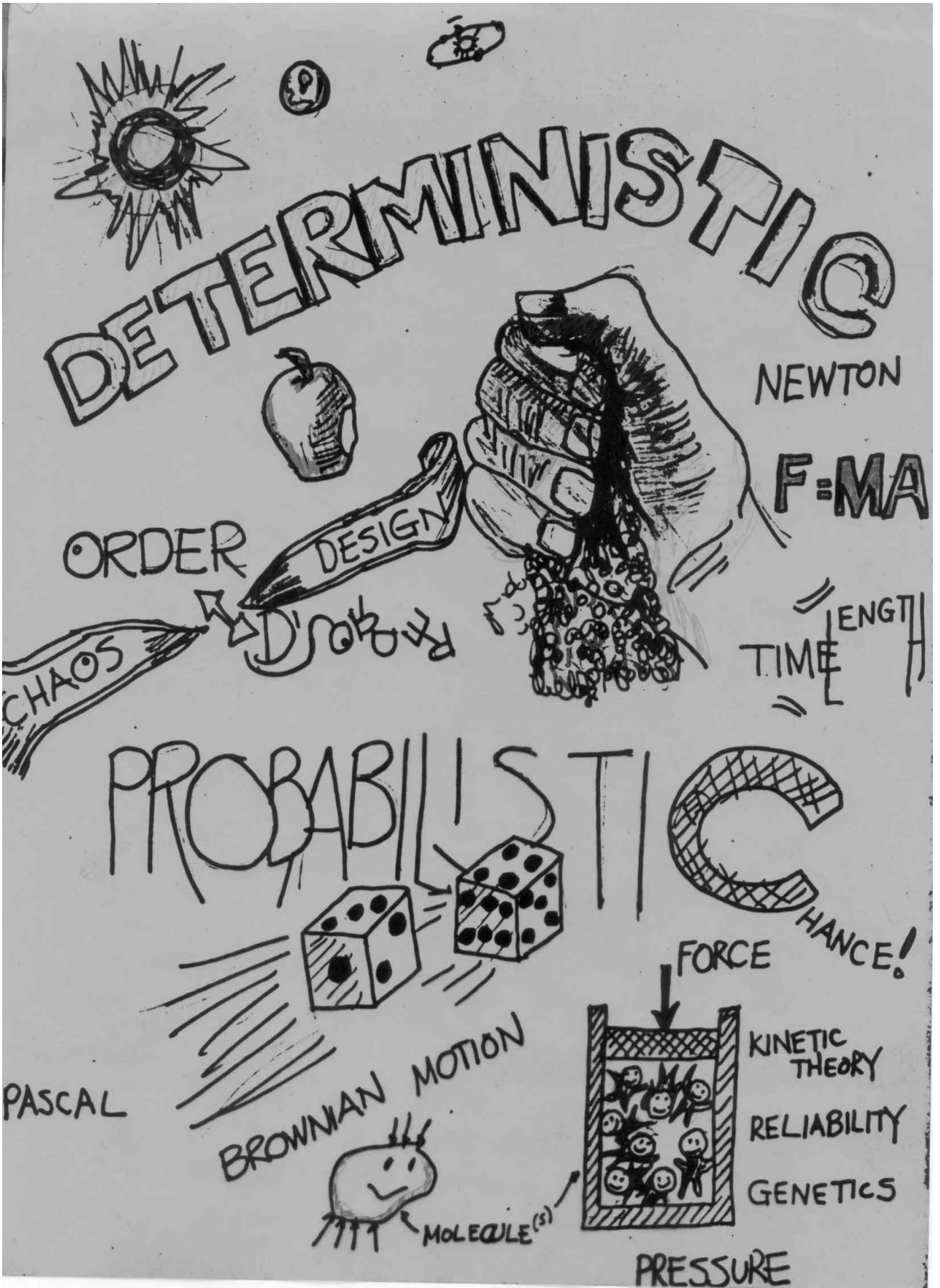
**PREDICTING PERFORMANCE OF THINGS**

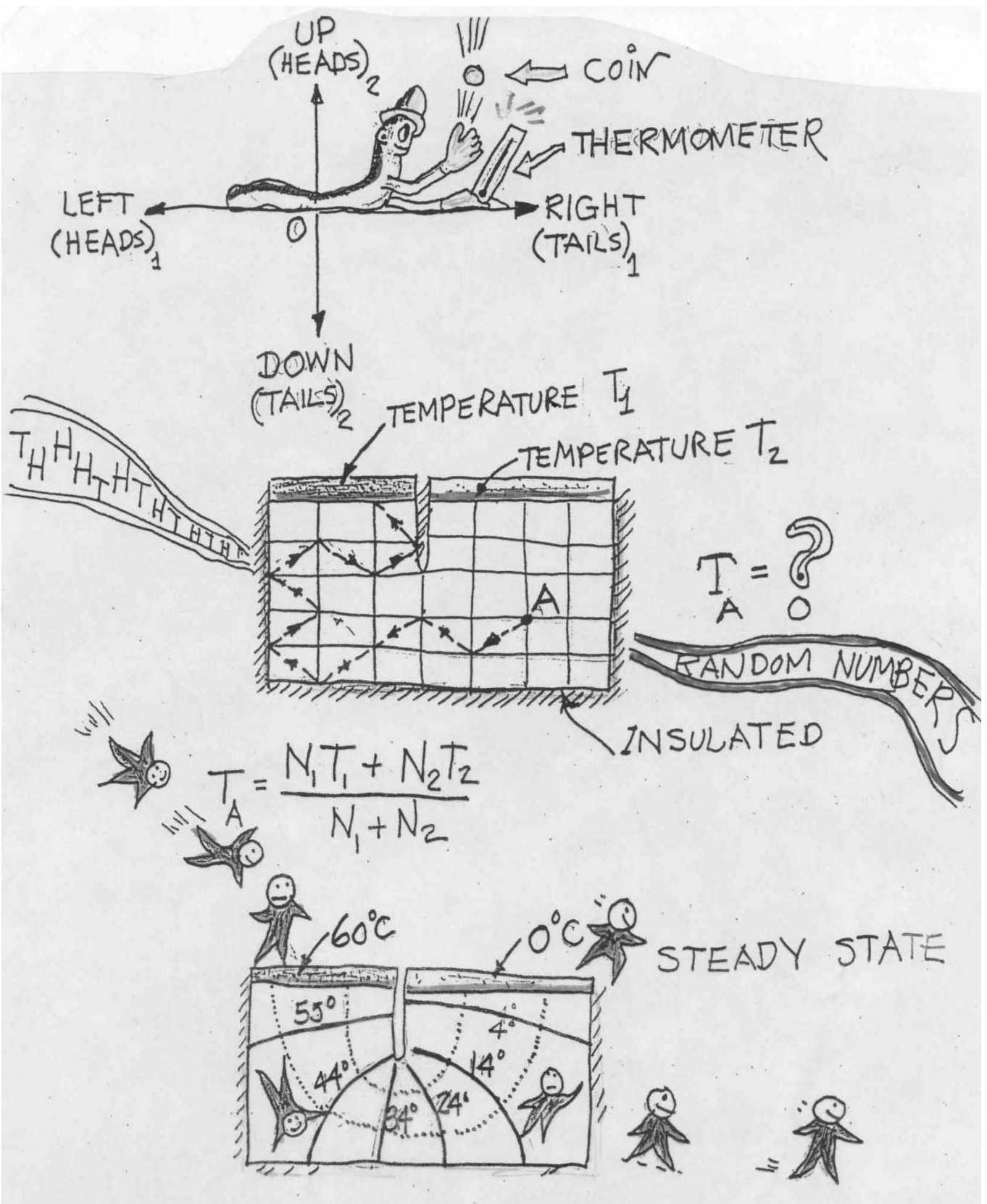
**NOT YET DONE!**

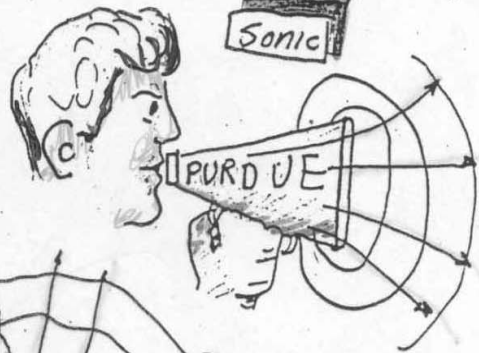
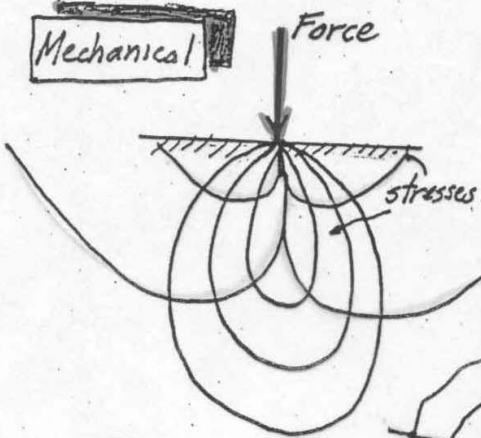
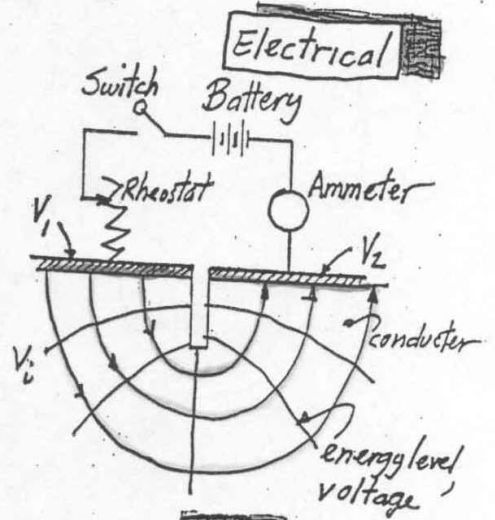
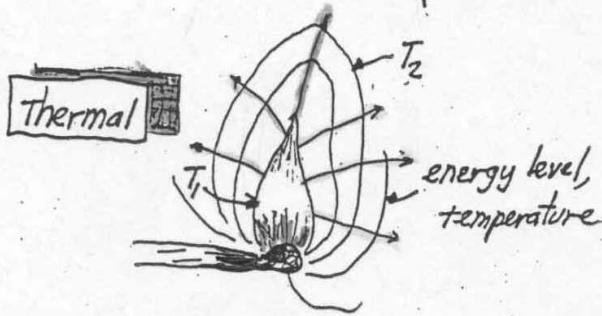
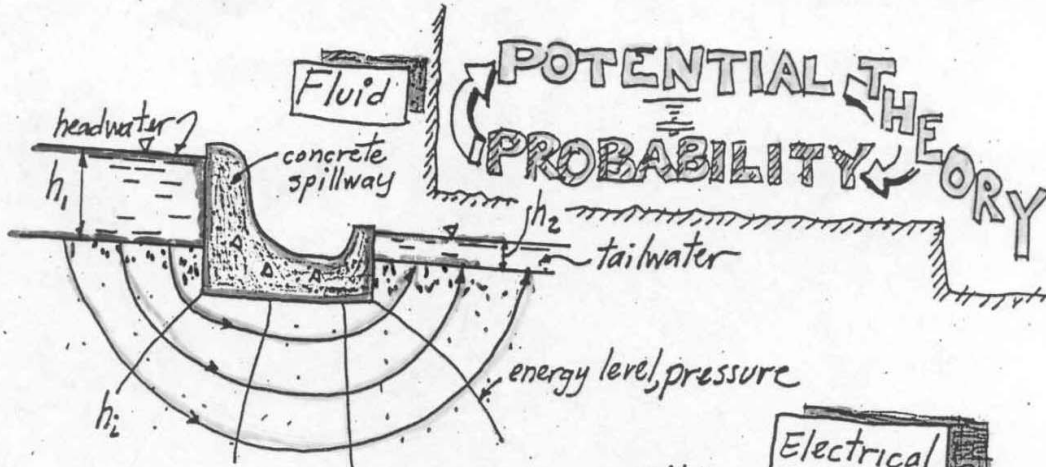


NEED BOTH







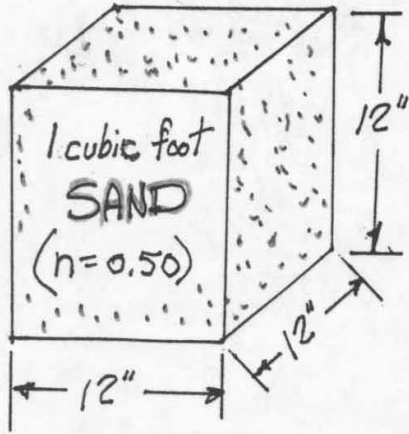


GRADIENT  
AND

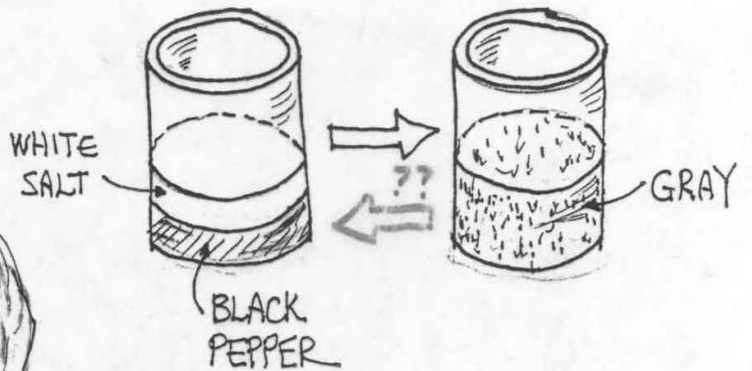
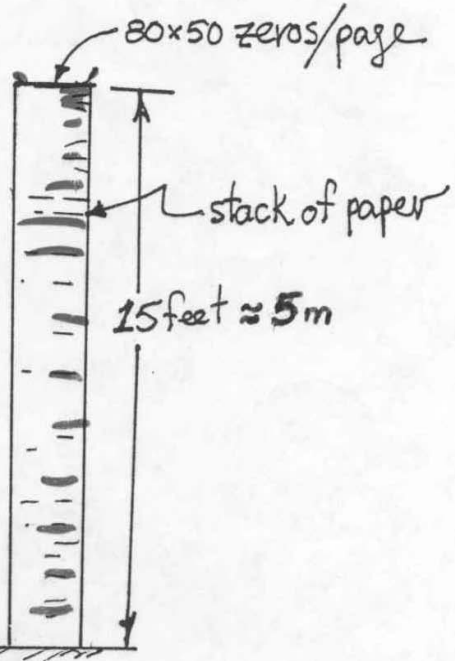
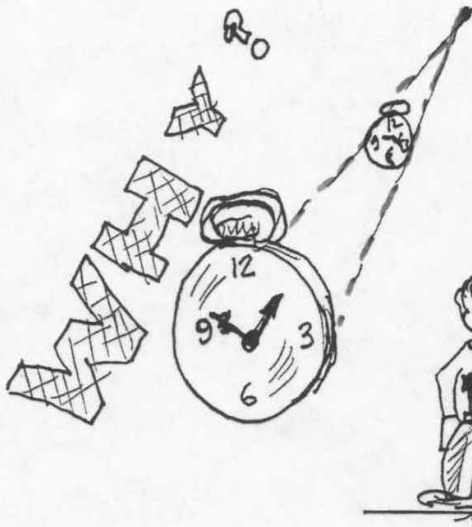
CONSERVATION OF ENERGY

OR CHANCE





$\approx 27,000,000$  particles  
 $\approx 10^{19}$  permutations



**THE**

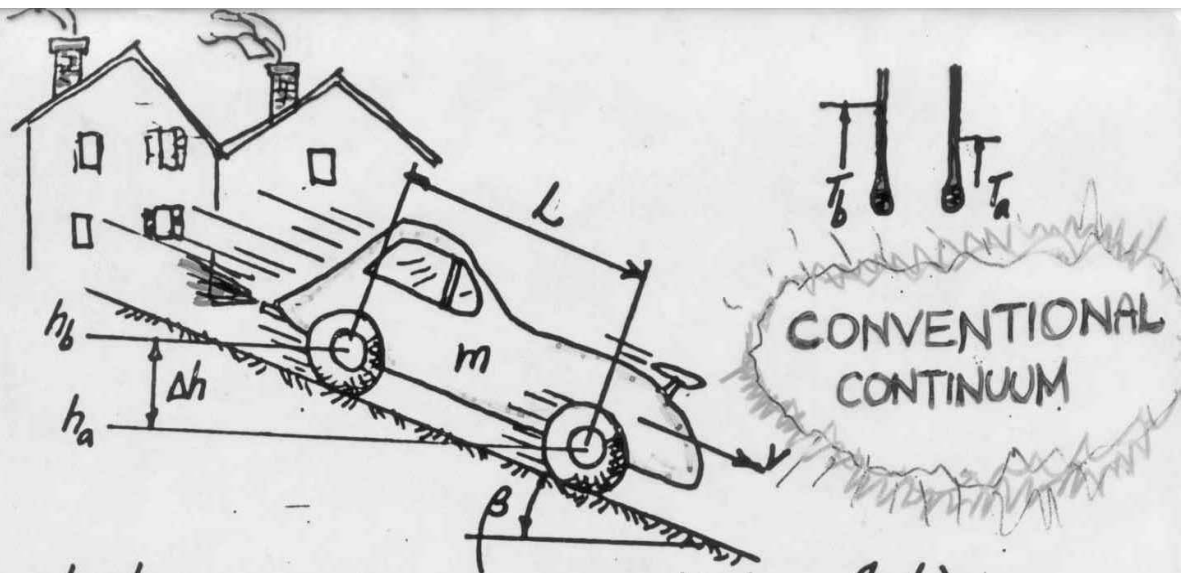


**PRINCIPLE**

**OF**

**MAXIMUM**

**ENTROPY**



(A)

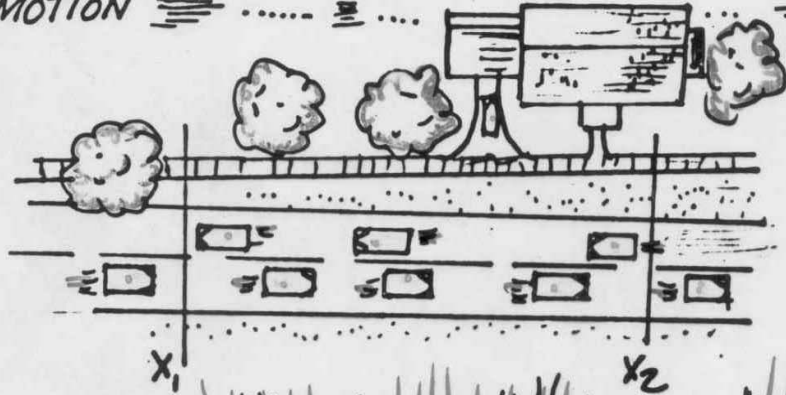
- velocity ..... gradient;  $v \propto (h_b - h_a)$
- current ..... voltage drop;  $i \propto (V_b - V_a)$
- heat flow ..... difference in temperature;  $\dot{q} \propto (T_b - T_a)$
- flow rate ..... pressure difference;  $w \propto (P_b - P_a)$
- force ..... change in velocity;  $F \propto (v_b - v_a)$

**PROPORTIONAL TO**

**MOTION**

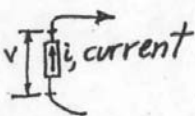
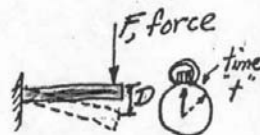


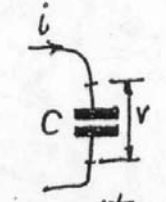
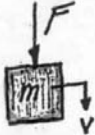
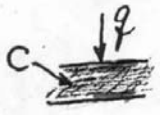

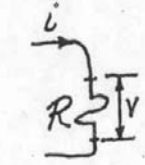
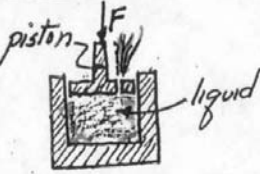


**CHANGE IN ENERGY!!!**

(B)



**LAW OF CONSERVATION OF CARS**

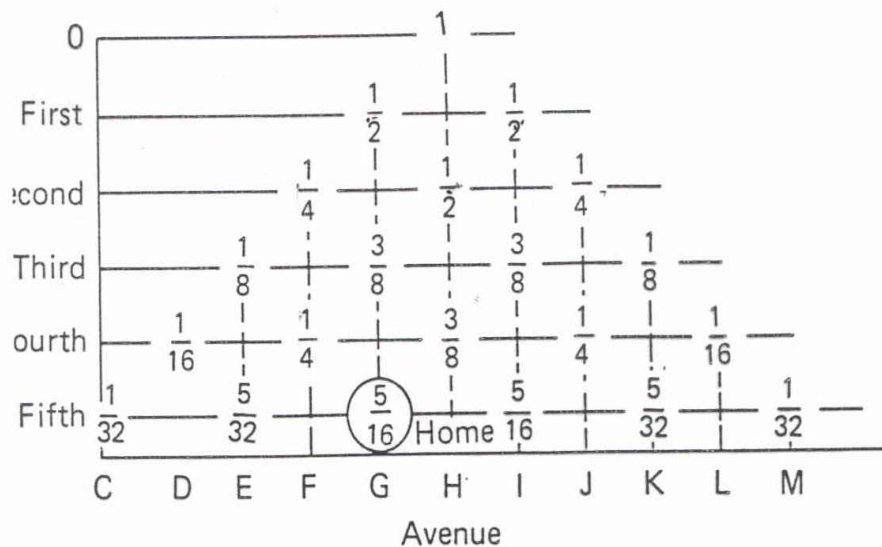
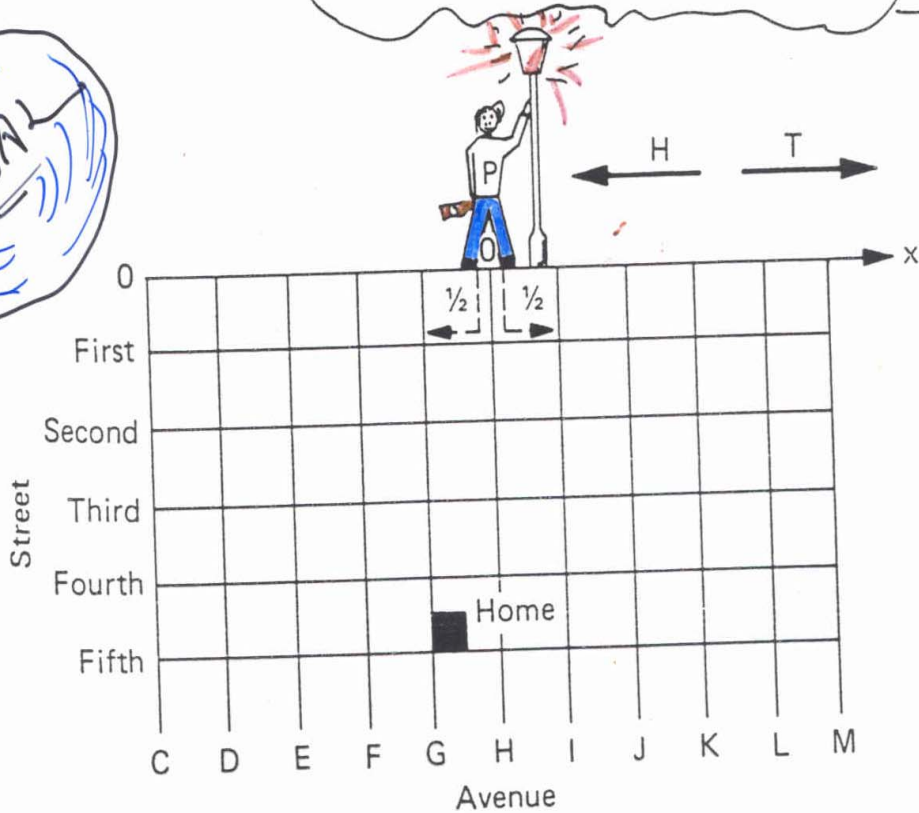
The net change in the number of vehicles on the section of highway between  $x_1$  and  $x_2$ , during any time interval, is the difference between the number entering and leaving that section!!!

Electrical	Mechanical	Thermal	Fluid
 $v$ , Voltage drop $i$ , current	 $F$ , force $v = D/t$ , Velocity $t$ , time	 $q$ , heat flow $T$ , Temperature	 $w$ , flow rate $p$ , pressure low high
 $C$ , Capacitor $i$ , current $v$ , voltage	 $m$ , Mass $F$ , force $v$ , velocity	 $C$ , Heat capacity $q$ , heat flow	 $w$ , flow rate Liquid storage
 $R$ , Resistor $i$ , current $v$ , voltage	 $F$ , force $v$ , velocity piston liquid Damper	 $R$ , Heat resistance $q$ , heat flow	 $w$ , flow rate long hose Liquid resistance
ohm's law	Newton's law	Fourier's law	Darcy's law

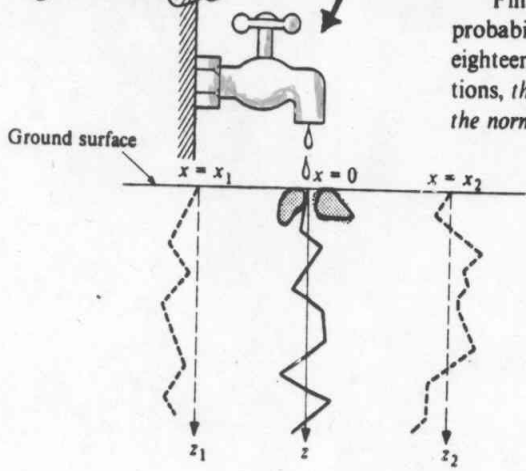
AT A POINT



# 2-D RANDOM WALK

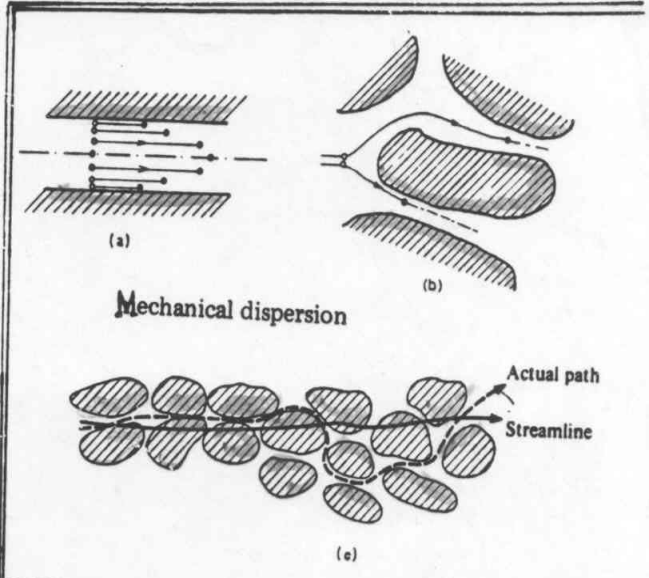


# Leaky Faucet Problem



# Central Limit Theorem

Finally, we give the most remarkable and most important theorem of all probability theory, the *central-limit theorem* (first introduced by De Moivre in the eighteenth century but so named by G. Polya in 1920). Under very general conditions, *the distribution of the sum of random variables converges (or approaches) to the normal distribution as the number of variables in the sum becomes large.*



$$P(x, t) = \frac{1}{\sqrt{4\pi Dt}} \exp\left[-\frac{x^2}{4Dt}\right]$$

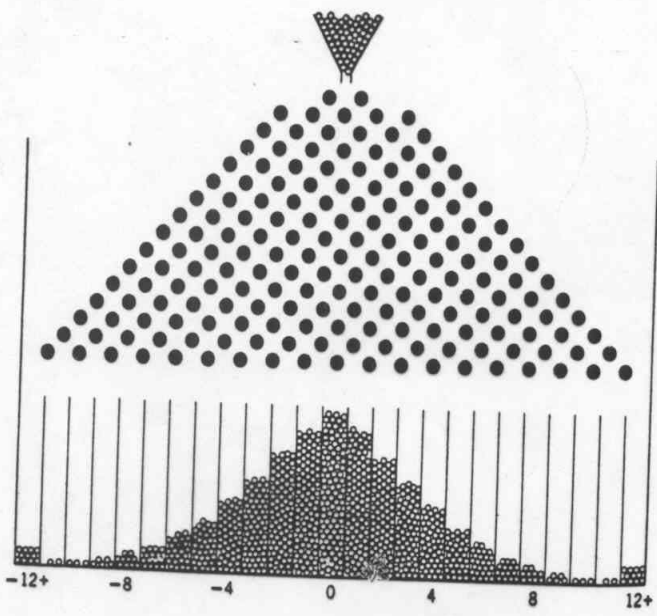
Normal/Gaussian Distribution

Dispersion Coef. ...

$$D = \frac{v_0 d}{2}$$

see  $\sigma_i$  below

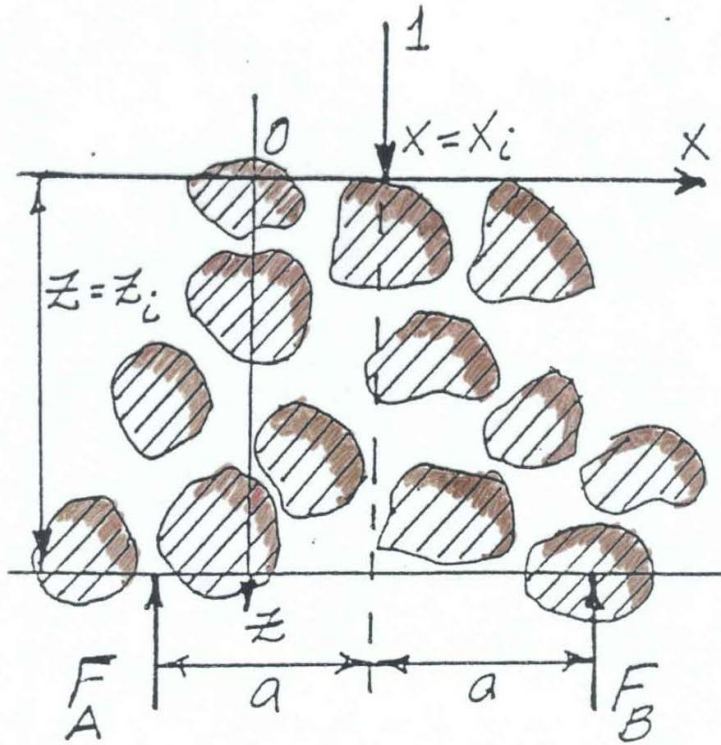
# Gaussian Plume Equation



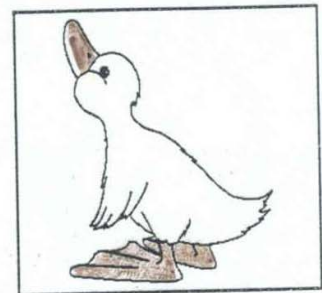
# Galton's Board

EXPECTED VALUE OF STRESS AT A POINT ?

$P[\text{particles touching in plane}] \rightarrow \odot$



$P[\text{stress} = 0] = ?$   
 $P[\text{stress} = \text{pore water pressure}] = ?$

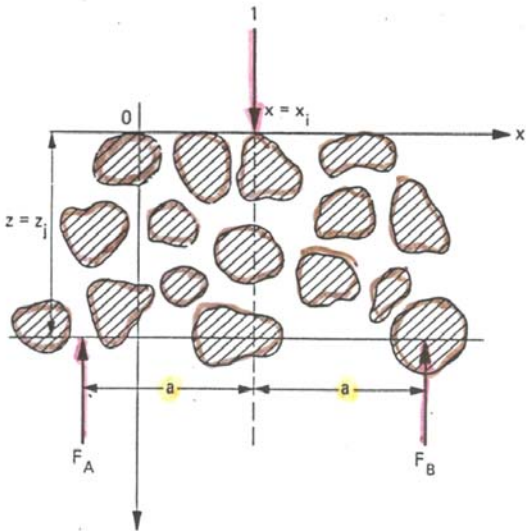


STRESS DISTRIBUTION

CENTRAL LIMIT THEOREM

ATTRACTOR??  
NO PROPERTY OF MATERIAL

Flamant solution



$$\left\{ \bar{s}_z(x, z) = \frac{P}{z\sqrt{2\nu\pi}} \exp\left[-\frac{x^2}{2\nu z^2}\right] \right\} \left\{ \sigma_z(x, z) = \frac{2Pz^3}{\pi(x^2 + z^2)^2} \right\}$$

$\frac{x}{z}$	$z\bar{s}_z = \left(\frac{2}{\pi}\right) \exp\left[-\frac{4x^2}{\pi z^2}\right]$	$z\sigma_z = \left(\frac{2}{\pi}\right) \left[1 + \frac{x^2}{z^2}\right]^{-2}$
0.0	0.64	0.64
0.1	0.63	0.62
0.2	0.61	0.59
0.3	0.57	0.54
0.4	0.52	0.47
0.5	0.46	0.41
0.6	0.40	0.34
0.8	0.28	0.24
1.0	0.18	0.16
1.2	0.10	0.11
1.5	0.04	0.06
1.8	0.01	0.04
2.0	0.004	0.03

$D = \pi/8$



3d

# CENTRAL LIMIT THEOREM

## TRANSMISSION OF VERTICAL STRESS

$$\bar{\sigma}_z = \frac{P}{2\pi v z^2} \exp\left[-\frac{x^2 + y^2}{2vz^2}\right] = \frac{P}{2\pi v z^2} \exp\left[-\frac{r^2}{2vz^2}\right]$$

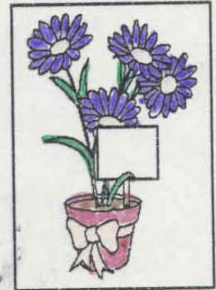
EXPECTED VALUE

$$\sigma_{z-\max} = \frac{3P}{2\pi z^2}$$

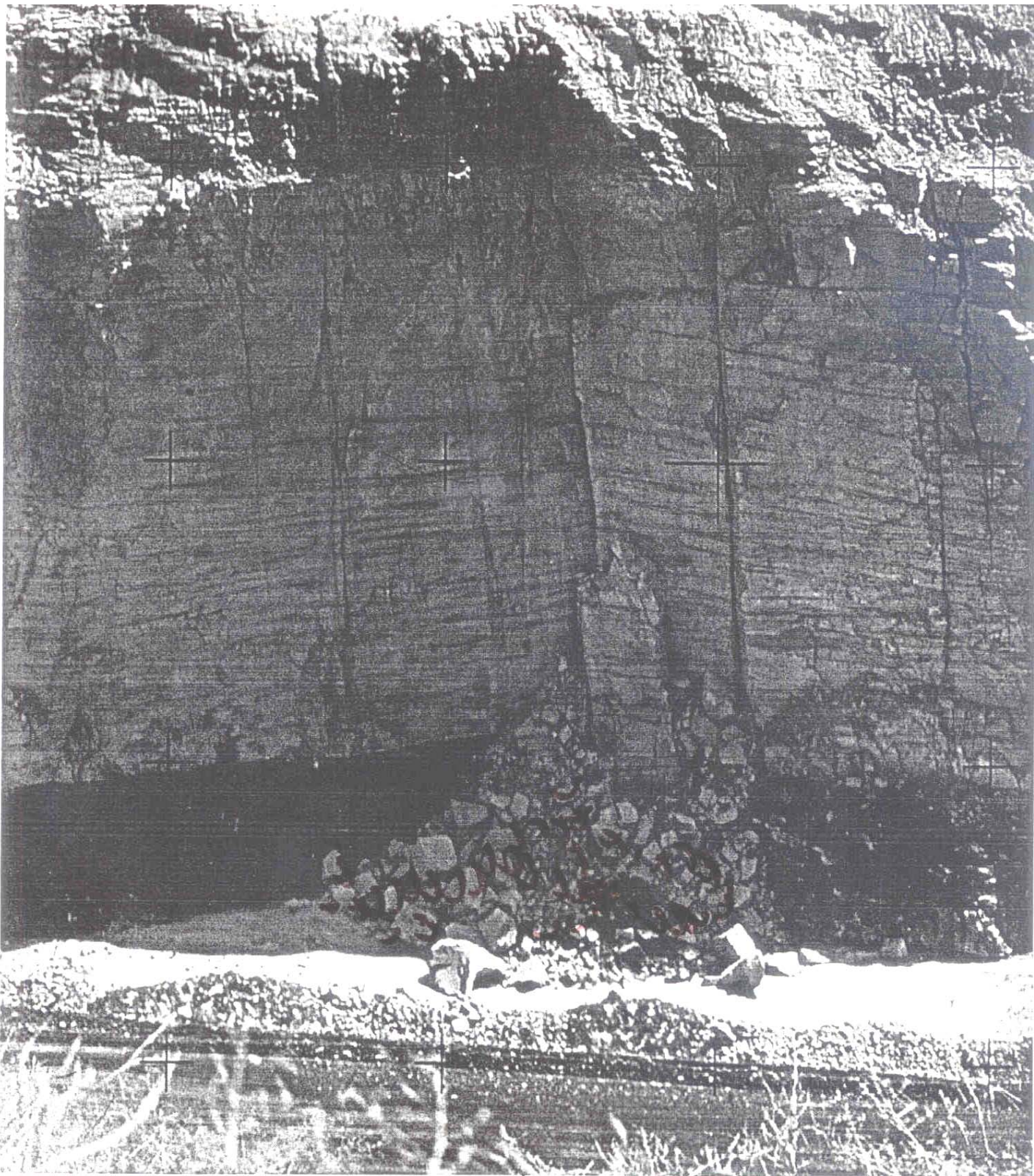
$$\bar{\sigma}_{z-\max} = \frac{P}{2\pi v z^2}$$

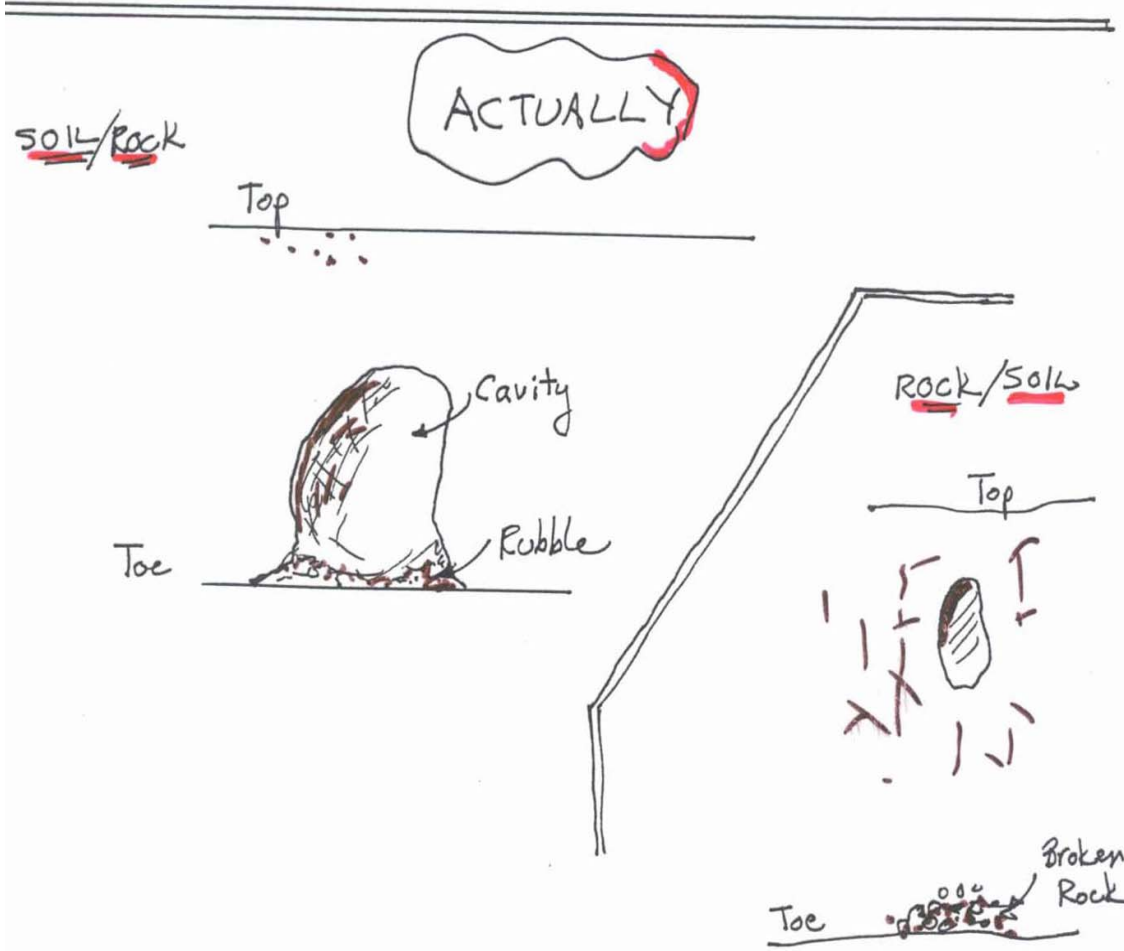
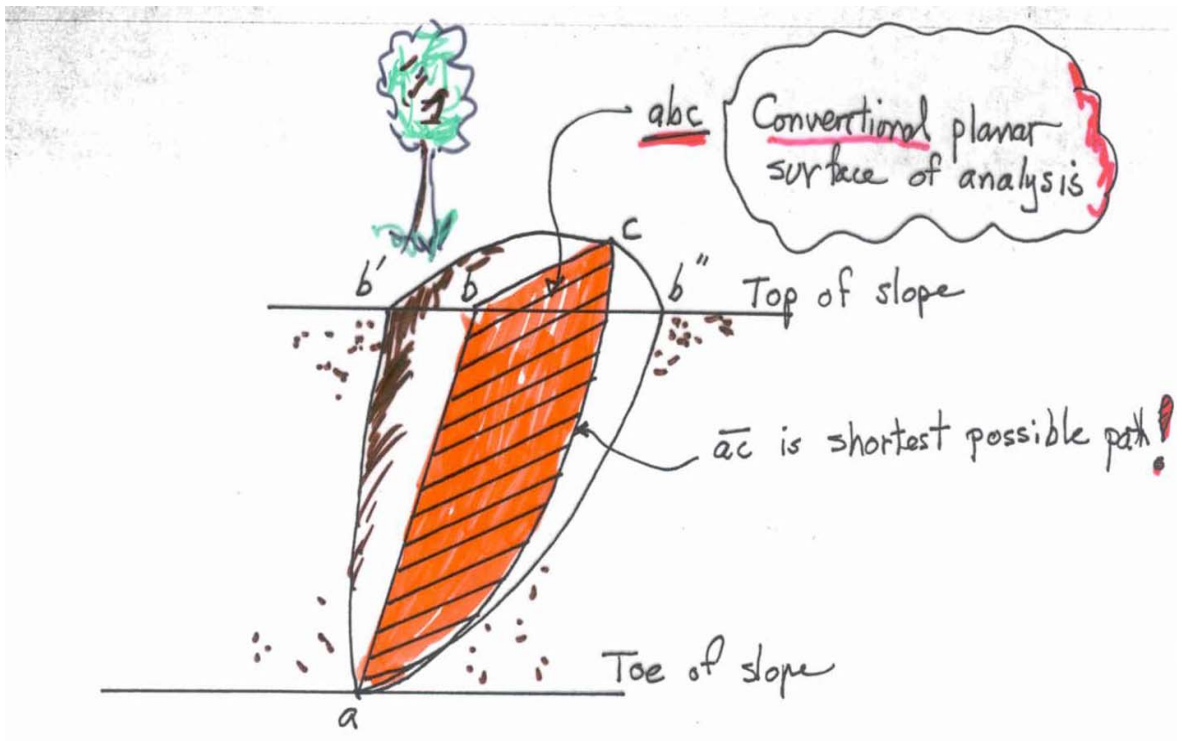
$v = 1/3$   
K.A.B

$\frac{r}{z}$	$\frac{z^2 \bar{\sigma}_z}{P}$	$\frac{z^2 \sigma_z}{P}$
0.0	0.48	0.48
0.1	0.47	0.47
0.2	0.45	0.43
0.4	0.38	0.33
0.6	0.28	0.22
0.8	0.18	0.14
1.0	0.11	0.08
1.2	0.06	0.05
1.5	0.02	0.03
2.0	0.001	0.01





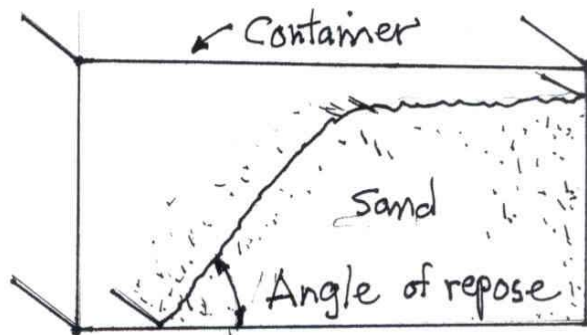




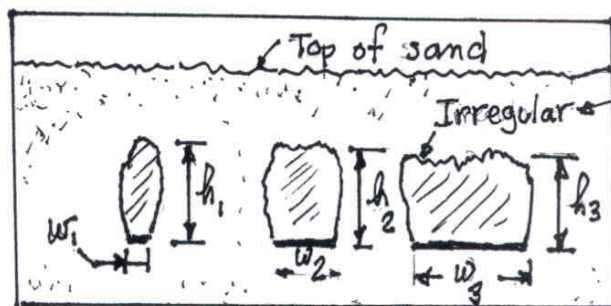


# EXPERIMENT WITH SAND: BRISBANE 7/01

(Side view)

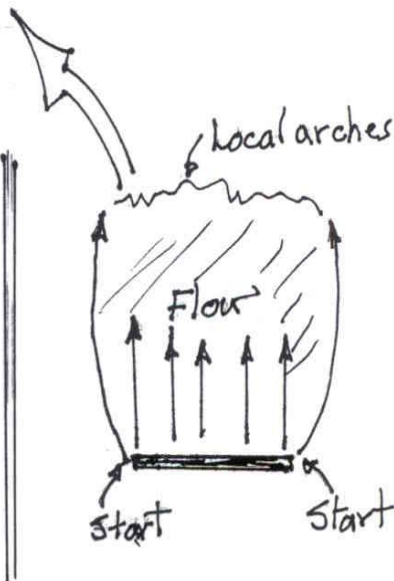
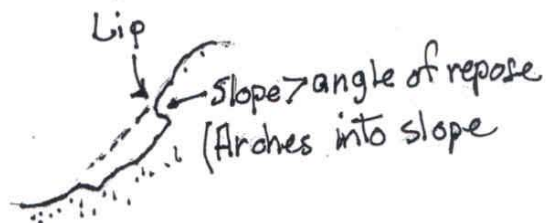


(Front view)



Local arches  
 $h_1 \approx h_2 \approx h_3$

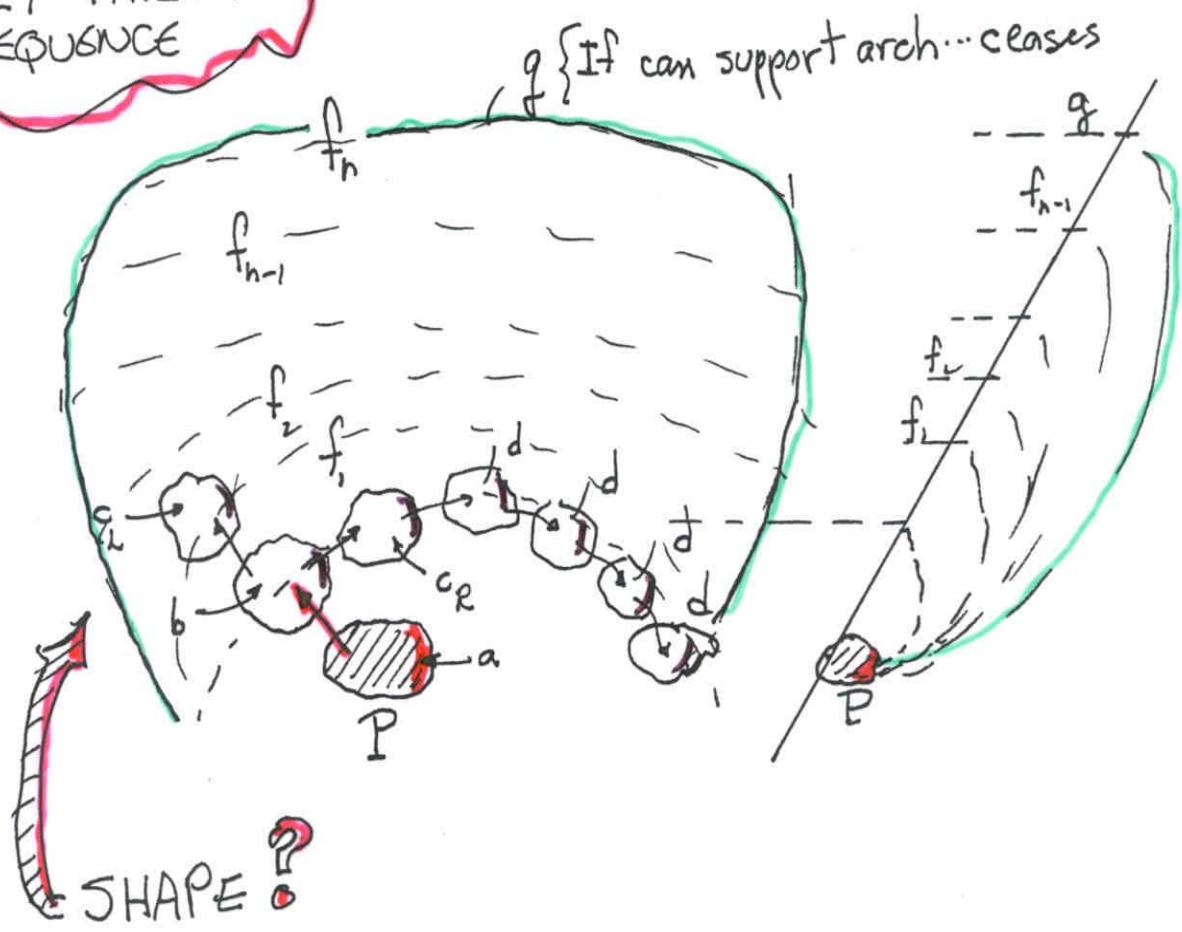
After failure  
 (Side view)



Repeated tests with gravel - Results similar  
BUT height of plume decreased with increasing  
 Particle size (up to 2"-3") ~ where  
 height is number of particles ~ Again height  
~~was~~ was independent of width of cut.



LIKELY FAILURE SEQUENCE



WHY DOES RUPTURE CEASE?  
ARCH CAN SUSTAIN LOAD!

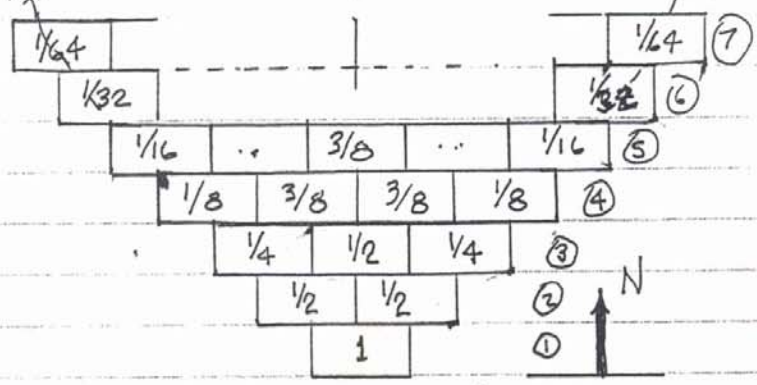
Rocks of side are so interlocked that vertical sides require NO lateral support

Region of, say  $p_f \leq 5\%$

$N = ?$

capture of  $1/32$

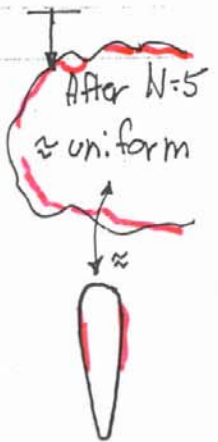
$R \leftarrow R = ?$



$\left\{ \begin{array}{l} 1/64 < 2\% \\ 1/32 < 4\% \end{array} \right\}$

<u>Along E</u>	
<u>N</u>	<u>Probability</u>
1	1
3	0.5
5	0.375
7	0.313
17	0.2
29	0.15
65	0.10
113	0.075
175	0.06
209	0.055
<u>250</u>	<u>0.050</u>

<u>Lateral to <math>\geq 0.05</math></u>	
<u>N</u>	<u>R (blocks from E)</u>
1	-
3	2
5	4
<u>7</u>	<u>6</u>
17	7
29	8
65	7
113	7
175	8
209	7
250	4



cohesionless sand. A detailed description of these tests will be presented in a companion volume on "Earth Tunneling with Steel Support." The test results led to the following conclusions regarding the prerequisites for arch action and the factors which determine the load on the roof support in tunnels through crushed rock and cohesionless sand located above the water table.

(a) The arch action is the inevitable consequence of the local stress relaxation produced by mining operations. The mechanics of the arch action are illustrated by Fig. 25. In this figure the ground arch is represented by the shaded area  $a c d b$ . The ground arch has a width  $B_1$ . While the tunnel is being excavated and the support installed, the mass of crushed rock or cohesionless sand constituting the ground arch

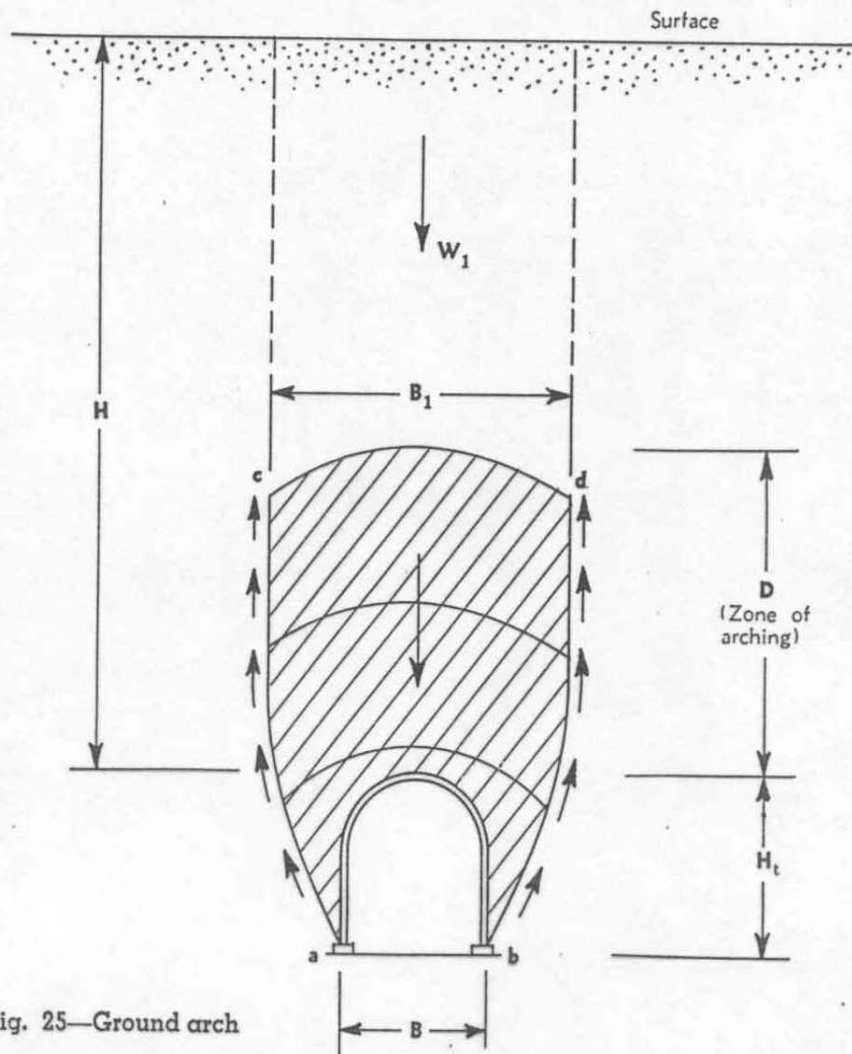


Fig. 25—Ground arch

tends to move into the tunnel. This movement is resisted by the friction along the lateral boundaries  $a c$  and  $b d$  of this mass. The friction forces transfer the major part of the weight of the overburden, with height  $H$  onto the material located on both sides of the tunnel and the roof support carries only the balance, equivalent to a height  $H_p$ .

(b) The thickness  $D$  of the ground arch is roughly equal to  $1.5 B_1$ . Above the ground arch the pressure conditions in the rock remain practically unaffected by the tunnel operations.

I was Jerry's first Ph.D. He was my academic father. We shared 40 magnificent years together at Purdue, often with two coffee breaks and lunch. Our discussions ran the gamut, from Monday morning quarterbacking to philosophy and, of course, liberal doses of soil mechanics. **It is said that nature abhors a vacuum. The vacuum that Jerry's (and Bill Dolch's) death created will never be filled.**